Brian — PS 18 — 2025-04-15 — Solution

EIWL3 Sections 41 and 42

My solutions to 41.9 and 41.10 are broken.

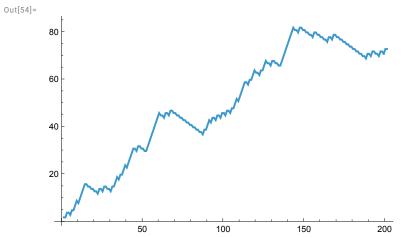
Exercises from EIWL3 Section 41

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ln[1] = (* 41.1 *) Cases[IntegerDigits[Array[#^2 &, 100]], {___, x__, y__, ___} /; x = y]
\texttt{Out[1]=} \ \left\{ \{1,\,0,\,0\}\,,\,\{1,\,4,\,4\}\,,\,\{2,\,2,\,5\}\,,\,\{4,\,0,\,0\}\,,\,\{4,\,4,\,1\}\,,\,\{9,\,0,\,0\}\,,\,\{1,\,1,\,5,\,6\}\,,\, (1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1,\,5,\,6)\,,\,(1,\,1
                      \{1, 2, 2, 5\}, \{1, 4, 4, 4\}, \{1, 6, 0, 0\}, \{2, 1, 1, 6\}, \{2, 2, 0, 9\},\
                     \{2, 5, 0, 0\}, \{3, 3, 6, 4\}, \{3, 6, 0, 0\}, \{3, 8, 4, 4\}, \{4, 2, 2, 5\},
                     \{4, 4, 8, 9\}, \{4, 9, 0, 0\}, \{5, 7, 7, 6\}, \{6, 4, 0, 0\}, \{6, 8, 8, 9\},
                     \{7, 2, 2, 5\}, \{7, 7, 4, 4\}, \{8, 1, 0, 0\}, \{8, 8, 3, 6\}, \{1, 0, 0, 0, 0\}\}
 In[2]:= (* 41.2 *) StringJoin /@
                     Cases[Array[Characters[RomanNumeral[#]] &, 100], {___, "L", ___, "I", ___, "X", ___}]
Out[2]= {XLIX, LIX, LXIX, LXXIX, LXXXIX}
 In[3]:= (* 41.3 *) f[list ] := Equal[list, Reverse[list]]
 ln[4]:= (* 41.4 *) (* So as not to fill up my document, I just took the first 20: *)
                Take[Cases[Partition[TextWords[WikipediaData["alliteration"]], 2, 1],
                         \{x_{,}, y_{,}\} /; Characters[x][1] = Characters[y][1]], 20]
out[4]= {{or, of}, {as, a}, {Peter, Piper}, {pickled, peppers}, {Irish, It},
                      {as, an}, {ideas, in}, {Icelandic, It}, {cartoon, characters},
                      {the, term}, {identical, initial}, {several, special},
                      {as, alliteration}, {stressed, syllables}, {as, an}, {lazy, languid},
                      {languid, line}, {as, alliteration}, {be, because}, {such, syllables}}
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In[5]:= {{"or", "of"}, {"as", "a"}, {"Peter", "Piper"}, {"pickled", "peppers"},
        {"Irish", "It"}, {"as", "an"}, {"ideas", "in"}, {"Icelandic", "It"},
        {"cartoon", "characters"}, {"the", "term"}, {"identical", "initial"},
        {"several", "special"}, {"as", "alliteration"}, {"stressed", "syllables"},
        {"as", "an"}, {"lazy", "languid"}, {"languid", "line"},
        {"as", "alliteration"}, {"be", "because"}, {"such", "syllables"}}
       (* Notice that this solution is case-sensitive. One could also convert the *)
       (* characters to lower-case and then test to get a case-insensitive test. *)
 out[5]= {{or, of}, {as, a}, {Peter, Piper}, {pickled, peppers}, {Irish, It},
        {as, an}, {ideas, in}, {Icelandic, It}, {cartoon, characters},
        {the, term}, {identical, initial}, {several, special},
        {as, alliteration}, {stressed, syllables}, {as, an}, {lazy, languid},
        {languid, line}, {as, alliteration}, {be, because}, {such, syllables}}
 ln[8]:= (* 41.5 *) Clear[x, y];
      (* I was getting gibberish due to having defined x and y elsewhere. \star)
      FixedPointList[
         (\# /. \{x_{--}, b_{-}, a_{-}, y_{--}\} /; b > a \rightarrow \{x, a, b, y\}) \&, \{4, 5, 1, 3, 2\}] // Grid
      45132
      4 1 5 3 2
      1 4 5 3 2
      1 4 3 5 2
 Out[9]= 13452
      1 3 4 2 5
      1 3 2 4 5
      12345
      12345
ln[10]:= (* 41.6 *) Clear[x, y];
      Transpose[FixedPointList[# /. \{x_{--}, b_{-}, a_{-}, y_{--}\} /; b > a \rightarrow \{x, a, b, y\} \&,
          RandomInteger[100, 50]]] // ArrayPlot
Out[11]=
ln[12] = (* 41.7 *) FixedPoint[(# + 2 / #) / 2 &, 1.0]
       (* This is a crafty way of computing Sqrt[2]. *)
Out[12]=
      1.41421
In[13]:= (* 41.8 *) FixedPointList[
       #/. {a_Integer, b_Integer} /; b \neq 0 \rightarrow \{b, Mod[a, b]\} \&, \{12345, 54321\}]
Out[13]=
      \{\{12345, 54321\}, \{54321, 12345\}, \{12345, 4941\},
        \{4941, 2463\}, \{2463, 15\}, \{15, 3\}, \{3, 0\}, \{3, 0\}\}
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ln[14]:= (* 41.9 *) Clear[x, y, z];
      FixedPointList[
       \# /. \{\{s[x][y][z] \rightarrow x[z][y[z]]\}, \{k[x][y] \rightarrow x\}\} \&, s[s][k][s[s[s]][s]]
Out[15]=
      $Aborted
      (* 41.10 *) IntegerDigits[Factorial[100]] /.
       {leading_.., remainder_} /; leading > 0 → leading
      {9, 3, 3, 2, 6, 2, 1, 5, 4, 4, 3, 9, 4, 4, 1, 5, 2, 6, 8, 1, 6, 9, 9, 2, 3, 8,
       8, 5, 6, 2, 6, 6, 7, 0, 0, 4, 9, 0, 7, 1, 5, 9, 6, 8, 2, 6, 4, 3, 8, 1, 6, 2,
       1, 4, 6, 8, 5, 9, 2, 9, 6, 3, 8, 9, 5, 2, 1, 7, 5, 9, 9, 9, 9, 3, 2, 2, 9, 9,
       1, 5, 6, 0, 8, 9, 4, 1, 4, 6, 3, 9, 7, 6, 1, 5, 6, 5, 1, 8, 2, 8, 6, 2, 5, 3,
       6, 9, 7, 9, 2, 0, 8, 2, 7, 2, 2, 3, 7, 5, 8, 2, 5, 1, 1, 8, 5, 2, 1, 0, 9, 1, 6,
       In[37]:= (* 41.11 *) Length /@ NestList[
        If[#[1] == 1, Join[Drop[#, 2], {0, 1}], Join[Drop[#, 2], {1, 0, 0}]] &, {1, 0}, 200]
Out[37]=
      {2, 2, 3, 3, 4, 4, 5, 6, 6, 7, 8, 9, 9, 10, 11, 11, 12, 12, 13, 13, 14, 14, 15, 16, 16, 17,
       17, 18, 19, 19, 20, 21, 22, 22, 23, 23, 24, 24, 25, 25, 26, 26, 27, 28, 29, 29, 30,
       30, 31, 32, 32, 33, 33, 34, 35, 35, 36, 37, 37, 38, 38, 39, 40, 40, 41, 42, 43, 43,
       44, 44, 45, 45, 46, 46, 47, 47, 48, 48, 49, 50, 50, 51, 52, 53, 53, 54, 55, 55, 56,
       56, 57, 58, 58, 59, 59, 60, 61, 61, 62, 62, 63, 64, 64, 65, 66, 67, 67, 68, 69, 69,
       70, 70, 71, 71, 72, 72, 73, 74, 74, 75, 76, 77, 77, 78, 78, 79, 79, 80, 80, 81, 82,
       82, 83, 84, 85, 85, 86, 87, 87, 88, 88, 89, 89, 90, 90, 91, 92, 92, 93, 93, 94, 95,
       95, 96, 97, 98, 98, 99, 100, 100, 101, 101, 102, 103, 103, 104, 104, 105, 106,
       106, 107, 108, 109, 109, 110, 111, 111, 112, 112, 113, 113, 114, 114, 115, 116,
       116, 117, 117, 118, 119, 119, 120, 121, 122, 122, 123, 123, 124, 124, 125, 125}
In[51]:= (* 41.12 *)switch[foo_] :=
       Module[{fooDropped = Drop[foo, 2]}, Switch[foo[1], 0, Join[fooDropped, {2, 1}],
          1, Append[fooDropped, 0], 2, Join[fooDropped, {0, 2, 1
            , 2}]]]
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Exercises from EIWL3 Section 42

ln[*]:= (* 42.1 *) StringReplace["1 2 3 4", " " \rightarrow "---"] Out[*]=

1---2---3---4

(* 42.2 *)

(* 42.3 *)

(* 42.4 *)

(* 42.5 *)

(* 42.6 *)

(* 42.7 *)

(* 42.8 *)