

UNIVERSITY OF CALIFORNIA
Los Angeles

Numerical Studies of Turbulence in LAPD

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of the requirements for the degree
Doctor of Philosophy in Physics

by

Brett Cory Friedman

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ABSTRACT OF THE DISSERTATION

Numerical Studies of Turbulence in LAPD

by

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The BOUT++ Code

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APPENDIX B

Grid Convergence