



Spring Semester 2023

AIRCRAFT AERODYNAMICS & FLIGHT MECHANICS

20.04.2023

Dr. Marc Immer ALR Aerospace

This lecture is adapted with permission from
the lecture "Ausgewählte Kapitel der
Flugtechnik" by Dr. Jürg Wildi

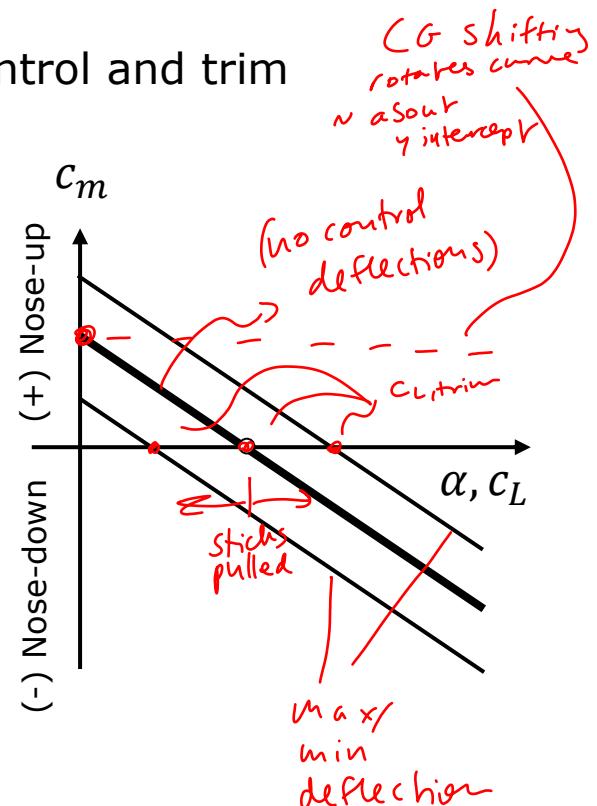
Know the difference between longitudinal stability, control and trim

$$c_{M_{CG}} = c_L \left(\frac{\tilde{x}_{CG} - \tilde{x}_{AC,W}}{l_{ref}} \right) + c_{M_{AC,W}} + c_{M_F} - c_{L_{\alpha,H}} \eta_H V_H(\alpha_H)$$

short form

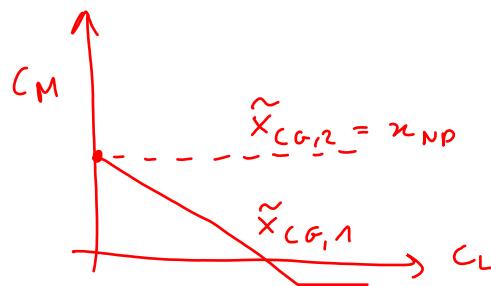
$$\frac{dc_{M_{CG}}}{dc_L} = \frac{\tilde{x}_{CG} - \tilde{x}_{AC,W}}{l_{ref}} + \frac{dc_{M_F}}{dc_L} - \frac{c_{L_{\alpha,H}}}{c_{L_{\alpha,W}}} \eta_H V_H \left(1 - \frac{d\varepsilon}{d\alpha} \right)$$

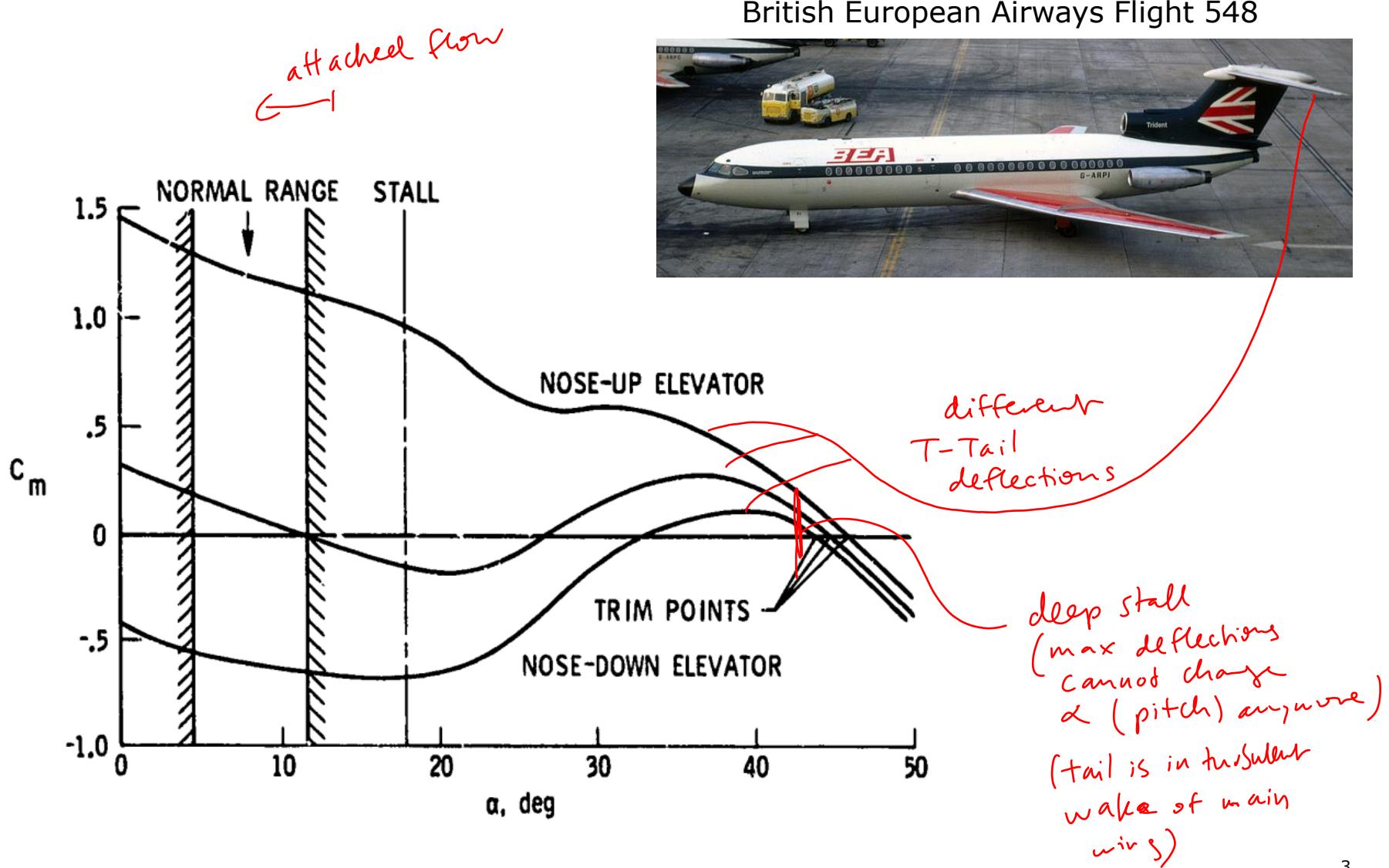
expanded in long form



NP: Neutral point – aerodynamic center of the aircraft

$$\frac{dc_M}{dc_L} = \frac{\tilde{x}_{CG} - \tilde{x}_{NP}}{l_{ref}}$$



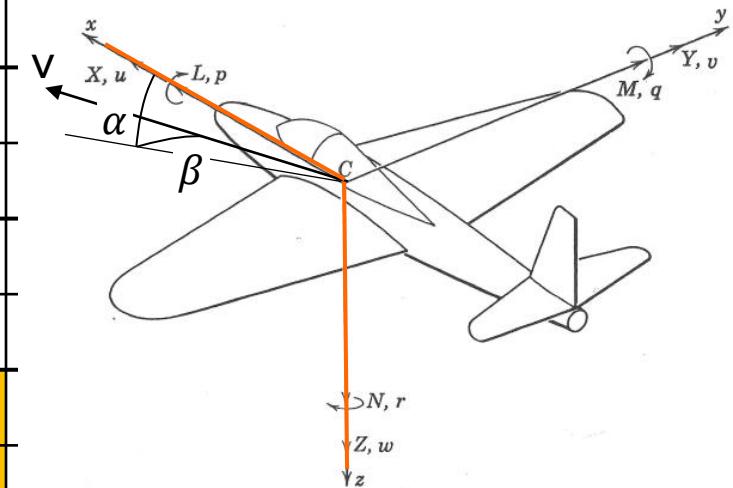
Deep Stall

Static Stability

Disturbance		Velocity			Incidence Angles		Angular Velocity		
Forces/Moments		u	v	w	$\beta = v / V$	$\alpha = w / V$	p	q	r
X-Force	$F_{A_x} + F_{T_x}$	$\frac{\partial}{\partial u}(F_{A_x} + F_{T_x}) < 0$							
		$c_{T_{xu}} - c_{D_u} < 0$							
Y-Force	$F_{A_y} + F_{T_y}$		$\frac{\partial}{\partial v}(F_{A_y} + F_{T_y}) < 0$				what we looked at		
			$c_{y\beta} < 0$						
Z-Force	$F_{A_z} + F_{T_z}$			$\frac{\partial}{\partial w}(F_{A_z} + F_{T_z}) < 0$					
				$c_{L\alpha} > 0$					
Roll-Moment	$L_A + L_T$				$\frac{\partial}{\partial \beta}(L_A + L_T) < 0$		$\frac{\partial}{\partial p}(L_A + L_T) < 0$		
					$c_{l\beta} < 0$		$c_{lp} < 0$		
Pitch-Moment	$M_A + M_T$	$\frac{\partial}{\partial u}(M_A + M_T) > 0$			$\frac{\partial}{\partial \alpha}(M_A + M_T) < 0$		$\frac{\partial}{\partial q}(M_A + M_T) < 0$		
		$c_{m_u} > 0$			$c_{m\alpha} < 0$		$c_{mq} < 0$		
Yaw-Moment	$N_A + N_T$				$\frac{\partial}{\partial \beta}(N_A + N_T) > 0$			$\frac{\partial}{\partial r}(N_A + N_T) < 0$	
					$c_{n\beta} > 0$				$c_{nr} < 0$

Directional and Lateral Static Stability

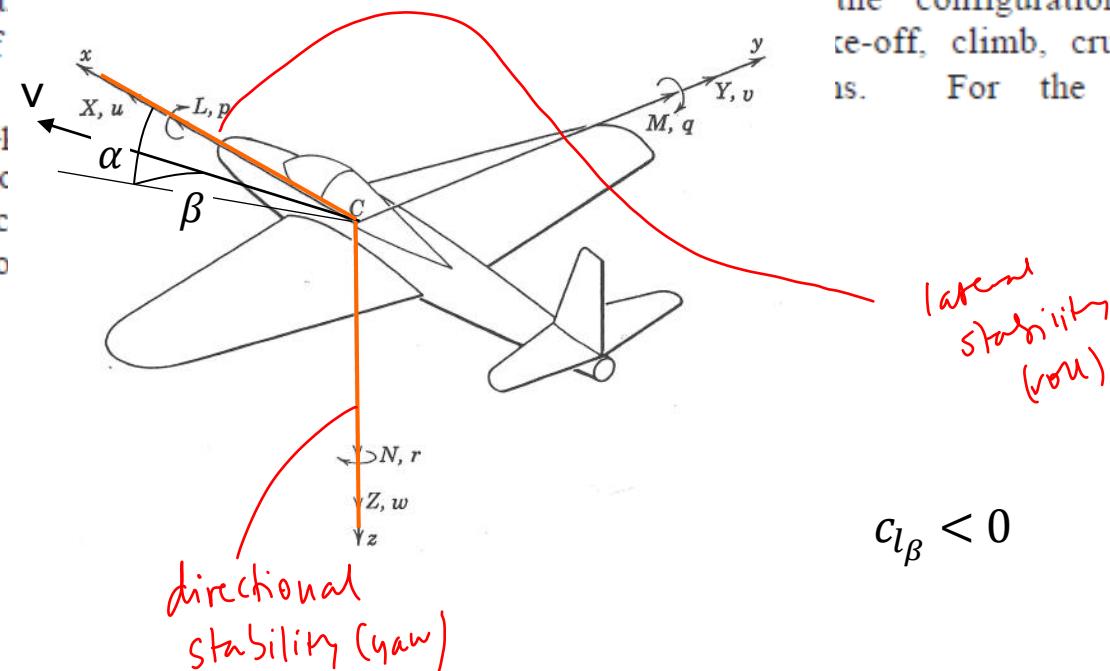
Disturbance		Velocity			Incidence Angles		Angular Velocity		
Forces/Moments		u	v	w	$\beta = v / V$	$\alpha = w / V$	p	q	r
X-Force	$F_{A_x} + F_{T_x}$	$\frac{\partial}{\partial u}(F_{A_x} + F_{T_x}) < 0$							
		$c_{T_{xu}} - c_{D_u} < 0$							
Y-Force	$F_{A_y} + F_{T_y}$		$\frac{\partial}{\partial v}(F_{A_y} + F_{T_y}) < 0$						
			$c_{y\beta} < 0$						
Z-Force	$F_{A_z} + F_{T_z}$			$\frac{\partial}{\partial w}(F_{A_z} + F_{T_z}) < 0$					
				$c_{L_\alpha} > 0$					
Roll-Moment	$L_A + L_T$				$\frac{\partial}{\partial \beta}(L_A + L_T) < 0$				
					$c_{l_\beta} < 0$				
Pitch-Moment	$M_A + M_T$	$\frac{\partial}{\partial u}(M_A + M_T) > 0$			$\frac{\partial}{\partial \alpha}(M_A + M_T) < 0$		$\frac{\partial}{\partial q}(M_A + M_T) < 0$		
		$c_{m_u} > 0$			$c_{m_\alpha} < 0$		$c_{m_q} < 0$		
Yaw-Moment	$N_A + N_T$				$\frac{\partial}{\partial \beta}(N_A + N_T) > 0$			$\frac{\partial}{\partial r}(N_A + N_T) < 0$	
					$c_{n_\beta} > 0$			$c_{n_r} < 0$	



CS 23.177 Static directional and lateral stability

(a) The static directional stability, as shown by the tendency to recover from a wings level sideslip with the rudder free, must be positive for any landing gear and flap position appropriate to the take-off, climb, cruise, approach and landing configurations. This must be shown with symmetrical power up to maximum continuous power and at speeds from 1·2 VS1 up to maximum allowable speed for the configuration being investigated. The angle of attack must be appropriate to the larger angles of sideslip unless a rudder is used or a configuration factor CS 23.143 is reached, which at speeds from 1·2 VS1 to maximum allowable speed the force must not reverse.

$$c_{n\beta} > 0$$

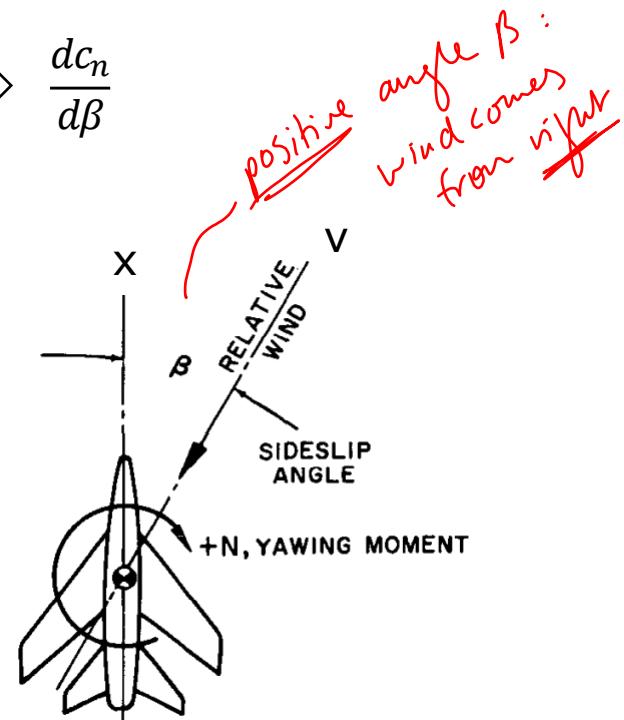
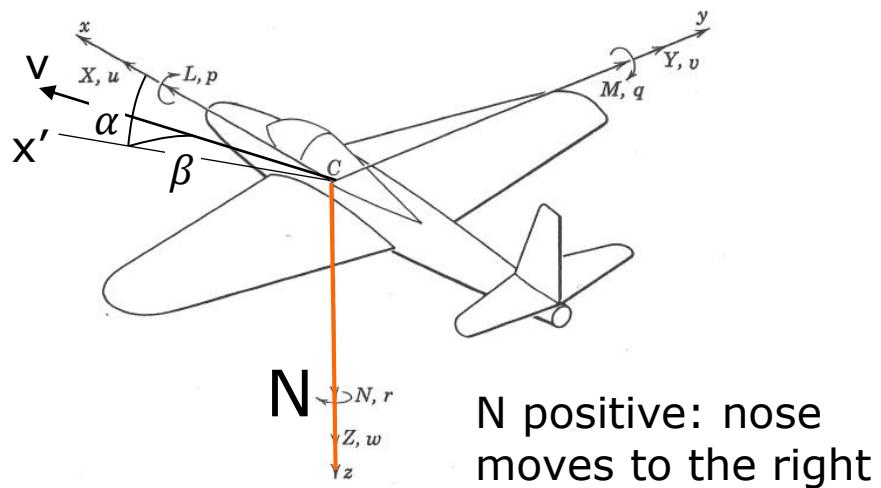


$$c_{l\beta} < 0$$

Directional Static Stability

A disturbance causes a sideslip angle β .
The airplane reacts with a yawing moment

$$\rightarrow \frac{dc_n}{d\beta}$$



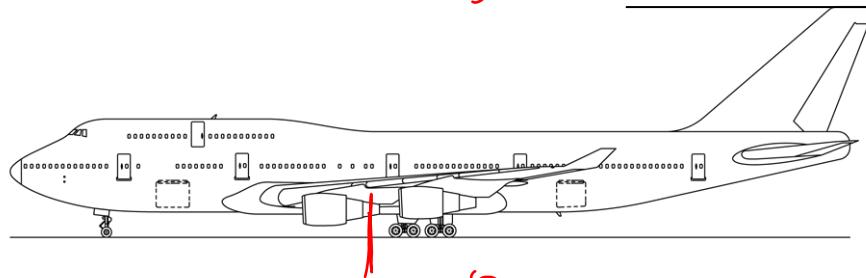
Positive directional static stability:

A positive sideslip angle results in a positive yawing moment

$$c_{n\beta} = \frac{dc_n}{d\beta} > 0$$

VTP – Vertical Tail Plane

Boeing 747-400

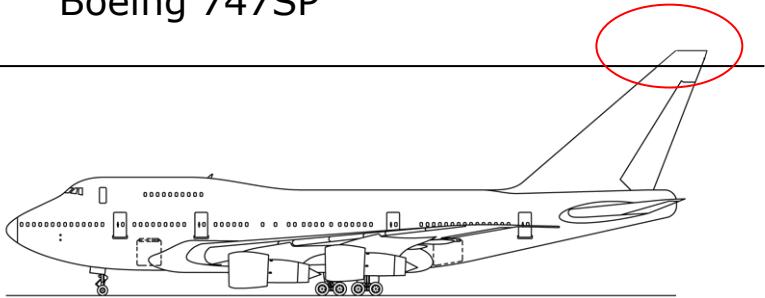


CG close to
main landing gear

very large tail as
we also need to maintain
stability/control if
critical (outboard) engine
fails on one side
(yaw disturbance)

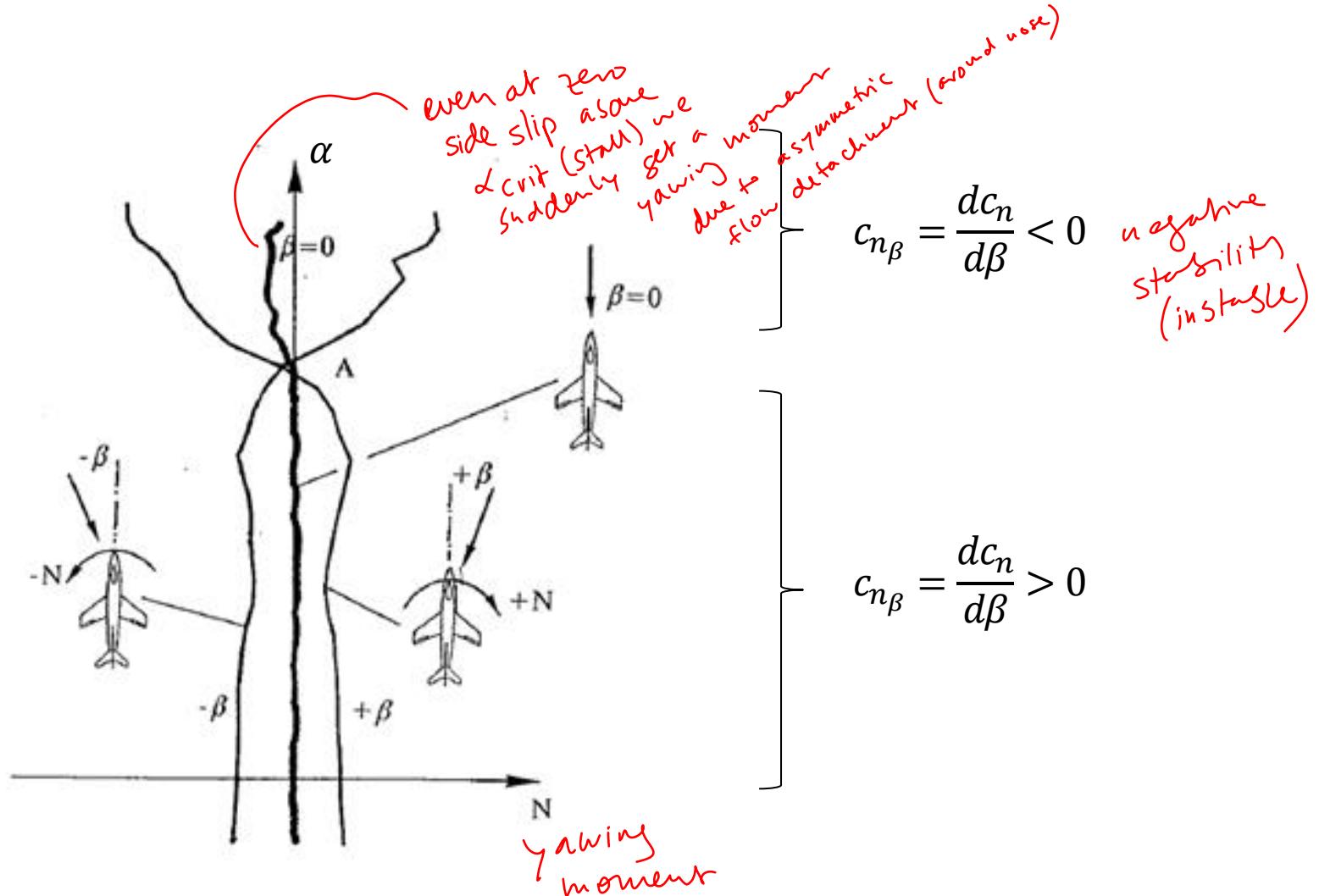


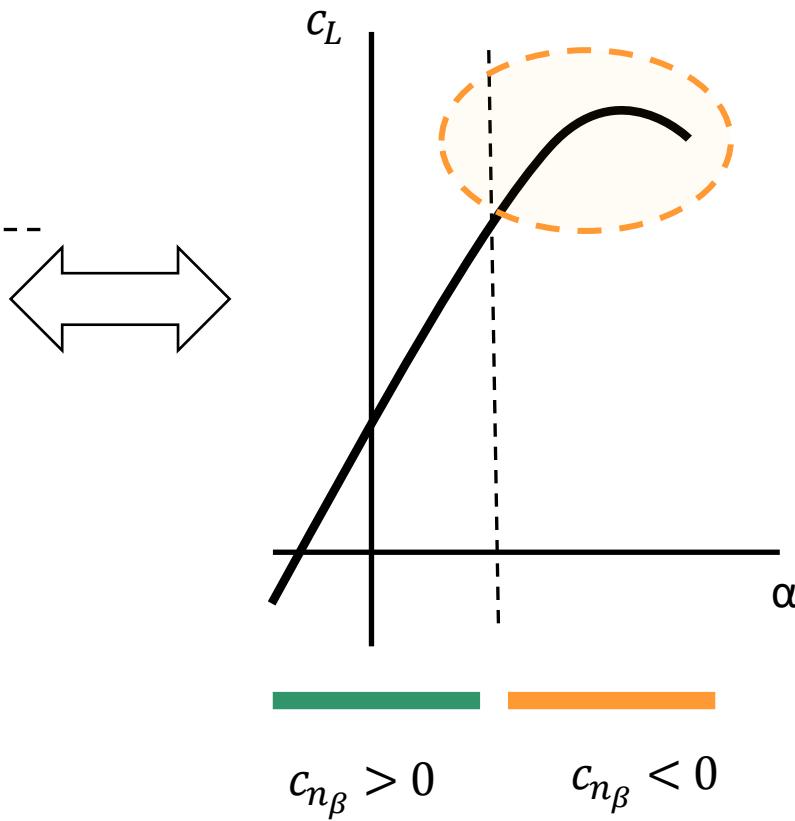
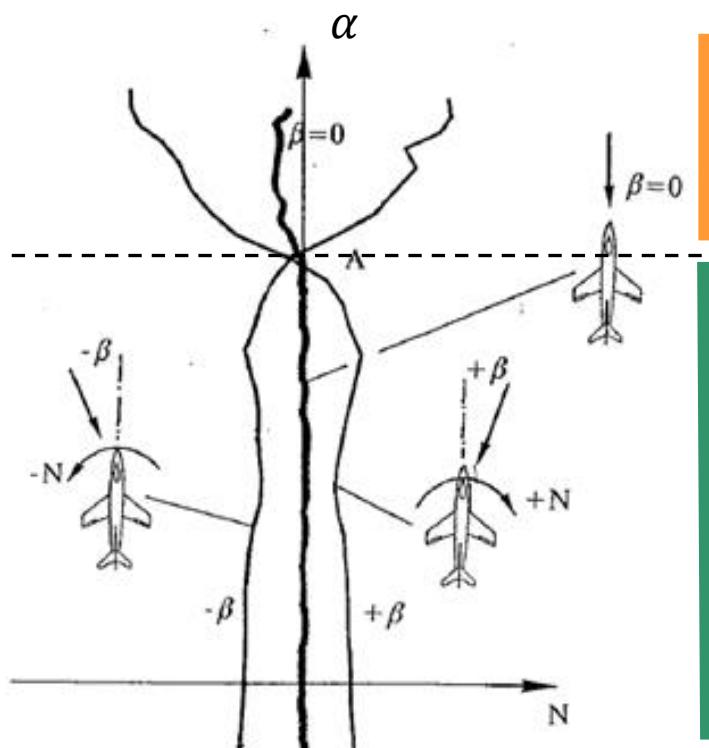
Boeing 747SP



Nose Strake

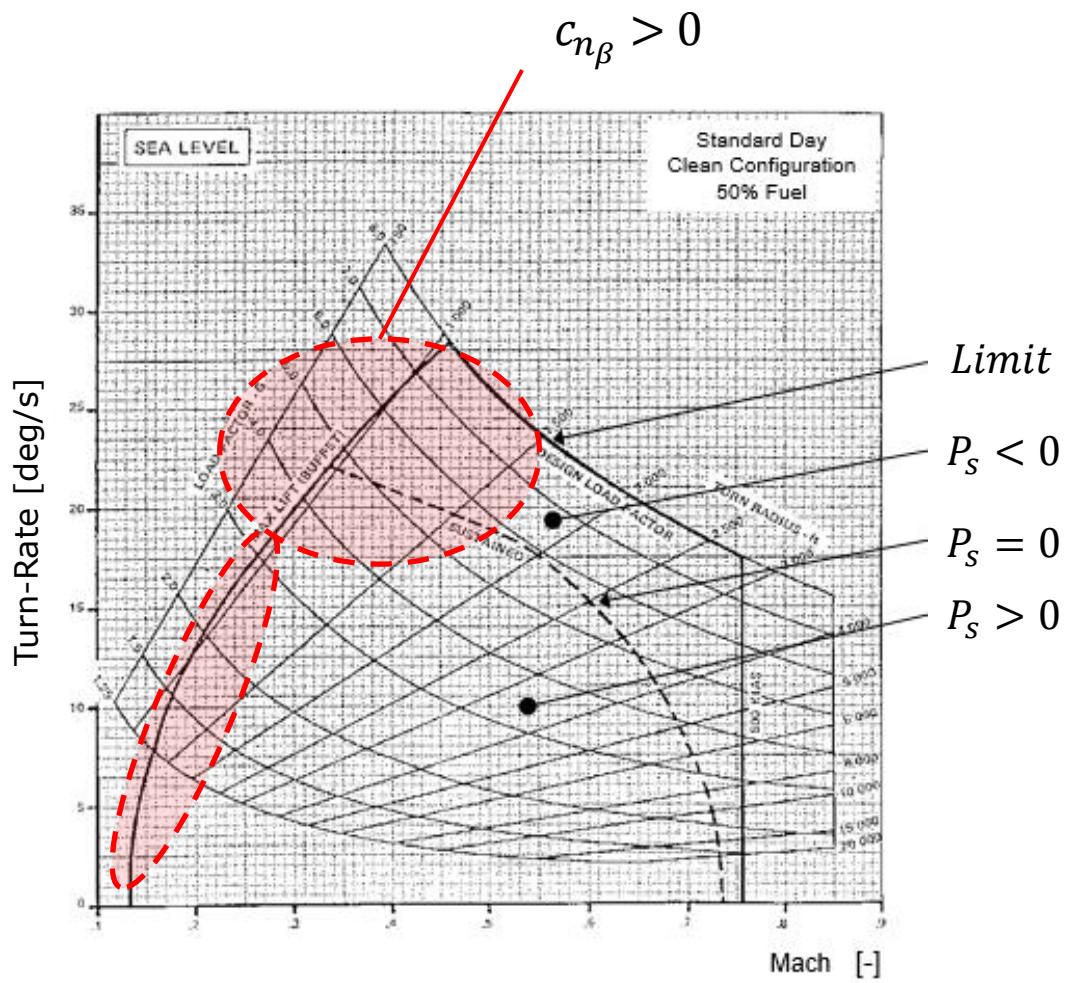
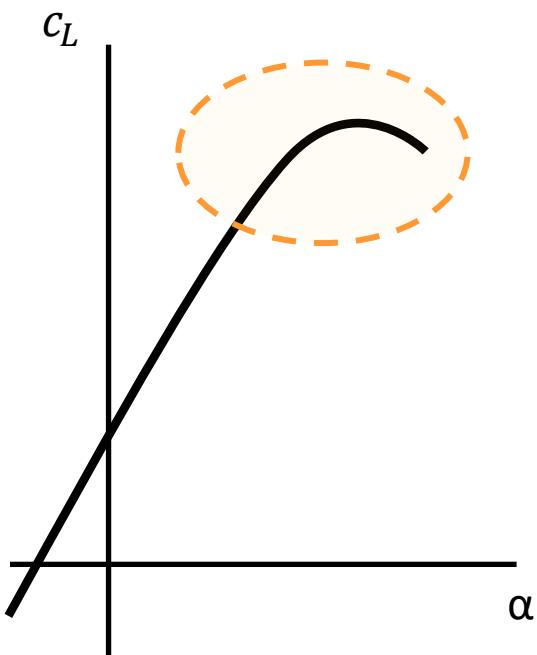




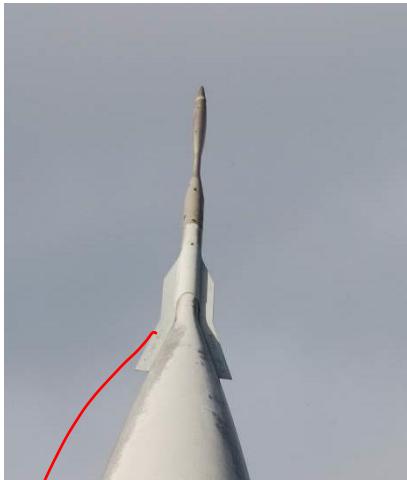


$$c_{n\beta} > 0$$

$$c_{n\beta} < 0$$



Directional Static Stability – Nose Strakes



nose strakes
force symmetric
flow detachment



fuselage
is destabilizing



nose strakes
allows higher AoA/C_l
until we get asym. flow
detachment (yaw disturbance)



Northrop F-5A

very small disturbances
at front of aircraft have
big effect, especially
directional static stability (raw)



Northrop F-5E



Lateral Static Stability

most important

Disturbance		Velocity			Incidence Angles		Angular Velocity		
Forces/Moments		u	v	w	$\beta = v / V$	$\alpha = w / V$	p	q	r
X-Force	$F_{A_x} + F_{T_x}$	$\frac{\partial}{\partial u} (F_{A_x} + F_{T_x}) < 0$							
		$c_{T_x u} - c_{D_u} < 0$							
Y-Force	$F_{A_y} + F_{T_y}$		$\frac{\partial}{\partial v} (F_{A_y} + F_{T_y}) < 0$						
			$c_{y\beta} < 0$						
Z-Force	$F_{A_z} + F_{T_z}$			$\frac{\partial}{\partial w} (F_{A_z} + F_{T_z}) < 0$					
				$c_{L\alpha} > 0$					
Roll-Moment	$L_A + L_T$				$\frac{\partial}{\partial \beta} (L_A + L_T) < 0$		$\frac{\partial}{\partial p} (L_A + L_T) < 0$		
					$c_{l\beta} < 0$		$c_{l_p} < 0$		
Pitch-Moment	$M_A + M_T$	$\frac{\partial}{\partial u} (M_A + M_T) > 0$			$\frac{\partial}{\partial \alpha} (M_A + M_T) < 0$		$\frac{\partial}{\partial q} (M_A + M_T) < 0$		
		$c_{m_u} > 0$			$c_{m_\alpha} < 0$		$c_{m_q} < 0$		
Yaw-Moment	$N_A + N_T$				$\frac{\partial}{\partial \beta} (N_A + N_T) > 0$			$\frac{\partial}{\partial r} (N_A + N_T) < 0$	
					$c_{n_\beta} > 0$				$c_{n_r} < 0$

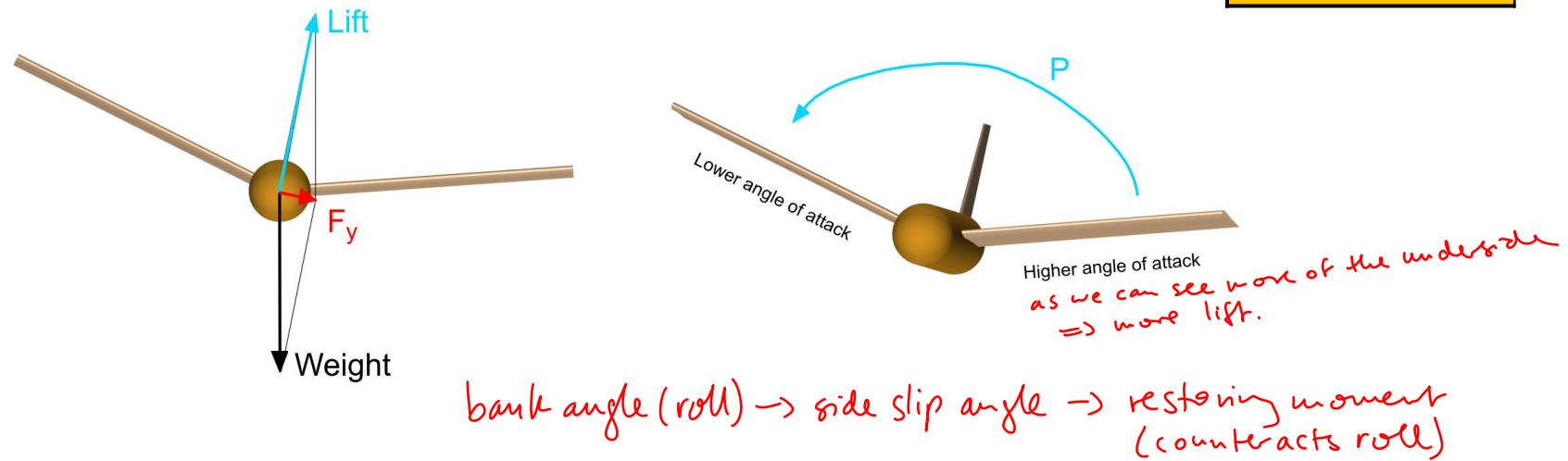
Lateral Stability - Dihedral Effect

There is no “pure” lateral (rolling) static stability derivative.

A disturbance in the roll angle results in side-force and therefore in a sideslip angle β

$$\frac{\partial}{\partial \beta} (L_A + L_T) < 0$$

$$c_{l\beta} < 0$$



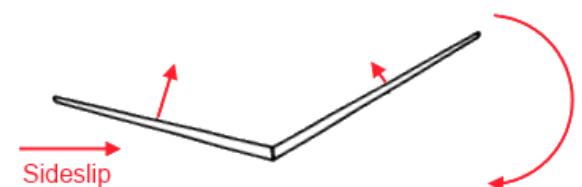
A sideslip angle β should result in a restoring rolling moment

$$c_{l\beta} < 0$$

wing dihedral : geometry
dihedral effect : lateral stability derivative

This **stability** can be provided by having a **dihedral angle** (V-shape of the wing) and/or wing sweep.

neg. dihedral angle : anhedral (inverted V)



Speed Stability

Aerodynamics & Flight Mechanics

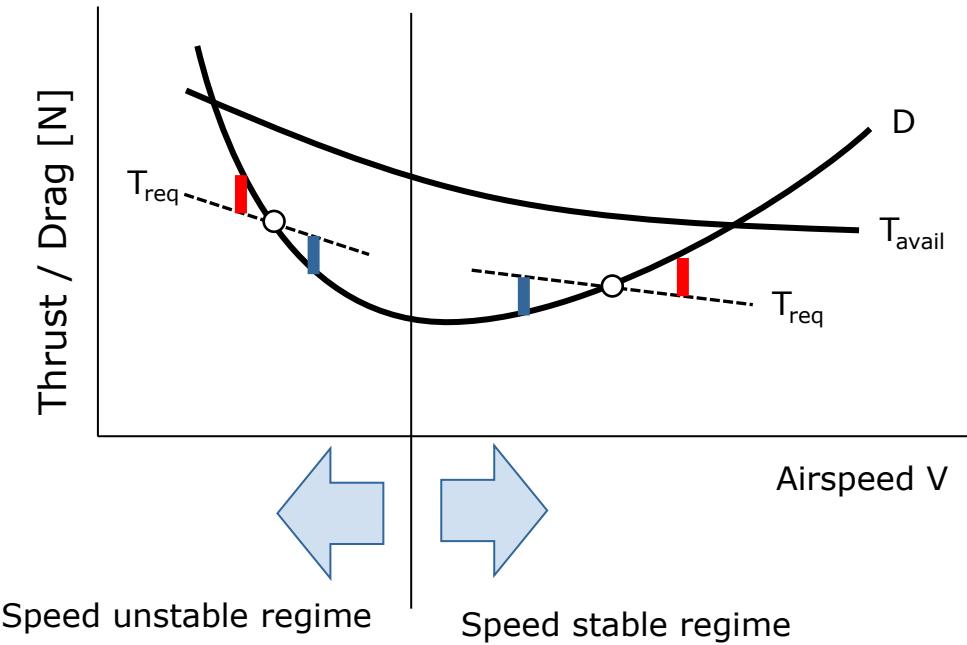
Stability & Control

Disturbance		Velocity			Incidence Angles		Angular Velocity		
Forces/Moments		u	v	w	$\beta = v / V$	$\alpha = w / V$	p	q	r
X-Force	$F_{A_x} + F_{T_x}$	$\frac{\partial}{\partial u}(F_{A_x} + F_{T_x}) < 0$							
		$c_{T_{xu}} - c_{D_u} < 0$							
Y-Force	$F_{A_y} + F_{T_y}$		$\frac{\partial}{\partial v}(F_{A_y} + F_{T_y}) < 0$						
			$c_{y\beta} < 0$						
Z-Force	$F_{A_z} + F_{T_z}$			$\frac{\partial}{\partial w}(F_{A_z} + F_{T_z}) < 0$					
				$c_{L_\alpha} > 0$					
Roll-Moment	$L_A + L_T$				$\frac{\partial}{\partial \beta}(L_A + L_T) < 0$		$\frac{\partial}{\partial p}(L_A + L_T) < 0$		
					$c_{l_\beta} < 0$		$c_{l_p} < 0$		
Pitch-Moment	$M_A + M_T$	$\frac{\partial}{\partial u}(M_A + M_T) > 0$			$\frac{\partial}{\partial \alpha}(M_A + M_T) < 0$		$\frac{\partial}{\partial q}(M_A + M_T) < 0$		
		$c_{m_u} > 0$			$c_{m_\alpha} < 0$		$c_{m_q} < 0$		
Yaw-Moment	$N_A + N_T$				$\frac{\partial}{\partial \beta}(N_A + N_T) > 0$			$\frac{\partial}{\partial r}(N_A + N_T) < 0$	
					$c_{n_\beta} > 0$			$c_{n_r} < 0$	

An increase in forward velocity u should result in a deceleration

$$\frac{\partial}{\partial u} (F_{Ax} + F_{Tx}) < 0$$

$$c_{Txu} - c_{D_u} < 0$$



$$\frac{d \text{ (axial force (drag, thrust))}}{d V}$$

we cannot neglect thrust!

Speed stability (u) is not required. An instability is manageable by the pilot

A sidewise velocity disturbance should result in an opposing sidewise aerodynamic force

$$\nu = \beta V$$

$$\frac{\partial}{\partial \nu} (F_{A_y} + F_{T_y}) < 0$$

$$c_{y\beta} < 0$$

Can be of importance in uncoordinated turn

A vertical velocity disturbance should result in an opposing vertical aerodynamic force.

Note: positive z-direction is downwards

$$\frac{\partial}{\partial w} (F_{Az} + F_{Tz}) < 0$$

$$c_{L\alpha} > 0$$

$$w = \alpha V$$

$$c_{L\alpha} = \frac{dc_L}{d\alpha} > 0$$

Note: positive lift is upwards (in negative z direction)

$c_{L\alpha}$ is usually positive within the normal flight regime ($c_L < c_{L_{max}}$)

Relates to the gust load factor and the damping of the short period mode

An increase in forward velocity u should result in a pitch-up moment. This increases the angle of attack (lift coefficient), causing a higher drag, resulting in a deceleration

$$\frac{\partial}{\partial u} (M_A + M_T) > 0$$

$$c_{m_u} > 0$$

$$c_{m_u} > 0$$

This stability condition relates to longitudinal static stability and becomes important in the transonic flight regime (around Mach 1)

→ "Mach-tuck / tuck under"
 center of pressure moves aft
 @ around Mach 1 (transonic)

Disturbance		Velocity			Incidence Angles		Angular Velocity		
Forces/Moments		u	v	w	$\beta = v / V$	$\alpha = w / V$	p	q	r
X-Force	$F_{A_x} + F_{T_x}$	$\frac{\partial}{\partial u}(F_{A_x} + F_{T_x}) < 0$							
		$c_{T_{xu}} - c_{D_u} < 0$							
Y-Force	$F_{A_y} + F_{T_y}$		$\frac{\partial}{\partial v}(F_{A_y} + F_{T_y}) < 0$						
			$c_{y\beta} < 0$						
Z-Force	$F_{A_z} + F_{T_z}$			$\frac{\partial}{\partial w}(F_{A_z} + F_{T_z}) < 0$					
				$c_{L_\alpha} > 0$					
Roll-Moment	$L_A + L_T$				$\frac{\partial}{\partial \beta}(L_A + L_T) < 0$		$\frac{\partial}{\partial p}(L_A + L_T) < 0$		
					$c_{l_\beta} < 0$		$c_{l_p} < 0$		
Pitch-Moment	$M_A + M_T$	$\frac{\partial}{\partial u}(M_A + M_T) > 0$			$\frac{\partial}{\partial \alpha}(M_A + M_T) < 0$		$\frac{\partial}{\partial q}(M_A + M_T) < 0$		
		$c_{m_u} > 0$			$c_{m_\alpha} < 0$		$c_{m_q} < 0$		
Yaw-Moment	$N_A + N_T$				$\frac{\partial}{\partial \beta}(N_A + N_T) > 0$			$\frac{\partial}{\partial r}(N_A + N_T) < 0$	
					$c_{n_\beta} > 0$				$c_{n_r} < 0$

The increase of the roll-rate p should result in an opposing rolling moment L

$$c_{l_p} < 0$$

$$\frac{\partial}{\partial p} (L_A + L_T) < 0$$

$$c_{l_p} < 0$$

Note: rolling rate gets damped, the roll angle itself does not $\rightarrow 0$

Important in dynamic maneuvers. For rigid airplanes and flight conditions without major regions of separated flow (stall), this stability condition is usually fulfilled.

The increase of the pitch-rate q should result in an opposing pitching moment M

$$\frac{\partial}{\partial q} (M_A + M_T) < 0$$

$$c_{m_q} < 0$$

$$c_{m_q} < 0$$

This is also called the **pitch damping derivative**.

This stability condition is usually required and generally fulfilled by conventional aircraft configurations

→ PIO : pilot induced oscillations → e.s.
F22 raptor crash

The increase of the yaw-rate r should result in an opposing yawing moment N

$$c_{n_r} < 0$$

$$\frac{\partial}{\partial r} (N_A + N_T) < 0$$

$$c_{n_r} < 0$$

Relates to the yaw damping and the so called “Dutch-Roll”. This stability condition usually needs to be fulfilled and is provided by the vertical tail.



20.03.2014: Dassault Neuron, Falcon F7X, Rafale

Example: Loss of Primary Controls

Baghdad, 22. Nov. 2003. A DHL Airbus A300F was hit by a surface-to-air missile on the left wing during climb.



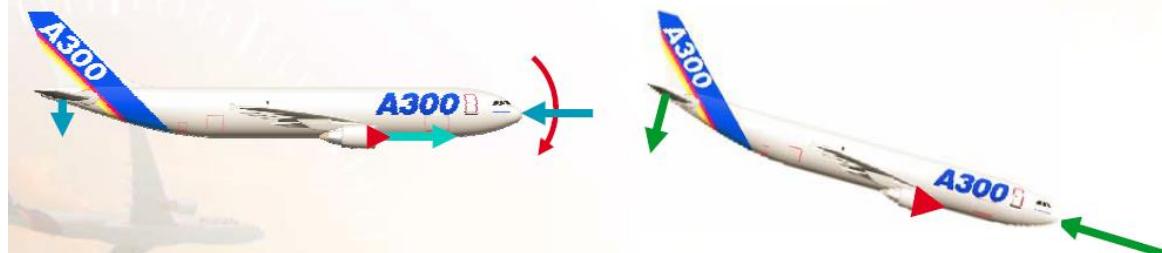
https://en.wikipedia.org/wiki/2003_Baghdad_DHL_attempted_shootdown_incident



Loss of all hydraulics (primary control surfaces)

- All hydraulics lost
 - Ailerons, rudder and elevators are « floating » in the wind (zero hinge moment)
 - THS is frozen
 - Spoilers are inoperative and prevented to deflect (sucked by the airflow) by a non return valve. But one of them is slightly leaking.
 - Slats and flaps configuration are retracted and frozen
- Left wing in fire and associated fuel tank is emptying
- A significative amount of the left wing surface is missing
- **BUT:**
BOTH ENGINES ARE STILL RUNNING

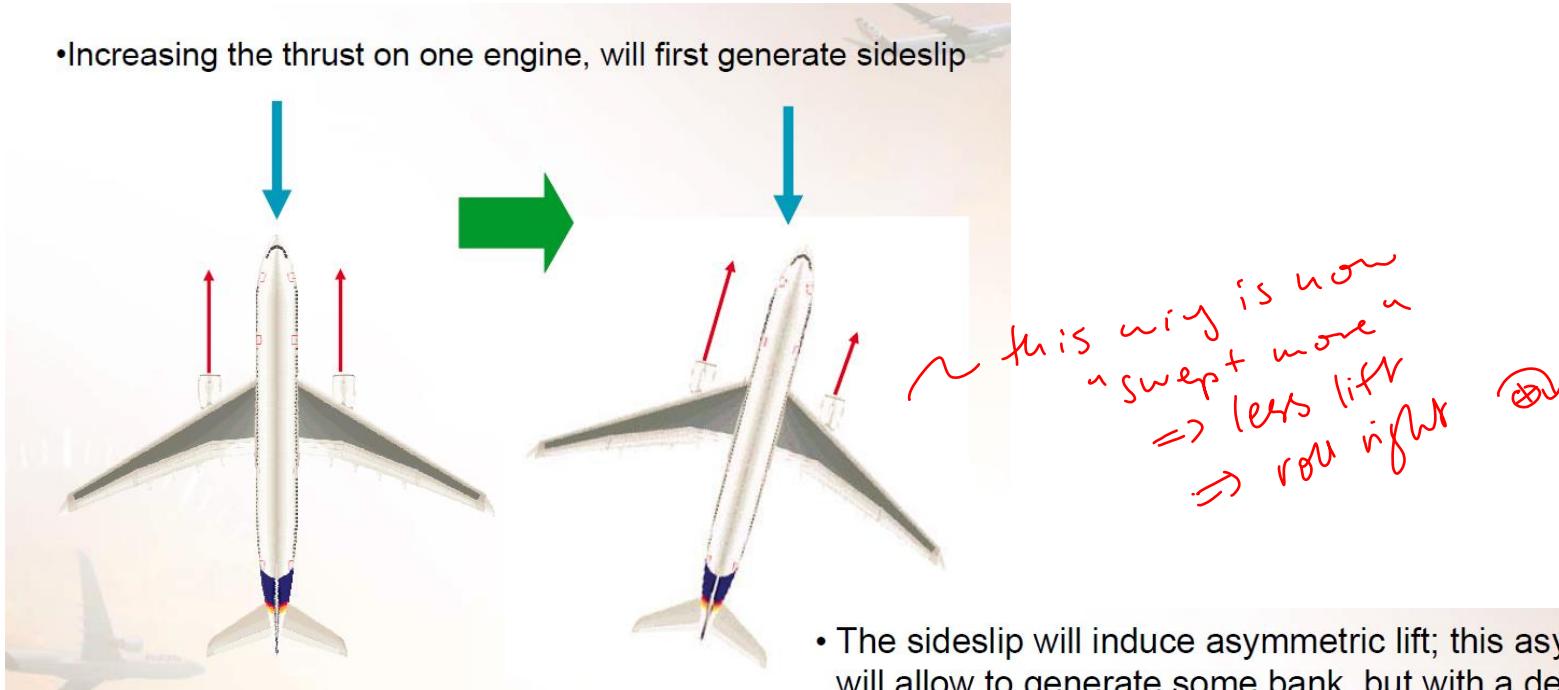
- When the controls froze, A/C was stabilized at a certain speed, with a given thrust and a given THS position
- A thrust variation (decrease) will create a pitch (down) moment
- This pitch down motion will continue until :
 - The thrust is restored at the adequate level, or
 - The speed has increased sufficiently so that the down lift of the tailplane compensates the pitch down moment created by the reduction of thrust.



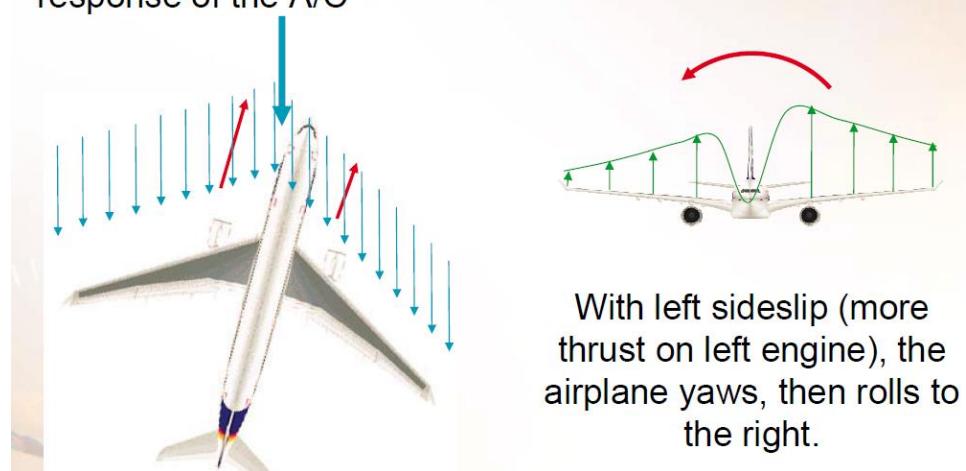
• THE THRUST BECOMES A PITCH CONTROL

- Speed becomes a consequence of the chosen combination of pitch and thrust.
- Note that against intuition (and initial reaction), a thrust reduction will finally induce a speed increase and vice versa.

- Increasing the thrust on one engine, will first generate sideslip



- The sideslip will induce asymmetric lift; this asymmetric lift will allow to generate some bank, but with a delayed response of the A/C



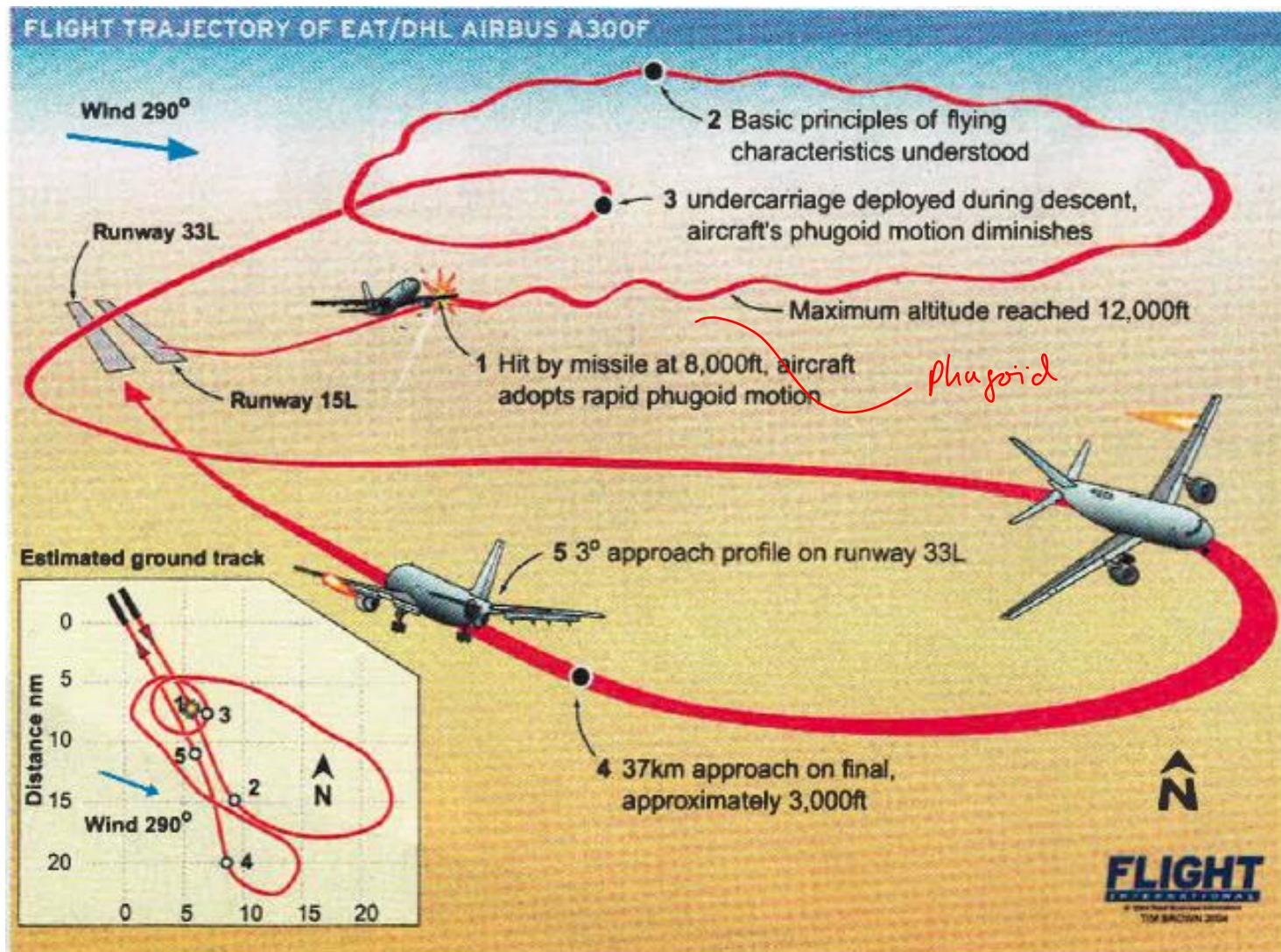
With left sideslip (more thrust on left engine), the airplane yaws, then rolls to the right.

nose goes up & down (oscillates)
i.e. trading pitch w/ airspeed

- ▶ Symmetrical change of **thrust** on both engines will allow to control **pitch** and then **vertical speed**. But pitch control will be loose due to the phugoid, making slope visualisation very difficult.
- ▶ Thrust being used for pitch control cannot then be used for speed control. Speed must be accepted as an uncontrolled result of the desired slope.
- ▶ When controlling the flight path, the crew will then have to accept the resulting speed and to control the slope through an active control of the pitch via the thrust.

- ▶ Assymetrical thrust application will allow to control the **roll**, but with a delayed response of the aircraft.

- ▶ Therefore, A/C control is achievable, but (at the least) demanding...





Éric Gennotte, Steeve
Michielsen and Mario Rofail

