LArTPC Detector Response Calculations Using Boundary Element Method

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Boundary Element Method (BEM) Overview

- 1 Discretize (mesh) boundary electrode surfaces.
- Define (Dirichlet) scalar potential on each mesh element (triangle).
- 3 Fit (Neumann) surface-normal boundary field.
- **4** Integrate Laplace equation $\nabla^2 \phi = 0$, evaluate at boundary.
- **6** Evaluate solution at points in the volume.

Compare BEM and FEM:

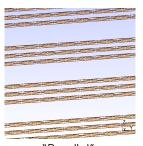
	BEM	FEM
domain:	2D surface mesh	3D volume mesh
easy:	away from surface	near to surface
fits:	boundary-normal field	volumetric field
eval:	arb. volume point	volume mesh points
both:	CPU and memory intensive, limited geometries	
external:	stepping and averaging current responses	

General Calculation Overview

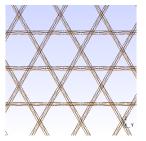
High-level steps:

- Drift fields: $\phi_{\textit{drift}} \to \vec{E}_{\textit{drift}} \to \mu \to \vec{v}_{\textit{drift}} \to \textbf{paths}$: $\{p\}$
 - $\vec{V}_{drift} = \mu(E_{drift})\vec{E}_{drift}(\vec{r}(t))$
 - Get path $\vec{r}_p(t)$ by stepping through velocity field \vec{v}_{drift} .
- Shockley-Ramo "weighting" potential for electrode k
 - $\phi_{\text{weight},k} \to \vec{E}_{\text{weight},k}$
 - Electrode k at 1V, all others at 0V.
- Current on wire k due to charge moving along path p:
 - $i_{k,p}(t) = q\vec{E}_{weight,k} \cdot \vec{V}_{driff}|_{p}$
- **Response function** for wire *k* is average over paths:
 - $< i_k(t) > = \frac{1}{N} \sum_{p=1}^{N} i_{k,p}(t)$
- \rightarrow for now: paths start on 1mm grid, 16mm in front of U-plane,
- → response is average over paths in half-pitch "wire region"

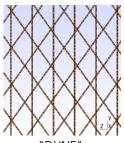
Wire Meshes



"Parallel": 3mm pitch and gap all wires parallel



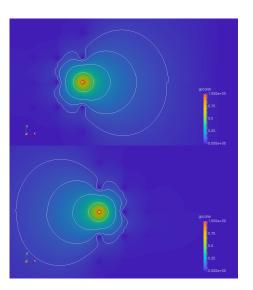
"MicroBooNE": 3mm pitch and gap 60° angles for U/V.

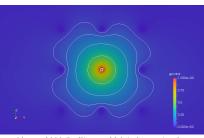


"DUNE": 5mm pitch and gap 35.7° angles for U/V.

- "Parallel" used to reproduce 2D calculations.
- Geometry parameterized to facilitate exploring different configurations.

Parallel Wires - Slice Through Weighting Potentials

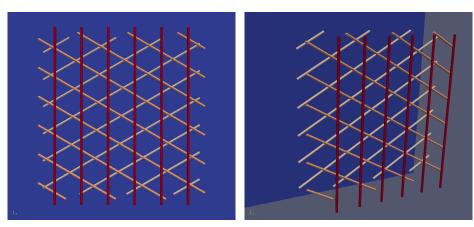




- U and W (left) and V (above) planes.
- X-Z slices through plane of symmetry.
- Lines: 5%, 10%, 20%, 40% weights.
- Initial qualitative agreement with Garfield 2D calculations.
- more exhaustive comparisons needed, but satisfactory enough to push on.

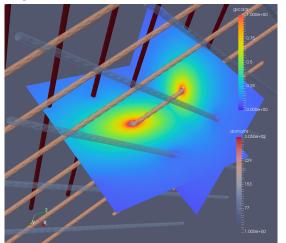
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MicroBooNE Geometry Patch



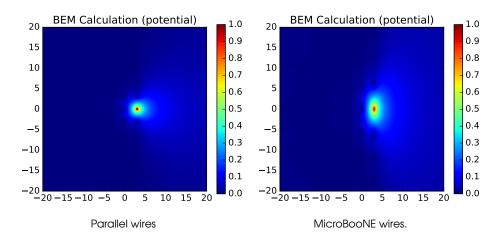
- Wires parameterized by pitch, angle, bounding box, radius.
- Single plane at +20mm for drift potential

V-plane \vec{E}_{weight} Slices



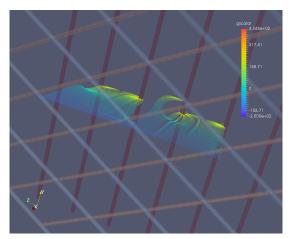
- Slices in X-Z and X-Y planes.
- Note mismatchs between evaluated voxel grid and wire mesh.

Weighting Potential - 2D vs. 3D wire pattern



Clear distortion in extent and shape. Not surprising.

Paraview stepping from line source

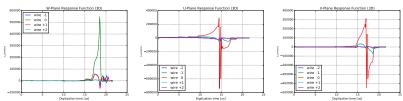


- Line source 2mm in front of U-plane, paths colored by drift potential.
- U-plane transparency violated due to imprecision right near U-wire.

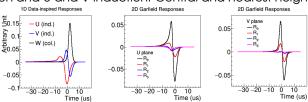
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Initial Response Functions

Preliminary and Subject to Change!



Collection and U and V Induction. Central and nearest neighbor wires.



Data inspired and 2D Garfield calculations.

Known Issues Needing Work

- Improve precision of fields near wires.
 - Voxelization \rightarrow **on-demand sampling** of ϕ_{drift} while stepping
 - Will remove big RAM pig, allow for batch processing.
 - Gives room for finer surface meshing.
- 2 Correct termination of paths.
 - Currently, stepping just knows fields (including interiors of wires!)
 - Must terminate stepping when path "hits" a wire.
- 3 Explore systematics in response function vs path location.
 - Understand spatial variations and properly smooth them.
- 4 Limited transverse coverage
 - Expect to need $\sim \pm 10$ wires (based on data obs.)
 - Problem scales somewhere between $N_{wires} o N_{wires}^2$
- 6 uBoone is "easy first test", next up:
 - DUNE wire crossing pattern
 - APA edge regions

The Software

https://github.com/brettviren/larf

- Expect a name change!
- Ready for other users and developers, welcome!
- Interfaces: simple command line program or Python modules.
- Supports fantastic Paraview visualization app.
- Provides various "management systems": configuration, data storage, result provenance, workflow.
- ightarrow Warning: documentation is trailing code development so let me know if you are interested in using/developing and I'll do some freshening.