Rania — Waves Exam 3

April 29, 2025

TOTAL SCORE / 25

Comments and Scores for Each Problem Are on Last Page

This exam tests your fluency with the core of the Wolfram Language, as it was presented in *An Elementary Introduction to the Wolfram Language, 3rd Edition (EIWL3)*, Sections 25-34 and 38-41. There is one problem with two or three parts corresponding to each section. *Tip: all of them are meant to be quick. If you get bogged down, move on.*

Directions:

After downloading this notebook, rename it with your first name in the filename. E.g., Eli-Exam3.nb, Harper-Exam3.nb, Hexi-Exam3.nb, Jeremy-Exam3.nb, Rania-Exam3.nb, Tahm-Exam3.nb, or Walker-Exam3.nb.

Then disconnect from the wifi and work the exam. Save your notebook early and often so that you don't lose work in progress.

Your answers always go into the Wolfram Language Input cells that begin with a comment, e.g.,

```
(* 1a *) foobar /@ Plus[Array]
```

All your answers should execute and re-execute without warnings or error messages.

You may refer to your downloaded copies of EIWL3, and anything else we developed in the course (like your cheat sheets!), but not to any web resources.

When you are done, save your notebook one last time, re-join the wifi, and then email it to me.

This exam was designed to require about 45 minutes, but if you need a full hour, that is ok. Everyone will stop at the one-hour mark.

1. Applying Functions (EIWL3 Section 25)

(a)

Use Map with a *levelspec* to put a frame around each individual number in the array Array [Plus, {10,10}] (we don't want frames around already-framed things — just one level of frames around the individual numbers).

```
In[103]:=
       (* 1a *)
       Map[Framed, Array[Plus, {10, 10}], {2}]
Out[103]=
                                                     11 |} ,
                                      8
                                          9
                                               10,
                                      9
                                                11
                                 8
                                           10
                                      10
               6
                             9
                                 10
                                       11
                                             12
                                                   13
                        8
                                                         14
                        9
                             10
                                  11 ,
                                        12
                                              13
                                                    14
                                                          15
                        10
                                    12
                                          13
                                     13
                                           14
                                                 15
                                                      16
               10
                                                  16
                     11
                          12
                                13
                                      14
                                            15
                                                        17
                                                             18
                                                         18
                11
                      12
                            13
                                       15
                                             16
                                                   17
                                                               19
                                 14
                     13,
                                                         19
                12
                                 15
                                       16
                                             17
                                                   18
                                                              20
                           14
```

(b)

Copy what you did in (a), but for this part, also turn the result into a grid using **Grid** and the "as an afterthought" syntax:

In[104]:= (* 1b *) Map[Framed, Array[Plus, {10, 10}], {2}] // Grid Out[104]=

2. Pure Anonymous Functions (EIWL3 Section 26)

(a)

Use the # and & notation to create an anonymous function that cubes whatever is given it, and then use /@ to apply it to every member of the list $\{1,2,3,4,5\}$.

```
In[105]:=
       (* 2a *)
        (\#^3\&)/@\{1, 2, 3, 4, 5\}
Out[105]=
       {1, 8, 27, 64, 125}
```

(b)

Use the #1, #2, and & notation to create an anonymous function that divides its first argument by its second argument. Combine this with Apply and a levelspec to apply the function to $\{\{1,2\},\{2,3\},\{3,4\},\{4,5\}\}$. Once you have this right, you will get $\{\frac{1}{2},\frac{2}{3},\frac{3}{4},\frac{4}{5}\}$.

In[106]:=

(* 2b *)

Apply[#1/#2 &, {{1, 2}, {2, 3}, {3, 4}, {4, 5}}, {1}]

Out[106]:=

$$\left\{\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}\right\}$$

3. Applying Functions Repeatedly (EIWL3 Section 27)

(a)

Use **Nest** to apply **Factorial** twice to {1,2,3,4}. If you have this right, 620,448,401,733,239,439,360,000 will be one of the elements of your answer.

(b)

Use **NestList** to apply **Factorial** three times to {1,2,3}, as well as showing the results of doing it 0, 1, and 2 times. If you have this right, you will have an insanely large result at the third step. Do not go any higher, or I do not know what will happen to your computer.

```
In[108]:=
              (* 3b *)
             NestList[Factorial, {1, 2, 3}, 3]
Out[108]=
              \{\{1, 2, 3\}, \{1, 2, 6\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2,
                   2 601 218 943 565 795 100 204 903 227 081 043 611 191 521 875 016 945 785 727 541 837 850 835 %
                     631\,156\,947\,382\,240\,678\,577\,958\,130\,457\,082\,619\,920\,575\,892\,247\,259\,536\,641\,565\,162\,052\,015\,\%
                     873\,791\,984\,587\,740\,832\,529\,105\,244\,690\,388\,811\,884\,123\,764\,341\,191\,951\,045\,505\,346\,658\,616\,
                     783 758 997 420 676 784 016 967 207 846 280 629 229 032 107 161 669 867 260 548 988 445 514
                     257\,193\,985\,499\,448\,939\,594\,496\,064\,045\,132\,362\,140\,265\,986\,193\,073\,249\,369\,770\,477\,606\,067\,\%
                     680\,670\,176\,491\,669\,403\,034\,819\,961\,881\,455\,625\,195\,592\,566\,918\,830\,825\,514\,942\,947\,596\,537 :
                     274 845 624 628 824 234 526 597 789 737 740 896 466 553 992 435 928 786 212 515 967 483 220 %
                     976 029 505 696 699 927 284 670 563 747 137 533 019 248 313 587 076 125 412 683 415 860 129
                     447\,566\,011\,455\,420\,749\,589\,952\,563\,543\,068\,288\,634\,631\,084\,965\,650\,682\,771\,552\,996\,256\,790\,\%
                     845\ 235\ 702\ 552\ 186\ 222\ 358\ 130\ 016\ 700\ 834\ 523\ 443\ 236\ 821\ 935\ 793\ 184\ 701\ 956\ 510\ 729\ 781\ \times 100
                     804\,354\,173\,890\,560\,727\,428\,048\,583\,995\,919\,729\,021\,726\,612\,291\,298\,420\,516\,067\,579\,036\,232\,
                     337 699 453 964 191 475 175 567 557 695 392 233 803 056 825 308 599 977 441 675 784 352 815
                     913 461 340 394 604 901 269 542 028 838 347 101 363 733 824 484 506 660 093 348 484 440 711
                     048\,457\,983\,786\,618\,703\,257\,405\,938\,924\,215\,709\,695\,994\,630\,557\,521\,063\,203\,263\,493\,209\,220\,
                     738 320 923 356 309 923 267 504 401 701 760 572 026 010 829 288 042 335 606 643 089 888 710
                     297 380 797 578 013 056 049 576 342 838 683 057 190 662 205 291 174 822 510 536 697 756 603
                     029\,574\,043\,387\,983\,471\,518\,552\,602\,805\,333\,866\,357\,139\,101\,046\,336\,419\,769\,097\,397\,432\,285\,
                     994 219 837 046 979 109 956 303 389 604 675 889 865 795 711 176 566 670 039 156 748 153 115
                     943\,980\,043\,625\,399\,399\,731\,203\,066\,490\,601\,325\,311\,304\,719\,028\,898\,491\,856\,203\,766\,669\,164\,\%
                     468\,791\,125\,249\,193\,754\,425\,845\,895\,000\,311\,561\,682\,974\,304\,641\,142\,538\,074\,897\,281\,723\,375\,\times 10^{-2}
                     955\,380\,661\,719\,801\,404\,677\,935\,614\,793\,635\,266\,265\,683\,339\,509\,760\,000\,000\,000\,000\,000\,000\,000
                     000 000 000 000 000 000 000 } }
```

4. Tests and Conditionals (EIWL3 Section 28)

(a)

Use PrimeQ and /@ to generate a True or False list that is twenty elements long expressing which numbers in Range [20] are prime.

```
In[109]:=
      (* 4a *)
      PrimeQ[#] & /@ Range[20]
Out[109]=
      {False, True, True, False, True, False, True, False, False,
       True, False, True, False, False, True, False, True, False)
```

(b)

Combine PrimeQ with Select to only list the numbers in Range [20] that are prime.

5. More About Pure Functions (EIWL3 Section 29)

(a)

Accomplish exactly the same thing as **Table** [n*(n-1)/2, {n,6}] using **Array** and a pure function.

(b)

Make some modifications to **FoldList[Plus, {1,2,3,4,5}]** so that it produces a list of the first 10 factorials. Instead of hand-coding the list up to 10, begin by first changing **{1,2,3,4,5}** to **Range [10]**.

6. Rearranging Lists (EIWL3 Section 30)

(a)

```
Use Transpose and one of the levelspec options to turn
      {{{1,uno},{2,dos},{3,tres}}},{{4,cuatro},{5,cinco},{6,seis}}} into
      {{{1,2,3},{uno,dos,tres}},{{4,5,6},{cuatro,cinco,seis}}}
In[115]:=
      (* 6a *)
      Transpose[
       {{{1, uno}, {2, dos}, {3, tres}}, {{4, cuatro}, {5, cinco}, {6, seis}}}, {1, 3, 2}]
Out[115]=
      {{{1, 2, 3}, {uno, dos, tres}}}, {{4, 5, 6}, {cuatro, cinco, seis}}}
      (b)
      Use Flatten and a levelspec option to turn
      {{{1,uno},{2,dos},{3,tres}},{{4,cuatro},{5,cinco},{6,seis}}} into
      {{1,uno},{2,dos},{3,tres},{4,cuatro},{5,cinco},{6,seis}}
In[116]:=
      Flatten[{{{1, uno}, {2, dos}, {3, tres}}, {{4, cuatro}, {5, cinco}, {6, seis}}}, 1]
Out[116]=
      {{1, uno}, {2, dos}, {3, tres}, {4, cuatro}, {5, cinco}, {6, seis}}
   7. Parts of Lists (EIWL3 Section 31)
      (a)
      Use the magical All position (you will need to use All more than once) to turn
      {{{Eli, Lerner},{Harper,Yonago},{Hexi,Jin}},{{Jeremy,Choy},{Rania,Zaki}}
      ,{Tahm,Loyd},{Walker,Harris}}} into
      {{Eli, Harper, Hexi}, {Jeremy, Rania, Tahm, Walker}}
In[117]:=
      (*7a*)
      #[All, All, 1] &@{{{Eli, Lerner}, {Harper, Yonago}, {Hexi, Jin}},
        {{Jeremy, Choy}, {Rania, Zaki}, {Tahm, Loyd}, {Walker, Harris}}}
Out[117]=
      {{Eli, Harper, Hexi}, {Jeremy, Rania, Tahm, Walker}}
```

Use a magical negative positional argument to extract {Jeremy,Rania,Tahm,Walker} from {{Eli, Harper, Hexi}, {Jeremy, Rania, Tahm, Walker}} and combine that with Take with a different magical *negative* argument to extract { Tahm, Walker }.

(b)

```
In[118]:=
       (*7b*)
      Take[{{Eli, Harper, Hexi}, {Jeremy, Rania, Tahm, Walker}}[-1], -2]
Out[118]=
       {Tahm, Walker}
```

8. Patterns (EIWL3 Section 32)

(a)

Use Cases to choose the lists that begin and end with the same letter in this list of lists (but look ahead to part (b) before you solve part (a)):

```
{
       {"a", "l", "u", "l", "a"},
       {"a", "l", "o", "h", "a"},
       {"a", "r", "a", "r", "a"},
       {"b", "o", "n", "u", "s"},
       {"c", "i", "v", "i", "c"},
       {"d", "e", "b", "e", "d"},
       {"e", "l", "b", "o", "w"},
       {"z", "a"},
       {"z", "z"}
      }
In[119]:=
      (* 8a *)
      (*cooler way to do both is x_/;x[1]=x[-1]*)
      Cases[{{"a", "l", "u", "l", "a"}, {"a", "l", "o", "h", "a"}, {"a", "r", "a", "r", "a"},
        {"b", "o", "n", "u", "s"}, {"c", "i", "v", "i", "c"}, {"d", "e", "b", "e", "d"},
        {"e", "l", "b", "o", "w"}, {"z", "a"}, {"z", "z"}}, {x_, __, x_}]
Out[119]=
      \{\{a, l, u, l, a\}, \{a, l, o, h, a\}, \{a, r, a, r, a\}, \{c, i, v, i, c\}, \{d, e, b, e, d\}\}
```

(b)

The pattern **BlankNullSequence** has the shorthand ___. Use ___ to improve the pattern you used in Part (a) so that the two-letter list {z,z} is also included in your result.

```
In[120]:=
       (* 8b *)
       Cases[{{"a", "l", "u", "l", "a"}, {"a", "l", "o", "h", "a"}, {"a", "r", "a", "r", "a"},
          {"b", "o", "n", "u", "s"}, {"c", "i", "v", "i", "c"}, {"d", "e", "b", "e", "d"},
          \{"e", "l", "b", "o", "w"\}, \{"z", "a"\}, \{"z", "z"\}\}, \{x_{\_}, \_\_, x_{\_}\}]
Out[120]=
       \{\{a, l, u, l, a\}, \{a, l, o, h, a\}, \{a, r, a, r, a\}, \{c, i, v, i, c\}, \{d, e, b, e, d\}, \{z, z\}\}
```

9. Assigning Names to Things (EIWL3 Section 38)

(a)

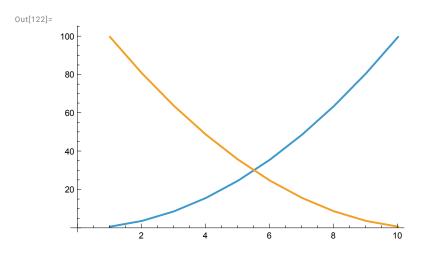
Use Module to compute x=Factorial[10], and then produce $\{x,x^2,x^3\}$.

```
In[121]:=
      (* 9a *)
      Module[{x = Factorial[10]}, {x, x^2, x^3}]
Out[121]=
       {3628800, 13168189440000, 47784725839872000000}
```

(b)

Inside Module, let rangeSquared=Range [10] ^2, and then produce a list line plot of rangeSquared joined with Reverse [rangeSquared].

```
In[122]:=
      (* 9b *)
      Module[{rangeSquared = Range[10]^2},
       ListLinePlot[{rangeSquared, Reverse[rangeSquared]}]
      ]
```



10. Immediate and Delayed Values (EIWL3 Section 39)

(a)

Make a one-character change to this expression,

Module $[x := RandomInteger[10]], \{x, x^2, x^3, x^4\}]$, so that it produces four different powers of the same random number instead of four different powers of different random numbers.

In[123]:=

```
Module [x:=RandomInteger[10]], \{x, x^2, x^3, x^4\}]
          (* 10a *)
         \texttt{Module}\big[\,\{x = \texttt{RandomInteger[10]}\,\}\,, \big\{x\,, x^2\,, x^3\,, x^4\big\}\,\big]
Out[123]=
          {1, 9, 512, 625}
Out[124]=
          {1, 1, 1, 1}
```

(b)

Make a one-character change to this expression,

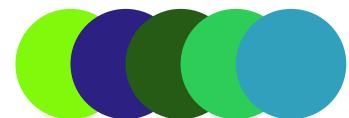
Module[{color=RandomColor[]},Graphics[Table[Style[Disk[{i,0}],color],{i ,5}]]], so that it produces five different-color disks.

In[125]:=

```
Module[{color=RandomColor[]},Graphics[Table[Style[Disk[{i,0}],color],{i,5}]]]
(* 10b *)
Module[{color:=RandomColor[]},Graphics[Table[Style[Disk[{i,0}],color],{i,5}]]]
```

Out[125]=





11. Defining Your Own Functions (EIWL3 Section 40)

(a)

Define a function **f** that takes a list of three elements and out of them makes a list of lists that contains all six possible orderings. Using **Permutations** will make this easy.

```
Include a test of your function as f[1,2,3] and make sure it gets
       \{\{1,2,3\},\{1,3,2\},\{2,1,3\},\{2,3,1\},\{3,1,2\},\{3,2,1\}\}.
In[127]:=
        (* 11a *)
       f[x_{y_{z}}, y_{z_{z}}] := Permutations[\{x, y, z\}]
       f[1, 2, 3]
Out[128]=
       \{\{1, 2, 3\}, \{1, 3, 2\}, \{2, 1, 3\}, \{2, 3, 1\}, \{3, 1, 2\}, \{3, 2, 1\}\}
```

(b)

Define a function g that gives 1 for g[0], and gives n * g[n-1] for any integer n greater than 0, but don't use an If statement! Include a test of your function as g[6] and make sure it gets 720.

```
In[129]:=
       (* 11b *)
       (*it took me a hot minute but this is just factorials!*)
       g[x_Integer] := x!
       g[0]
       g[6]
       (*6*g[5]*)
       (*g[100]
        100*g[99]*)
Out[130]=
       1
Out[131]=
       720
```

12. More About Patterns (EIWL3 Section 41):

(a)

Use the replacement rule notation — e.g., / • and -> — to exchange the first and last element in any list

```
containing two or more elements and test your replacement using the list
      {alpha, beta, gamma, delta, epsilon}.
In[132]:=
       (* 12a *)
       {alpha, beta, gamma, delta, epsilon} /.
       \{a_{n}, middleStuff_{n}, c_{n}\} \rightarrow \{a \rightarrow c, middleStuff, c \rightarrow a\}
       (*{a, b, c} /. a \rightarrow x
          {alpha, beta,gamma, delta, epsilon }*)
Out[132]=
       \{alpha \rightarrow epsilon, beta, gamma, delta, epsilon \rightarrow alpha\}
      (b)
      Starting with Characters/@RomanNumeral [Range [100], select all the sequences correspond-
      ing to the Roman numerals that have XXX in them. Only wants ones with three consective XXs
In[133]:=
       (* 12b *)
      Cases[Characters /@ RomanNumeral[Range[100]], {___, "X", "X", "X", ___}]
Out[133]=
       {{X, X, X}, {X, X, X, I}, {X, X, X, I, I}, {X, X, X, I, I, I}, {X, X, X, I, V},
        \{X, X, X, V\}, \{X, X, X, V, I\}, \{X, X, X, V, I, I\}, \{X, X, X, V, I, I, I\},
        {X, X, X, I, X}, {L, X, X, X}, {L, X, X, X, I}, {L, X, X, X, I, I},
        {L, X, X, X, I, I, I}, {L, X, X, X, I, V}, {L, X, X, X, V}, {L, X, X, X, V, I},
        {L, X, X, X, V, I, I}, {L, X, X, X, V, I, I, I}, {L, X, X, X, I, X}}
      (c)
      Use StringJoin to turn what you got in 12(b) into
       ,LXXXII,LXXXIII,LXXXIV,LXXXV,LXXXVI,LXXXVII,LXXXVIII,LXXXIX}.
In[134]:=
       (* 12c *)
      StringJoin /@
       Cases[Characters /@ RomanNumeral[Range[100]], {___, "X", "X", "X", ___}]
Out[134]=
       {XXX, XXXI, XXXII, XXXIII, XXXIV, XXXV, XXXVI, XXXVII, XXXVIII, XXXIX, LXXX,
        LXXXI, LXXXII, LXXXIII, LXXXIV, LXXXV, LXXXVII, LXXXVIII, LXXXIX}
```

1. Applying Functions $\frac{2}{2}$ / 2
Perfect. Surprisingly (to me), only two people got this one!
2. Pure Anonymous Functions <u>2</u> /2
Perfect. Lots of people didn't get 2(b)!
3. Applying Functions Repeatedly 2 / 2
Perfect.
4. Tests and Conditionals <u>2</u> / 2
Nice. Although in 4(a) there is a slicker form of PrimeQ that avoids PrimeQ[#]&.
5. More About Pure Functions 2/2
Perfect, and your observation that this is just Factorial is correct.
6. Rearranging Lists <u>2</u> /2
Perfect, although check out my solution for an extra cute levelspec option.
7. Parts of Lists/ 2
8. Patterns/ 2
9. Assigning Names to Things / 2
10. Immediate and Delayed Values / 2
11. Defining Your Own Functions / 2
12. More About Patterns/3