

# Aggregation and Design of Information in Asset Markets with Adverse Selection

Vladimir Asriyan  
CREI

William Fuchs  
UT Austin and UC3M

Brett Green  
Wash U.

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# Introduction

Since Hayek (1945), information aggregation has been an important topic in economics and finance.

- Typically, analyzed in the literature in the context of centralized markets for homogenous assets.

This paper: study information aggregation in the context of decentralized markets for heterogeneous but correlated assets.

- ① Does the aggregate trading behavior in the market reveal the underlying fundamentals?
- ② Is laissez-faire equilibrium efficient, i.e., is there scope for an optimal design of disclosure policies?

# Introduction

## Our framework:

- Many sellers ( $N$ ), each privately informed about quality of her asset.
- Buyers compete, are uninformed, and face a lemons problem à la Akerlof.
- Asset qualities are correlated with an unobservable *aggregate state of nature*, i.e., there are more bad assets in the low state.
- Trade occurs over time. Key feedback:

(Expected) info arrival  $\implies$  Trading behavior  $\implies$  (Actual) info arrival

Our objective: study a large market ( $N \uparrow \infty$ ) and its information properties from both positive and normative perspectives.

# The Model

# Sellers

- There are two trading dates,  $t = 1, 2$ .
- There are  $N$  sellers,  $i = \{1, \dots, N\}$ . Each seller owns an indivisible asset.
- Each seller is privately informed about the type of her asset, denoted by  $\theta_i \in \{L, H\}$ . Seller values asset of type  $\theta$  at  $c_\theta$ , with  $c_L < c_H$ .
- The payoff to a seller with asset of type  $\theta$  who agrees to trade at price  $p$  at time  $t$  is:

$$(1 - \delta^{t-1})c_\theta + \delta^{t-1}p$$

where  $\delta$  is the discount factor. If the seller never trades, her payoff is  $c_\theta$ .

## Buyers

- Each seller has multiple potential trading partners or “buyers.” Buyers value asset of type  $\theta$  at  $v_\theta$ , with  $v_L < v_H$ .
- There is common knowledge of gains from trade:  $v_\theta > c_\theta$ .
- Each period, given their information, buyers bid for the assets.
- The payoff to a buyer who purchases an asset of type  $\theta$  at price  $p$  is:

$$v_\theta - p$$

If the buyer does not trade, his payoff is 0.

# Uncertainty and correlation

There is an unobserved state of nature  $S \in \{l, h\}$ :

- Unconditional distribution is:

$$\mathbb{P}(\theta_i = L) = \mathbb{P}(S = l) = 1 - \pi_0.$$

- Conditional distribution of asset types is:

$$\mathbb{P}(\theta_i = L | S = l) = \lambda > 1 - \pi_0.$$

## Two assumptions

**Assumption 1 (Lemons Condition)**  $\pi_0 v_H + (1 - \pi_0) v_L < c_H$ .

**Assumption 2 (No Separation)**  $v_L < (1 - \delta)c_L + \delta v_H$ .

These assumptions rule out the first-best efficient outcome and ensure that dynamic considerations are relevant.

# Equilibrium

# Equilibrium structure

We use Perfect Bayesian Equilibrium (PBE) as our equilibrium concept.

- ① Buyers' offers are optimal given the seller's strategy and other buyers' strategy.
- ② Seller's optimize given the other seller's strategy and expected offers from buyers.
- ③ Beliefs are updated by Bayes Rule.

# Equilibrium structure

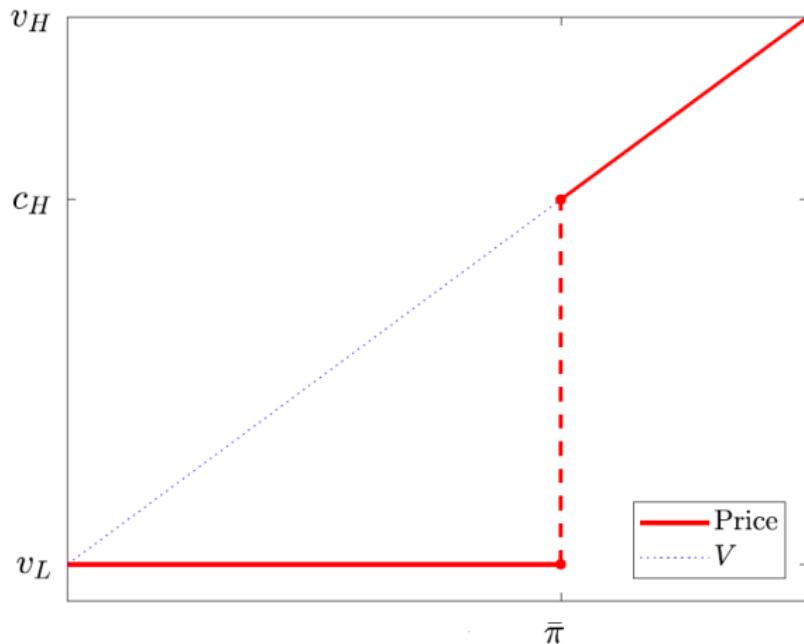
Second (last) period is a static Akerlof:

- ① Buyers' update their beliefs, based on past trading information.
- ② Buyers bid the expected value, conditional on seller acceptance.
- ③ Sellers accept/reject and game ends.

First period:

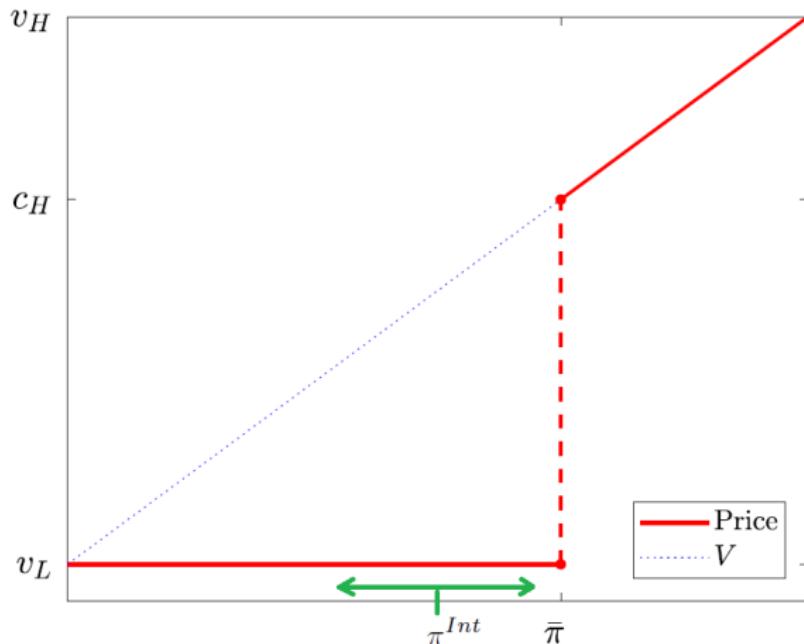
- ① Buyers make low offer.
  - Due to Skimming Property + Lemons Condition.
- ② High types do not trade; low types trade with probability  $\sigma \in (0, 1)$ .
  - All equilibria turn out to be symmetric, i.e.,  $\sigma_i = \sigma \forall i$ .
  - No Separation Condition  $\implies \sigma < 1$ . Endogenous information  $\implies \sigma > 0$ .

## Price function in the second period



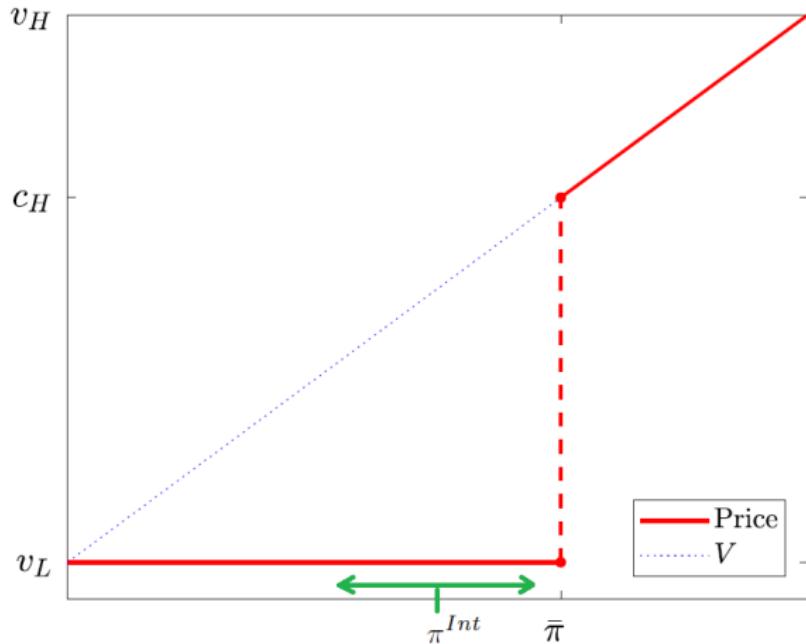
Note: Price in the second period is non-linear in  $\bar{\pi}$  due to adverse selection.

## Price function in the second period



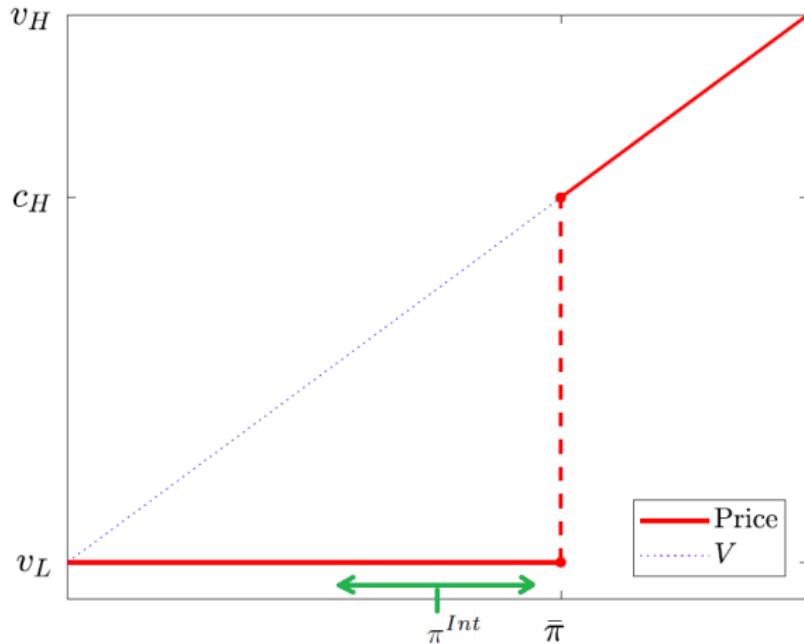
$\pi$  depends on own trading prob.  $\sigma_i$  which moves beliefs from  $\pi_0$  to  $\pi^{INT}$  and then information arrival generates a distribution of posteriors.

# Option value effect



**Option value effect:** information arrival  $\implies$  high prices conditional on good news.  
 Since  $\pi_0 < \bar{\pi}$ , this effect is strong (weak) when  $\sigma_i$  is low (high).

# Option value effect



**Option value effect:** information arrival  $\implies$  high prices conditional on good news.  
 Of course, both  $\sigma_i$  and the distribution of news (through  $\sigma_{-i}$ ) are endogenous.

# Trading incentives in the first period

- Given the Lemons Condition only low types trade in the first period. Prior is too low to have the pooling offer attract the high type to sell.
  - No high types trades.
  - Low types must trade with positive probability.
- Given the No Separation Condition low types cannot trade with probability 1 otherwise the price would be too high the second period and they would regret having traded.
- In equilibrium, low type must be indifferent between accepting  $v_L$  the first period or waiting to trade in the second period.

## Trading incentives in the first period

In equilibrium, low type must be indifferent to trade in the first period:

$$v_L = Q_L(\sigma) \equiv (1 - \delta)c_L + \delta\mathbb{E}_L \{F_L(\pi)\}$$

where:

- $Q_L$  is the low type's continuation value,
- $\pi$  is the buyers' (random) posterior belief that the seller is a high type,
- $F_L$  is the low type's expected payoff as a function of belief  $\pi$ .
  - Essentially, equals the second period asset price.

# Equilibrium summary

Finding an equilibrium boils down to finding  $\sigma$  such that:

$$v_L = Q_L(\sigma)$$

- Equilibrium exists.
- There might be multiple equilibria.

We want to study the information properties of the equilibria as the market size  $N$  becomes large.

# Information aggregation

# Information aggregation

For a given  $N$ , let  $p_N$  denote the buyers' posterior belief that the state is  $h$ , upon observing trading behavior in the first period.

- Note: information revealed by second period trades is payoff irrelevant.

## Definition

There is information aggregation along a given sequence of equilibria if

$$p_N \rightarrow \mathbb{1}\{S = h\} \text{ as } N \rightarrow \infty \text{ in probability.}$$

Let  $\sigma_N$  denote the equilibrium trading probability when market size is  $N$ .

- If  $\sigma_N$  were uniformly bounded away from 0, information would aggregate:
  - In state  $s$ , the fraction of trades would converge to population mean  $\sigma_N \cdot \mathbb{P}(\theta_i = L | S = s)$ .
- But what if  $\sigma_N \rightarrow 0$ ?

As it turns out, neither of these two cases is pathological!

## Fictitious economy

It is useful to consider a ‘fictitious’ economy where:

- Aggregate state  $S$  is revealed before trade at  $t = 2$ .  
⇒ Seller  $i$  does not care about other sellers’ trading behavior.
- Equilibrium same as with only one seller and exogenous information.

At  $t = 2$ , buyers update their beliefs about seller  $i$  based on two pieces of info:

- Seller  $i$  rejected trade at  $t = 1$ .
- Aggregate state is  $S$ .

# Fictitious economy

## Lemma

*The unique equilibrium of the fictitious economy involves zero probability of trade in the first period (i.e.,  $\sigma_i = 0$ ) if and only if*

$$Q_L^{i,\text{fict}}|_{\sigma_i=0} \geq v_L, \quad (*)$$

*which holds if and only if  $\lambda$  and  $\delta$  satisfy the following:*

$$\lambda \geq \bar{\lambda} \equiv 1 - \frac{\pi(1 - \bar{\pi})}{1 - \pi}$$

*and*

$$\delta \geq \bar{\delta}_\lambda \equiv \frac{v_L - c_L}{\lambda v_L + (1 - \lambda) V \left( 1 - \frac{(1 - \lambda)(1 - \pi)}{\pi} \right) - c_L}.$$

# Main results on information aggregation

## Theorem 1 (Aggregation Properties)

- (i) If  $(\star)$  holds strictly, then information aggregation fails along any sequence of equilibria.
- (ii) If  $(\star)$  does not hold, then there exists a sequence of equilibria along which information aggregates.

Intuition for failure of aggregation:

- Under aggregation,  $Q_L^i$  converges to  $Q_L^{i,fict}$ . But if  $Q_L^{i,fict} > v_L$ , trade must collapse to zero for large but finite  $N$ , a contradiction.
- In non-aggregating eqm,  $\sigma_N$  declines to zero at rate  $N^{-1}$ , and the distribution of trades in state  $s$  converges to Poisson with mean  $\sigma_N \cdot N \cdot \mathbb{P}(\theta_i = L | S = s)$ .

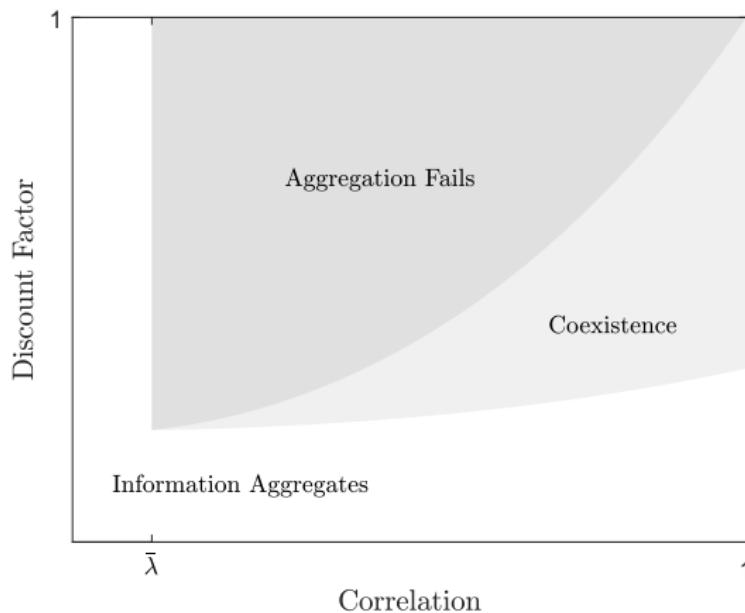
**But**, even if  $(\star)$  does not hold, there is no guarantee of information aggregation...

# Main results on information aggregation

## Theorem 2 (Coexistence)

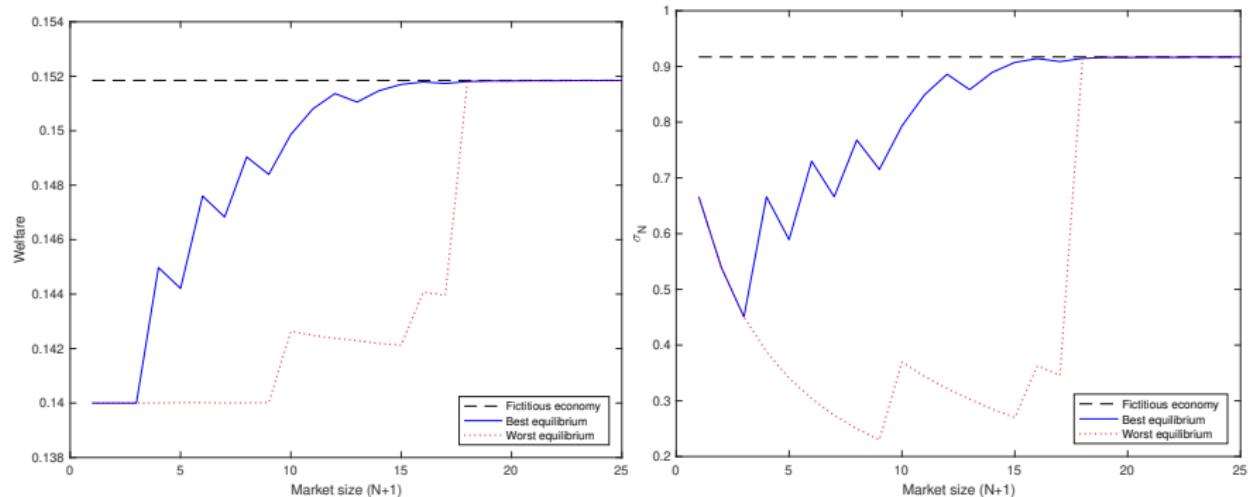
*There exists a  $\hat{\delta} < 1$  such that whenever  $\delta \in (\hat{\delta}, \bar{\delta}_\lambda)$  and  $\lambda$  is sufficiently large, there is coexistence of sequences of equilibria along which information aggregates with sequences of equilibria along which aggregation fails. If  $\lambda < \bar{\lambda}$  or  $\delta$  is sufficiently small, then information aggregates along all sequences of equilibria.*

# Main result 1: when does information aggregate?

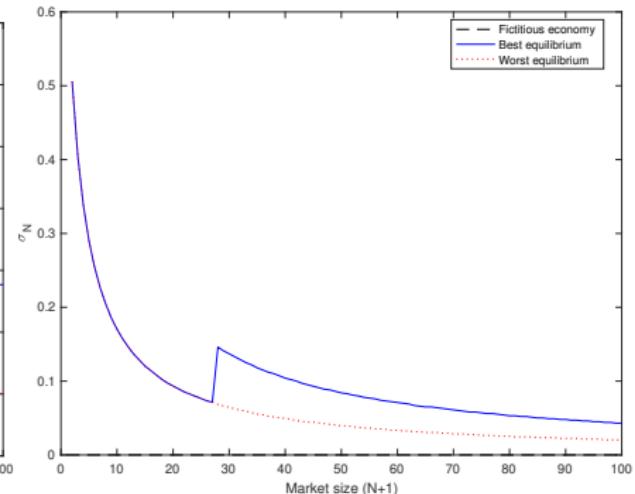
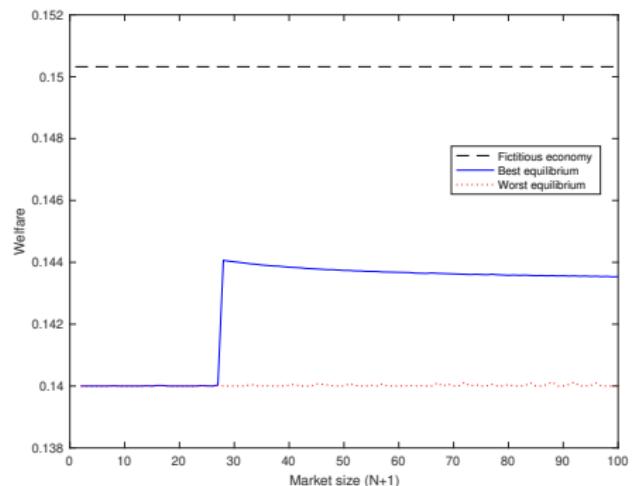


Option value effect too strong in *dark-shaded* region, but too weak in *unshaded* region; its strength is endogenous to equilibrium played in *light-shaded* region.

# Welfare and trade when information aggregates



# Welfare and trade when information does not aggregate



# Trading behavior and welfare

When information **aggregates**:

- Equilibrium becomes the same as fictitious economy,
- Strategic interactions among sellers vanish,
- Conditional on  $S$ , uncertainty about trading volume and prices vanishes.

When information **fails to aggregate**:

- Equilibrium different from fictitious economy:
  - # of trades | state  $S \sim \text{Poisson}$  with parameter  $\sigma_N N \mathbb{P}(\theta^i = L|S)$ .
  - Welfare strictly lower than in fictitious economy.
- Strategic interactions **remain**,
- Conditional on  $S$ , uncertainty about trading volume and prices **remains**.

**Question:** Is info production in the laissez-faire equilibrium efficient?

## Simple information policies

Consider a social planner who can control what information and when it is available to agents.

Can she ensure that information aggregates? If so, how? Does she face a tradeoff between aggregation and maximization of trading surplus?

### Reporting lags:

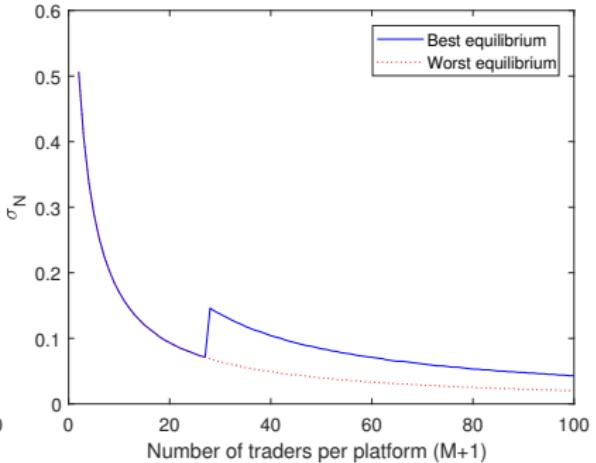
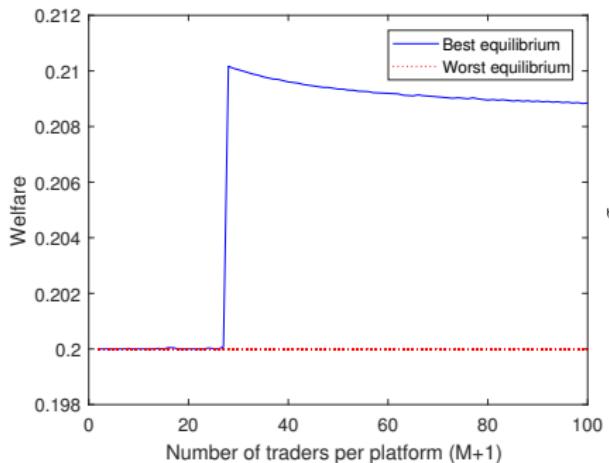
- Traders for one asset observe information about other trades with delay.
- Sufficiently long reporting lag reduces incentives to delay trade and ensures that information aggregates (albeit, with delay).
- **But**, a uniform reporting lag alone yields low trading surplus as it does not allow information to mitigate the adverse selection problem.

### Segmented platforms:

- Traders observe information in real time only on their platform.
- Size of the platform can be chosen to ensure that reporting lags are not detrimental for welfare, and it may be finite.

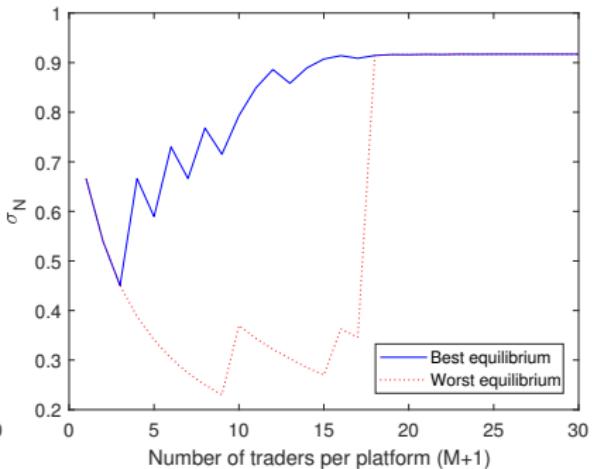
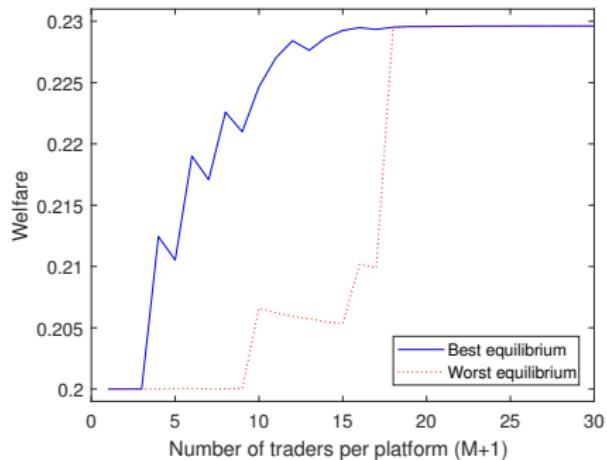
# Segmented platforms

Welfare and trade when (absent intervention) information does not aggregate



# Segmented platforms

Welfare and trade when (absent intervention) information aggregates

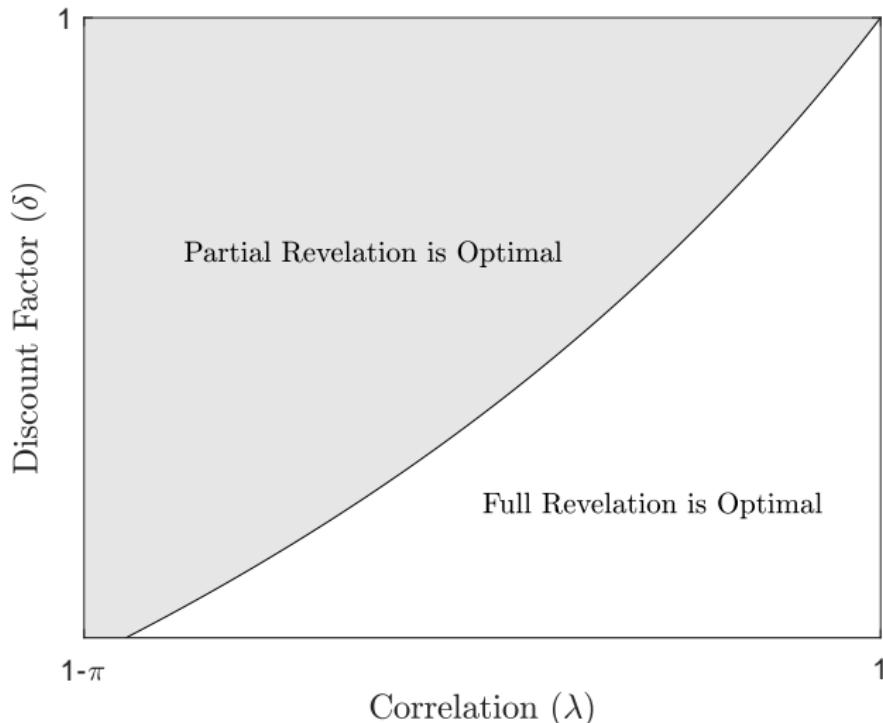


## Optimal information policy

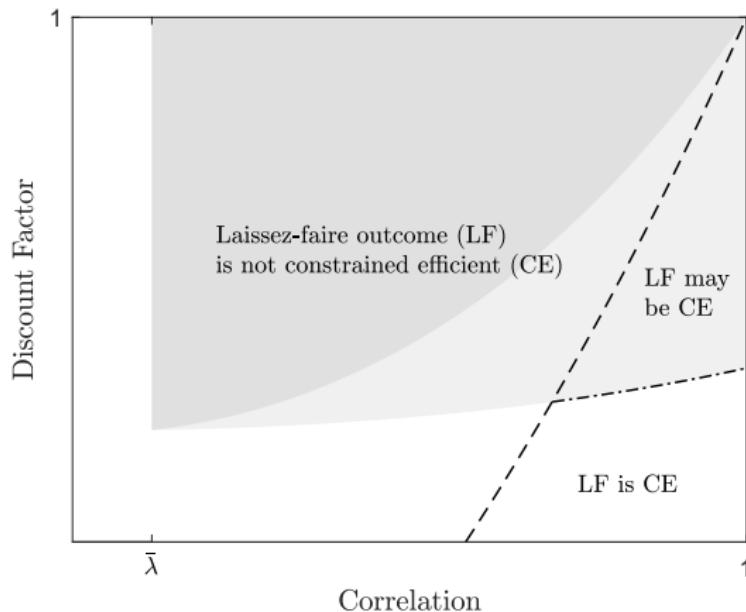
# Optimal information policy

- We suppose that the planner observes trading behavior at  $t = 1$  and chooses what information about it to make public at  $t = 2$ .
  - Application: transparency policies in asset markets.
- Her objective is to maximize expected discounted gains from trade.
- **Novel feedback:** the planner's information policy influences trading behavior and, thus, the information content of whatever she communicates.
  - E.g., she cannot choose an informative policy that implies  $\sigma = 0$ .
- Two-step approach:
  - First, consider problem where planner actually knows state  $S$ , and use it to obtain an upper bound on the planner's value in actual problem.
  - Second, construct an information policy that maps observed trades to "messages," which attains this upper bound as  $N \uparrow \infty$ .

# Graphical illustration

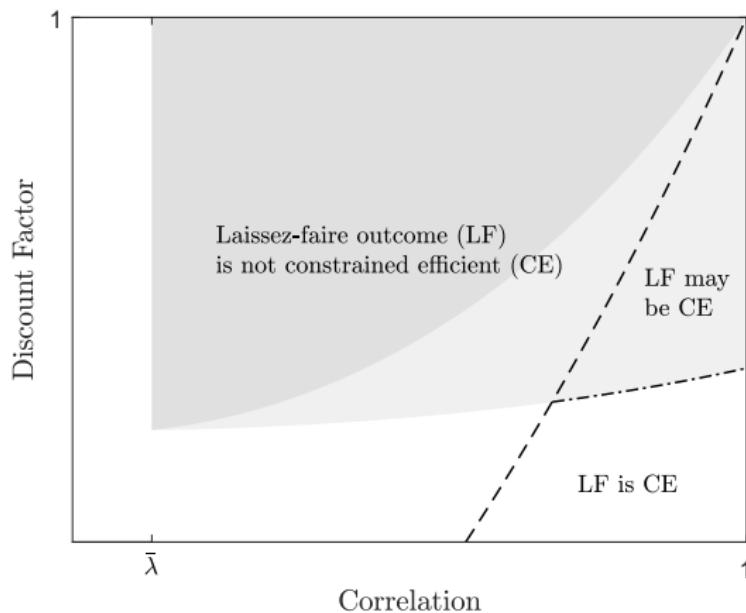


## Main result 2: normative properties



When laissez-faire is inefficient, optimal policy conceals high state w.p.>0 in order to weaken the option value effect and accelerate trade (Pareto optimal).

## Main result 2: normative properties



**Endogenous information constrains policy:** when  $\lambda$  and  $\delta$  are large, the planner would want to reveal the state; but then she would not learn it in the first place!

# Conclusions

We study information aggregation properties of dynamic markets with adverse selection and correlated assets.

- We provide necessary and sufficient conditions, under which information aggregation must fail along any sequence of equilibria (LLN fails!).
- If these conditions are violated, there can be a coexistence of aggregating and non-aggregating equilibria.
- Implications for policies that enhance information dissemination in markets:
  - Information design with endogenous information.
  - Reporting lags + segmented trading platforms.
  - Information design: optimality of partial revelation.