

1

Describe informally the languages accepted by the following FAS:

b.

It only has one end state. It represents any pattern of 1s or 0s, but doesn't have a pattern for 10 or 01 after s_1 and s_2 which will be followed by a sequence of 00 and 11 respectively.

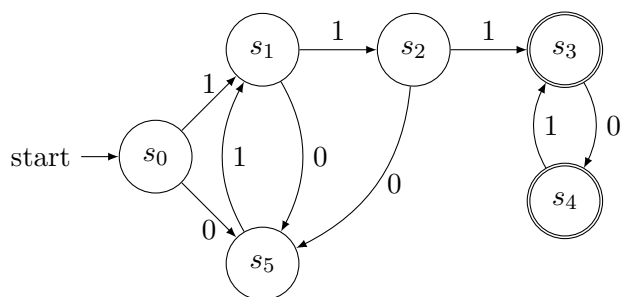
c.

Will contain a lot of a's and b's. Subset of aab and baa will appear.

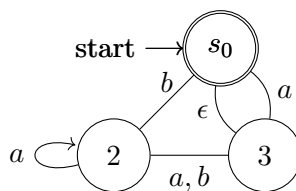
2

Construct an FA accepting each of the following languages:

- b. $w \in \{0,1\}^* | w$ contains '111' as a substring and does not contain '00' as a substring



- c. $w \in \{a,b,c\}^* | \#a \pmod 2 = \#b \pmod 3$



4

Different programming languages use different notations to represent integers. Construct a regular expression for each one of the following:

c. Currency, in dollars, represented as a positive decimal number rounded to the nearest one-hundredth. Such numbers begin with the character \$, have commas separating each group of three digits to the left of the decimal point, and end with two digits to the right of the decimal point, for example, \$8,937.43 and \$7,777,777.77.

$$\$([1 \dots 9]([0 \dots 9]|\epsilon)([0 \dots 9]|\epsilon)(, [0 \dots 9][0 \dots 9][0 \dots 9])^*|0) . [0 \dots 9][0 \dots 9]$$

5

Write a regular expression for each of the following languages:

e. Given an alphabet $\Sigma = \{+, -, \times, \div, (,), \text{id}\}$, L is the set of algebraic expressions using addition, subtraction, multiplication, division, and parentheses over **ids**.

$$L = \text{id} \left((+ | - | \times | \div) \text{id} \right)^+$$

An exception is that parenthesis cannot be matched with regular expression.

7

Consider the three regular expressions:

$(ab|ac)^*$

$(0|1)^*11001^*$

$(01|10|00)^*11$

- a. Use Thompson's construction to construct an NFA for each RE.

- b. Convert the NFAs to DFAs.

- c. Minimize the DFAs.