Rania — PS 4 — 2025-01-29

Very nice! Some comments below and on p. 10.

10/10

Section 11 Problems Cont.

```
In[73]:=
In[74]:= (*11.16 Word cloud of last letters in words from WordList[]*)
     WordCloud[StringTake[StringReverse[WordList[]], 1]]
     (*11.17 Roman numberals for the year 1959*)
                                                    Your solution to 11.18 returns {13} instagad of 13. I did
     RomanNumeral[1959]
                                                   Max[StringLength[RomanNumeral[Range[2020]]]].
     (*11.8 Maximum string length of any Ruman numeral year from 1 to 20*)
     Take[Reverse[Sort[StringLength[Table[RomanNumeral[x], {x, 1, 2020}]]]], 1]
     (*11.19 Word cloud of first charc of the Roman numerals up to 100*)
     WordCloud[StringTake[Table[RomanNumeral[x], {x, 1, 100}], 1]]
     (*11.20 Using Length to find the length of Russian alphabet*)
     StringLength[StringJoin[Alphabet["Russian"]]]
     (*11.21 Upercase Greek alphabet*)
     ToUpperCase[Alphabet["Greek"]]
     (*11.22 Bar Chart of letter numbers in "wolfram"*)
     BarChart[LetterNumber["wolfram"]]
     (*11.23 FromLetterNumber to make a string of 1000 random letters*)
     StringJoin[FromLetterNumber[RandomInteger[25, 1000] + 1]]
     (*11.24 Random five letter words*)
                                                                         Nice that you did
     Table[StringJoin[FromLetterNumber[RandomInteger[25, 5] + 1]], 1000]RandomInteger[25]+1
                                                                         not RandomInteger[26]
     (*11.25 Wolfram translated in Greek*)
                                                                         which will produce some
     Transliterate["wolfram", "Greek"]
                                                                         space characters.
     (*11.26 10 copies of wolf, ram emojis*)
     StringJoin[Table["♣$;, 10]]
     (*11.27 Arabic alphabet translated to English*)
     Transliterate[Alphabet["Arabic"], "English"]
     (*11.28 "A" in a black-white image*)
     ColorNegate[Rasterize[Style["A", 200]]]
     (*11.29 Interactive selector of a character in alphabet as an image*)
     Manipulate[Rasterize[Style[FromLetterNumber[n], 100]], {n, 1, 26, 1}]
     (*11.30 Interactive selector of black-
      on-white outlines from the alphabet by a menu*)
     Manipulate[ColorNegate[EdgeDetect[Rasterize[Style[letter, 100]]]]],
      {letter, Alphabet[]}]
     (*11.31 "Vision simulator" blurs letter "A" from to 50*)
```

Manipulate[Blur[Rasterize[Style["A", 100]], n], {n, 1, 50, 2}]

Out[74]=



Out[75]=

MCMLIX

Out[76]=

 $\{13\}$

Out[77]=

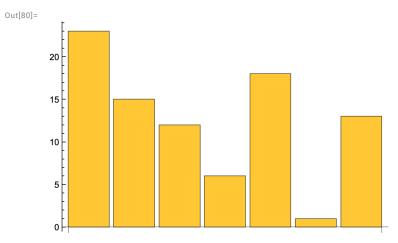


Out[78]=

33

Out[79]=

{A, B, Γ , Δ , E, Z, H, Θ , I, K, Λ , M, N, E, O, Π , P, Σ , T, Υ , Φ , X, Ψ , Ω }



Out[81]=

yhzncxwkkwvyggzksnanfpqrjedjnbwauetwajxppercbjoevqoakbapzmzrxalhllqaqtpuxabxgavnw viclthgcbhmocstcemgepmpncenygsiunvrtldzeyguohmfshrimevdkfeiwwdnlvguaurychdrywa hlakgbjrravnsuxtnnqedmslwxzwuipcypbglmhbjfriklyvbhhuxmzxipylnhuloifotzrbjqhtby kktceqjekyoazsuydxdzjwxbqmjzeajngzrvpmxenvawyfftromxnskgzdzkkmewyzvrbnjyayxhxe qcnabbvwdnbjubuzinpijqvmznwixzayuewfqrwugnlyydcrkcgtqxlugweksavnochlzwnxuaijgl jnlpzssiidlaxrkyjzoptxcppuhibfhnznpyfxycaaababmkcfdhwywljvccnlpbumebdflelpisbn bybyeewhicckjnukvlzcxnteyjyprlaccgmticcpjjniokmcwmxivtcdeiubvdowktmzfdbmrhqicd tpmjphqaxisfawyifupkftokdrinpeqntdyzesbhegnxcorkgszmfhtkploutfvwkpxvdveojjuzju uaxvzheqokevxgzwnlclgvitevltzudibdufudqztkjczorreevhiokngastbisaoigidvlxdjitvx hvvjkshxqbgjiosehpucfgkxubfaathurgnwxbjoxnviexamlekqdllftmvwxsdcytblexpaazfgof cyvslpkdyicgerhdxvjtfybpbtowliiaodltrcxhyyiccpzsnhpypquadxtpsqrqobdcedccdzlmbh yiopcnxztnuqugghjrxhitfgadqbemqvzcrhlwvdeegqgjzofuugmgnimcsuzisuovhwresvkwjzre hkuxcxaxsynkznbqdaubheebhaqxgyumeulqkiaryvdgwkrzvkgfqbtpabgap

Out[82]=

{netkf, pnlvk, gjbdy, gcsat, tbakj, ureaa, ewhpb, oujcv, xosgs, btfki, pwkek, bhork, pliky, nafaa, fjvyr, qsmon, prfuo, ypxly, batbu, faerq, mzrbc, lrmkk, zpzcu, muaeq, foyuv, gxntk, ynfhc, uogni, jgimu, qmehg, sdkug, bepnp, dztjt, nfinu, emfig, lvopt, ebohv, krvtk, zvsrg, dusgv, cetoi, sxvhy, mfkez, ohfhv, ogirz, wgatc, zjtoq, wduim, eyged, dqhfe, dzupm, exfud, zsumd, swdfu, fhfou, ttbsh, rqmtb, uldkt, ifjpj, fnvrr, nyydb, gcxvs, itlqu, rbgfy, jhoec, gqpzq, xnkxi, pzkan, ayhnw, eykhz, dfkqt, nlejn, gumnv, awqnd, pjmva, tkddb, wrsjh, wxeza, yxcbt, qwttx, mqmxg, fzoeq, rhczf, wassx, jhkvr, wpzry, yndmh, ckoxl, bmrve, txlff, wghmp, caufq, loiys, gydhe, rutnx, cqszx, uaidw, cfrst, xdyqw, eadpi, vngqp, wyxek, jjxsv, mtpwy, aafoc, gdfzg, vrtju, kxraz, wcfer, qsdfx, lqeri, vygtu, zbhtk, cbmqp, eodyw, kuveu, hbiyx, cicxx, rcxng, zfcfg, ahtst, yaqed, ercra, bjduj, fkrgu, zrrci, zkgac, sqfoh, nmuew, zjqjo, toajo, cjxeq, cvhoa, iwlim, euvtt, lvfla, kohla, nehop, wztqs, muzjq, msxja, spthx, eysge, catdx, ozflg, hqexd, urrkp, myhvu, peptp, vnyte, vwswn, jekjc, yxwlx, meuqm, ypezu, etnks, omuwl, erjst, izhxa, lrenz, oqtnm, perfu, gggso, fushr, qlfgs, mtuzj, xzagb, mrfsy, mrylk, zltku, mlpnz, zcrhk, wtjgp, qwxrj, oduij, yembg, bmuxc, fvdjy, dubml, qekwd, faeov, gpwxk, gimso, fpezg, hhvpy, jlxud, ogbia,

yzrre, jmxep, ailro, ydntk, ntexa, sbyev, lxjzb, tjvsy, nduoz, taehn, laxlg, ayzjo, imrju, bfikz, xsjpq, mtzol, ydgkq, mhope, gygfc, ljddf, jkwmg, sliqs, ygizc, ntxoo, lyomq, fhhxm, nebjp, byghn, zhnii, tqdye, xdqtu, jhqac, exuoh, ztfqe, ynweh, cylyj, cdqer, oebps, izhmg, gfoqo, axxxx, qvaez, scfmx, xfvat, rcebw, mktdn, uozkb, ujrhp, vgirh, cuugx, klfjl, bdvja, rrwya, vdfpr, nwkne, sodbn, dikvg, luklg, ptqtf, pstyp, xbgjx, ojjaa, syrzw, bddnz, ntzmb, urcdh, kygws, tjpxq, uayft, tgmhc, ovjvd, gsywz, bxpgu, pqlxo, rsgpg, fspel, ntgsh, diimp, vmeym, yjfos, bfyfq, aufpq, zodws, wjlzt, wlvoo, jbdfc, maqfd, oollq, gwyae, hmhnd, fxfew, dwnsb, ianhw, gmxch, zfhph, tthfd, zgkdf, sakdi, idago, pqkus, tcqvr, ofrwu, tvxzy, qsnyq, xoboe, xqcxu, kakqj, tzkdd, haehe, hbdah, hvtmv, xsjuc, vejlb, rkcpm, stihe, erxic, bwdib, gftqv, jufzr, zekkd, levix, ydtlw, pqqjk, pvtpy, wiscv, khugb, aqbfk, mtiks, msnpr, papfm, nyjcz, lvkmr, gcbei, hovdl, dmopx, zktxj, exuip, vtqbh, yzrrv, wzogv, xtdwn, dgwrk, covla, iyjdk, zkbyg, houht, qufsb, vhmzs, pxemr, esacv, usfjq, ksixc, rnmyy, nasfg, mmgxe, heahj, bwdgn, jlcyw, odoov, menuh, uimlk, jsvtj, druvo, ytaum, zdmgp, wnyhu, cggpz, aqmyw, cgqwu, luvja, yagqz, jfitb, ojnkm, famuc, ftlmo, cgicu, bhqwh, gpmzg, pmikx, xgouv, aanzi, icpqy, tfqtt, poaib, nmydl, fvswz, jvplj, dkchm, uqths, qnxan, bqjwt, nkeil, vclaj, iunxp, vplxx, yhlmk, gxdua, urvjk, fnopn, dutbe, tjzjt, fbshy, xtpuy, kwbff, katjj, oqabg, uwctw, lcmrk, wajka, pomfb, lzucx, idnwm, goctc, yuzig, fzdla, vlkdu, gyjgz, tafpe, xeedv, xwdhr, mzpvp, floym, yknvz, xevjk, igted, bgynd, omttp, tzwwq, rjzru, grsfu, mmish, lscmu, nfgtm, owkgi, yzqbp, uejfa, umudd, aduua, mupqr, whjsw, kmvhf, jpgok, fhdns, rzxax, sgxkd, hfpwy, llzsb, gzvyq, bwmze, italo, dinur, bsngr, mfjys, hrpkk, eeyop, yehpn, bgcts, cqebp, fqmyr, plpdd, vfdmt, rshho, rsrip, czdnr, ljgmf, ssomm, ucehl, cuojx, xhuhy, oxekl, ttajc, dvkmu, pvyjj, lzbfh, jhntv, srpuh, tbbks, qjlot, sksjc, gzpwq, qcacp, hrkpx, ruvds, mwsay, kyxww, qfiux, sbfvc, dklfs, ulzcb, wlmoh, jyrfc, pgseg, ygkbz, agabo, dhpsh, jcroq, rtnnl, dfygp, scshz, wzosb, kkxrf, voefq, llirv, dwpic, kdnes, eudgz, ycvmg, qnoqu, gkqfm, kfwwx, uprsu, ewdzd, jlsiv, coers, tkjvz, zofqj, lpgqu, mdalf, ujlsx, lgnob, monut, tlzap, mzfdw, sirbn, pduji, heifs, rxzjt, yajem, mfcnp, pscfz, owoih, itesb, dencc, fhyhy, jjmsz, pyzcq, dtdqh, othbb, iegpr, oksvc, oauwv, wfthj, fskmu, mnffw, dvqsj, pqpvx, ykcap, jwrna, isual, sxtkr, lszwk, ruacj, ivlmc, msmau, mtdew, amqil, ebwpz, hdobr, icxon, kiwea, mwabv, eimom, hrfky, tfhsi, hlqmw, imgyk, sdsqu, fdxjq, pxrjq, gjoah, baugn, ujdkg, ntikt, nadbd, kdubs, tccyj, pgvtq, relxo, xhctz, amqop, whwwy, xhxvl, kspcp, eepce, zdgno, awvte, hdece, wpevn, vuwsu, knpmy, xbjoz, bdbwp, qsgrc, qltar, tssvn, jjujn, zzywe, xpmqv, ooigt, lranu, rofke, cvehw, qoqcc, rlytq, ralcx, wjneh, ammjo, fadth, mqmpg, sccfr, xwmvv, xbumd, aajhc, wotwp, uyxfz, scbvo, tiqhu, erhhy, aaali, mqung, puznk, eaqvr, xatqn, gswlg, xqxmt, vwlrx, yjygh, wercv, agfvo, lebgf, byjgn, znbai, hlmfc, ynwci, dzxwa, fodfs, loucd, hwhoj, zoadi, uvrop, lvhnu, womsk, mwvxs, spwhe, hzuxy, twjai, jmvcx, ygajj, xqrao, owmza, riitu, avuer, ccnba, yekxb, uczwq, bcsyu, fnafx, zqcbr, wljno, fzthk, bdctc, fowim, dvqju, nzeky, cbbkz, jwfve, hjzhl, qqhid, xiwqg, mctgh, izzbc, tyrvn, ljsae, kmpch, hrhka, zqunc, quexx, ljjoj, ldrdv, poajt, idetp, nzpux, mjaaw, xyfcz,

```
wacvo, ldgli, ulrss, npslv, tykdp, zpbtl, yesli, mqtml, rwshk, wuxnd, lnbms,
tzacq, xnnuv, xknqb, ouoop, sogib, fkghr, asnpp, neabh, vvkxh, xxqfn, vuqme,
kuwkd, deleo, pqdfa, wzjxz, gexxo, vmqdb, ttabi, pkiyd, vjhxz, bapgb, lexfj,
dnodq, cwbkb, bhbed, zlvqc, fwzsk, zlgrv, jzrgp, rcwzk, lhhbv, vgklh, xrljh,
ppfya, cgswh, ydymw, bxwrv, iobpl, xualt, fwapn, hzcxk, zmxuu, bqwri, pltjd,
gnrli, hmyuf, xpspz, quchs, uraas, naicq, hbard, oxzri, tuhii, zkjzp, mdsbh,
lncjo, sfryh, yokll, jbard, vbqkw, ylogf, rxlsg, kfsrv, ecpek, zycrn, jjrki,
ptidb, glanh, crpum, avxfi, oyjyg, kddlv, euxwa, dzqnb, mhdjd, tnlou, kusdo,
dnoqv, yakzg, hvdwj, tdbkd, pkgci, wuwxj, aaxec, xnqfo, fmaxe, gftxe, ynfqb,
xwozb, uyrnx, mqdge, pjrew, olejs, cysey, qigry, xsaca, kmwhr, cglvq, vjbur,
rliua, mltiv, yhvqj, jhkpr, uivps, zvnvm, pdhqc, mryof, tgrhy, lgtck, agwxj,
ldjxb, jgwes, prkdd, qntmg, xqkvb, ywhci, qvidx, dwgvu, whvwy, anbcv, gpuoe,
egxol, kehaf, fmgin, lxezq, lkfcb, obnkv, yesei, euwen, hrvbo, eiwbv, terph,
ryspu, sugrq, wpxxz, ipxvg, eephv, yrhgn, dummq, fuhmv, nqaxv, xqoai, daoiu,
eurjh, vrjth, zvdkk, duvjp, qgiad, vtzsu, otvxl, kwjjz, knijy, vponk, roaic,
ccgxy, dubfg, rpcyj, jtcci, ybjei, kxzuv, fbxkb, aaksb, grgxq, cflrb, pcpme,
bavku, fmqwm, rdjgy, jvikh, gosbj, hhken, jqyoy, lxowo, uvzuz, bypup, wvkma,
nrzwd, mtbin, lzhzv, zizfi, zgmih, bfxju, hioad, mzcmd, aymtf, mqxgh, mrcsz,
kqmrv, pdewn, epfpz, lqsgm, oenpj, cvoiy, jphrv, smden, jictm, hyeqt, csdvi,
tblwt, rvzex, qobqo, nldic, lxwdk, okbuu, vzazc, atljh, wqwsp, vdxxf, yjlup,
phacc, kwgrv, zsizx, wmfmm, nezhd, syckj, gcmxp, iodok, qtlbq, xuqdh, lfozt,
mcmky, pkzbr, fnzct, lskqo, evooz, cpvja, efdai, tdyfv, qnzvr, coego, tgzgy,
qcrba, fpcys, vhmax, gmgcc, hkcss, dhvyh, fewyo, armis, ctjbb, mdxgy, qzvpc,
nwrso, qggwz, ojsqb, jjqqe, inolp, phtks, jfslx, moaza, ekjed, wlglt,
iviin, fcrzs, npcqe, dioyo, nyzzo, naira, naugo, bnxbv, xwfnm, gpfdm, pxjtu,
aflle, fbejt, bxhvw, esetg, jrhyf, qhhhk, zrhwt, qbdmz, fyqtz, jospu, wzfma,
keoxw, rneil, bpktn, jhnyx, zwlkk, ckekr, xtoum, ziufy, crenx, zbbxm, uaqnp,
gxwll, pzjzn, phrkc, hvkxn, nqlka, yomnd, umglv, qacoo, qvrvb, cmstg, gynvb,
wxvfj, rvcwg, cxgsl, tjjmq, uqbuc, kybli, uaemu, jucak, lekal, araqb, fmykd,
phdnt, xztcz, zasvj, aimne, gkkfu, nhuas, mirhd, aipdf, jbprb, dcqfy, qesqu}
```

Out[83]=

βολφραμ

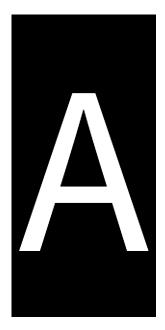
Out[84]=



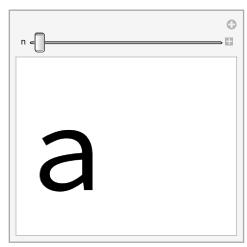
Out[85]=

{a, b, t, tḥ, j, ḥ, kḥ, d, dḥ, r, z, s, sḥ, ṣ, ḍ, ṭ, ẓ, ʿ, gḥ, f, q, k, l, m, n, h, w, y}

Out[86]=



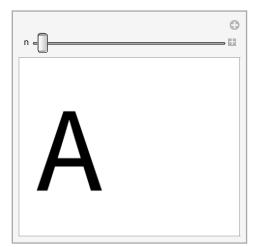
Out[87]=



Out[88]=



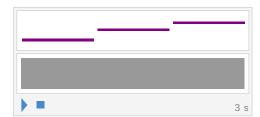
Out[89]=



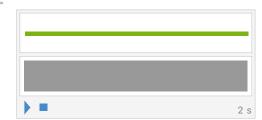
Section 12 Problems

```
ln[90]:= (*12.1 Sequence of notes with pitches 0,4,7*)
     Sound[{SoundNote[0], SoundNote[4], SoundNote[7]}]
     (*12.2 Two seconds of A note on Cello*)
     Sound[SoundNote["A", 2.0, "Cello"]]
     (*12.3 Riff of notes from pitch 0 → 48 in steps of 1,
     with each note lasting 0.05 seconds*)
     Sound[Table[SoundNote[p, .05], {p, 0, 48, 1}]]
     (*12.4 Sequence of notes going from pitch 12→0 in steps of 1*)
     Sound[Reverse[Table[SoundNote[p, 1], {p, 1, 12}]]]
     (*12.5 Sequence of 5 notes,
     staring at middle C and going up by octave at a time*)
     Sound[Table[SoundNote[p, 1], {p, 5, (8 * 4 + 5), 8}]]
     (*12.6 Sequence of 10 notes on a trumpet with random pitches from 0 \rightarrow
      12 and duration 0.2 seconds*)
     Sound[Table[SoundNote[RandomInteger[12], .2, "Trumpet"], 10]]
     (*12.7 Sequence of 10 notes with random pitches up
      to 12 and random durations up to 10 tenths of a second*)
     Sound[Table[SoundNote[RandomInteger[12], RandomInteger[10] / 10], 10]]
     (*12.8 0.1-second notes with pitches given by the digits of 2^31*)
     Sound[Table[SoundNote[p, .1], {p, IntegerDigits[2^31]}]]
     (*12.9 Sound from letters in CABBAGE, each note for 0.3 seconds in guitar*)
     Sound[Table[SoundNote[p, .3, "Guitar"], {p, Characters["CABBAGE"]}]]
     (*12.10 0.1-second notes with pitches given
       by the letter numbers of the characters in "wolfram"*)
     Sound[Table[SoundNote[p, .1], {p, LetterNumber["wolfram"]}]]
```





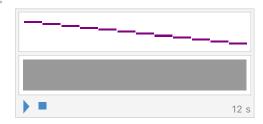
Out[91]=



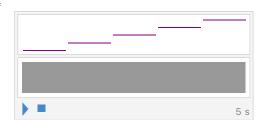
Out[92]=



Out[93]=



Out[94]=



Out[95]=











Section 13 Problems

12 24 36 48 60 72 84 96 108 120 132 144

```
In[100]:=
      (*13.1 A 12×12 multiplication table *)
      Grid[Table[a * b, {a, 12}, {b, 12}]]
      (*13.2 A 5x5 for Roman Numerals*)
      Grid[RomanNumeral[Table[a*b, {a, 5}, {b, 5}]]]
      (*13.3 10x10 grid of random colors*)
      Grid[Table[RandomColor[], 10, 10]]
      (*13.4 10×10 grid of randomly colored random integers between 0 and 10*)
      Grid[Table[Style[RandomInteger[10], RandomColor[]], 10, 10]]
      (*13.5 Grid of all possible strings
       consisting of pairs of letters of the alphabet*)
      Grid[Table[StringJoin[{a}, {b}], {a, Alphabet[]}, {b, Alphabet[]}]]
      (*13.6 Visualize {1,4,3,5,2} with a pie chart, number line,
      line plot and bar chart.Place these in a 2x2 grid*)
      numList = \{1, 4, 3, 5, 2\}
      Grid[{{PieChart[numList], NumberLinePlot[numList]},
                                                                  Yes, it can be very compact:)
        {ListLinePlot[numList], BarChart[numList]}}] (*ALL IN THE SYNTAX!*)
      (*13.7 Array plot of hue values x*y where x and y run from 0 \rightarrow
                                                                        The hue plots are cool. On this one
       1 in steps of 0.05*)
                                                                        he meant you to divide by 400!
      ArrayPlot[Table[Hue[(x * y) / 20], \{x, 20\}, \{y, 20\}]](*THIS IS SO COOL*)
                                                                        I did
      (*13.8 Array plot of hue values x/y,
                                                                        ArrayPlot[
      where x and y each run from 1 to 50 in steps of 1*)
                                                                          Table[Hue[i j],
      ArrayPlot[Table[Hue[(x/y)], \{x, 50\}, \{y, 50\}]]
                                                                          {i, Range[0, 1, 0.05]},
      (*13.9 Array plot of the lengths of Roman
                                                                          {j, Range[0, 1, 0.05]}
       numeral strings in a multiplication table up to 100×100*)
      ArrayPlot[Table[StringLength[RomanNumeral[a*b]], {a, 100}, {b, 100}]]
                                                           I thought the last one was perhaps
                                                           the coolest.
Out[100]=
      1 2 3 4 5 6 7 8
                                 10 11 12
                             9
      2 4 6 8 10 12 14 16 18
                                 20 22 24
      3 6 9 12 15 18 21 24 27
                                 30
                                    33 36
      4 8 12 16 20 24 28 32 36
                                40
                                    44 48
      5 10 15 20 25 30 35 40 45
                                 50
                                    55
                                         60
      6 12 18 24 30 36 42 48 54
                                 60
                                     66 72
      7 14 21 28 35 42 49 56 63 70
                                    77
                                         84
      8 16 24 32 40 48 56 64 72 80
                                    88 96
      9 18 27 36 45 54 63 72 81 90 99 108
      10 20 30 40 50 60 70 80 90 100 110 120
      11 22 33 44 55 66 77 88 99 110 121 132
```

Out[101]=

Ι II III IV V II IV VI VIII X III VI IX XII XV IV VIII XII XVI XX Χ XV XX XXV

Out[102]=



Out[103]=

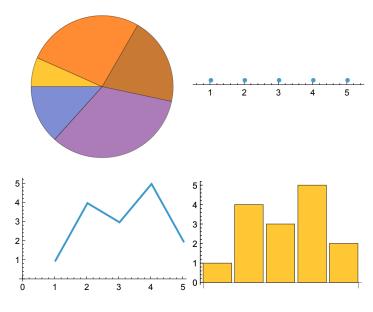
Out[104]=

aa ab ac ad ae af ag ah ai aj ak al am an ao ap aq ar as at au av aw ax ay az ba bb bc bd be bf bg bh bi bj bk bl bm bn bo bp bq br bs bt bu bv bw bx by bz ca cb cc cd ce cf cg ch ci cj ck cl cm cn co cp cq cr cs ct cu cv cw cx cy cz da db dc dd de df dg dh di dj dk dl dm dn do dp dq dr ds dt du dv dw dx dy dz ea eb ec ed ee ef eg eh ei ej ek el em en eo ep eq er es et eu ev ew ex ey ez fa fb fc fd fe ff fg fh fi fj fk fl fm fn fo fp fq fr fs ft fu fv fw fx fy fz ga gb gc gd ge gf gg gh gi gj gk gl gm gn go gp gq gr gs gt gu gv gw gx gy gz ha hb hc hd he hf hg hh hi hj hk hl hm hn ho hp hq hr hs ht hu hv hw hx hy hz ia ib ic id ie if ig ih ii ij ik il im in io ip iq ir is it iu iv iw ix iy iz ja jb jc jd je jf jg jh ji jj jk jl jm jn jo jp jq jr js jt ju jv jw jx jy jz ka kb kc kd ke kf kg kh ki kj kk kl km kn ko kp kq kr ks kt ku kv kw kx ky kz la lb lc ld le lf lg lh li lj lk ll lm ln lo lp lq lr ls lt lu lv lw lx ly lz ma mb mc md me mf mg mh mi mj mk ml mm mn mo mp mg mr ms mt mu mv mw mx my mz na nb nc nd ne nf ng nh ni nj nk nl nm nn no np ng nr ns nt nu nv nw nx ny nz oa ob oc od oe of og oh oi oj ok ol om on oo op oq or os ot ou ov ow ox oy oz pa pb pc pd pe pf pg ph pi pj pk pl pm pn po pp pq pr ps pt pu pv pw px py pz qa qb qc qd qe qf qg qh qi qj qk ql qm qn qo qp qq qr qs qt qu qv qw qx qy qz ra rb rc rd re rf rg rh ri rj rk rl rm rn ro rp rq rr rs rt ru rv rw rx ry rz sa sb sc sd se sf sg sh si sj sk sl sm sn so sp sq sr ss st su sv sw sx sy sz ta tb tc td te tf tg th ti tj tk tl tm tn to tp tq tr ts tt tu tv tw tx ty tz ua ub uc ud ue uf ug uh ui uj uk ul um un uo up ug ur us ut uu uv uw ux uy uz va vb vc vd ve vf vg vh vi vj vk vl vm vn vo vp vq vr vs vt vu vv vw vx vy vz wa wb wc wd we wf wg wh wi wj wk wl wm wn wo wp wq wr ws wt wu wv ww wx wy wz xa xb xc xd xe xf xg xh xi xj xk xl xm xn xo xp xq xr xs xt xu xv xw xx xy xz ya yb yc yd ye yf yg yh yi yj yk yl ym yn yo yp yq yr ys yt yu yv yw yx yy yz za zb zc zd ze zf zg zh zi zj zk zl zm zn zo zp zq zr zs zt zu zv zw zx zy zz

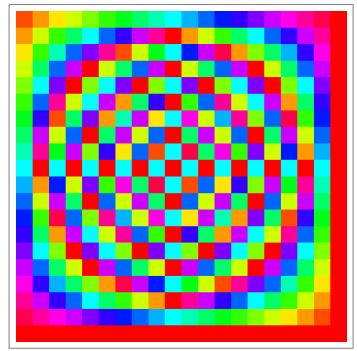
Out[105]=

$$\{1, 4, 3, 5, 2\}$$

Out[106]=



Out[107]=



Out[108]=

