# Relational Algebra (and SQL)

# Reading

Ramakrishnan Sections 4.1 and 4.2

Helpful Reference

https://en.wikipedia.org/wiki/Relational\_algebra

# Queries: ask your data a question

Declarative language: ask what you want, now how Meaning: Queries are high level, "readable"

Not Turing complete (can't execute any algorithm)

Supports easy, efficient access to large databases Domain specific language for data access

SQL: Data Definition Language (DDL)

Data Manipulation Language (DML)

# Basic Single Table SELECT

# SELECT (output) FROM (input) WHERE (condition)

```
SELECT * FROM Students
SELECT name FROM Students
SELECT name FROM Students WHERE age < 21
SELECT name, login FROM Students WHERE gpa >= 3
```

sid	name	login	age	gpa
1	eugene	ewu	20	2.5
2	luis	gravano	25	3.5
3	martha	martha	32	3.9

# Single Table Semantics

#### conceptual evaluation method:

- 1. FROM clause: retrieve Students relation
- 2. WHERE clause: Check conditions, discard tuples that fail
- 3. SELECT clause: Delete unwanted fields

Real evaluation is *much* more efficient, but must produce the same answers.

# Ambiguous names

E.g. Students: (sid, name, ...)

Enrolled: (sid, cid, grade)

Qualified names: Use table name: Students.age

Rename: AS (optional): shortcuts, ambiguity, clarity

SELECT S.sid, S.name FROM Students AS S SELECT S.sid, S.name FROM Students S

# Related data: Multiple tables

# What does this return?

# SELECT S.name, E.cid FROM Students S, Enrolled E WHERE S.sid = E.sid AND E.grade = 'A'

#### **Enrolled**

sid	cid	grade
1	2	Α
1	3	В
2	2	A+

SELECT S.name, E.cid

FROM Students S, Enrolled E

WHERE S.sid = E.sid AND

E.grade = 'A'

#### **Students**

sid	name
1	eugene
2	luis

#### Result

name	cid
eugene	2

#### Multi-Table Semantics

- Modify the FROM clause evaluation
  - 1. FROM clause: compute *cross-product* of Students and Enrolled

#### Enrolled

sid	cid	grade
	2	Α
1	3	В
2	2	A+

#### **Students**

sid	name
1	eugene
2	luis

#### Cross-product

sid	cid	grade	sid	name
I	2	Α	1	eugene
I	3	В	I	eugene
2	2	A+	I	eugene
1	2	Α	2	luis
1	3	В	2	luis
2	2	A+	2	luis

#### Multi-Table Semantics

#### Modify the FROM clause evaluation

- 1. FROM clause: compute *cross-product* of Students, Enrolled
- 2. WHERE clause: Check conditions, discard tuples that fail
- 3. SELECT clause: Delete unwanted fields

# Formal Relational Query Languages

Formal basis for real languages e.g., SQL

#### Relational Algebra

Function of operations applied to relations

Operational: step-by-step execution plans

#### **Relational Calculus**

Logical, describes what data users want (not operational, fully declarative)

#### **Definitions**

Relation (for this lecture)

Instance is a set of tuples

Schema defines field names and types (domains)

Students(sid int, name text, major text, gpa int)

Fields: Reference by name: (e.g. major)

Reference by position starting at 1: (e.g. 3)

Names are for humans; positions for "intermediate" results

#### **Definitions**

Query is a function over relation instances

$$Q(R_1,...,Rn) = R_{result}$$

Schemas of input and output relations are *fixed* and well defined by the query Q.

# Relational Algebra Overview

Core 5 operations

PROJECT  $(\pi)$ 

SELECT  $(\sigma)$ 

UNION (U)

SET DIFFERENCE (-)

CROSSPRODUCT (x)

Additional operations

RENAME (p)

INTERSECT (∩)

JOIN (⋈)

DIVIDE (/)

# Instances Used Today: Library

Students, Reservations

RI

sid	rid	day
1	101	10/10
2	102	11/11

Use positional or named field notation

SI

sid	name	gpa	age
I	eugene	4	20
2	barak	3	21
3	trump	2	88

Field names in results inherited from input relations (unless specified)

**S2** 

sid	name	gpa	age
4	aziz	3.2	21
2	barak	3	21
3	trump	2	88
5	rusty	3.5	21

# Project

$$\pi_{\langle attr1,...\rangle}(A) = R_{result}$$

Extract desired fields (subset of columns)

Schema is subset of input schema in the projection list

 $\pi_{\langle a,b,c\rangle}(A)$  has output schema (a,b,c) w/ types carried over

# **Project**

**S2** 

sid	name	gpa	age
4	aziz	3.2	21
2	barak	3	21
3	trump	2	88
5	rusty	3.5	21

$$\pi_{\text{name,age}}(S2) =$$

name	age
aziz	21
barak	21
trump	88
rusty	21

# Project

**S2** 

sid	name	gpa	age
4	aziz	3.2	21
2	barak	3	21
3	trump	2	88
5	rusty	3.5	21

$$\pi_{age}(S2) = \frac{21}{88}$$

Where did all the rows go? Real systems typically don't remove duplicates. Why?

#### Select

$$\sigma_{}(A) = R_{result}$$

Select subset of rows that satisfy condition *p*Won't have duplicates in result. Why?
Result schema same as input

#### Select

SI

sid	name	gpa	age
1	eugene	4	20
2	barak	3	21
3	trump	2	88

$$\sigma_{age < 30} (S1) =$$

sid	name	gpa	age
I	eugene	4	20
2	barak	3	21

$$\pi_{\text{name}}(\sigma_{\text{age} < 30} (S1)) = \begin{bmatrix}
\text{name} \\
\text{eugene} \\
\text{barak}
\end{bmatrix}$$

$$A + B = B + A$$
 $A * B = B * A$ 
 $A + (B * C) = (B * C) + A$ 
 $Associativity:$ 
 $A + (B + C) = (A + B) + C$ 
 $A + (B * C) = (A + B) * C$ 

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 $A + (B * C) = (A + B) * C$ 

$$\pi_{\text{age}}(\sigma_{\text{age} \leq 30} \text{ (SI)})$$

	sid	name	gpa	age	
		eugene	4	20	
O <sub>age</sub> <30	2	barak	3	21	
	3	trump	2	88	

sid	name	gpa	age
1	eugene	4	20
2	barak	3	21

$$\pi_{age}(\sigma_{age < 30} (SI))$$

	sid	name	gpa	age	
$\pi_{age}$	I	eugene	4	20	
age	2	barak	3	21	

age
20
21

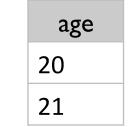
$$\sigma_{\text{age} < 30}(\pi_{\text{age}}(S1))$$

-	sid	name	gpa	age	
	I	eugene	4	20	
$\pi_{age}$	2	barak	3	21	
	3	trump	2	88	

age	
20	
21	
88	

$$\sigma_{\text{age} < 30}(\pi_{\text{age}}(SI))$$

-	sid	name	gpa	age	
	I	eugene	4	20	
$\pi_{age}$	2	barak	3	21	
	3	trump	2	88	



Does Project and Select commute?

$$\pi_{\text{age}}(\sigma_{\text{age} < 30} (SI)) = \sigma_{\text{age} < 30}(\pi_{\text{age}}(SI))$$

What about

$$\pi_{\text{name}}(\sigma_{\text{age}<30} (SI))$$
?

#### Does Project and Select commute?

$$\pi_{\text{age}}(\sigma_{\text{age} < 30} (SI)) = \sigma_{\text{age} < 30}(\pi_{\text{age}}(SI))$$

What about

$$\pi_{\text{name}}(\sigma_{\text{age} < 30} (SI)) := \sigma_{\text{age} < 30}(\pi_{\text{name}}(SI))$$

#### Does Project and Select commute?

$$\pi_{\text{age}}(\sigma_{\text{age} < 30} (SI)) = \sigma_{\text{age} < 30}(\pi_{\text{age}}(SI))$$

What about

$$\pi_{\text{name}}(\sigma_{\text{age} < 30} \text{ (SI)}) \mathrel{!=} \sigma_{\text{age} < 30}(\pi_{\text{name, age}}(\text{SI}))$$

#### Does Project and Select commute?

$$\pi_{\text{age}}(\sigma_{\text{age} < 30} (SI)) = \sigma_{\text{age} < 30}(\pi_{\text{age}}(SI))$$

#### What about

$$\pi_{\text{name}}(\sigma_{\text{age} < 30} (SI)) = \pi_{\text{name}}(\sigma_{\text{age} < 30}(\pi_{\text{name, age}}(SI)))$$

#### OK!

# Union, Set-Difference

A op B = 
$$R_{result}$$

A, B must be union-compatible

Same number of fields

Field i in each schema have same type

Result Schema borrowed from first arg (A)

Student(sid int, age int) U Class(cid int, max int) = ?

# Union, Set-Difference

A op B = 
$$R_{result}$$

A, B must be union-compatible

Same number of fields
Field i in each schema have same type

#### Result Schema borrowed from first arg (A)

Student(sid int, age int) U Class(cid int, max int) = R<sub>result</sub>(sid int, age int)

# Union, Intersect, Set-Difference

S

sid	name	gpa	age
I	eugene	4	20
2	barak	3	21
3	trump	2	88

**S2** 

sid	name	gpa	age
4	aziz	3.2	21
2	barak	3	21
3	trump	2	88
5	rusty	3.5	21

SIUS2 =

sid	name	gpa	age	
I	eugene	4	20	
4	aziz	3.2	21	
5	rusty 3.5		21	
3	trump	2	88	
2	barak	3	21	

# Union, Intersect, Set-Difference

SI

sid	name	gpa	age	
I	eugene	4	20	
2	barak	3	21	
3	trump	2	88	

**S2** 

sid	name	gpa	age	
4	aziz	3.2	21	
2	barak	3	21	
3	trump 2		88	
5	rusty	3.5	21	

$$SI-S2 =$$

sid	name	gpa	age
I	eugene	4	20

#### Note on Set Difference & Performance

Most operators are monotonic increasing size of inputs → outputs grow can compute *incrementally* 

Set Difference is *not monotonic:* 

compute A - Badd data to B:  $B2 = B \cup X$ compute A - B2could be smaller than A - B

Set difference is blocking:

For T – S, must wait for all S tuples before any results

Intersect: A ∩ B

Keep tuples in both A and B

Can be defined with Set Difference  $A \cap B = A - (A - B)$ 

#### **Cross-Product**

$$A(a_1,...,a_n) \times B(a_{n+1},...,a_m) = R_{result}(a_1,...,a_m)$$

Each row of A paired with each row of B

Result schema: Combine A and B's fields, inherit if possible

Conflict: students and reservations have sid field

# **Cross-Product**

SI

sid	name	gpa	age	
I	eugene	4	20	
2	barak	3	21	
3	trump	2	88	

RI

sid	rid	day
1	101	10/10
2	102	11/11

SIxR1 =

(sid)	name	gpa	age	(sid)	rid	day
I	eugene	4	20	I	101	10/10
2	barak	3	21	I	101	10/10
3	trump	2	88	I	101	10/10
I	eugene	4	20	2	102	11/11
2	barak	3	21	2	102	11/11
3	trump	2	88	2	102	11/11

#### Rename

Explicitly defines/changes field names of schema

$$\rho(C(1 \rightarrow sid1, 5 \rightarrow sid2), S1 \times R1)$$