

Homework 3

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Due 2/21/2018

Question 1

```
library(lpSolve)

## Problem 1
# Original Setup
c = c(-1,4)
A = matrix(c(-10,5,1,20,10,0),3,2)
dir = rep('<=',3)
b = c(22,49,5)

sol = lp("max",c,A,dir,b, compute.sens = TRUE)
sol$solution

## [1] 3.8 3.0

sol$objval

## [1] 8.2

# x1 >= 4
A2 = matrix(c(-10,5,1,-1,20,10,0,0),4,2)
dir2 = rep('<=',4)
b2 = c(22,49,5,-4)

sol2 = lp("max",c,A2,dir2,b2, compute.sens = TRUE)
sol2$solution

## [1] 4.0 2.9

sol2$objval

## [1] 7.6

# x1 >= 4, x2 >= 3
A3 = matrix(c(-10,5,1,-1,0,20,10,0,0,-1),5,2)
dir3 = rep('<=',5)
b3 = c(22,49,5,-4, -3)

sol3 = lp("max",c,A3,dir3,b3, compute.sens = TRUE)
sol3$status

## [1] 2

# x1 >= 4, x2 <= 2
A4 = matrix(c(-10,5,1,-1,0,20,10,0,0,1),5,2)
dir4 = rep('<=',5)
b4 = c(22,49,5,-4, 2)
```

```
sol4 = lp("max",c,A4,dir4,b4, compute.sens = TRUE)
sol4$status
```

```
## [1] 0
```

```
sol4$solution
```

```
## [1] 4 2
```

```
sol4$objval
```

```
## [1] 4
```

```
# x1 <= 3
```

```
A5 = matrix(c(-10,5,1,1,20,10,0,0),4,2)
```

```
dir5 = rep('<=',4)
```

```
b5 = c(22,49,5,3)
```

```
sol5 = lp("max",c,A5,dir5,b5, compute.sens = TRUE)
```

```
sol5$solution
```

```
## [1] 3.0 2.6
```

```
sol5$objval
```

```
## [1] 7.4
```

```
# x1 <= 3, x2 >= 3
```

```
A6 = matrix(c(-10,5,1,1,0,20,10,0,0,-1),5,2)
```

```
dir6 = rep('<=',5)
```

```
b6 = c(22,49,5,3,-3)
```

```
sol6 = lp("max",c,A6,dir6,b6, compute.sens = TRUE)
```

```
sol6$status
```

```
## [1] 2
```

```
# x1 <= 3, x2 <= 2
```

```
A7 = matrix(c(-10,5,1,1,0,20,10,0,0,1),5,2)
```

```
dir7 = rep('<=',5)
```

```
b7 = c(22,49,5,3,2)
```

```
sol7 = lp("max",c,A7,dir7,b7, compute.sens = TRUE)
```

```
sol7$solution
```

```
## [1] 1.8 2.0
```

```
sol7$objval
```

```
## [1] 6.2
```

```
# x1 <= 3, x2 <= 2, x1 <= 1
```

```
A8 = matrix(c(-10,5,1,1,0,1,20,10,0,0,1,0),6,2)
```

```
dir8 = rep('<=',6)
```

```
b8 = c(22,49,5,3,2,1)
```

```
sol8 = lp("max",c,A8,dir8,b8, compute.sens = TRUE)
```

```
sol8$solution
```

```
## [1] 1.0 1.6
```

```
sol8$objval
```

```
## [1] 5.4
```

```
#  $x_1 \leq 3$ ,  $x_2 \leq 2$ ,  $x_1 \leq 1$   
A9 = matrix(c(-10,5,1,1,0,-1,20,10,0,0,1,0),6,2)  
dir9 = rep('<=',6)  
b9 = c(22,49,5,3,2,-2)  
  
sol9 = lp("max",c,A9,dir9,b9, compute.sens = TRUE)  
sol9$solution
```

```
## [1] 2 2
```

```
sol9$objval
```

```
## [1] 6
```

```
# Check with int.vec  
c = c(-1,4)  
A = matrix(c(-10,5,1,20,10,0),3,2)  
dir = rep('<=',3)  
b = c(22,49,5)  
  
sol = lp("max",c,A,dir,b, int.vec = 1:2)  
sol$solution
```

```
## [1] 2 2
```

```
sol$objval
```

```
## [1] 6
```

Question 2

```
## Problem 2  
c = c(9,5,6,4)  
A = matrix(0,8,4)  
A[1,] = c(6,3,5,2)  
A[2,] = c(rep(1,4))  
A[3:6,] = diag(1,4)  
A[7,] = c(1,1,0,0)  
A[8,] = c(0,0,1,1)  
dir = c(rep('<=',6),rep('>=',2))  
b = c(11,4,1,1,1,1,1,1)  
  
sol = lp("max",c,A,dir,b, int.vec = 1:4)  
sol$solution
```

```
## [1] 1 1 0 1
```

```
sol$objval
```

```
## [1] 18
```

Question 3

```
## Problem 3
c = rep(1,12)
b = rep(1,12)
dir = rep('>=',12)

A = matrix(0,12,12)
A[1,] = c(1,0,1,0,1,0,1,1,1,0,0,0)
A[2,] = c(0,1,0,0,0,0,0,1,1,0,0,0)
A[3,] = c(1,0,1,0,0,0,1,1,1,0,0,0)
A[4,] = c(0,0,0,1,0,0,0,0,0,1,0,0)
A[5,] = c(1,0,0,0,1,0,1,0,0,0,0,0)
A[6,] = c(0,0,0,0,0,1,0,0,0,1,1,0)
A[7,] = c(1,0,1,0,1,0,1,0,0,0,0,0)
A[8,] = c(1,1,1,0,0,0,0,1,1,0,0,0)
A[9,] = c(1,1,1,0,0,0,0,1,1,0,0,0)
A[10,] = c(0,0,0,1,0,1,0,0,0,1,1,1)
A[11,] = c(0,0,0,0,0,1,0,0,0,1,1,1)
A[12,] = c(0,0,0,0,0,0,0,0,0,1,1,1)

sol = lp("min",c,A,dir,b, int.vec = 1:12)
sol$solution
```

```
## [1] 1 0 0 0 0 0 0 1 0 1 0 0
```

```
sol$objval
```

```
## [1] 3
```

Question 4

```
## Problem 4
c = c(20,9,12,4,16,21,8)
b = c(233,148,106)
dir = c(rep('>=',3))

A = matrix(0,3,7)
A[1,] = c(4,0,0,1,2,1,3)
A[2,] = c(0,3,0,1,0,2,1)
A[3,] = c(0,0,3,1,1,0,0)

sol = lp("min",c,A,dir,b, int.vec = 1:16)
sol$solution
```

```
## [1] 0 0 0 107 0 0 42
```

```
sol$objval
```

```
## [1] 764
```

Question 5

```
## Problem 5
c = c(330,300,330,rep(360,4))
b = c(5,13,12,10,14,8,6)
dir = c(rep('>=',7))

A = matrix(1,7,7)
A[1,2:3] = 0
A[2,3:4] = 0
A[3,4:5] = 0
A[4,5:6] = 0
A[5,6:7] = 0
A[6,] = c(0,1,1,1,1,1,0)
A[7,1:2] = 0

sol = lp("min",c,A,dir,b, int.vec = 1:7)
sol$solution

## [1] 1 8 2 0 3 0 1

sol$objval

## [1] 4830
```