Math 2551 Worksheet Section 13.1

- 1. Given the position of a particle in the xy-plane at time t: $\vec{r}(t)=e^t\hat{i}+\frac{2}{9}e^{2t}\hat{j},\,t=\ln 3,$
 - (a) find an equation in x and y whose graph is the path of the particle.
 - (b) find the particle's velocity and acceleration vectors at the given value of t.
 - (c) Sketch the path of the particle and include the particle's velocity and acceleration vectors at the given value of t.

- 2. Given the position of a particle in the xy-plane at time t: $\vec{r}(t) = (2\cos t)\hat{i} + (3\sin t)\hat{j} + 4t\hat{k}, t = \pi/2,$
 - (a) find the particle's velocity and acceleration vectors.
 - (b) write the particle's velocity at the given value of t as the product of its speed and direction.

 $3. \,$ Find the parametric equations for the line that is tangent to the curve

$$\vec{r}(t) = \left\langle \ln t, \frac{t-1}{t+2}, t \ln t \right\rangle, \text{ at } t = 1.$$