

# Oscillations and Waves Exam 3

April 29, 2025

This exam tests your fluency with the core of the Wolfram Language, as it was presented in *An Elementary Introduction to the Wolfram Language, 3rd Edition (EIWL3)*, Sections 25-34 and 38-41. There is one problem with two or three parts corresponding to each section. **Tip: all of them are meant to be quick. If you get bogged down, move on.**

## Directions:

After downloading this notebook, rename it with your first name in the filename. E.g., *Eli-Exam3.nb*, *Harper-Exam3.nb*, *Hexi-Exam3.nb*, *Jeremy-Exam3.nb*, *Rania-Exam3.nb*, *Tahm-Exam3.nb*, or *Walker-Exam3.nb*.

Then disconnect from the wifi and work the exam. Save your notebook early and often so that you don't lose work in progress.

**Your answers always go into the Wolfram Language Input cells that begin with a comment, e.g.,**

```
(* 1a *) foobar /@ Plus[Array]
```

**All your answers should execute and re-execute without warnings or error messages.**

You may refer to your downloaded copies of *EIWL3*, and anything else we developed in the course (like your cheat sheets!), but not to any web resources.

When you are done, save your notebook one last time, re-join the wifi, and then email it to me.

This exam was designed to require about 45 minutes, but if you need a full hour, that is ok. Everyone will stop at the one-hour mark.

## 1. Applying Functions (*EIWL3* Section 25)

(a)

Use **Map** with a *levelspec* to put a frame around each individual number in the array **Array[Plus, {10, 10}]** (we don't want frames around already-framed things — just one level of frames around the individual numbers).

```
In[1]:= (* 1a *) Map[Framed, Array[Plus, {10, 10}], {2}]
```

Out[1]=

2	3	4	5	6	7	8	9	10	11
3	4	5	6	7	8	9	10	11	12
4	5	6	7	8	9	10	11	12	13
5	6	7	8	9	10	11	12	13	14
6	7	8	9	10	11	12	13	14	15
7	8	9	10	11	12	13	14	15	16
8	9	10	11	12	13	14	15	16	17
9	10	11	12	13	14	15	16	17	18
10	11	12	13	14	15	16	17	18	19
11	12	13	14	15	16	17	18	19	20

(b)

Copy what you did in (a), but for this part, also turn the result into a grid using **Grid** and the “as an afterthought” syntax:

```
In[2]:= (* 1b *) Map[Framed, Array[Plus, {10, 10}], {2}] // Grid
```

Out[2]=

2	3	4	5	6	7	8	9	10	11
3	4	5	6	7	8	9	10	11	12
4	5	6	7	8	9	10	11	12	13
5	6	7	8	9	10	11	12	13	14
6	7	8	9	10	11	12	13	14	15
7	8	9	10	11	12	13	14	15	16
8	9	10	11	12	13	14	15	16	17
9	10	11	12	13	14	15	16	17	18
10	11	12	13	14	15	16	17	18	19
11	12	13	14	15	16	17	18	19	20

## 2. Pure Anonymous Functions (EIWL3 Section 26)

(a)

Use the **#** and **&** notation to create an anonymous function that cubes whatever is given it, and then use **/@** to apply it to every member of the list **{1,2,3,4,5}**.

```
In[3]:= (* 2a *) #^3 & /@ {1,2,3,4,5}
Out[3]= {1, 8, 27, 64, 125}
```

(b)

Use the **#1**, **#2**, and **&** notation to create an anonymous function that divides its first argument by its second argument. Combine this with **Apply** and a *levelspec* to apply the function to **{{1,2},{2,3},{3,4},{4,5}}**. Once you have this right, you will get  $\{\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}\}$ .

```
In[4]:= (* 2b *) Apply[#1 / #2 &, {{1,2},{2,3},{3,4},{4,5}}, 2]
Out[4]= {1/2, 2/3, 3/4, 4/5}
```

## 3. Applying Functions Repeatedly (EIWL3 Section 27)

(a)

Use **Nest** to apply **Factorial** twice to **{1,2,3,4}**. If you have this right, 620,448,401,733,239,439,360,000 will be one of the elements of your answer.

```
In[5]:= (* 3a *) Nest[Factorial, {1,2,3,4}, 2]
Out[5]= {1, 2, 720, 620 448 401 733 239 439 360 000}
```

(b)

Use **NestList** to apply **Factorial** three times to **{1,2,3}**, as well as showing the results of doing it 0, 1, and 2 times. If you have this right, you will have an insanely large result at the third step. Do not go any higher, or I do not know what will happen to your computer.



```
In[8]:= (* 4b *) Select[Range[20], PrimeQ]
Out[8]= {2, 3, 5, 7, 11, 13, 17, 19}
```

## 5. More About Pure Functions (E/WL3 Section 29)

(a)

Accomplish exactly the same thing as `Table[n*(n-1)/2, {n,6}]` using `Array` and a pure function.

```
In[9]:= (* 5a *) Array[#*(#-1)/2 &, 6]
Out[9]= {0, 1, 3, 6, 10, 15}
```

(b)

Make some modifications to `FoldList[Plus, {1,2,3,4,5}]` so that it produces a list of the first 10 factorials. Instead of hand-coding the list up to 10, begin by first changing `{1,2,3,4,5}` to `Range[10]`.

```
In[10]:= (* 5b *) FoldList[Times, Range[10]]
Out[10]= {1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800}
```

## 6. Rearranging Lists (E/WL3 Section 30)

(a)

Use `Transpose` and one of the *levelspec* options to turn `{{{1,uno},{2,dos},{3,tres}},{{4,cuatro},{5,cinco},{6,seis}}}` into `{{{1,2,3},{uno,dos,tres}},{{4,5,6},{cuatro,cinco,seis}}}`

```
In[11]:= (* 6a *)
Transpose[{{{1,uno},{2,dos},{3,tres}},{{4,cuatro},{5,cinco},{6,seis}}},2↔3]
Out[11]= {{{1, 2, 3}, {uno, dos, tres}}, {{4, 5, 6}, {cuatro, cinco, seis}}}
```

(b)

Use `Flatten` and a *levelspec* option to turn `{{{1,uno},{2,dos},{3,tres}},{{4,cuatro},{5,cinco},{6,seis}}}` into `{{1,uno},{2,dos},{3,tres},{4,cuatro},{5,cinco},{6,seis}}`

```
In[12]:= (* 6b *) Flatten[{{{1,uno},{2,dos},{3,tres}},{{4,cuatro},{5,cinco},{6,seis}}},1]
Out[12]= {1, uno, 2, dos, 3, tres, 4, cuatro, 5, cinco, 6, seis}
```

## 7. Parts of Lists (EIWL3 Section 31)

(a)

Use the magical **All** position (you will need to use **All** more than once) to turn

`{{{Eli, Lerner},{Harper,Yonago},{Hexi,Jin}},{Jeremy,Choy},{Rania,Zaki},  
{Tahm,Loyd},{Walker,Harris}}}` into  
`{{Eli,Harper,Hexi},{Jeremy,Rania,Tahm,Walker}}`

```
In[13]:= (* 7a *) {{{Eli, Lerner},{Harper,Yonago},{Hexi,Jin}},
           {{Jeremy,Choy},{Rania,Zaki},{Tahm,Loyd},{Walker,Harris}}}[[All,All,1]]
Out[13]=
{{Eli, Harper, Hexi}, {Jeremy, Rania, Tahm, Walker}}
```

(b)

Use a magical *negative positional argument* to extract `{Jeremy,Rania,Tahm,Walker}` from  
`{{Eli,Harper,Hexi},{Jeremy,Rania,Tahm,Walker}}` and combine that with **Take** with a  
different magical *negative* argument to extract `{Tahm,Walker}`.

```
In[14]:= (* 7b *) Take[{{Eli,Harper,Hexi},{Jeremy,Rania,Tahm,Walker}}[[-1]],-2]
Out[14]=
{Tahm, Walker}
```

## 8. Patterns (EIWL3 Section 32)

(a)

Use **Cases** to choose the lists that begin and end with the same letter in this list of lists (but look ahead to part (b) before you solve part (a)):

```
{
  {"a", "l", "u", "l", "a"},
  {"a", "l", "o", "h", "a"},
  {"a", "r", "a", "r", "a"},
  {"b", "o", "n", "u", "s"},
  {"c", "i", "v", "i", "c"},
  {"d", "e", "b", "e", "d"},
  {"e", "l", "b", "o", "w"},
  {"z", "a"},
  {"z", "z"}
}
```

```
In[15]:= (* 8a *) Cases[{
  {"a", "l", "u", "l", "a"},
  {"a", "l", "o", "h", "a"},
  {"a", "r", "a", "r", "a"},
  {"b", "o", "n", "u", "s"},
  {"c", "i", "v", "i", "c"},
  {"d", "e", "b", "e", "d"},
  {"e", "l", "b", "o", "w"},
  {"z", "a"},
  {"z", "z"}
},
{x_, __, x_}
]
```

```
Out[15]= {{a, l, u, l, a}, {a, l, o, h, a}, {a, r, a, r, a}, {c, i, v, i, c}, {d, e, b, e, d}}
```

(b)

The pattern **BlankNullSequence** has the shorthand `___`. Use `___` to improve the pattern you used in Part (a) so that the two-letter list `{z, z}` is also included in your result.

```
In[16]:= (* 8b *) Cases[{
  {"a", "l", "u", "l", "a"},
  {"a", "l", "o", "h", "a"},
  {"a", "r", "a", "r", "a"},
  {"b", "o", "n", "u", "s"},
  {"c", "i", "v", "i", "c"},
  {"d", "e", "b", "e", "d"},
  {"e", "l", "b", "o", "w"},
  {"z", "a"},
  {"z", "z"}
},
{x_, ___, x_}
]
```

```
Out[16]= {{a, l, u, l, a}, {a, l, o, h, a}, {a, r, a, r, a}, {c, i, v, i, c}, {d, e, b, e, d}, {z, z}}
```

## 9. Assigning Names to Things (EIWL3 Section 38)

(a)

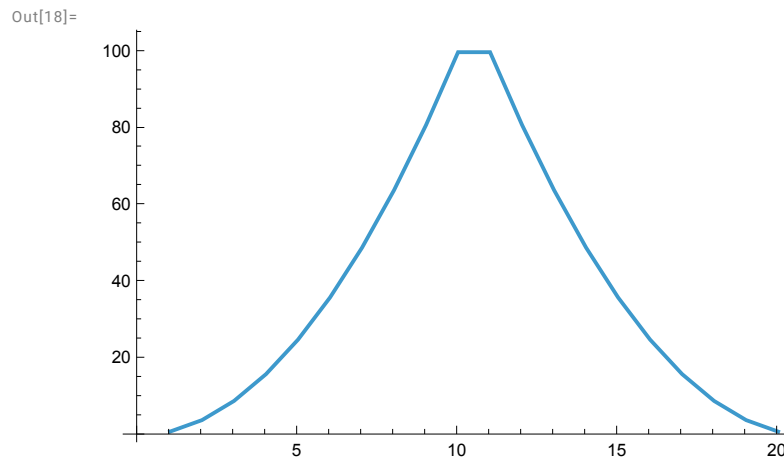
Use **Module** to compute `x=Factorial[10]`, and then produce `{x,x^2,x^3}`.

```
In[17]:= (* 9a *) Module[{x = Factorial[10]}, {x, x^2, x^3}]
Out[17]= {3 628 800, 13 168 189 440 000, 47 784 725 839 872 000 000}
```

(b)

Inside **Module**, let **rangeSquared=Range[10]^2**, and then produce a list line plot of **rangeSquared** joined with **Reverse[rangeSquared]**.

```
In[18]:= (* 9b *) Module[{rangeSquared=Range[10]^2},
  ListLinePlot[Join[rangeSquared, Reverse[rangeSquared]]]]
```



## 10. Immediate and Delayed Values (E/IWL3 Section 39)

(a)

Make a one-character change to this expression,

**Module[{x:=RandomInteger[10]}, {x, x^2, x^3, x^4}]**, so that it produces four different powers of the same random number instead of four different powers of different random numbers.

```
In[19]:= (* 10a *) Module[{x=RandomInteger[10]}, {x, x^2, x^3, x^4}]
Out[19]= {9, 81, 729, 6561}
```

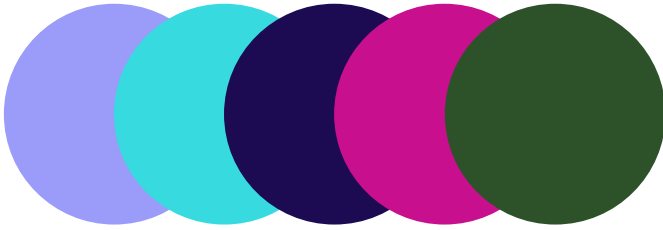
(b)

Make a one-character change to this expression,

**Module[{color=RandomColor[]}, Graphics[Table[Style[Disk[{i,0}], color], {i, 5}]]]**, so that it produces five different-color disks.



```
In[20]:= (* 10b *) Module[{color:=RandomColor[]},
Graphics[Table[Style[Disk[{i,0}],color],{i,5}]]]
Out[20]=
```



## 11. Defining Your Own Functions (EIWL3 Section 40)

### (a) Wording on 11(a) could use improvement.

Define a function **f** that takes a list of three elements and out of them makes a list of lists that contains all six possible orderings. Using **Permutations** will make this easy.

Include a test of your function as **f[1,2,3]** and make sure it gets **{{1,2,3},{1,3,2},{2,1,3},{2,3,1},{3,1,2},{3,2,1}}**.

```
In[21]:= (* 11a *) f[x_, y_, z_] := Permutations[{x, y, z}]
f[1, 2, 3]
Out[22]=
{{1, 2, 3}, {1, 3, 2}, {2, 1, 3}, {2, 3, 1}, {3, 1, 2}, {3, 2, 1}}
```

### (b) Wording on 11(b) could also use improvement.

Define a function **g** that gives **1** for **g[0]**, and gives **n\*g[n-1]** for any integer **n** greater than **0**, *but don't use an If statement!* Include a test of your function as **g[6]** and make sure it gets **720**.

```
In[23]:= (* 11b *) g[0] = 1; g[n_] := n * g[n - 1]
g[6]
Out[24]=
720
```

## 12. More About Patterns (EIWL3 Section 41)

### (a)

Use the replacement rule notation — e.g., **/.** and **->** — to exchange the first and last element in any list containing two or more elements and test your replacement using the list **{alpha, beta, gamma, delta, epsilon}**.

```
In[25]:= (* 12a *) {alpha, beta, gamma, delta, epsilon} /. {x_, y___, z_} -> {z, y, x}
Out[25]= {epsilon, beta, gamma, delta, alpha}
```

(b)

Starting with `Characters/@RomanNumeral[Range[100]]`, select all the sequences corresponding to the Roman numerals that have XXX in them.

```
In[26]:= (* 12b *) Cases[Characters /@ RomanNumeral[Range[100]], {___, "X", "X", "X", ___}]
Out[26]= {{X, X, X}, {X, X, X, I}, {X, X, X, I, I}, {X, X, X, I, I, I}, {X, X, X, I, V},
  {X, X, X, V}, {X, X, X, V, I}, {X, X, X, V, I, I}, {X, X, X, V, I, I, I},
  {X, X, X, I, X}, {L, X, X, X}, {L, X, X, X, I}, {L, X, X, X, I, I},
  {L, X, X, X, I, I, I}, {L, X, X, X, I, V}, {L, X, X, X, V}, {L, X, X, X, V, I},
  {L, X, X, X, V, I, I}, {L, X, X, X, V, I, I, I}, {L, X, X, X, I, X}}
```

(c)

Use `StringJoin` to turn what you got in 12(b) into

`{XXX,XXXI,XXXII,XXXIII,XXXIV,XXXV,XXXVI,XXXVII,XXXVIII,XXXIX,LXXX,LXXXI,LXXXII,LXXXIII,LXXXIV,LXXXV,LXXXVI,LXXXVII,LXXXVIII,LXXXIX}`.

```
In[27]:= (* 12c *)
StringJoin /@ Cases[Characters /@ RomanNumeral[Range[100]], {___, "X", "X", "X", ___}]
Out[27]= {XXX, XXXI, XXXII, XXXIII, XXXIV, XXXV, XXXVI, XXXVII, XXXVIII, XXXIX, LXXX,
  LXXXI, LXXXII, LXXXIII, LXXXIV, LXXXV, LXXXVI, LXXXVII, LXXXVIII, LXXXIX}
```