

**Q.** Yara Inc is listed on the NYSE with a stock price of \$40 - the company is not known to pay dividends. We need to price a call option with a strike of \$45 maturing in 4 months. The continuously-compounded risk-free rate is 3%/year, the mean return on the stock is 7%/year, and the standard deviation of the stock return is 40%/year. What is the Black-Scholes call price?

$$C_0 = S_0 N(d_1) - (X/e^{(rt)})N(d_2)$$

where,

$$d_1 = (\ln(S_0/X) + (r + 1/2\sigma^2)t)/\sigma\sqrt{t}$$

$$d_2 = d_1 - \sigma\sqrt{t}$$

Stock price,  $S_0 = \$40$

Exercise price,  $X = \$45$

Interest rate,  $r = 0.03$  (10% per year)

Time to expiration,  $t = 0.33$  (3 months)

Standard deviation,  $\sigma = 0.40$  (50% per year)

$Nd$  = value of the cumulative standard normal distribution evaluated at  $d$

### **Solution**

$$d_1 = (\ln(40/45) + (0.03 + 0.5(0.4)^2)0.33)/0.4\sqrt{0.33}$$

$$d_1 = -0.11778303565 + 0.0363/0.2299$$

$$d_1 = -0.3544$$

$$d_2 = -0.3544 - 0.2299$$

$$d_2 = -0.5843$$

$$Nd_1 = 0.3632$$

$$Nd_2 = 0.2810$$

$$C_0 = 40*0.3632 - (45/e^{(0.03*0.33)})*0.2810$$

$$C_0 = 14.528 - 12.52$$

$$C_0 = 2.008$$