

$$X^2 = \sum (y - y_{\text{fit}})^2$$

$$= \sum_i (y_{\text{fit}_i} - y_i)^2$$

$$= \sum_i (mx_i + b - y_i)^2$$

take first deriv, set = 0.  
wrt  $m$ , then  $b$

$$\frac{d}{dm} \sum ( )^2 (x_i) = 0$$

$$\sum_i (mx_i^2 + bx_i - y_i x_i) = 0$$

$$m \sum_i x_i^2 + b \sum_i x_i - \sum_i x_i y_i = 0$$

and

$$2 \sum_i ( ) = 0$$

$$\sum (mx_i + b - y_i) = 0$$

$$m \sum_i x_i + bN - \sum_i y_i = 0$$

Define  $CX = \frac{1}{N} \sum_i x_i$

$$CXX = \frac{1}{N} \sum_i x_i^2$$

$$C_{xy} = \frac{1}{N} \sum_i x_i y_i$$

$$C_y = \frac{1}{N} \sum_i y_i$$

$$m C_{xx} + b C_x - C_{xy} = 0$$

$$m C_x + b - C_y = 0$$

$$b = C_y - m C_x$$

$$\cancel{m C_{xx}} + (C_y - \cancel{m C_x}) C_x - C_{xy} = 0$$

$$m [C_{xx} - C_x C_x] = C_{xy} - C_y C_x$$

$$m = \frac{C_{xy} - C_y C_x}{C_{xx} - C_x C_x} = \frac{C_{xy}(1 - C_x)}{C_x(1 - C_x)}$$

$$b = c_y - c_x \left[ \frac{c_{xy} - c_y c_x}{c_{xx} - c_x c_x} \right]$$

$$= c_y - \frac{c_x (c_{xy} - c_y c_x)}{c_{xx} - c_x c_x}$$

$$= \frac{c_y (c_{xx} - \cancel{c_x c_x}) - c_x c_{xy} + \cancel{c_x c_x c_y}}{c_{xx} - c_x c_x}$$

$$= \frac{c_{xx} c_y - c_x c_{xy}}{c_{xx} - c_x c_x}$$

