Model Order Selection in Reversible Image Watermarking

Ming Chen, Zhenyong Chen, Xiao Zeng, Zhang Xiong

Abstract-Digital watermarking is becoming increasingly important in a large number of applications such as copyright protection, content authentication and document annotation. Thanks to its capability of exactly recovering the original host, reversible image watermarking, a kind of digital watermarking, is favored in fields sensitive to image quality like military and medical imaging. This paper presents theoretical examination and experimental analysis of model order selection in reversible image watermarking. It involves two modeling tools: prediction and context modeling. Classic prediction models are compared and evaluated using specially derived criteria for reversible image watermarking. Among them, the CALIC, a tool combining the Gradient-Adjusted Prediction with a context modeling, stands out as the best by providing the most competitive modelfitness with relatively low complexity. In addition, full context prediction, a model unique to reversible image watermarking is also discussed. By exploiting redundancy to greater extent, it achieves highly fitted modeling at a very low order. Experimental results demonstrate that it is capable of providing even better performance than the CALIC with only negligible computation.

Index Terms—Full context prediction, model order selection, prediction-error expansion, reversible image watermarking

I. Introduction

IGITAL media is rapidly changing the way people work and entertain. Along with the digital infrastructure of digital signal recorders, processors, communicators, players and broadcasters, many digital media related applications and techniques are emerging and evolving. Digital watermarking is such a promising technique. In Wikipedia, digital watermarking is "the process of possibly irreversibly embedding information into a digital signal". In Cox's book [1], watermarking is defined as "the practice of imperceptibly altering a work to embed a message about that work". Both definitions highlight its main character of information embedding. Digital watermarking is mostly used in copyright protection. It can work either in an active way to allege ownership of intellectual property, or in a passive way to identify and prosecute copyright violators. When applied to content authentication, fragile watermarks vulnerable to malicious manipulation are embedded into digital documents before transmission on unsafe channels. Once the digital copies are transmitted, their integrity and authenticity can be verified by detecting those

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Ming Chen (e-mail: mingchen@cse.buaa.edu.cn), Zhenyong Chen (e-mail: chzhyong@buaa.edu.cn), Xiao Zeng (e-mail: zengxiao29@cse.buaa.edu.cn), and Zhang Xiong (e-mail: xiongz@buaa.edu.cn) are all with the School of Computer Science and Engineering, Beihang University, Beijing, 100191 China.

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fragile watermarks [2]. Digital watermarking is also capable of managing and annotating digital documents by embedding descriptive information. A well known case is the watermarking of videos taken by Unmanned Aerial Vehicle (UAV) of the US army [3]. Other applications of digital watermarking include broadcast monitoring, transaction tracking, access control, legacy enhancement and even more [1].

Although hosts are altered imperceptibly, digital watermarking still introduces permanent distortion due to replacement. quantization, round-off or truncation [4]. This distortion is intolerable when exact representation of the original host is demanded, e.g. the watermarking for valuable documents such as military images. In these scenarios, reversible watermarking, which can recover the original host through watermark extracting, is desired and required. Since the first invention of reversible watermarking in 1997 [5], many reversible watermarking schemes have been proposed. In quite recent years, a set of schemes using prediction-error expansion [6]-[13] were reported to provide outstanding performance in both embedding capacity and image fidelity. These schemes accomplish reversible watermark embedding by expanding the differences between original and predicted values of pixels, i.e., prediction-errors. Prediction-error expansion is a generalization of difference expansion (DE) [14] by applying expansion to prediction-errors instead of inter-pixel differences. Since prediction-errors have been proved to be of excellent decorrelating abilities, they are superior to inter-pixel differences in expandability.

In reversible image watermarking using prediction-error expansion, the calculation of prediction-errors is a significant and computation-consuming part of the whole process. It involves a prediction stage and an optional context modeling stage. Prediction decorrelates pixels by exploiting low order redundancy within local areas, whereas context modeling achieves further decorrelation by exploiting high order structures, such as texture patterns, via a feedback mechanism. For both modeling tools, a proper model order is important. Model order affects the system performance and the implementation complexity in opposite directions. To balance these two effects, many model order selection criteria have been proposed. A well known criterion is the Akaike Information Criterion (AIC) named after Akaike [15], which selects a model that minimizes the expected error using maximum likelihood estimation (MLE). The other one is the Minimum Description Length (MDL) introduced by Rissanen [16], which takes the simplest model sufficiently describes the data to be the best. Both the AIC and the MDL criteria achieve efficient tradeoff by incorporating terms that penalize the selected model order as it goes high.

There also exist some derivatives of AIC and MDL, and other criteria based on different theories. Though the model order selection criteria such as AIC and MDL are theoretically well established, they are not directly applicable in practical scenarios. In real applications, the penalty associated with model order should be related to the overall system performances and the implementation complexity, which are not well embodied in these criteria. To provide guidance in the specific application background of reversible image watermarking, we need special studies regarding this topic.

In this paper, we study the model order selection in reversible image watermarking via theoretical examination and experimental analysis. To achieve an efficient tradeoff for reversible image watermarking, specific measures of the model-fitness and the implementation complexity in reversible image watermarking are derived. Then a set of models, in both prediction and context modeling with orders varying from low to high, are studied and compared in the derived measures. They include many well-known predictors including the JPEG predictors, the MED predictor [17], the GAP predictor [18], the least-square predictor [19]-[21], and the CALIC context modeling scheme [18], [22]. Although these models are borrowed from predictive image compression, our study will show very different results which are explainable because of the distinctive model-fitness criteria in reversible image watermarking. Unlike the case in predictive image compression, the prediction context in reversible image watermarking is no longer restricted to half enclosing causal pixels. Without this limit, we can model the prediction in a more efficient manner and achieve higher model-fitness with even lower model order.

The rest of this paper is organized as follows. Reversible image watermarking using prediction-error expansion is introduced in Section II. Measures for the model-fitness and the implementation complexity are derived in Section III. Then the model order selection issue in prediction and context modeling are discussed respectively in Section IV and Section V. Full context prediction, the modeling technique unique to reversible image watermarking, is studied in Section VI. Experimental results of concrete reversible watermarking schemes employing studied techniques are presented and evaluated in Section VII. Finally, conclusions are drawn in Section VIII.

II. REVERSIBLE IMAGE WATERMARKING USING PREDICTION-ERROR EXPANSION

A reversible watermarking system, depicted in Fig. 1, consists of two main procedures, i.e., embedding and extracting. Essentially, reversible watermarking exploits redundancy in host to provide extra payload for watermark. So it is desired that the host image is transformed into a domain where pixels are well decorrelated. Prediction-error is such a domain, which is verifiable in those latest reversible image watermarking schemes [7]–[13], [23]. As to the data embedding strategy, difference expansion (DE) [14] is an outstanding one in both embedding capacity and image quality. Applying DE to prediction-error, we identify a set of schemes with excellent performance, i.e., reversible image watermarking using prediction-error expansion.

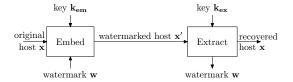


Fig. 1. A reversible watermarking system. "Embed" combines the host \mathbf{x} with watermark data \mathbf{w} to form a composite signal \mathbf{x}' under the control of a encryption key $\mathbf{k_{em}}$. Importantly, \mathbf{x}' is necessarily close to \mathbf{x} in perception. "Extract" separates the watermark data \mathbf{w} from the composite signal \mathbf{x}' and recover the original host \mathbf{x} with a decryption key $\mathbf{k_{ex}}$. The transmission of \mathbf{x}' is considered to be noise-free in this paper.

$X_i(11)$	$X_i(8)$	$X_i(6)$	$X_i(9)$	$X_i(12)$		x_{nnw}	x_{nn}	x_{nne}	
$X_i(7)$	$X_i(3)$	$X_i(2)$	$X_i(4)$	$X_i(10)$	x_{nww}	x_{nw}	x_n	x_{ne}	x_{nee}
$X_i(5)$	$X_i(1)$	X_i			x_{ww}	x_w	x		
		(a)					(b)		

Fig. 2. Prediction context. (a) X_i is the pixel to be predicted and $X_i(t)$ is its tth nearest causal pixel. (b) x represents the pixel to be predicted. N, W and E stand for the directions of north, west and east, e.g. x_n stands for the pixel north to x.

A. Prediction-Error Expansion

Prediction-errors are the differences between original pixel values and their predicted values. The calculation of predicted values involves two modeling tools. The first one is prediction, which is a low-order modeling technique that try to give a reasonable guess of current sample X_i from previous samples $X_i(t)$. Consider the linear prediction model, the predicted value \hat{x}_i of sample X_i is

$$\hat{x}_i = \sum_{t=1}^n a_t x_i(t),\tag{1}$$

where n is the model order, $x_i(t)$ is the value of sample $X_i(t)$, and a_t is the corresponding predictor coefficient. The prediction-error is

$$e_i = x_i - \hat{x}_i, \tag{2}$$

where x_i is the real value of current sample. For images, the signal samples, i.e., pixels, are two-dimensionally distributed. The previous sample $X_i(t)$ is the tth nearest causal pixel surrounding X_i as Fig. 2(a) illustrates. The causal pixels $X_i(1)X_i(2)\ldots X_i(n)$ form a half enclosing region around the predicted pixel, and this region is called prediction context. In later discussion, we also adopt the notations in Fig. 2(b) to represent prediction context, and we indiscriminatingly use x to denote the current pixel to be predicted as well as its real value. These simplifications allow us to refer to pixels in an intuitive manner.

The other modeling tool, being optional, is context modeling. It is a high-order modeling technique that can refine prediction-error through an error feedback mechanism. Let $\bar{\epsilon}_i$ be the feedback, then the former prediction is modified via

$$\dot{x}_i = \hat{x}_i + \bar{\epsilon}_i,\tag{3}$$

where \dot{x}_i is the new predicted value with the error feedback. Then the prediction-error is adjusted accordingly via

$$\epsilon_i = x_i - \dot{x}_i. \tag{4}$$

Once prediction-errors e (be either e_i or ϵ_i) are obtained, they are expanded to e' to embed watermark w. Since expansion methods are reversible, original e and w can be restored if e' is known. In sum, the process of reversible image watermarking using prediction-error expansion is:

- During embedding, predicted pixel value \hat{x} (be either \hat{x}_i or \dot{x}_i) is obtained first. Prediction-error $e = x \hat{x}$ is calculated, and reversibly expanded to e' with watermark w embedded simultaneously. Lastly, watermarked pixel is obtained $x' = \hat{x} + e'$.
- During extracting, the original predicted value \hat{x} and the expanded prediction-error $e' = x' \hat{x}$ are obtained. With inverse expansion, the embedded watermark w is extracted and the prediction-error e is recovered. Then the original pixel is restored $x = \hat{x} + e$.

B. Bitshifting Expansion

One popular reversible expansion method is bitshifting expansion [14]. The bitshifting prediction-error expansion is

$$e' = 2e + b, (5)$$

where e is prediction-error, and b is a binary bit, either '0' or '1'. During extracting, the bit can be extracted via $b = e' \mod 2$, and the original prediction-error can be restored via $e = \lfloor e'/2 \rfloor$. Let $e_{j-1} \cdots e_1 e_0$ be the binary representation of e, then the watermarked prediction-error e' is $e_{j-1} \cdots e_1 e_0 b$ in binary form. We can view the expansion as a process that bitshifts e left by 1 and embeds b as the least significant bit. That is the very reason it is named bitshifting expansion. It is worth notice that not all prediction-errors are expandable due to distortion concerns and pixel overflow and underflow. Actually, only differences smaller than a threshold T are expanded for data embedding. To tell expanded differences from unexpanded ones, a bitmap marking all expanded differences, named *location map*, is used and recorded as overhead information. Comparing watermarked pixels with original ones, it is easy to derive the induced distortion

$$\Delta x = x' - x = \hat{x} + e' - x = e + b. \tag{6}$$

Since prediction-errors are mostly tiny and we expand only those smaller than a threshold T, we can restrict Δx within a small range and let the distortion be imperceptible.

C. Additive Expansion

Another expansion method, proposed by the authors [9], is additive expansion. Additive prediction-error expansion is based on statistical feature of prediction-errors and it can be viewed as an operation of the histogram of prediction-errors. To ease discussion, we consider positive and negative prediction-errors uniformly by adopting absolute histogram which flips the left histogram to the right. Let $hist(\cdot)$ be the histogram function, i.e., hist(e) is the number of occurrence

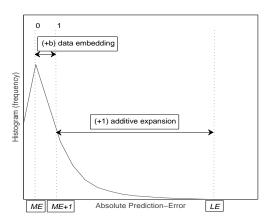


Fig. 3. Absolute histogram of prediction-error and additive prediction-error expansion. Absolute histogram bin ME+1 is first vacated by shifting all bins within [ME+1, LE) right by 1, where LE is always empty. Then prediction-errors in bin ME is used to embed bits. A prediction-error embedded with 1 is move to bin ME+1, otherwise it remains in bin ME.

when the prediction-error assumes value e, absolute histogram $habs(\cdot)$ is

$$habs(e) = \begin{cases} hist(e) + hist(-e), & e > 0\\ hist(e), & e = 0 \end{cases}$$
 (7)

Fig. 3 depicts the shape of $habs(\cdot)$, wherein ME is the value most absolute prediction-errors assume, and LE is the value least absolute prediction-errors assume. Namely,

$$ME = \arg \max_{e \ge 0} habs(e) LE = \arg \min_{e \ge 0} habs(e)$$
 (8)

It is obvious that ME identifies the peak of $habs(\cdot)$, while LE identifies the valley of $habs(\cdot)$. Based on these definitions, additive prediction-error expansion is formulated as

$$e' = \begin{cases} e + sign(e) \times b, & |e| = ME \\ e + sign(e) \times 1, & |e| \in [ME + 1, LE) \end{cases}$$
(9)

where $sign(\cdot)$ is a sign function

$$sign(e) = \begin{cases} 1, & e \ge 0 \\ -1, & e < 0 \end{cases} . \tag{10}$$

Note that, in additive expansion (9), only prediction-errors satisfying |e| = ME are used indeed for embedding data. As b is either 0 or 1, the change of pixel $\Delta x = x' - x = e' - e$ will never be larger than 1. Therefore, the distortion caused by additive expansion is tiny and the change of watermarked image is imperceptible. It is easy to estimate the embedding capacity of additive expansion with habs(ME).

During extracting, bits can be extracted easily through

$$b = \begin{cases} 0, & |e'| = ME \\ 1, & |e'| = ME + 1 \end{cases}$$
 (11)

Since (9) does not change the sign of prediction-error, i.e. $sign(e') \equiv sign(e)$, the original prediction-error can be recovered through

$$e = \begin{cases} e' - sign(e') \times b, & |e'| \in [ME, ME + 1] \\ e' - sign(e') \times 1, & |e'| \in (ME + 1, LE] \end{cases}$$
 (12)

III. MEASURES OF MODEL-FITNESS AND IMPLEMENTATION COMPLEXITY

Like most signal processing systems, a better model brings better performance in reversible image watermarking. However, when the model is better fitted, the system becomes generally more complicated. A practical compromise is to tradeoff between the two conflicting goals of high system performance and low implementation complexity by selecting a proper model order. Towards this purpose, we need model-fitness indicators directly related to the overall system performance and measures of the implementation complexity.

A. Model-Fitness Indicators

Unlike the case in predictive image compression, where minimization of conditional entropy of all prediction-errors is the ultimate goal, conditional entropy of all prediction-errors is not a good criterion for reversible image watermarking. Instead, embedding capacity and image quality (fidelity) are two most important performance criteria for reversible image watermarking. Embedding capacity is the amount of extra data that can be carried in the host image as watermark. It is measured with the number of embedded bits. Image quality (fidelity) measures the visual difference between the watermarked image and the original image. It can be estimated with subjective and objective measures. While subjective measure concerns the visual impact on human eyes, objective measure gauges the values of pixels. One popular objective measure is the peak signal-noise ratio (PSNR) defined as

$$PSNR = 10 \log_{10} \frac{(2^d - 1)^2 W H}{\sum_{i=1}^{W} \sum_{j=1}^{H} (p[i, j] - p'[i, j])^2}$$
 (13)

where d is the bit depth of pixel, W the image width, Hthe image height, and p[i, j], p'[i, j] is the *i*th-row *j*th-column pixel in the original and watermarked image respectively. It is possible to directly use number of bits and PSNR to judge the model-fitness in reversible image watermarking, but it is not quite convenient to take two different criteria as a whole. Moreover, these two criteria are mutually exclusive. Embedding capacity is greatly constrained when high image quality is required, or it is hard to preserve high image fidelity when large capacity is pursued. So a convenient alternative is to derive specific model-fitness indicators for reversible image watermarking. As there are two different expansion methods, i.e., bitshifting expansion and additive expansion, we consider them separately. Denote by IB the indicator of bitshifting prediction-error expansion, and by IA the indicator of additive prediction-error expansion. Then our goal is to find proper IB and IA that can precisely measure the model-fitness as well as the performance of the reversible watermarking scheme. Primarily, the modeling tools used in reversible image watermarking serve the purpose of calculating predictionerrors. When the model is better fitted, we obtain smaller prediction-errors that can greatly favor the embedding capacity and image quality for both bitshifting expansion and additive expansion. Therefore, it is likely to obtain good IB and IA by counting small prediction-errors.

We consider IB first. The embedding capacity and image quality of bitshifting prediction-error expansion is controlled by a threshold of prediction-error. The threshold controls image quality by adjusting the number of changed pixels and the range of pixel changes. When the threshold is small, only smaller prediction-errors will be expanded, namely fewer pixels will be altered. Moreover, pixel change of bitshifting expansion is $\Delta x = e + b$. Since smaller prediction-errors cause smaller changes, less distortion will be introduced. The threshold controls the embedding capacity through its impacts on overall capacity and overhead cost. Given a threshold T, the overall capacity of bitshifting expansion approximates $\sum_{i=0}^{T-1} habs(i)$. Different from the additive expansion where the expense of overhead information is negligible, the overhead cost of bitshifting expansion is more expensive due to the space occupied by the location map. Thus the compression rate of the location map plays a significant role in determination of the pure embedding capacity. As a binary bitmap, it is hard to achieve a satisfactory compression rate of the location map when 0 and 1 are equally distributed in a random way. Nevertheless, it can be compactly compressed when it becomes sparse. The density of the location map is chiefly determined by T in a way that it becomes sparser when T becomes larger. Therefore, to provide a satisfactory pure capacity, the threshold cannot be very small. It is studied in [24] that a proper pure embedding capacity can be obtained at a threshold about 10. So we adopt

$$IB = \frac{\sum_{i=0}^{9} habs(i)}{NP} \tag{14}$$

as the model-fitness indicator for bitshifting expansion. In (14), NP is the number of pixels in the host image. IB is easy to obtain and it can correctly reflect the two performance criteria simultaneously. On the one hand, when IB goes larger, more bits can be embedded, and less overhead is needed as the location map becomes sparser and more compressible. Therefore IB is of positive relation to the embedding capacity. On the other hand, the larger IB becomes, the more likely the threshold T will assume a small value. In turn, less distortion will be caused.

In additive expansion, embedding capacity approximates the value of the highest histogram bin of absolute predictionerrors, namely habs(ME), as depicted in Fig. 3. And the overhead cost of additive expansion is relatively negligible to the overall capacity. Hence, habs(ME) can efficiently reflect the contribution of model-fitness to embedding capacity, thus we define IA as

$$IA = habs(ME). (15)$$

Then we will show that IA can also be applied to evaluate the contribution of model-fitness to image quality. From (9), we can see that prediction-errors within [ME+1, LE) are altered by 1, whereas prediction-errors satisfying |e|=ME are modified by adding the embedded bit b. We see that pixels are changed at most by 1. Taking the watermark to be embedded as a random bit sequence, it is expected that half of the prediction-errors satisfying |e|=ME are changed by 1 while the other half are kept intact. As prediction-errors with absolute value larger than LE are rare in practical

images, the prediction-errors subjected to |e|>LE are proportionally negligible. Therefore, it is proper and convenient to only consider prediction-errors within $(-LE,\, LE)$. Then the number of pixels that are changed by 1 can be estimated with $NP-\sum_{i=0}^{ME-1}habs(i)-habs(ME)/2$. Mostly, when prediction-errors are more concentrated in the middle, $\sum_{i=0}^{ME-1}habs(i)$ grows simultaneously with habs(ME). So when habs(ME) becomes large, fewer pixels are modified, and less distortion is introduced. This is also verifiable in the experimental results in [9], [10], where higher PSNR values (image quality) are obtained when more bits are embedded.

B. Complexity Measures

After indicators of model-fitness are derived, we also need proper measures of the implementation complexity to study the tradeoff between the two conflicting criteria of reversible image watermarking. For prediction-error expansion using either bitshifting or addition, the expansion process is rather simple, whereas the complexity of different predictors varies within a rather wide dynamic range. So it is reasonable to use the complexity of the predictor to approximate implementation complexity. In later discussion, predictors will be grouped into stationary predictors, context-based adaptive predictors, and LS-based adaptive predictor for comparison. We will study the complexity of predictors by analyzing the computation cost of their formulas as well as their running time in implementations. For analysis of computational cost, we count the number of operations like add (addition and subtraction), shift (bitshift), mul (multiplication), and comparison (conditional statement). Since most muls in prediction are integer muls with fixed small integer, they are decomposed to add and shift operations for faster computation [25]. For example, 10x are calculated as (x+(x << 2)) << 1. In our experiments, those predictors are all implemented and tested with Matlab. The test platform is a PC running Ubuntu with a CPU of Intel Core Duo T7500 and a RAM of 2GB. All test images are standard 8-bit grayscale test images sized 512×512 .

IV. Low-order Modeling in Reversible Image Watermarking

Prediction is the first of the two provably good modeling tools (the other being context modeling) [26]. The prediction model assumes smoothness of image data, which mostly holds within small local areas consisting of only the nearest pixels. Therefore, the order of a practical prediction model is generally low and varies from a couple to several. Predictors behave differently according to the variance of model order and model coefficients, and the selection of an appropriate model order is subjected to the way the model coefficients are determined. Based on the strategy of model coefficients determination, prediction can be classified to be stationary and adaptive. The model orders of stationary predictors are generally lower than that of adaptive predictors, while adaptive predictors are more precise in general.

A. Stationary Prediction

In stationary prediction, the coefficients are constants. Good examples, as tabulated in Table I, are those predictors used

TABLE I STATIONARY PREDICTORS

Order	Name	Expression	Description
	JM1	x_n	JPEG Mode 1
1	JM2	x_w	JPEG Mode 2
	JM3	x_{nw}	JPEG Mode 3
2	JM7	$(x_n + x_w)/2$	JPEG Mode 7
	JM4	$x_n + x_w - x_{nw}$	JPEG Mode 4
3	JM5	$x_w + (x_n - x_{nw})/2$	JPEG Mode 5
	JM6	$x_n + (x_w - x_{nw})/2$	JPEG Mode 6
4	SGAP	$(x_w + x_n)/2 + (x_{ne} - x_{nw})/4$	Simplified GAP

TABLE II
PERFORMANCES OF STATIONARY PREDICTORS GROUPED BY MODEL
ORDER

Order	IA	IB (%)	Time (ms)
1	36207	74.32	3.6
2	42572	80.02	5.3
3	36686	77.80	5.0
4	43132	81.13	6.7

in different modes of the old JPEG standard [27]. Another stationary predictor included in Table I is a simplified version of the Gradient-Adjusted Predictor we will discuss later. It has been studied in [9] for reversible image watermarking, where it demonstrates very competitive performance at a low computational complexity.

The computational complexities of the eight stationary predictors increase as their model orders rise. The first three 1-order predictors are simplest. No extra operation is needed for the predicted value and the computation of prediction-error is a single add operation. The computation cost of the 2-order JM7 is one add plus one shift. The first 3-order predictor JM4 needs two adds to predict, while other two 3-order predictors, JM5 and JM6, both calculate predicted values with two adds and one shift. The only 4-order SGAP predictor works with three adds and two shifts. The highest order of these stationary predictors is just 4, and even the most complicated one is very easy in computation. We have tested these predictors on standard test images. The results are listed in Table III. By grouping predictors with their model order, the average result is listed in Table II. It is clear that the 4-order predictor, namely SGAP, is of much better performance than other low order predictors. It is well studied in [28] that the four nearest causal neighbors of a pixel are usually found to be most effective for prediction. Although the running time of SGAP is the longest among the four, it is still very fast to calculate the whole predicted image within just 6.7ms in average.

B. Context-based Adaptive Prediction

The effectiveness of stationary prediction assumes smoothness of image data. However, when there exist abrupt changes in local areas, stationary prediction fails to fully exploit the correlation within images. By detecting those abrupt changes, the performance of linear prediction can be improved. This is how adaptive prediction schemes gain improvements over stationary prediction schemes in predictive image compression. For adaptive prediction, the predictor coefficients are adaptively adjusted to the locality of predicted pixel. A common

Image	JI	M1	JI	M2	JI	М3	JI	M7	JI	M4	JI	M5	JI	M6	SC	SAP
	IΑ	IB (%)	ΙA	IB (%)	IΑ	IB (%)	IΑ	IB (%)								
Lena	57089	90.40	47921	84.88	44974	81.80	59684	90.22	46804	89.67	52252	89.93	55571	91.96	63773	92.23
Baboon	17425	49.48	19242	54.60	15242	45.43	21049	56.61	16166	48.43	19224	54.76	18431	52.79	20987	56.59
Plane	61215	85.20	61731	86.21	53796	80.28	69988	87.88	61040	89.78	67649	90.07	66312	89.37	70461	88.90
Boat	31799	76.42	28390	70.95	25963	65.98	33203	77.95	25113	69.64	29220	74.55	29816	76.29	33921	79.30
Goldhill	33006	74.89	34951	76.86	27632	66.35	38044	80.94	31661	77.81	36528	80.89	35323	80.73	38215	81.76
Tiffany	42117	81.66	39939	77.30	37518	73.89	42816	82.20	28969	76.04	35469	79.36	36734	81.07	41463	82.81
Peppers	34710	83.08	34358	81.57	36850	80.49	38066	85.83	23850	70.82	29521	79.31	29875	79.87	38258	86.71
Couple	30581	76.75	29739	75.46	22784	63.89	37724	78.52	32598	81.25	35264	80.68	37082	82.12	37981	80.74
Average	38493	77 23	37034	75 98	33095	69.76	42572	80.02	33275	75 43	38141	78 69	38643	79 27	43132	81 13

TABLE III
PERFORMANCES OF STATIONARY PREDICTORS IN SEPARATE

choice in optimization of predictor coefficients is the least-square (LS) based adaptive prediction, which is also called the autoregressive adaptive prediction [19]–[21]. Also well known is the context-based adaptive prediction [29]. Here, we examine the simpler context-based adaptive prediction first.

Two context-based adaptive predictors are considered in this paper. The first is the 3-order median edge detector (MED) predictor adopted by the lossless image compression standard JPEG-LS [17] and the second is the 4-order gradient-adjusted predictor (GAP) invented for the CALIC codec [18], [22]. MED is a context-based adaptive predictor combining three simple fixed predictors and selecting their median as predicted value. It tends to pick x_n when a vertical edge exists left of the current pixel, or x_w when a horizontal edge exists above the current pixel, or $x_w + x_n - x_{nw}$ when no edge is detected. It is a 3-order piecewise linear predictor

$$\hat{x} = a_1 x_w + a_2 x_n + a_3 x_{nw} \tag{16}$$

where model coefficients $\sum_{i=1}^{3} a_i$ are adaptively adjusted in the following manner.

$$\begin{array}{lll} \text{if} & x_{nw} \geq x_n \geq x_w & \text{or} & x_{nw} \leq x_n \leq x_w \\ & a_1 = 1, a_2 = a_3 = 0 & \text{(horizontal edge)} \\ \text{elseif} & x_{nw} \geq x_w \geq x_n & \text{or} & x_{nw} \leq x_w \leq x_n \\ & a_2 = 1, a_1 = a_3 = 0 & \text{(vectical edge)} \\ \text{else} & \\ & a_1 = a_2 = 1, a_3 = -1 & \text{(no edge)} \end{array} \tag{17}$$

In (17), the process of classifying a pixel into one of the three cases requires at most three comparisons, and the calculation of the predicted value needs at most two adds.

The GAP predictor is a 4-order piecewise linear predictor

$$\hat{x} = a_1 x_w + a_2 x_n + a_3 x_{nw} + a_4 x_{ne}. \tag{18}$$

It divides the intensity gradients near the predicted pixel into seven cases and adjusts the four model coefficients accordingly. The intensity gradients are estimated with horizontal and vertical intensity gradient indicators

$$d_{h} = |x_{w} - x_{ww}| + |x_{n} - x_{nw}| + |x_{n} - x_{ne}| d_{v} = |x_{w} - x_{nw}| + |x_{n} - x_{nn}| + |x_{ne} - x_{nne}| , (19)$$

. and the seven cases are sharp horizontal edge, sharp vertical edge, horizontal edge, vertical edge, weak horizontal edge, weak vertical edge, and no edge. Let $\Delta d=d_v-d_h$ be the criterion for classifying intensity gradient, the four coefficients

of GAP are adjusted accordingly in (20).

if
$$\Delta d > 80$$
 (sharp horizontal edge) $a_1 = 1, a_2 = a_3 = a_4 = 0$ elseif $\Delta d > 32$ (horizontal edge) $a_1 = 3/4, a_2 = 1/4, a_3 = -1/8, a_4 = 1/8$ elseif $\Delta d > 8$ (weak horizontal edge) $a_1 = 5/8, a_2 = 3/8, a_3 = -3/16, a_4 = 3/16$ elseif $\Delta d \geq -8$ (no edge) $a_1 = 1/2, a_2 = 1/2, a_3 = -1/4, a_4 = 1/4$ elseif $\Delta d \geq -32$ (weak vertical edge) $a_1 = 3/8, a_2 = 5/8, a_3 = -3/16, a_4 = 3/16$ elseif $\Delta d \geq -80$ (vertical edge) $a_1 = 1/4, a_2 = 3/4, a_3 = -1/8, a_4 = 1/8$ else (sharp vertical edge) $a_2 = 1, a_1 = a_3 = a_4 = 0$

During the computation of GAP, we substitute conditional statement (comparison) for absolute function and decompose fixed multiplications 3x, 6x and 10x into (x + x << 1), (x + x << 1) << 1, and (x + x << 2) << 1. So we need 6 comparisons plus 11 adds to obtain Δd and at most 7 adds plus 7 shifts to calculate the predicted value. Experimental results of MED and GAP is given in Table IV. It is argued in [29] that the 3-order MED is contrarily better than the 4-order more complicated GAP for predictive image compression. However, in reversible image watermarking, the result is different. For bitshifting prediction-error expansion, GAP has larger IB than MED in average, and for additive prediction-error expansion, GAP leads MED by about 3300 in IA. It is worth notice that the simplified GAP (SGAP) considered in Sect. IV-A presents larger IA than that of MED, but with much less computation. That is why it was highlighted in [9]. Although the running time of MED and GAP is longer than those of the stationary predictors, it is still fast to finish the whole computation within less than 100ms.

C. LS-based Adaptive Prediction

Early research efforts have already demonstrated the effectiveness of both one-dimensional (1D) and two-dimensional (2D) autoregressive models for adaptive predictive coding of digitized images [28], [30]. 1D models offer advantages of simplicity, while 2D models have superior modeling capability. In [31], Das and Loh offered a tradeoff between the two by proposing two 1D multiplicative autoregressive models, which provide comparable performance to 2D models at a

TABLE IV
PERFORMANCES OF CONTEXT-BASED ADAPTIVE PREDICTORS

Image	M	ED	G.	AP	
	IA	IB (%)	IA	IB (%)	
Lena	56822	91.69	63703	92.46	
Baboon	20360	56.42	21685	58.22	
Plane	68921	90.81	71741	90.74	
Boat	31955	79.09	35046	81.66	
Goldhill	38941	83.70	39670	83.87	
Tiffany	39563	82.81	42076	83.94	
Peppers	32467	82.91	38199	87.00	
Couple	37365	86.20	40908	85.35	
Average	40799	81.70	44129	82.91	
Time(ms)	36		92		

low complexity level. Later, Wu et al [19] proposed a so called piecewise 2D autoregression (P2AR) as an alternative to their GAP predictor in CALIC image coder [18], in which extra computation is traded for lower bit rate. They also developed a fast algorithm for computing and updating covariance of regression variables on a pixel-by-pixel basis to make their scheme computationally feasible. It is studied in edgedirected prediction (EDP) [20] that the LS-based adaptive prediction owes its superiority to the better adaptation around the edge compared with context-based adaptive prediction. Based on this discovery, the computational complexity of LSbased adaptive prediction is further reduced by performing the autoregression on a edge-by-edge basis instead of on the pixel-by-pixel basis. Inspired by the same edge-directed feature of LS-based prediction, Kau and Lin [21] proposed a edge detector to foretell the existence of edges. In the socalled edge-look-ahead (ELA) scheme, only when an edge is detected in advance will the autoregression be performed. The edge detector works fine and their scheme provides better compression ratio than the EDP scheme does. It is also proved in [21] that the performance of ELA is quite near the case when autoregression is performed pixel-by-pixel. In this paper, we consider ELA to study the model order selection problem of LS-based adaptive prediction in reversible image watermarking.

Suppose N is the order of prediction model and M is the number of pixels within the training area of the autoregression process. The LS-based adaption process is to find a LS solution for equation

$$\mathbf{Pa} = \mathbf{y} \tag{21}$$

where

$$\mathbf{P} = \begin{bmatrix} x_{i-1}(1) & x_{i-1}(2) & \cdots & x_{i-1}(N) \\ x_{i-2}(1) & x_{i-2}(2) & \cdots & x_{i-2}(N) \\ \vdots & \vdots & \ddots & \vdots \\ x_{i-M}(1) & x_{i-M}(2) & \cdots & x_{i-M}(N) \end{bmatrix}$$
(22)

is an $M \times N$ matrix with its jth-row kth-column element being the kth predictor coefficient of the jth nearest pixel of x_i , $\mathbf{a} = [a_1, a_2, \dots, a_N]^T$ is the ith coefficient vector to be determined, and $\mathbf{y} = [x_{i-1}, x_{i-2}, \dots, x_{i-M}]^T$ is the vector of x_i 's M training pixels. The LS solution to (21) is

$$\mathbf{a} = (\mathbf{P}^{\mathbf{T}}\mathbf{P})^{-1}\mathbf{P}^{\mathbf{T}}\mathbf{y}.\tag{23}$$

If **P** is of rank N, which is the generally case, (23) can be solved with Cholesky decomposition at a cost of about $N^3/6$ multiplications. Otherwise, it can be solved with the more complicated singular value decomposition (SVD). It is noted that the calculation of a involves matrix multiplication and is thus costly in computation. If undertaken pixel-by-pixel, the whole scheme becomes impractical. Considering the adaption mainly takes effect around edges [20], it is performed only when an edge is detected by the proposed detector in [21] or the prediction-error is larger than a predefined threshold.

For LS-based prediction, the order N can assume various values below M. For predictive image compression, better performances are reported when higher model orders are adopted in [21]. To obtain the results for reversible image watermarking, we have implemented and tested ELA on standard test images when different orders are set. The results are presented in Table V. Being quite different from the cases in predictive image compression, IB and IA are both optimal when the model order is four, i.e. N=4. This conclusion almost holds in separate for each of the eight images. This outcome strongly disagrees with the fact that higher order prediction takes more pixels into account and consumes more computation. However, this is reasonable. Since reversible image watermarking expands merely tiny prediction-errors, only when the prediction works accurately will the resulting prediction-error be eligible for data embedding. As we know, prediction of the value of a pixel is a somewhat guess work based on the values of its neighbors. So prediction is precise only when there is correlation between the pixel and its neighbors. In smooth areas, the correlation is close and linear. Generally, smoothness happens most frequently within small local areas. When the prediction context goes larger, though it is possible to make prediction more reasonable through LS estimation, it is difficult to make precise prediction, namely it is hard to obtain a small prediction-error. Even the entropy of the whole prediction-errors decreases as model order becomes up to 4 or higher, the proportion of small predictionerrors (small enough to be expandable) goes down instead. So if LS-based prediction is considered for reversible image watermarking, 4 is likely to be a proper model order that promises an appropriate tradeoff between model-fitness and computational complexity. When the optimal model order 4 is assumed, both IB and IA are better than the cases of contextbased adaptive predictions. However, the improvement seems to be quite costly with such a long running time.

V. HIGH-ORDER MODELING IN REVERSIBLE IMAGE WATERMARKING

Though being one of the oldest and most successful modeling tools in data compression, prediction alone cannot achieve total decorrelation. Many excellent predictive image compression schemes (e.g., [17], [18], [22]) use some form of context modeling (i.e. encoding based on higher order conditional probability models) [26] to further exploit correlation following the prediction stage. With the high-order context modeling technique, prediction-errors can be corrected via an error feedback mechanism by learning from its mistakes

Image	N	= 2	N	= 4	N	= 6	N	= 8	N :	= 10
	IΑ	IB (%)	IA	IB (%)	IΑ	IB (%)	ΙA	IB (%)	IΑ	IB (%)
Lena	54754	93.71	61243	95.29	60918	94.67	59404	93.68	57915	91.70
Baboon	22113	63.12	23650	65.46	23235	63.65	21644	59.87	19066	53.36
Plane	60243	91.66	63452	92.51	64116	91.71	62284	90.33	60421	87.52
Boat	33596	84.08	38523	87.56	38898	86.82	37704	84.96	34968	80.29
Goldhill	39037	86.23	40287	86.49	39487	85.26	37656	82.54	34268	77.15
Tiffany	41259	86.02	43737	89.18	43310	88.11	41423	86.16	38499	82.52
Peppers	36797	88.65	45090	92.28	45646	91.31	43995	89.72	40475	85.99
Couple	40658	87.96	41007	88.44	40330	86.83	37953	84.13	34243	78.93
Average	41057	85.18	44624	87.15	44493	86.05	42758	83.92	39982	79.68
Time(s)	10	0.9	1	1.8	1.	3.2	1.	3.5	1	7.9

 $\label{thm:constraint} TABLE\ V$ Performances of ELA prediction with different model orders

under a given context in the past [18], [22]. This means smaller prediction-errors can be obtained with context modeling, which can in turn boost the performance of reversible image watermarking. In this section, we apply this high-order modeling technique to reversible image watermarking and study how implementation complexity and performance is influenced. The specific context modeling process we are discussing here is the CALIC scheme [18], which works on the basis of GAP.

A. Context Formation and Error Feedback

The prediction stage only removes part of the redundancy in the image. Another form of redundancy lies in the correlation between the variance of prediction-errors and the variance of prediction context around the predicted pixel. To model this correlation, an error energy estimator

$$C_v = d_h + d_v + 2|e_w|, (24)$$

is defined to represent the variance of prediction context. In (24), $e_w = x_w - \hat{x}_w$ is the prediction-error of the previous pixel x_w , d_h and d_v are from (19). For predictive image compression, C_v is also the coding context, on which the prediction-error is conditioned during entropy coding. This is because coding $p(e|C_v)$ is more efficient than coding merely p(e). To be efficient in practical application, C_v is quantized into 8 levels with the following quantizer

$$Q(C_v) = \begin{cases} 0 & , & 0 \le C_v < 5\\ 1 & , & 5 \le C_v < 15\\ 2 & , & 15 \le C_v < 25\\ 3 & , & 25 \le C_v < 42\\ 4 & , & 42 \le C_v < 60\\ 5 & , & 60 \le C_v < 85\\ 6 & , & 85 \le C_v < 140\\ 7 & , & 140 \le C_v \end{cases}$$

$$(25)$$

There is also redundancy within higher order image structures like texture patterns and local activity that can be further decorrelated. So, texture context C_t representing the texture pattern of prediction context is formed as well

$$C_t = (c_0, c_1, c_2, c_3, c_4, c_5, c_6, c_7)$$

$$= (x_n, x_w, x_{nw}, x_{ne}, x_{nn}, x_{ww}, 2x_n - x_{nn}, 2x_w - x_{ww})$$
(26)

It is then quantized to an 8-bit number $B=Q(C_t)=b_7b_6b_5b_4b_3b_2b_1b_0$ using the predicted value \hat{x} as threshold in (27), where c_k is the kth component of C_t .

$$b_k = \begin{cases} 0 & , & c_k \ge \hat{x} \\ 1 & , & c_k < \hat{x} \end{cases} \quad 0 \le k \le 7 \tag{27}$$

By combining the quantized error energy $\delta = \lfloor Q(C_v)/2 \rfloor$ $(0 \le \delta < 4)$, and the quantized texture context $\beta = Q(C_t)$ $(0 \le \beta < 144)$ [18], compound modeling contexts, denoted by $C(\delta, \beta)$, are eventually formed.

The error feedback mechanism of context modeling works in this way: during prediction of every pixel x, we predict its value \hat{x} with GAP and model its context to get $C(\delta,\beta)$, then we study the prediction bias of former pixels within the same context and add it to \hat{x} . Prediction bias of each compound context is measured with the conditional expectations of prediction-error, i.e. $E(\epsilon|C(\delta,\beta))$. It is approximated with the corresponding sample means $\bar{\epsilon}(\delta,\beta)$, which involves only accumulating the prediction-errors in each compound context and counting the occurrence of each context. For each compound context $C(\delta,\beta)$, we denote by $N(\delta,\beta)$ the occurrence, and by $S(\delta,\beta)$ the sum of prediction-errors. Every time when a compound context $C(\delta,\beta)$ is encountered, we calculate the sample mean with

$$\bar{\epsilon}(\delta, \beta) = S(\delta, \beta)/N(\delta, \beta).$$
 (28)

Then we obtain the new predicted value \dot{x} and its error ϵ through

$$\dot{x} = \hat{x} + \bar{\epsilon}; \quad \epsilon = x - \dot{x},$$
 (29)

where \hat{x} is the predicted value of x given by GAP, and $\bar{\epsilon}$ is the sample mean of the compound context of x. After that, the corresponding $S(\delta,\beta)$ and $N(\delta,\beta)$ are updated with the new prediction-error ϵ

$$S(\delta, \beta) = S(\delta, \beta) + \epsilon; N(\delta, \beta) = N(\delta, \beta) + 1. \tag{30}$$

To reduce the memory use, once $N(\delta, \beta)$ reaches 128, $S(\delta, \beta)$ and $N(\delta, \beta)$ are rescaled by setting

$$S(\delta, \beta) = S(\delta, \beta)/2; N(\delta, \beta) = 64. \tag{31}$$

Rescaling is an inexpensive way of adapting the context error model to time-varying sources, which has the benefit of aging the observed data.

TABLE VI
PERFORMANCE OF CALIC PREDICTION WITH CONTEXT MODELING

Image	ΙA	IB (%)
Lena	65257	93.25
Baboon	22291	59.59
Plane	72835	91.68
Boat	38326	83.87
Goldhill	41404	84.70
Tiffany	43126	84.94
Peppers	43356	88.92
Couple	42379	86.48
Average	46122	84.18
Time(ms)	2	30

B. Reversible watermarking with Context Modeling

For reversible watermarking with context modeling, the difference to be expanded is ϵ . After data is embedded with expansion, ϵ becomes ϵ' , and the watermarked pixel becomes $x' = \dot{x} + \epsilon'$. Since prediction and context modeling use only causal pixel, using the same method we can recalculate the same \dot{x} during extracting. With \dot{x} , it is easy to obtain ϵ' and then to extract data and restore ϵ through the inverse expansion. Finally, we recover the original pixel by $x = \dot{x} + \epsilon$.

In the process of the CALIC context modeling, the model order can go as high as 128. If the aging effect brought by rescaling is considered, the model order can be even higher. However, the computational complexity is well controlled with proper quantization and reasonable approximation. It is analyzed in [18] that computation of the whole CALIC prediction process, including GAP and the context modeling, requires no more than 13 adds, 1 muls, 5 shifts, 17 comparisons, and 3 absolute operations. We have also implemented the CALIC prediction on Matlab. The results are presented in Table VI. The running time of the CALIC prediction is about 230 milliseconds for a 512×512 grayscale image in average. It is a slow process if compared with MED or GAP, but it is rather fast if we are comparing it with ELA. If implemented with faster programming language like C, the CALIC prediction is expected to run faster and can become feasible in real application on modern computers. Most importantly, CALIC prediction provides the best performance for additive expansion, i.e. the largest IA, among all predictors considered so far, even better than that of ELA with the optimal model order. Its performance for bitshifting expansion is also better than MED and GAP, but not as good as ELA.

VI. FULL CONTEXT PREDICTION IN REVERSIBLE IMAGE WATERMARKING

By far, all predictors we have discussed, including the CALIC context modeling technique, are directly borrowed from predictive image compression. These modeling tools share one feature in common. That is, all of them are confined to utilize a half enclosing context containing only causal pixels. This situation is due to the fact that when it is required to reconstruct the same predicted values during the extracting process, only causal pixels are available or restored at that moment. This fact has greatly constrained the accuracy of prediction. To overcome this restriction, some image compression schemes tried to provide a completely enclosing context via

interlaced prediction [22], or hierarchical interpolation (HINT) [32]. However, in almost all of them, a part of the pixels need to be predicted ahead in a less accurate manner, which induces performance inefficiency. Instead, for reversible watermarking with additive prediction-error expansion, there exists a highly efficient strategy to achieve the same goal. With this strategy, it is able to build a full context for all pixels, so excellent model-fitness can be achieved at a very low implementation complexity. This is called full context prediction.

A. Formation of Full Context

Quite recently, we found it is possible to fully exploit watermarked pixels to build a full prediction context containing all the eight nearest pixels, which produces a novel reversible image watermarking scheme demonstrated of very competitive performances [10]. The motive of the idea is intuitive. The reason why predictive image compression utilizes only causal pixels is later processed pixels, i.e., non-causal pixels, are completely unknown when they are needed to recalculate the same predicted values. However, this is not the case in reversible image watermarking. During the watermark extracting process, it is true that non-causal pixels are not known in exact, but what different is that we know the watermarked values of those non-causal pixels. Moreover, to guarantee high image fidelity, watermarking only modify pixels within a very small range. Particularly, the additive expansion changes pixels at most by 1 (see (9)). It means, even watermarked, pixels are still very close to their original values, namely they are still of significant correlation with the predicted pixels. By exploiting this correlation remained in watermarked pixels, we can promote the prediction accuracy to a higher level. With this in mind, we present a approach, which utilizes non-causal watermarked pixel to provide a full prediction context.

To build full contexts for all predicted pixels, the host image is first divided into four subimages. Let the host image be $I=\{x(i,j)|1\leq i\leq H, 1\leq j\leq W\}$ and W and H be the width and height. The four subimages are

$$\begin{array}{lll} U_1 & = & \{x(2i,2j) & | & 1 \leq i \leq H', 1 \leq j \leq W'\} \\ U_2 & = & \{x(2i,2j+1) & | & 1 \leq i \leq H', 1 \leq j \leq W'\} \\ U_3 & = & \{x(2i+1,2j) & | & 1 \leq i \leq H', 1 \leq j \leq W'\} \\ U_4 & = & \{x(2i+1,2j+1) | & 1 \leq i \leq H', 1 \leq j \leq W'\} \end{array} \tag{32}$$

where $W' = \lfloor (W-2)/2 \rfloor$ and $H' = \lfloor (H-2)/2 \rfloor$. Now, considering the four subimages separately, we can construct full contexts for all pixels of all subimages. Without loss of generality, we process the subimages in the sequence of U_1 , U_2 , U_3 , and U_4 , namely we watermark U_2 after U_1 is watermarked and so forth. For a pixel in every single subimage, its full contexts consist of the eight nearest pixels, which are within the other three subimages. Let U_k be the kth subimage to be watermarked and U_k' be the watermarked result of U_k , then the full contexts of U_k contains pixels in $U_1' \dots U_{k-1}' U_{k+1} \dots U_4$. In the above case, the full contexts of the four subimages U_1 , U_2 , U_3 , and U_4 are formed by pixels in $U_2U_3U_4$, $U_1'U_3U_4$, $U_1'U_2'U_4$ and $U_1'U_2'U_3'$. After all subimages are processed, we obtain four watermarked

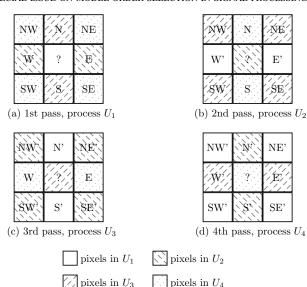


Fig. 4. Full context prediction. This figure depicts the data embedding process of the four subimages, which are considered separately in sequence. Watermarked pixels, marked with apostrophe, are also utilized to form prediction context. All pixels in (a) are original; x_w and x_e in (b) are watermarked; x_{nw} , x_{ne} , x_{sw} and x_{se} in (c) are watermarked; all pixels (except x) in (d) are watermarked.

subimages $U_1'U_2'U_3'U_4'$ and the resulting watermarked image I' as a whole. The whole process is also illustrated in Fig. 4.

To extract watermark and restore the original host, we divide the watermarked image I' into the same four subimages and consider them separately in the inverse order, i.e. in the sequence of U_4' , U_3' , U_2' , and U_1' . For each subimage U_k' , we extract embedded data from it and recover U_k' to U_k through the inverse transform of additive prediction-error expansion. When U_k' is being processing, subimages $U_1' \dots U_{k-1}'$ are still watermarked, whereas subimages $U_{k+1} \dots U_k$ are already restored. Therefore, we can reconstruct full contexts for U_k' using pixels from $U_1' \dots U_{k-1}' U_{k+1} \dots U_k$, which are the same as in the embedding process. Finally, we restore all four subimages $U_1U_2U_3U_4$ and the original image I as a whole.

B. Reversible Watermarking with Full Context

Based on the full context we provide in the previous section, we can develop some new predictors for reversible image watermarking using additive prediction-error expansion. To study the model order selection problem of prediction with full context, we consider four different predictors which are derived from the seven different prediction modes in JPEG. We name them FP1, FP2, FP3 and FP4 respectively. FP1 is a 4-order predictor formulated as

$$\hat{x} = \frac{x_w + x_s + x_e + x_n}{4}. (33)$$

FP1 can be deemed as a full context version of predictor JM1, JM2 and JM7. FP2 is a 4-order predictor derived from JM3

$$\hat{x} = \frac{x_{sw} + x_{se} + x_{nw} + x_{ne}}{4}.$$
 (34)

FP3 is a 8-order predictor corresponding to JM4

$$\hat{x} = \frac{2x_w + 2x_s + 2x_e + 2x_n - x_{sw} - x_{se} - x_{nw} - x_{ne}}{4}.$$
(35)

TABLE VII PERFORMANCE OF FULL CONTEXT PREDICTION

Image	FP1	FP2	FP3	FP4
Lena	70675	62011	53381	63645
Baboon	24682	19741	22401	24619
Plane	78346	66259	70935	78013
Boat	38476	35025	28499	34532
Goldhill	45678	35766	38973	44354
Tiffany	47064	40233	38223	44049
Peppers	39877	49841	23593	30278
Couple	43485	32275	41946	45268
Average	48535	42644	39744	45595
Time(ms)	6.6	5.6	12.3	13.0

It is also easy to obtain the full context counterpart of JM5 and JM6 as

$$\hat{x} = \frac{3x_w + 3x_s + 3x_e + 3x_n - x_{sw} - x_{se} - x_{nw} - x_{ne}}{8},$$
(36)

which is FP4 of order 8. All these four predictors are simple and easy in computation. FP1 and FP2 involve only 3 adds and 1 shift, FP3 involves 7 adds and 2 shifts, and FP4 needs 11 adds and 2 shifts. Their performances in reversible image watermarking have been tested, and the results are given in Table VII. We note that only IA is covered in Table VII because full context prediction is particular to additive prediction-error expansion. It is clear that FP1 stands out as the best predictor with full context despite the fact that it is 4-order and utilizes only the four nearest pixels. It is best in average and separately for six of all eight test images among the four predictors. Most importantly, FP1 possesses the best performance among all predictors we considered in this paper, even better than the more complicated ELA and the high-order CALIC. What is more, it runs really fast.

VII. EXPERIMENTAL RESULTS

So far, we have discussed the model order selection problem in specially derived criteria. To evaluate our study in standard criteria, we present the performances of concrete reversible watermarking schemes with embedding capacity and image quality measured in number of bits and PSNR values. First, we will validate our study by justifying our criteria of IB and IA with standard performances criteria in reversible watermarking. Then, to establish the competitiveness of our study, we compare performances of our schemes with other state-of-theart schemes in standard criteria.

A. Validation of IB and IA

It is discussed in Section III that our criteria IB and IA are capable of judging watermarking performances of embedding capacity and image quality in a correct and unitary manner. Here, we qualify them with experimental results. Consider IB first. Instead of examining all models again, we choose the top three predictors that provide the largest IB. They are the 4-order LS-based adaptive predictor ELA (IB=87.15%), the high-order predictor CALIC (IB=84.18%) with context modeling, the 4-order context-based adaptive predictor GAP (IB=82.91%). We have implemented reversible watermarking schemes using bitshifting prediction-error expansion with the

TABLE VIII
PERFORMANCES OF BITSHIFTING PREDICTION-ERROR EXPANSION
SCHEMES

Schemes	ELA		CAL	IC	GAP		
	Capacity	PSNR	Capacity	PSNR	Capacity	PSNR	
Lena	201211	37.2	185293	37.3	180824	37.2	
Baboon*	68934	31.0	69721	30.2	60994	30.2	
Plane	181011	37.4	173085	37.8	167639	37.8	
Boat	115595	35.5	77338	35.3	57408	35.2	
Goldhill	106106	35.7	85173	35.5	77587	35.4	
Tiffany	133795	36.1	105105	35.9	99859	35.9	
Peppers	155929	35.9	122438	35.5	101374	35.2	
Couple	127074	35.8	106361	35.7	96306	35.6	
Average	136207	35.6	115564	35.4	105241	35.3	
IB	87.15%		84.18	3%	82.91%		

^{*}The threshold for the complex image Baboon is adjusted to 20, or else the compressed location map is even larger than the capacity it can provide.

TABLE IX
PERFORMANCES OF ADDITIVE PREDICTION-ERROR EXPANSION SCHEMES

Schemes	FP1		CAL	IC	ELA		
	Capacity	PSNR	Capacity	PSNR	Capacity	PSNR	
Lena	70599	49.6	65229	49.5	61215	49.5	
Baboon	24606	48.6	22263	48.6	23622	48.7	
Plane	78258	50.1	72803	49.9	63419	49.6	
Boat	38384	48.9	38288	48.9	38484	49.0	
Goldhill	45602	49.0	41376	48.9	40259	49.0	
Tiffany	44466	49.1	40310	49.1	41164	49.2	
Peppers	39791	48.9	43324	49.0	45058	49.1	
Couple	43160	49.0	42170	49.0	40793	49.1	
Average	48108	49.1	45720	49.1	44251	49.1	
IA	48535		461	22	44624		

three different predictors. The experiment results are tabulated in Table VIII, where threshold T=10 and embedded data is a random bit sequence. The listed capacities are pure capacity, which have deducted overhead cost including JBIG2 compressed location map. Note that we have employed the technique in [24] to make location maps more compressible. It is verifiable in our results that larger IB indicates larger capacity and higher PSNR.

We adopt the same strategy to evaluate IA. The top three predictors that provide the largest IA are the 4-order full context predictor FP1 (IA=48535), the high-order predictor CALIC (IA=46122) with context modeling, and the 4-order LS-based adaptive predictor ELA (IA=44624). From the experimental results shown in Table IX, we can see that IA approximates the pure capacity for every single image and for all in average. As to the image quality, the PSNR values obtained by the three predictors are the same in average.

B. Performance Comparisons

In this subsection, the proposed reversible watermarking schemes are compared with other state-of-the-art schemes to demonstrate the merits of our study. The proposed reversible watermarking scheme we considered here is the one with full context prediction, in which we take every subimage as a single embedding plane. Two other schemes are implemented for comparison. The first is the one proposed by Lin et al in [33], which embeds bits into three-pixel differences. As far as we know, it provides the largest pure embedding capacity at low PSNR standards among the schemes reported in other

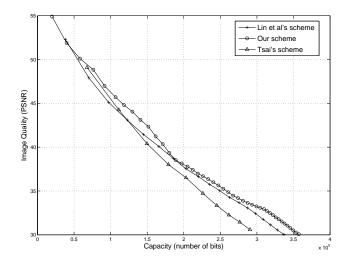


Fig. 5. Performance comparison. The test image is 8-bit grayscale Lena.

literature. The other scheme compared is proposed by Tsai et al in [11], which is the latest scheme using prediction-error expansion. Tsai et al's scheme uses a linear predictor for calculation of prediction-error. However, the exact form of the linear predictor is not given in their paper. In our implementation, we take the best linear predictor, namely the SGAP, to be the one. The results are shown in Fig. 5, where our scheme provides larger capacities than the other two at both low and high PSNR standards.

VIII. CONCLUSION

This paper presents a practical study of the model order selection problem in reversible image watermarking. The reversible image watermarking schemes considered here are a set of state-of-the-art schemes with good performance in both embedding capacity and image quality, which utilize prediction-error expansion for data embedding. Two involved modeling tools, namely prediction and context modeling, are studied, and the related tradeoff problems between modelfitness and implementation complexity are examined. To arrive at a proper model order that well balances the system performance and the implementation complexity, we have considered different models with the corresponding model orders varying from low to high. Among considered classic predictors intended for predictive image compression, the CALIC, which combines the GAP prediction with a context modeling, stands out as the best choice. For reversible image watermarking using prediction-error expansion, it provides the most competitive model-fitness with relatively low complexity despite its high model order. Besides, we have studied a special prediction specific to reversible image watermarking using additive prediction-error expansion, which is named full context prediction. It makes full use of watermarked pixels to build a prediction context completely enclosing the predicted pixel. The prediction accuracy is thus greatly improved. Hence, a simple stationary 4-order full context predictor is capable of providing even better performance than the CALIC predictor at a negligible computational cost.

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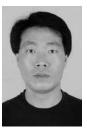
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Ming Chen received his B.S. degree in Computer Science and Technology from Beihang University, Beijing, China, in 2007. He is currently pursuing the M.S. degree in Computer Science in the School of Computer Science and Engineering, Beihang University, Beijing, China.

His research interests include multimedia security and wireless sensor network.



Zhenyong Chen received his B.S. and Ph.D. degree in Precision Instruments and Mechanology from Tsinghua University, Beijing, China, in 1998 and 2003 respectively. He was a Postdoctoral researcher in Department of Computer Science and Technology, Tsinghua University, from 2004 to 2005. Since 2006, he is an associate professor of the School of Computer Science and Engineering of Beihang University.

His research interests include information hiding, digital watermarking, and digital rights management.



Xiao Zeng received his B.S. degree in Computer Science and Technology from Beihang University, Beijing, China, in 2004. He is currently pursuing the Ph.D. degree in Computer Science in the School of Computer Science and Engineering, Beihang University, Beijing, China.

His research interests include digital watermarking, digital rights management, and multimedia signal processing.



Zhang Xiong received his M.S. degree in Computer Science from Beihang University, Beijing, China, in 1984. He became a teacher in Beihang University since 1984. From 1989 to 1992, he was a visiting professor in Michigan State University, MI, USA. He is currently a professor in Beihang University, Beijing, China.

His research interests include multimedia signal processing and software engineering.