The non-calculus and calculus ways of promple computing (r+ar)2-12 problem g First let us dispense with the need for calculus in part (a). The question is what is the 1128 change in 1/2 if we change it to (r+Ar)2 where ar << r. We want to know (new value Minus old value is what we're computing)  $\frac{1}{(\Gamma + \Delta V)^2} - \frac{1}{r^2} = \frac{1}{r^2} \left[ \frac{1}{(1 + \frac{\Delta r}{V})^2} - 1 \right]$ common V factor of tz  $=\frac{1}{r^2}\frac{1-\left(1+\frac{\Delta r}{r}\right)^2}{1+\left(\frac{\Delta r}{r}\right)^2}\frac{1-\frac{\Delta r}{r}-\left(\frac{\Delta r}{r}\right)^2}{1+\left(\frac{\Delta r}{r}\right)^2}$ then denominator then FOIL ing to think hard about what can and cannot be neglected - perhaps it helps to be concrete and imagine ar = 0.01 Exactly what you'd get if you threw the "small in full power of derivatives at the problem instead of algebra and approximations as follows: what is the calculus method? We use  $f(x+\Delta x)-f(x) \approx f'(x)\Delta x$  and apply  $i + f_0$   $g(r) = \frac{1}{r^2} \cdot g'(r) = -\frac{2}{r^3} \cdot \frac{1}{r^3} \cdot \frac{$  $g(r+\Delta r)-g(r) \approx g'(r)\Delta r = -Z\Delta r$ 

## Problem 2-8

(a) In the preamble on the previous page, we established  $\Delta(r^2) = -2 \frac{\Delta r}{r^3}$ If the initial r is  $r_0$  and the final r is  $r_0 + \Delta r$  then  $\Delta(r^2) = -\frac{Z\Delta r}{r^3}$ So,  $\Delta g = \Delta(\frac{F}{m}) = \Delta(\frac{GM}{r^2})$   $= GM\Delta(\frac{f}{r^2})$ 

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