## Brian — PS 21 — 2025-04-25 — Solution

EIWL3 Sections 47 and 48

## Exercises from EIWL3 Section 47

```
In[39]:= (* 47.1 *) Total[Array[# (#+1) &, 1000]]

Out[39]:= 334334000

In[40]:= (* 47.2 *) Nest \left[\frac{1}{1+\#} &, x, 10\right]

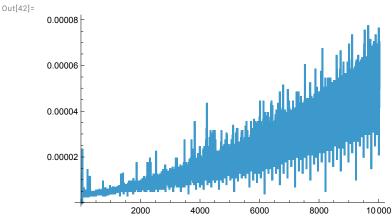
Out[40]:= \frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1+\frac{1}{1+\frac{1+\frac{1}{1+\frac{1+\frac{1}{1+\frac{1+\frac{1}{1+\frac{1+\frac{1}{1+\frac{1+\frac{1}{1+\frac{1+\frac{1}{1+\frac{1+\frac{1+\frac{1}{1+\frac{
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In[41]:= (\* 47.3 \*) Flatten[Array[{#1, #2} &, {10, 10}]]

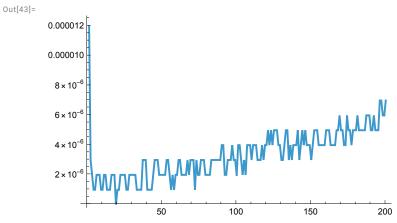
Out[41]=

{1, 1, 1, 2, 1, 3, 1, 4, 1, 5, 1, 6, 1, 7, 1, 8, 1, 9, 1, 10, 2, 1, 2, 2, 2, 3, 2, 4, 2, 5, 2, 6, 2, 7, 2, 8, 2, 9, 2, 10, 3, 1, 3, 2, 3, 3, 3, 4, 3, 5, 3, 6, 3, 7, 3, 8, 3, 9, 3, 10, 4, 1, 4, 2, 4, 3, 4, 4, 4, 5, 4, 6, 4, 7, 4, 8, 4, 9, 4, 10, 5, 1, 5, 2, 5, 3, 5, 4, 5, 5, 6, 5, 7, 5, 8, 5, 9, 5, 10, 6, 1, 6, 2, 6, 3, 6, 4, 6, 5, 6, 6, 6, 7, 6, 8, 6, 9, 6, 10, 7, 1, 7, 2, 7, 3, 7, 4, 7, 5, 7, 6, 7, 7, 7, 8, 7, 9, 7, 10, 8, 1, 8, 2, 8, 3, 8, 4, 8, 5, 8, 6, 8, 7, 8, 8, 8, 9, 8, 10, 9, 1, 9, 2, 9, 3, 9, 4, 9, 5, 9, 6, 9, 7, 9, 8, 9, 9, 10, 10, 1, 10, 2, 10, 3, 10, 4, 10, 5, 10, 6, 10, 7, 10, 8, 10, 9, 10, 10}

 $ln[42] = (* 47.4 *) ListLinePlot[Array[{#, Timing[#"][1]} &, 10000]]$ 



## In[43]:= (\* 47.5 \*) ListLinePlot[Array[{#, Timing[Sort[RandomSample[Range[#], #]]][1]} &, 200]]



In[44]:=

## Exercises from EIWL3 Section 48

(\* Counts[StringTake[#,2]&/@WordList[]]\*)

(\* 48.1 \*) (\* Correct this code: \*)

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(* Counts[StringTake[#,Min[2,StringLength[#]]]&/@WordList[]] *)
                                    (* or, if you aren't interested in the one-letter cases, *)
                                    Counts[StringTake[#, 2] & /@ Select[WordList[], StringLength[#] ≥ 2 &]]
Out[49]=
                                    \langle | aa \rightarrow 2, ab \rightarrow 170, ac \rightarrow 217, ad \rightarrow 191, ae \rightarrow 26, af \rightarrow 72, ag \rightarrow 81, ah \rightarrow 5, ai \rightarrow 55, AI \rightarrow 1,
                                          aj \rightarrow 1, ak \rightarrow 2, al \rightarrow 204, am \rightarrow 139, an \rightarrow 330, ao \rightarrow 3, ap \rightarrow 165, Ap \rightarrow 1, aq \rightarrow 14,
                                          ar \rightarrow 207, as \rightarrow 198, AS \rightarrow 1, at \rightarrow 99, au \rightarrow 117, Au \rightarrow 1, av \rightarrow 46, aw \rightarrow 30, ax \rightarrow 12,
                                         ay \rightarrow 2, az \rightarrow 4, ba \rightarrow 448, BA \rightarrow 1, be \rightarrow 359, bi \rightarrow 208, bl \rightarrow 254, bo \rightarrow 302, br \rightarrow 306,
                                          bu \rightarrow 255, by \rightarrow 14, ca \rightarrow 612, ce \rightarrow 126, ch \rightarrow 442, ci \rightarrow 89, cl \rightarrow 265, cn \rightarrow 1, co \rightarrow 1589,
                                         CO \rightarrow 1, cr \rightarrow 337, cu \rightarrow 184, cy \rightarrow 45, cz \rightarrow 3, da \rightarrow 152, dB \rightarrow 1, de \rightarrow 884, De \rightarrow 1, dh \rightarrow 2,
                                         di \rightarrow 827, DN \rightarrow 1, do \rightarrow 244, DO \rightarrow 1, dr \rightarrow 172, du \rightarrow 113, dw \rightarrow 9, dy \rightarrow 29, ea \rightarrow 72,
                                          eb \rightarrow 7, ec \rightarrow 45, ed \rightarrow 39, ee \rightarrow 4, e' \rightarrow 2, ef \rightarrow 45, eg \rightarrow 28, eh \rightarrow 1, ei \rightarrow 16, ej \rightarrow 3,
                                         el \rightarrow 136, em \rightarrow 144, en \rightarrow 316, eo \rightarrow 1, ep \rightarrow 53, eq \rightarrow 41, er \rightarrow 56, es \rightarrow 63, et \rightarrow 42,
                                          eu \rightarrow 25, ev \rightarrow 76, ew \rightarrow 2, ex \rightarrow 416, ey \rightarrow 21, fa \rightarrow 276, fe \rightarrow 174, Fe \rightarrow 1, fi \rightarrow 251,
                                          fj \rightarrow 1, fl \rightarrow 266, fo \rightarrow 335, F0 \rightarrow 1, fr \rightarrow 228, Fr \rightarrow 1, fu \rightarrow 138, ga \rightarrow 193, ge \rightarrow 153,
                                          gh \rightarrow 15, gi \rightarrow 65, gl \rightarrow 136, gn \rightarrow 13, go \rightarrow 124, Go \rightarrow 1, gr \rightarrow 347, gu \rightarrow 120, gy \rightarrow 19,
                                          ha \rightarrow 363, he \rightarrow 321, hi \rightarrow 127, HI \rightarrow 1, h' \rightarrow 1, hm \rightarrow 1, ho \rightarrow 340, hu \rightarrow 134, hy \rightarrow 116,
                                         ia \rightarrow 4, ib \rightarrow 4, ic \rightarrow 27, id \rightarrow 55, if \rightarrow 2, ig \rightarrow 18, il \rightarrow 54, im \rightarrow 324, in \rightarrow 1244, io \rightarrow 10,
                                          ip \rightarrow 1, IQ \rightarrow 1, ir \rightarrow 90, is \rightarrow 36, it \rightarrow 17, iv \rightarrow 3, ja \rightarrow 72, Ja \rightarrow 1, je \rightarrow 47, ji \rightarrow 32,
                                          jo \rightarrow 76, ju \rightarrow 86, Ju \rightarrow 2, ka \rightarrow 20, kc \rightarrow 1, ke \rightarrow 40, kh \rightarrow 3, kH \rightarrow 1, ki \rightarrow 88, kl \rightarrow 4,
                                          kn \rightarrow 51, ko \rightarrow 10, kp \rightarrow 1, kr \rightarrow 5, ku \rightarrow 3, kv \rightarrow 1, kW \rightarrow 1, la \rightarrow 301, le \rightarrow 224, li \rightarrow 293,
                                          ll \rightarrow 2, lo \rightarrow 226, lu \rightarrow 102, ly \rightarrow 20, ma \rightarrow 589, lo \rightarrow 2, lo \rightarrow 363, lo \rightarrow 409, lo \rightarrow 2,
                                         \texttt{mo} \rightarrow \texttt{392}, \ \texttt{Mo} \rightarrow \texttt{1}, \ \texttt{ms} \rightarrow \texttt{1}, \ \texttt{mu} \rightarrow \texttt{206}, \ \texttt{my} \rightarrow \texttt{33}, \ \texttt{na} \rightarrow \texttt{129}, \ \texttt{ne} \rightarrow \texttt{208}, \ \texttt{ni} \rightarrow \texttt{87}, \ \texttt{no} \rightarrow \texttt{304}, 
                                         No \rightarrow 1, nt \rightarrow 1, nu \rightarrow 86, ny \rightarrow 4, oa \rightarrow 15, ob \rightarrow 126, oc \rightarrow 46, o' \rightarrow 2, 0c \rightarrow 1, od \rightarrow 19,
                                         oe \rightarrow 2, of \rightarrow 47, og \rightarrow 3, oh \rightarrow 5, oi \rightarrow 12, ok \rightarrow 3, ol \rightarrow 20, om \rightarrow 19, on \rightarrow 34, oo \rightarrow 7,
                                         op \rightarrow 86, or \rightarrow 114, os \rightarrow 28, ot \rightarrow 7, ou \rightarrow 125, ov \rightarrow 215, ow \rightarrow 11, ox \rightarrow 19, oy \rightarrow 1,
                                         oz \rightarrow 1, pa \rightarrow 553, pe \rightarrow 487, pf \rightarrow 1, pH \rightarrow 1, ph \rightarrow 160, pi \rightarrow 217, pl \rightarrow 228, pn \rightarrow 4,
                                         po \rightarrow 402, pr \rightarrow 815, ps \rightarrow 50, pt \rightarrow 3, pu \rightarrow 225, py \rightarrow 22, qu \rightarrow 194, ra \rightarrow 307, re \rightarrow 1228,
                                          \mathsf{rh} \to \mathsf{39}, \ \mathsf{ri} \to \mathsf{148}, \ \mathsf{ro} \to \mathsf{206}, \ \mathsf{ru} \to \mathsf{122}, \ \mathsf{ry} \to \mathsf{1}, \ \mathsf{sa} \to \mathsf{321}, \ \mathsf{Sa} \to \mathsf{1}, \ \mathsf{sc} \to \mathsf{334}, \ \mathsf{se} \to \mathsf{552},
                                         Se \rightarrow 1, sh \rightarrow 377, si \rightarrow 241, sk \rightarrow 94, sl \rightarrow 196, sm \rightarrow 77, sn \rightarrow 115, so \rightarrow 300, sp \rightarrow 400,
                                          sq \rightarrow 56, st \rightarrow 697, su \rightarrow 519, Su \rightarrow 1, sv \rightarrow 1, sw \rightarrow 119, sy \rightarrow 100, ta \rightarrow 270, te \rightarrow 313,
                                          th \rightarrow 283, Th \rightarrow 1, ti \rightarrow 167, TN \rightarrow 1, to \rightarrow 253, tr \rightarrow 476, ts \rightarrow 3, tu \rightarrow 119, Tu \rightarrow 1,
                                         \mathsf{TV} \to \mathsf{1}, \mathsf{tw} \to \mathsf{49}, \mathsf{ty} \to \mathsf{42}, \mathsf{ub} \to \mathsf{2}, \mathsf{ud} \to \mathsf{1}, \mathsf{UF} \to \mathsf{1}, \mathsf{ug} \to \mathsf{3}, \mathsf{uk} \to \mathsf{2}, \mathsf{ul} \to \mathsf{24}, \mathsf{um} \to \mathsf{14},
                                         un \rightarrow 1335, UN \rightarrow 1, up \rightarrow 75, ur \rightarrow 36, us \rightarrow 25, ut \rightarrow 18, uv \rightarrow 2, ux \rightarrow 1, va \rightarrow 143,
                                         ve \rightarrow 170, vi \rightarrow 214, VI \rightarrow 1, vo \rightarrow 84, vu \rightarrow 15, wa \rightarrow 252, we \rightarrow 127, We \rightarrow 1, wh \rightarrow 165,
                                        \texttt{wi} \rightarrow \texttt{186, wo} \rightarrow \texttt{166, wr} \rightarrow \texttt{68, xe} \rightarrow \texttt{6, xi} \rightarrow \texttt{1, xy} \rightarrow \texttt{3, ya} \rightarrow \texttt{26, ye} \rightarrow \texttt{36, yi} \rightarrow \texttt{6, yo} \rightarrow \texttt{27, ye} \rightarrow \texttt{36, ye} 
                                         yt \rightarrow 2, yu \rightarrow 7, za \rightarrow 3, ze \rightarrow 19, zi \rightarrow 15, zl \rightarrow 1, zo \rightarrow 13, zu \rightarrow 1, zw \rightarrow 1, zy \rightarrow 3 \mid > 1
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