

# Simulating neural computation and information processing (with *Brian*)

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# Course material

The jupyter notebooks for the practical introductions to neural simulation will be made available at:

[github.com/brian-team/brian-material/tree/master/2024-TD-Brian-Sorbonne](https://github.com/brian-team/brian-material/tree/master/2024-TD-Brian-Sorbonne)

# Plan for today

Practical introduction to neural modeling

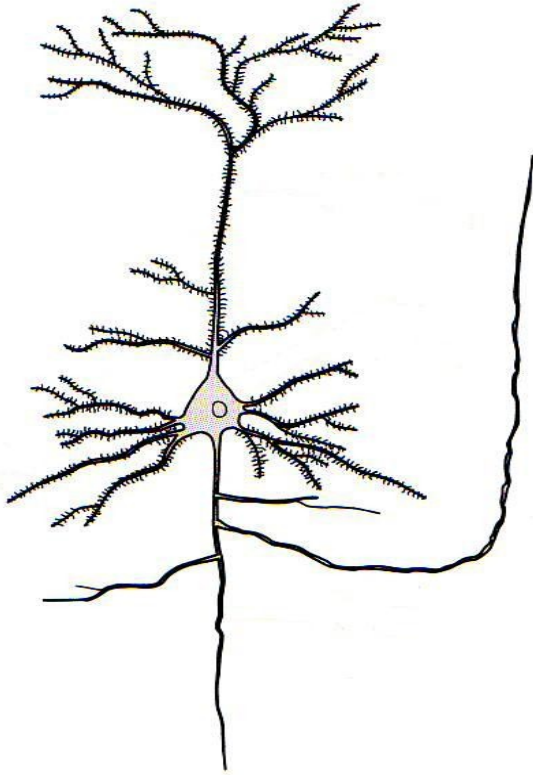
**Part 1:** neurons

**Part 2:** networks of neurons

**Part 3:** case study (binaural sound localisation)

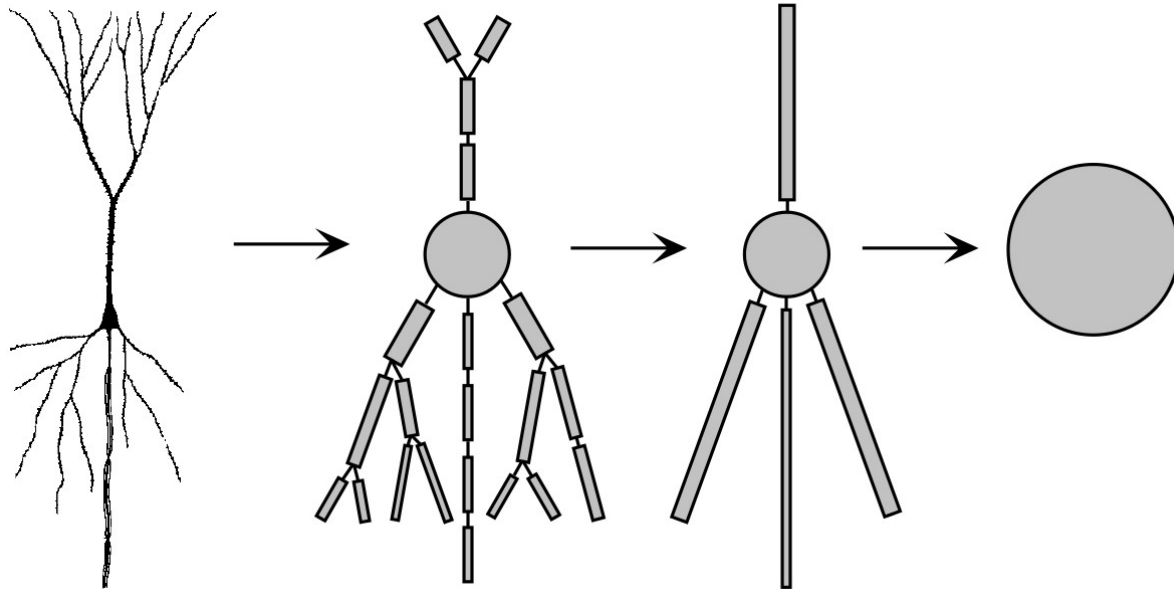
Each part:

some slides + practical simulation in Brian



# Part 1: Neurons

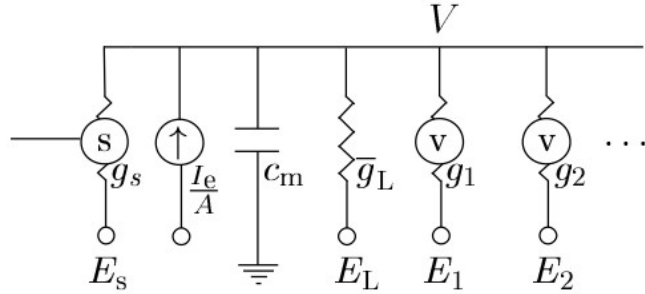
# Modelling neurons



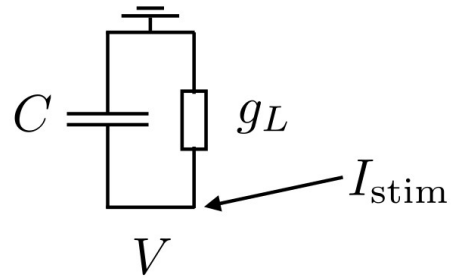
Detailed neuronal morphologies → point-neuron models

# Modelling neurons

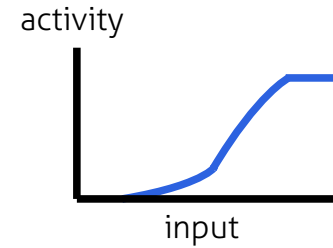
## Point-neuron models



Hodgkin-Huxley formalism



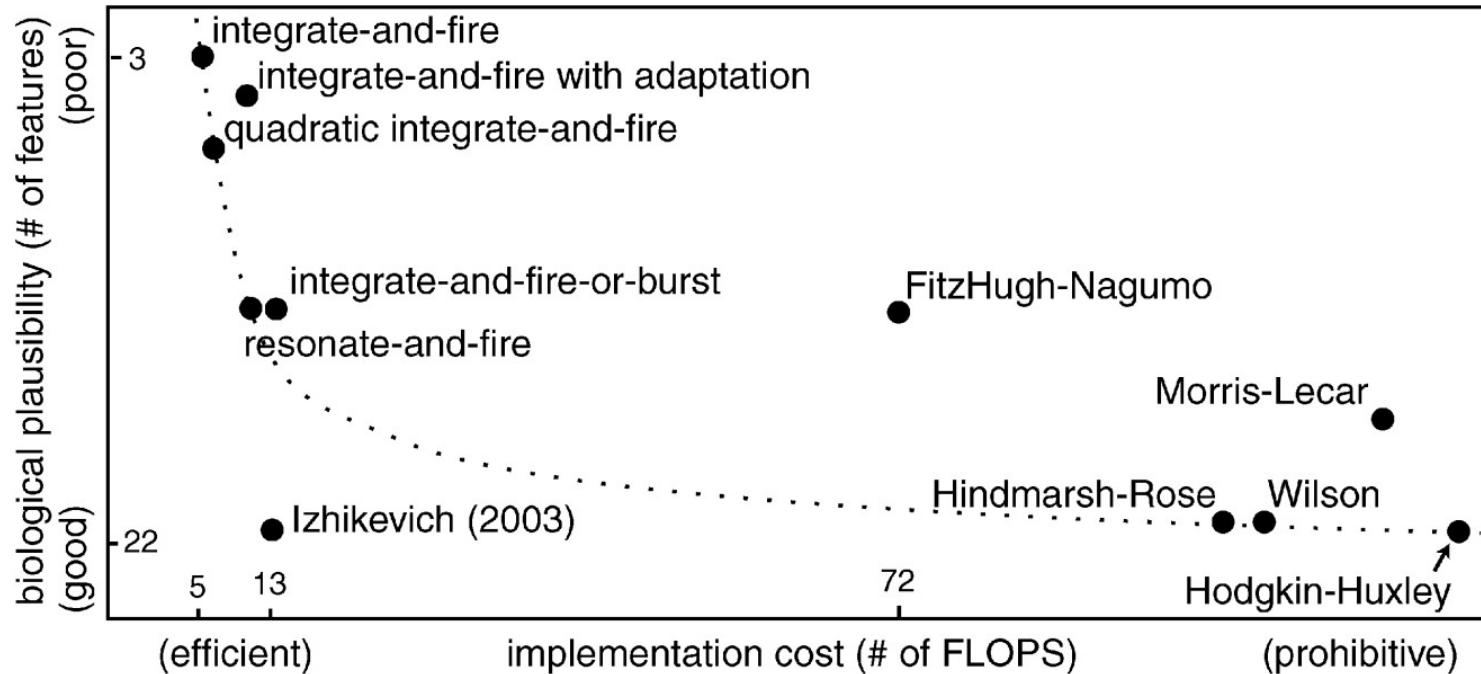
integrate-and-fire model



firing rate models

# Modelling neurons

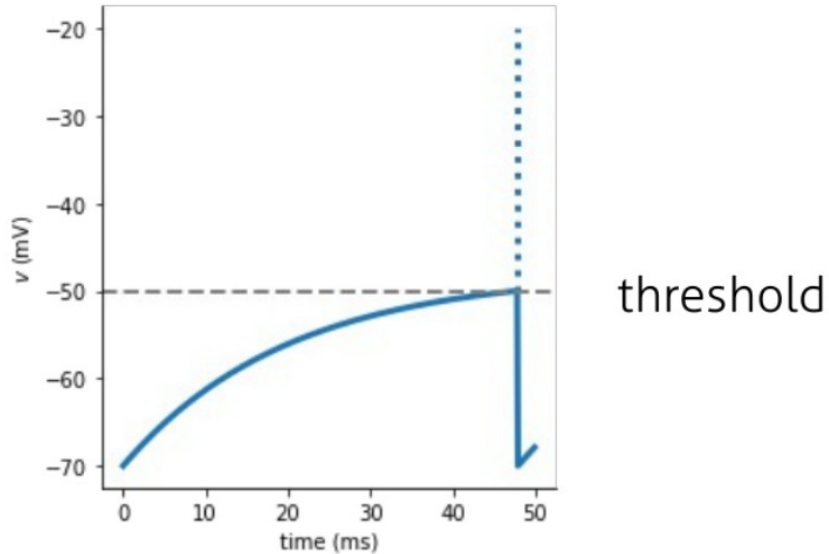
## Point-neuron models



# Integrate-and-fire neuron

$$C \frac{dV}{dt} = g_L(V_{\text{rest}} - V) + I_{\text{stim}}$$

$$V(t) > V_{\text{threshold}} \rightarrow \text{spike} + V(t) = V_{\text{reset}}$$



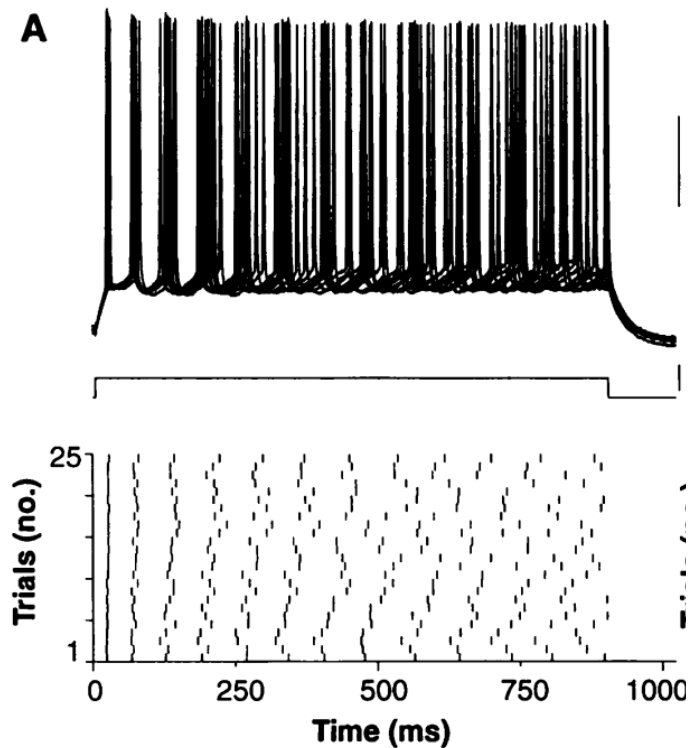


# Computing with spikes

- An argument that is sometimes made:  
“Spike timing in individual neurons is unreliable (‘noisy’). Therefore, only the firing rate (averaged over neurons or over time) matters, not the time of individual spikes.”
- Is spike timing really “unreliable”?

# Computing with spikes

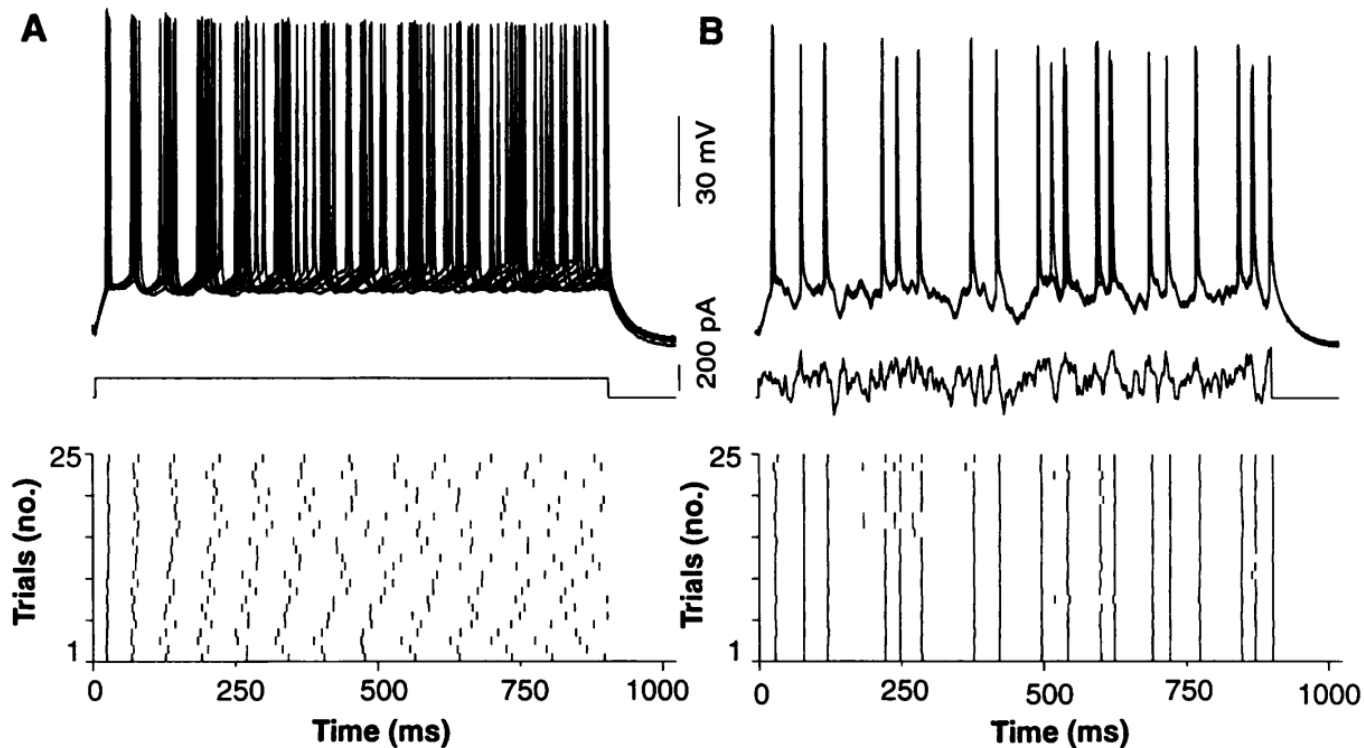
Constant current injection = **unreliable** spike times



# Computing with spikes

Constant current injection = **unreliable** spike times

Fluctuating current injection = **reliable** spike times



Let's try with

**BRIAN**

The

**BRIAN**

simulator

# Brian's approach

- *Interface*: Mathematical model descriptions
  - Flexible system to define models with equations
  - Takes care of numerical integration / synaptic propagation
  - Physical units
- *Behind the scenes*: Code generation
  - High-level descriptions transformed into low-level code
  - Transparent to user

# More info

**Website:** <https://briansimulator.org>

**Documentation:** <https://brian2.readthedocs.io>

**Discussion forum:** <https://brian.discourse.group>

## Articles:

Stimberg, Marcel, Romain Brette, and Dan FM Goodman. "Brian 2, an Intuitive and Efficient Neural Simulator." *ELife* 8 (2019): e47314. <https://doi.org/10.7554/eLife.47314>.

Stimberg, Marcel, Dan F. M. Goodman, Victor Benichoux, and Romain Brette. "Equation-Oriented Specification of Neural Models for Simulations." *Frontiers in Neuroinformatics* 8 (2014). <https://doi.org/10.3389/fninf.2014.00006>

## Part 2: Networks

# Modelling networks of neurons

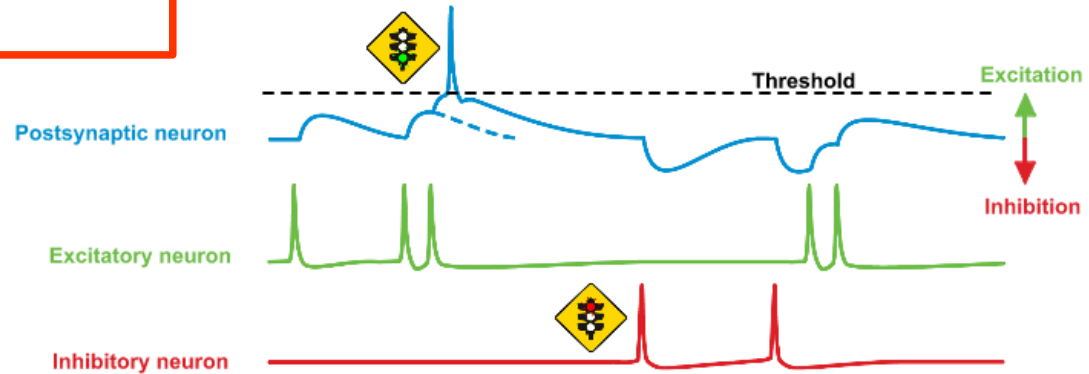
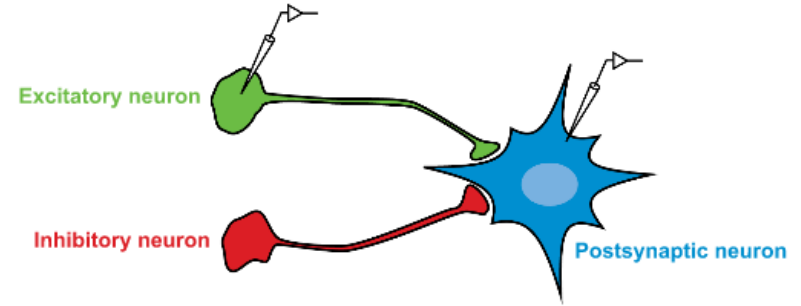
## Synapses

?

Why can we talk about excitatory/inhibitory *neurons* and not just synapses?

!

→ "Dale's law"  
Neurons release the same neurotransmitter(s) on every synapse





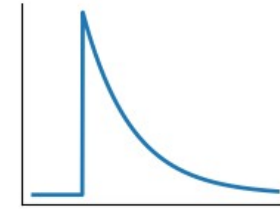
# Synaptic models

## Synapses

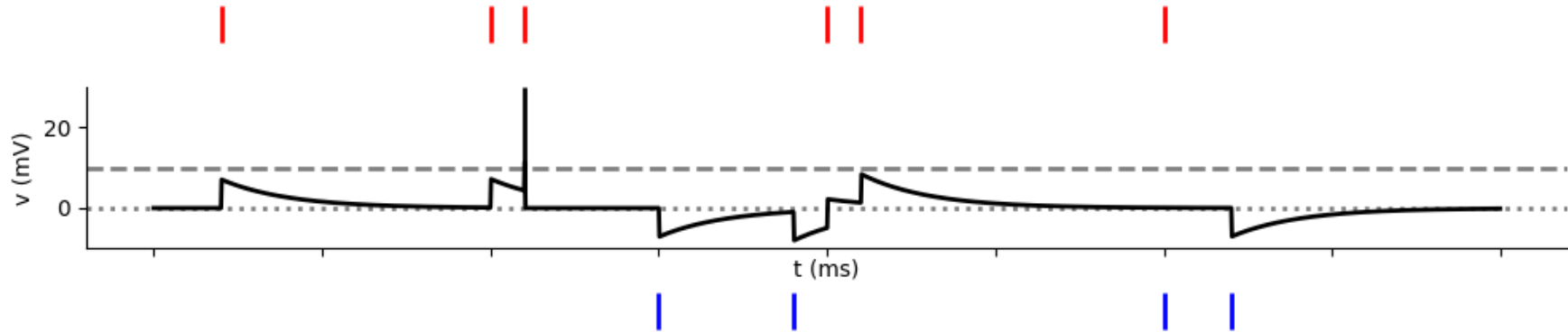
For each spike: increase  $V_m$  by  $J_{ij}$

weight from j to i

membrane potential



“delta synapse”

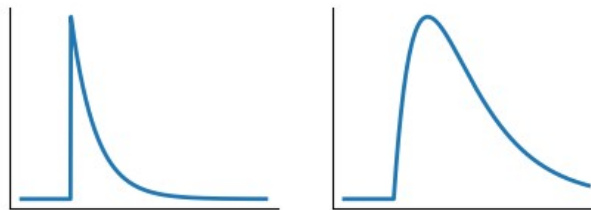


# Synaptic models

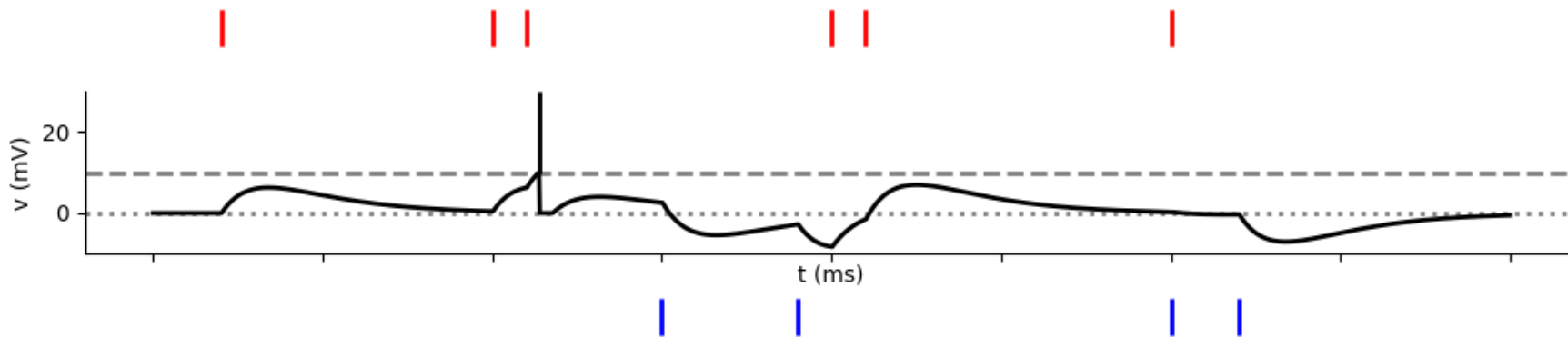
## Synapses

For each spike: increase  $I_{syn}$  by  $J_{ij}$   
Between spikes:  $I_{syn}$  exponentially decays to 0

synaptic current    membrane potential



Current-based  
synapse



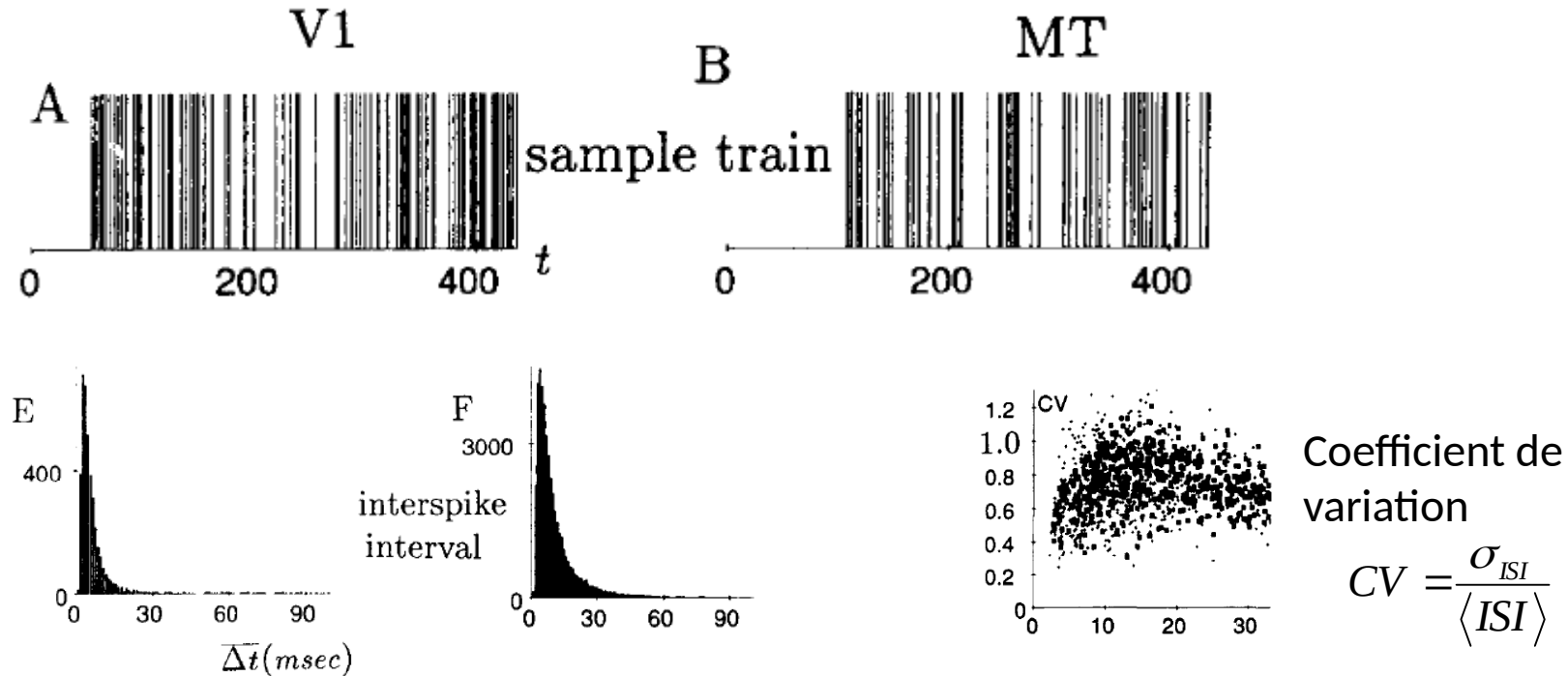
# Input integration in neurons

- Cortical neurons: ~10000 synapses
- If spikes at synapses are independent
  - total input relatively constant
  - neuron should fire regularly

*Note: “regularly” and “reliable” are different things!*

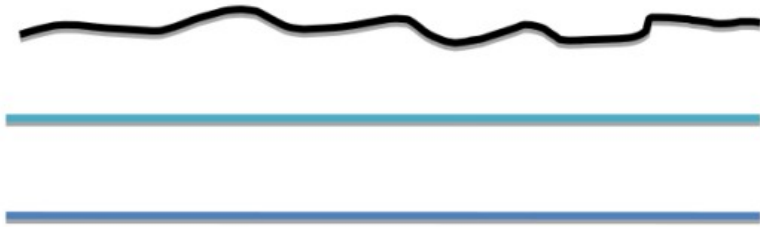
# Irregularity of spike trains

Cortical neurons fire irregularly (in vivo)



# Mean-driven vs. fluctuation-driven

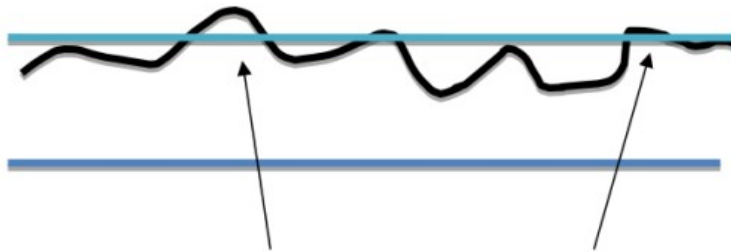
Mean-driven



$$\langle I \rangle > I_{\text{threshold}}$$

Small variability (average of many inputs)

Fluctuation-driven



$$\langle I \rangle < I_{\text{threshold}}$$

0

Let's try with

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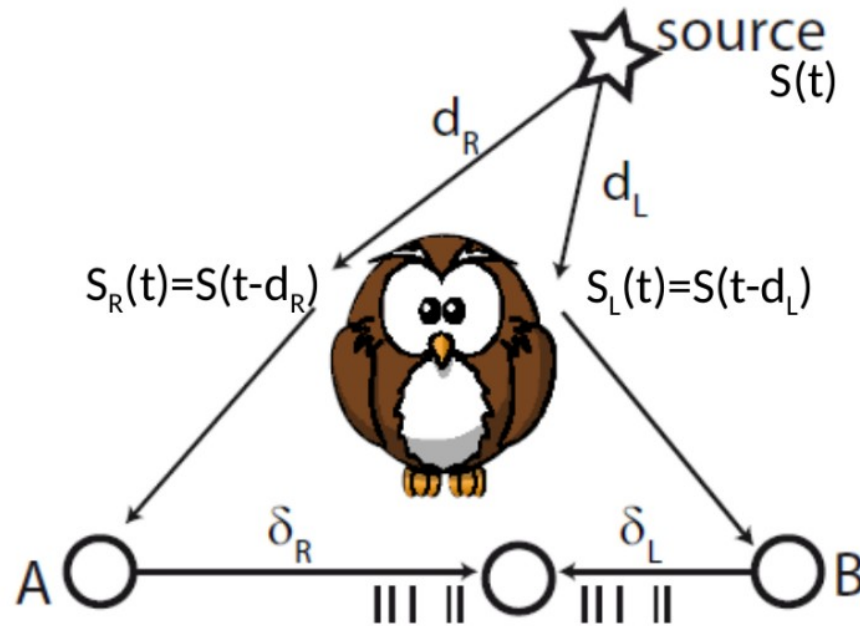
spikes can only occur at times when the input fluctuates above the mean

# Part 3: Case study

## Binaural sound localisation

# Binaural sound localisation

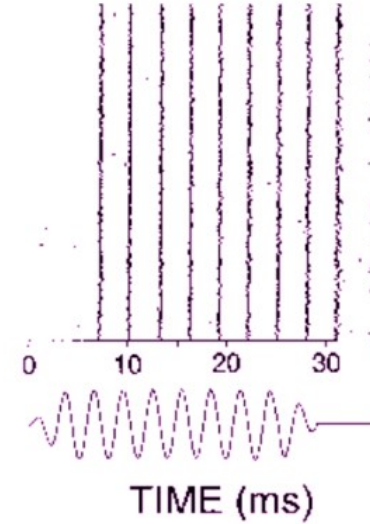
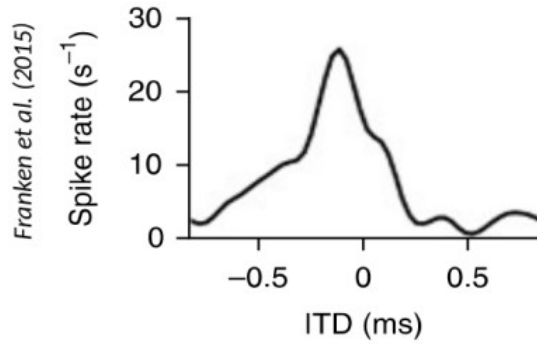
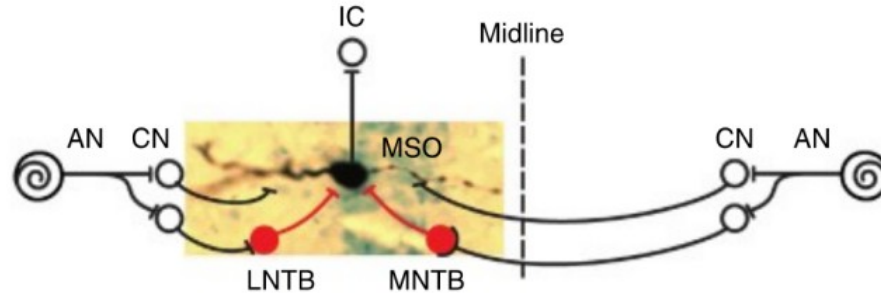
The Jeffress model



Interaural time delay  
(ITD)

# Binaural sound localisation

Anatomical structures from the ear to the brainstem



Louage et al. (2005)

Let's try with

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