

# ECE 477: Sound Source Localization

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Binaural Hearing



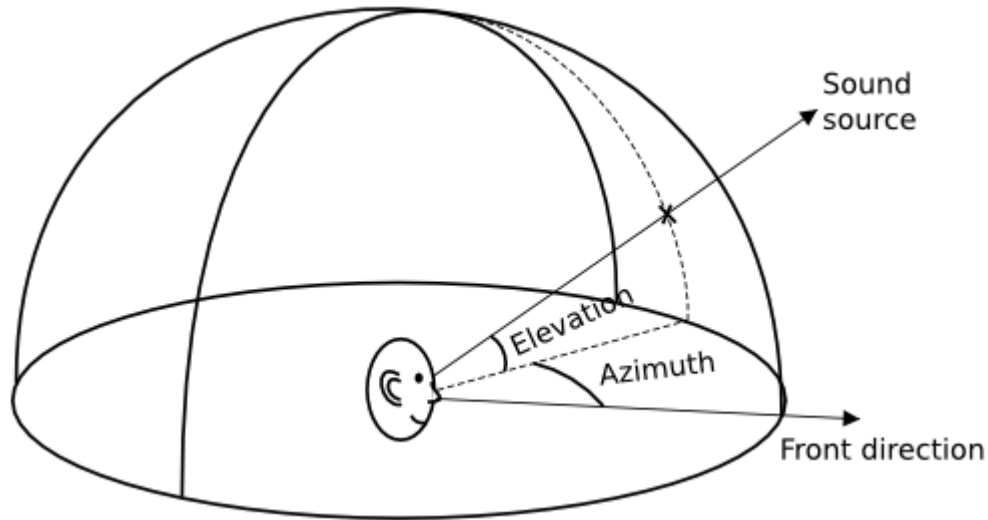
Monaural Hearing



# Outline:

- 1) Sound Localization and Its Importance
- 2) Early History of Sound Localization
- 3) Current Approaches and Algorithms
  - a) Cross-Channel Algorithm
  - b) Monaural Source Separation for Localization
  - c) Deep Convolutional Neural Networks (DCNN)
  - d) Probabilistic Neural Networks (PNN) and Cross-Correlation
  - e) Comparison of Main Approaches
- 4) Limitations of Past and Present
- 5) Future Directions

# Aim of Sound Source Localization



Human Auditory Model



Computer Auditory Scene  
Analysis

# IMPORTANCE

## Difficulties Experienced By Hearing Aid and Cochlear Implant Users

Speech Understanding in Noise

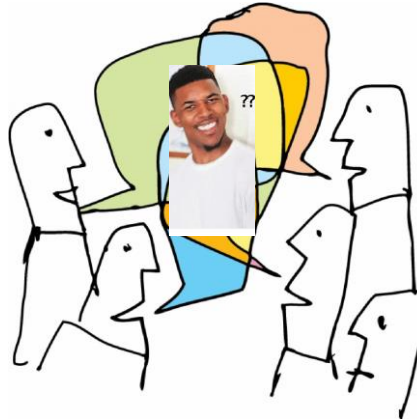
Localization in Noise



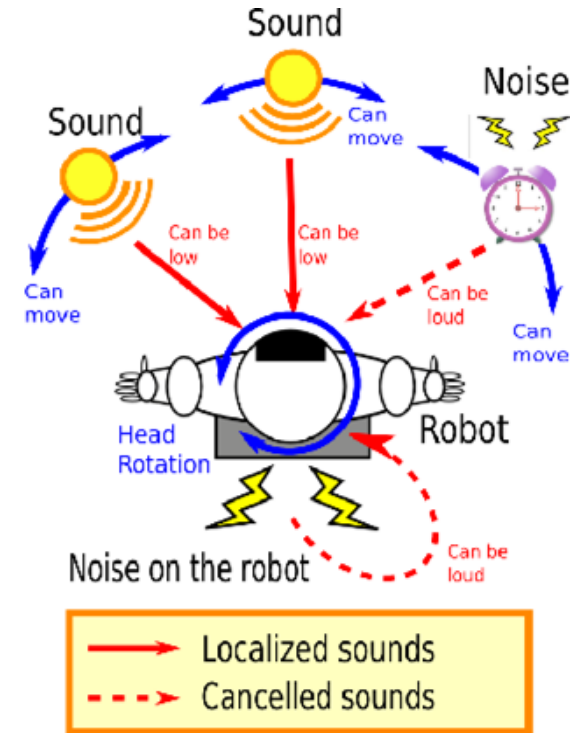
Cochlear Implant User

## Sound Source Localization in Robotics

Human Interaction



"Cocktail Party Problem"



1. Kerber and Seeber (2012)
2. Rascon et al. (2017)

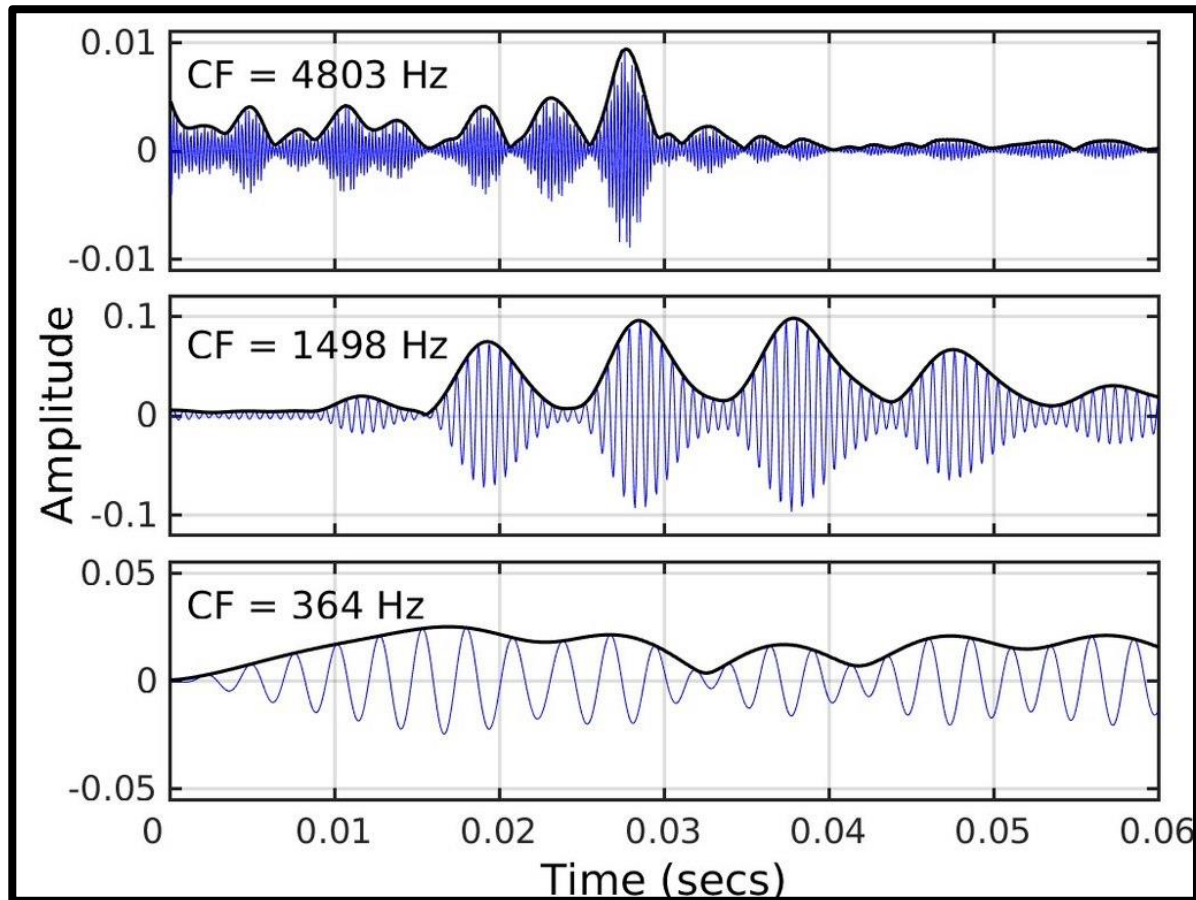
## Acoustic Cues

Interaural Level Differences  
(ILDs)

Interaural Time Differences  
(ITDs)

in the envelope (speech)

in the waveform (pitch & music)



1. Kerber and Seeber (2012)
2. Michael Stone (2018)

# Early History of Sound Localization:

*XII. On Our Perception of Sound Direction - Lord Rayleigh, 1907*

*The localization of actual sources of sound - S.S Stevens and E.B.*

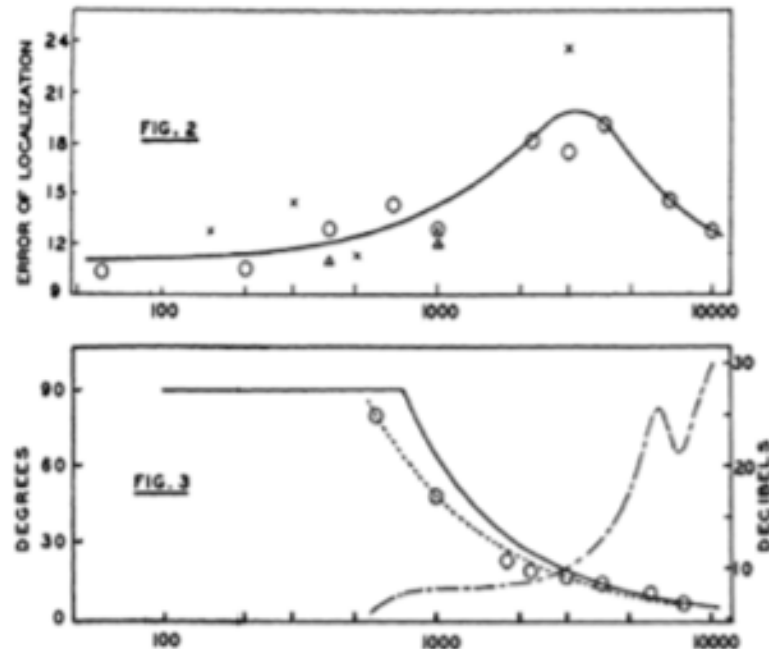
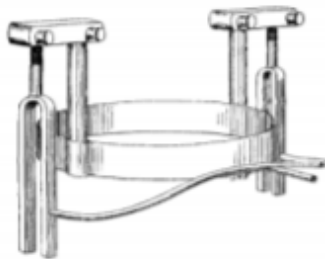
*Newman, 1934*

**Early papers establishing the basis behind ITD and ILD**

Low frequency sounds are accounted by phase differences (ITD)

High frequency sounds are accounted for by level differences (ILD)

Intermediate range where localization is poorest



**Figure 1: A)** Early designed tuning forks attached to the head for localization studies **B)** stimulus generation of pure tones conducted on a pedestal (on the roof of the Harvard Biology building) **C)** Plots depicting error of localization in respect to phase and level.

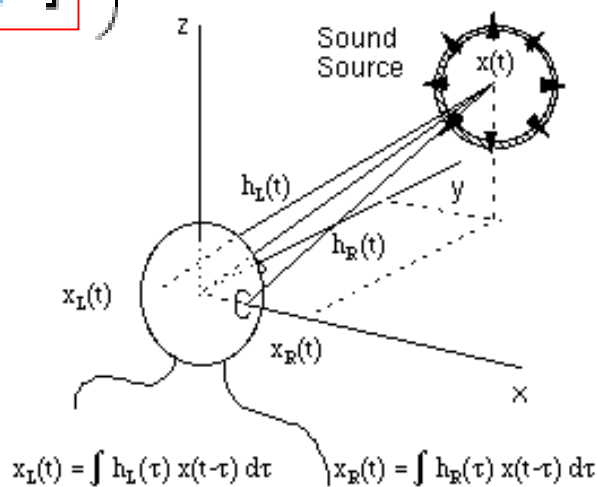
# MacDonald & Tran (2006): Cross-Channel Sound Localizer

Head-Related Transfer Functions (1 for each microphone, ).

Inverse algorithm

$$\min_{\hat{\theta}, \hat{\phi}} \sum \left( R_{Left} * \left[ H_{Left}^{(\hat{\theta}, \hat{\phi})} \right]^{-1} - R_{Right} * \left[ H_{Right}^{(\hat{\theta}, \hat{\phi})} \right]^{-1} \right)^2$$

Digital Recordings of sound from left and right microphones (in ear canal of mannequin)



# MacDonald & Tran (2006): Cross-Channel Sound Localizer

Head-Related Transfer Functions (1 for each microphone, ).

Using commutability and transitivity of convolution operator...

$$\min_{\hat{\theta}, \hat{\phi}} \sum \left( R_{Left} * H_{Right}^{(\hat{\theta}, \hat{\phi})} - R_{Right} * H_{Left}^{(\hat{\theta}, \hat{\phi})} \right)^2$$

Essentially “convolves” each recording by the transfer function of the opposite microphone and obtains location coordinates at minimum

Digital Recordings of sound from left and right microphones (in ear canal of mannequin)



# MacDonald & Tran (2006): Cross-Channel Sound Localizer

## Strengths

Highly accurate in quiet environments with 2-sensors and works well in mildly noisy environments with 4-sensors

Frequency based cues minimize error caused by front-back reversals

## Issues

Head Related Transfer Functions are predetermined, but that's not the case in practice

Performance is likely to decrease in reverberant environments

Experiments were done at fixed sound source elevation. Unsure of how results will be when elevation is varied.

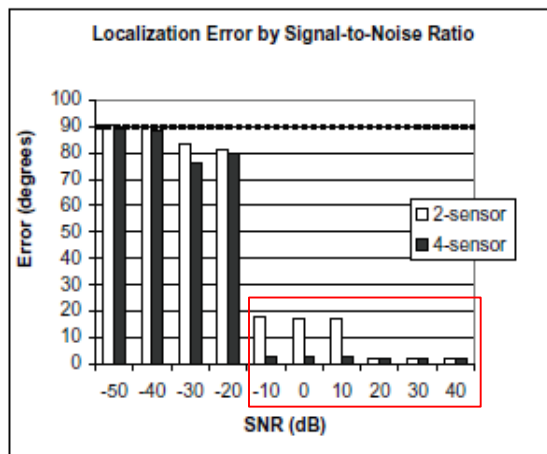


Figure 1

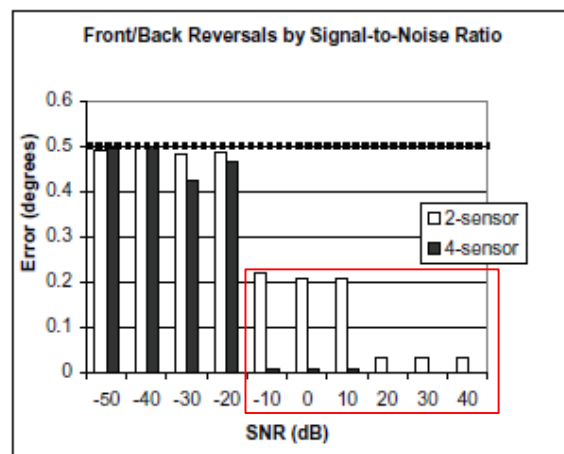


Figure 2

# Carlos et al. (2013): Spherical Cross-Channel Algorithm for Binaural Sound Localization

Assuming the HRTFs of the robot's head are known is apparently “impractical”, so a spherical generalization is made.

*FT of a source signal emitted from  
a punctual source*

*Head-related transfer functions  
positioned at a specific point*

$$I_L(r, \theta, \varphi, \omega) = H_L(r_s, \theta_s, \varphi_s, \omega) S(\omega) H_R(r, \theta, \varphi, \omega)$$
$$I_R(r, \theta, \varphi, \omega) = H_R(r_s, \theta_s, \varphi_s, \omega) S(\omega) H_L(r, \theta, \varphi, \omega)$$

## Source Position Estimation

$$(\hat{r}_s, \hat{\theta}_s, \hat{\varphi}_s) = \arg \max_{r, \theta, \varphi} \{ \text{corr} [(I_L(r, \theta, \varphi, \omega), I_R(r, \theta, \varphi, \omega))] \}$$

*Traditional Pearson's  
correlation coefficient*

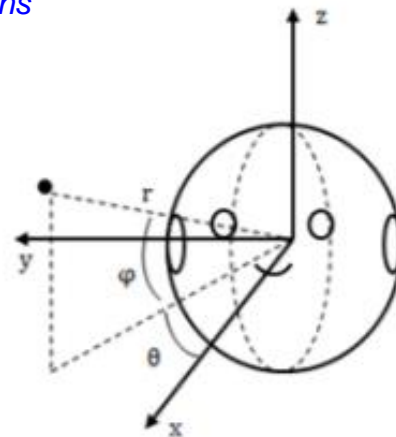


Fig. 1. Front view of the spherical head. A point's position is defined according to the standard LISTEN spherical coordinates system with the distance  $r$ , the azimuth  $\theta$  and elevation  $\varphi$  [13].

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$$H^s(r, \beta, \omega) = \frac{P_s(r, \beta, \omega)}{P_f(r, \omega)} = \frac{rce^{-j r \omega / c}}{ja^2 \omega} \sum_{m=0}^{\infty} (2m+1) P_m[\cos(\beta)] \frac{h_m(r\omega/c)}{h'_m(a\omega/c)}$$

$$H_L^s(r, \theta, \omega) = H^s\left(r, -\frac{\pi}{2} - \theta, \omega\right),$$

$$H_R^s(r, \theta, \omega) = H^s\left(r, \frac{\pi}{2} - \theta, \omega\right).$$

$c$  = speed of sound  
 $a$  = head radius  
 $P_m$  = legendre polynomial  
 $H_m$  = Hankel functions

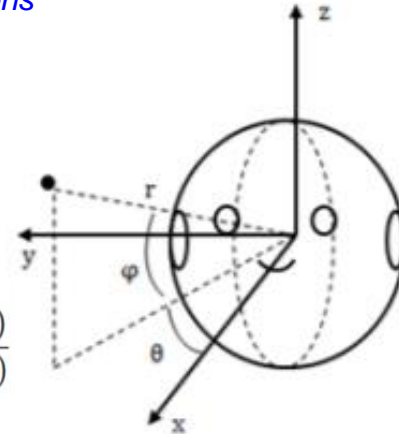


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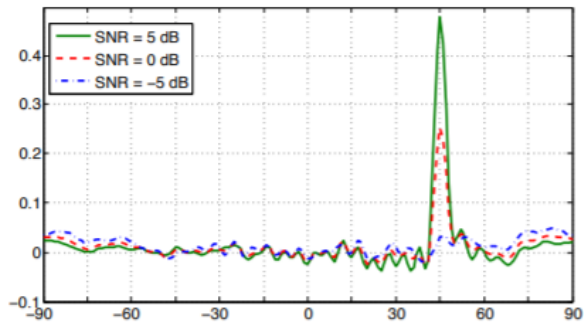


Fig. 3. Correlation coefficient as a function of the azimuth  $\theta$  for  $\text{SNR}_{\text{dB}} = \{-5, 0, 5\}$  dB, with a source emitting from  $\theta_s = 45^\circ$  and a spherical head.

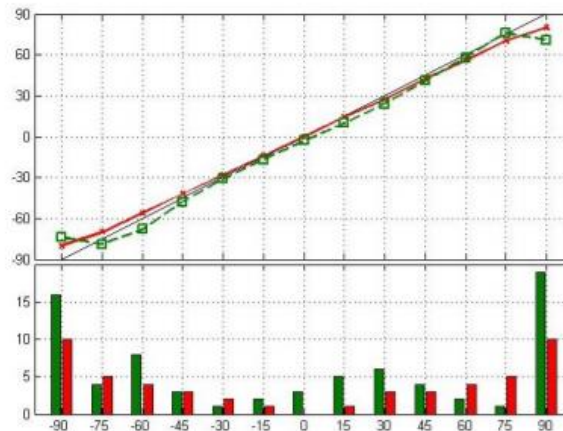


Fig. 7. (Top) Experimental mean estimated azimuth  $\hat{\theta}$  as a function of the real angle for a spherical head (red) or a KEMAR head (dotted, green). (Bottom) Absolute value of the mean angular error for the two heads.

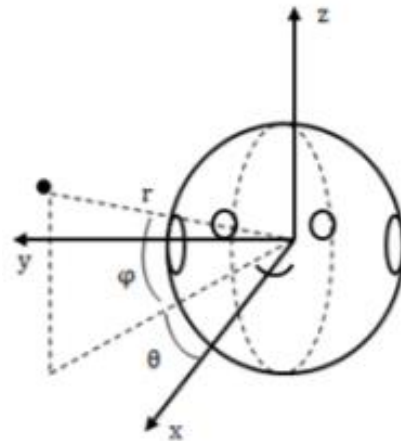


Fig. 1. Front view of the spherical head. A point's position is defined according to the standard LISTEN spherical coordinates system with the distance  $r$ , the azimuth  $\theta$  and elevation  $\varphi$  [13].

**Spherical approximation of the head works very well at the 13 tested positions with a  $4^\circ$  mean angular error (error at  $10^\circ$  in lateral directions).**

**Spherical accuracy > KEMAR head accuracy**

# Woodruff et al. (2012): Monoaural Source Segregation

## Binaural Pathway

Azimuth-dependent Gaussian Mixture Model of interaural time differences (ITDs) and interaural level differences (ILDs).

## Monoaural Pathway

Multipitch Tracking (HMM-based)

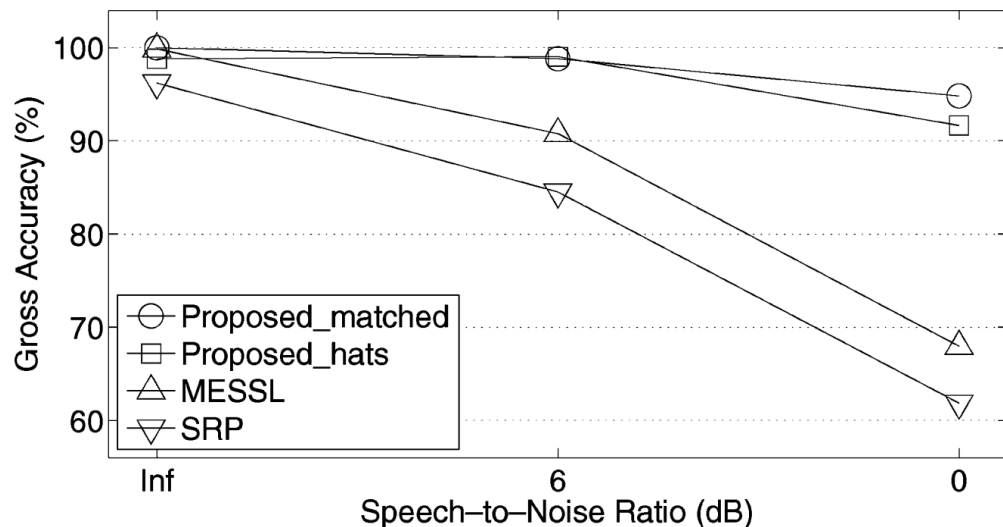
Pitch-Based Grouping

Onset/Offset Based Segmentation

## Localization Framework

Maximum likelihood

Head and  
Torso  
Simulator  
(HATS)



Gross accuracy (%) as a function of noise level for the HATS evaluation set.

# Yalta et al. (2016): Sound Source Localization Using Deep Learning Models

## Input

Data Preparation: Audio stimuli consisted of Japanese utterances (216 training, 72 evaluation). Training was done on HEARBO robot

STFT(N-channel audio → Power info was extracted and normalized at each frequency bin (W))

STFT frames were stacked to dimension H. Final input to DCNN is a  $N \times W \times H$  dimensional file.

## Output

STFT of for one channel is obtained to evaluate its RMS power. If frames have  $RMS = -120$ , it's labeled "silent". Otherwise, the target label is set to the detected angle of the receiving audio

Calculated Correct Detection Rate and Correct Accuracy Rate for Evaluation

# Yalta et al. (2016): Sound Source Localization Using Deep Learning Models

## *Training and Preparation (Continued)*

- **HEARBO robot was equipped with microphone array (8 and 16 channels)**
- **Experiment setting: 4x7 m room with 200 ms of reverberation every 5 degrees.**
- **33750 files were selected for training at EACH angle (total preparation of audio files for 360 degrees = 2,430,000).**
- **Distribution include sound mixtures with and without noise (Clean, 30, 10, 5, 0, -5, -10, -20, and -30 dB).**

**Loss function: Cross Entropy**

$$-\sum_{c=1}^M y_{o,c} \log(p_{o,c})$$

M = number of classes (in this case, 360 angles)

Y = binary indicator (0 or 1) dependent on if angle 'c' is correct to observation 'o'

P = predicted probability

# Yalta et al. (2016): Sound Source Localization Using Deep Learning Models

Residual learning speeds up the learning process and improves training convergence.

Made variations of the general DCNN architecture (Plain vs.. ResNet1..ResNet4). Compared to SEVD-MUSIC

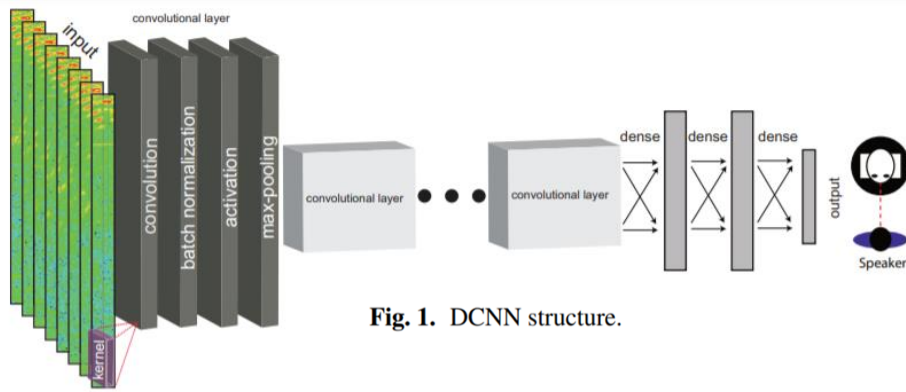


Fig. 1. DCNN structure.

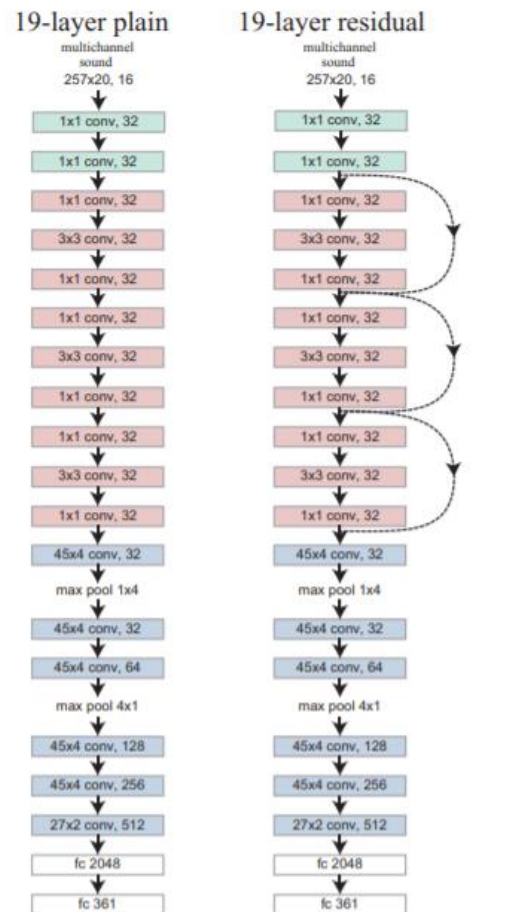


Fig. 4. Network architecture. Left: plain network. Right: residual network. The dotted line shortcut represents a  $1 \times 1$  convolutional layer.



# Yalta et al. (2016): Sound Source Localization Using Deep Learning Models

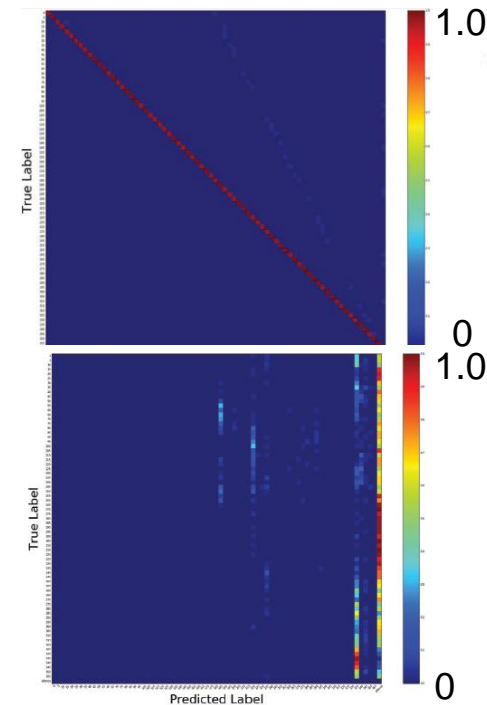


Fig. 9. ResNet4 angle prediction confusion matrix. Top: Clean. Bottom: -35 dB SNR.

**Table 4.** Microcone (array of 7 microphones) block accuracy.

SNR (dB)	SEVD-MUSIC	ResNet1
-35	<b>1.39</b>	1.39
-30	<b>1.39</b>	1.39
-25	<b>1.39</b>	1.39
-20	<b>1.42</b>	1.39
-15	<b>2.64</b>	2.06
-10	<b>9.10</b>	6.42
-5	<b>21.16</b>	16.94
0	<b>36.12</b>	33.61
5	<b>50.99</b>	49.69
10	<b>66.75</b>	64.61
15	<b>81.26</b>	78.11
30	<b>97.42</b>	95.36
45	<b>98.01</b>	97.39
Clean	<b>98.17</b>	97.50

**Table 6.** HEARBO accuracy rate.

SNR (dB)	PlainNet	ResNet1	ResNet2 TanH/ELU	ResNet3	ResNet4
-35	-99.40	-0.05	-21.47	-17.24	-60.15
-30	-93.91	2.83	-16.69	-16.03	-32.75
-25	-84.83	7.97	-4.35	-12.15	-12.46
-20	-61.85	19.46	15.38	-4.30	1.08
-15	-13.04	40.05	36.14	-2.69	14.3
-10	21.18	55.81	46.15	23.60	14.58
-5	38.68	61.73	50.88	41.70	11.98
0	48.43	62.96	53.53	49.75	18.81
5	54.51	63.07	56.80	55.80	33.72
10	58.74	63.51	59.45	60.42	48.63
15	62.40	65.50	61.94	63.77	59.06
30	68.06	69.60	69.24	70.08	69.82
45	71.04	71.70	72.30	72.04	72.11
Clean	70.89	71.53	72.01	71.90	71.46

Confusion matrix y-axis = probability from 0 to 1.0

# Sun et al. (2018): Generalized Cross Correlation Classification Algorithm (GCA)

## Nonlinear Classification Problem

$$X = H \otimes s(t) + n_m(t)$$

$$c_s = \text{classify}(X, \sum \text{feature}_i)$$

## Probabilistic Neural Network (PNN)

input layer

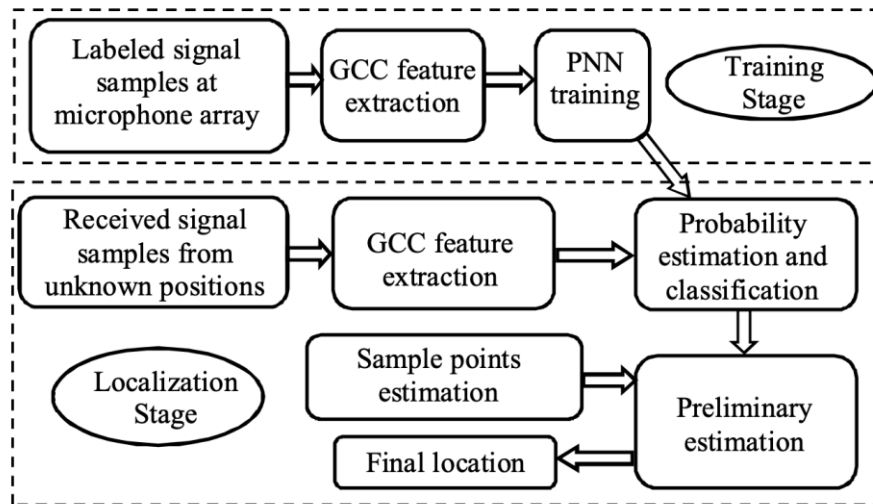
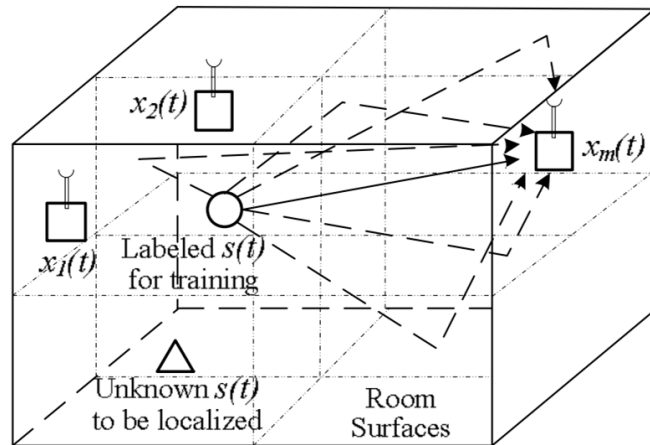
pattern layer

summation layer

decision layer

## Generalized Cross Correlation (GCC)

At the beginning of the PNN training, the enclosed room is divided into a number of  $K$  equal-dimension rectangular clusters.



Flow Chart of The Proposed GCA

# Comparison of Main Approaches (Methodology)

## MacDonald & Tran (2006): Cross-Channel Algorithm

**Pros:** Models auditory system of humans by using acoustic cues (ILDs and ITDs) and frequency related cues to estimate SSL via a control system's approach

**Cons:** Measures HRTF per estimation, which is impractical in real world applications

## Woodruff et al. (2012): Monaural Source Separation

**Pros:** Uses monaural multipitch tracking to distinguish multiple sound sources in order to assist a binaural input with azimuth estimation.

## Carlos et al. (2013): Spherical Cross Correlation

**Pros:** Relies on spherical generalization for modeling HRTFs. **Cons:** (1) spherical modeling cannot account for front-back reversals. (2) Humans don't have spherical heads.

## Yalta et al. (2016): DCNN

**Pros:** Uses DCNN with real world impulse response and end-to-end training to perform sound source localization.

**Con:** Current architecture is still not optimized, needs to be further explored. Current training might now allow for angle detection below 1°

## Sun et al. (2018): GCA

**Pros:** Extracts generalized cross correlation (GCC) features and then estimates sound source location using probabilistic neural network (PNN).

# Comparison of Main Approaches (Big Picture Results)

## **MacDonald & Tran (2006): Cross-Channel Algorithm**

Algorithm performs well above chance levels up to a SNR of -10 dB.

## **Woodruff et al. (2012): Monaural Source Separation**

Algorithm is able to localize multiple sound sources well above chance level up to a SNR of 0 dB.

## **Carlos et al. (2013): Spherical Cross Correlation**

Algorithm can localize sounds in 3 dimensions well above chance level up to a SNR of 0 dB.

## **Yalta et al. (2016): DCNN**

DCNN model with residual layers (ResNet1, ResNet2) performs well above chance level up to a SNR -5 dB.

## **Sun et al. (2018): GCA**

For 20 different acoustic environments, GCA can localize sounds in 3 dimensions well above chance level up to SNR of -10 dB and a  $T_{60}$  of 600 ms.

# Limitations of Past and Current Approaches

## Past Approaches

Past approaches were only able to localize the azimuth angle of the sound source

## Current Approaches

Current approaches must balance the model's accuracy and computational complexity.

Current approaches cannot perform accurately above an SNR of -10 dB and do not perform well with reverberation times of 400 and 600 ms.

# Future Research Directions

## Future Improvements

### **Dynamic Acoustic Environment**

Few studies are working on this challenge.

### **Few datasets devoted to sound source localization.**

More training datasets will improve performance of future neural network models.

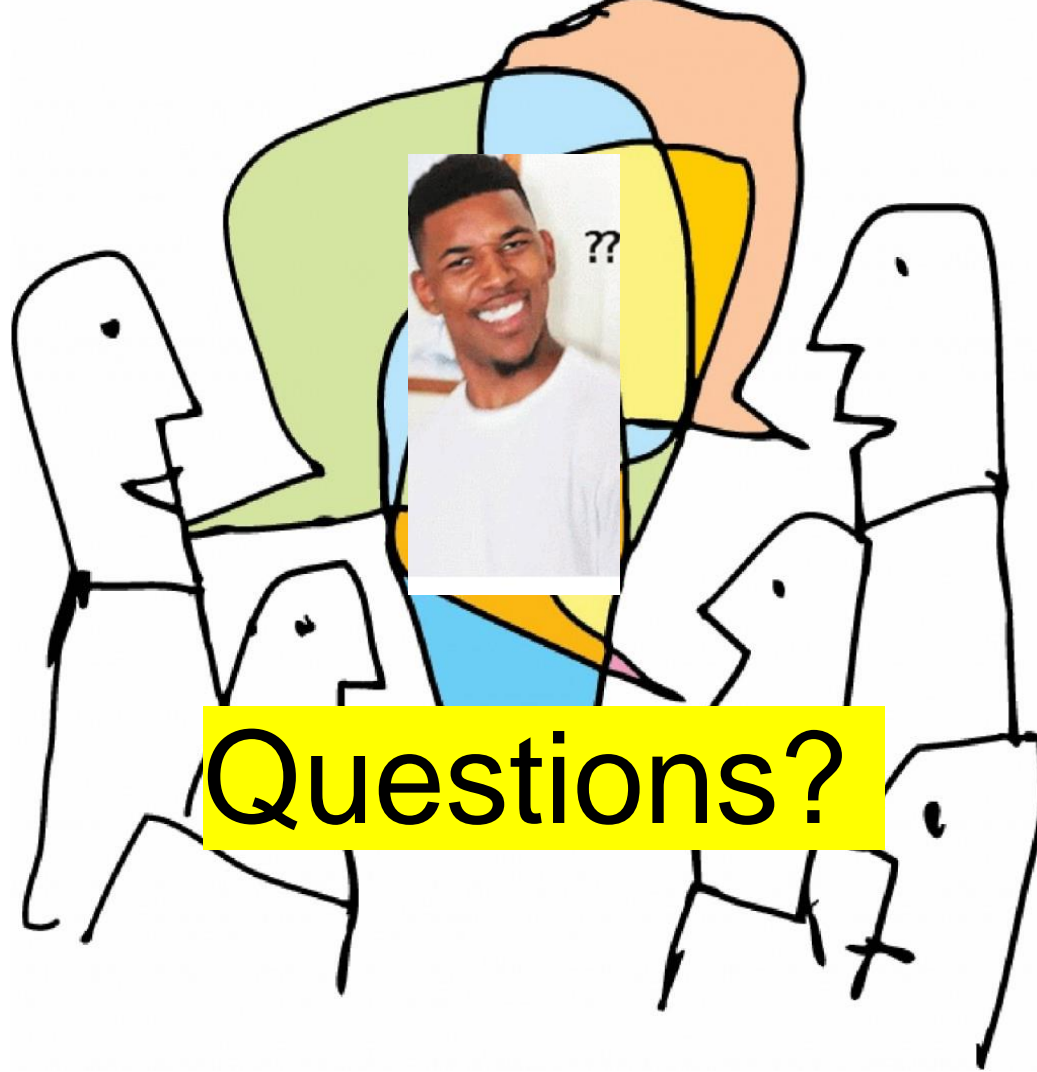
## Future Applications

### **Simple Integration into existing platforms**

SSL implementation in different types of robots

### **Integration of SSL in robotic tasks**

Service-Robots for Elderly Care



**Questions?**

# References

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