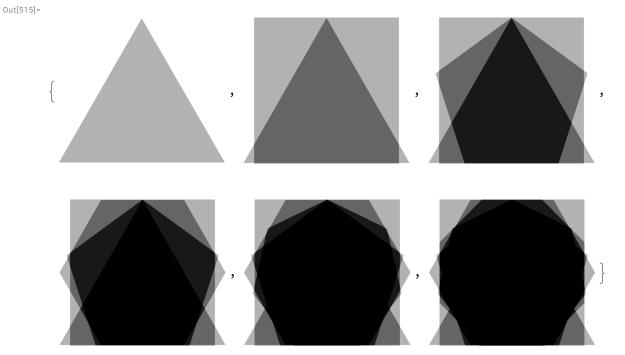
# Harper — PS 11 — 2025-03-18 EIWL Sections 29, 30

### Section 29

```
In[510]:=
      Array[Prime[#] &, 100]
Out[510]=
       {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79,
        83, 89, 97, 101, 103, 107, 109, 113, 127, 131, 137, 139, 149, 151, 157, 163,
        167, 173, 179, 181, 191, 193, 197, 199, 211, 223, 227, 229, 233, 239, 241, 251,
        257, 263, 269, 271, 277, 281, 283, 293, 307, 311, 313, 317, 331, 337, 347, 349,
        353, 359, 367, 373, 379, 383, 389, 397, 401, 409, 419, 421, 431, 433, 439,
        443, 449, 457, 461, 463, 467, 479, 487, 491, 499, 503, 509, 521, 523, 541}
In[511]:=
      Array[Prime[#+1] - Prime[#] &, 100]
Out[511]=
       {1, 2, 2, 4, 2, 4, 2, 4, 6, 2, 6, 4, 2, 4, 6, 6, 2, 6, 4, 2, 6, 4, 6, 8, 4, 2,
        4, 2, 4, 14, 4, 6, 2, 10, 2, 6, 6, 4, 6, 6, 2, 10, 2, 4, 2, 12, 12, 4, 2, 4,
        6, 2, 10, 6, 6, 6, 2, 6, 4, 2, 10, 14, 4, 2, 4, 14, 6, 10, 2, 4, 6, 8, 6, 6, 4,
        6, 8, 4, 8, 10, 2, 10, 2, 6, 4, 6, 8, 4, 2, 4, 12, 8, 4, 8, 4, 6, 12, 2, 18, 6}
In[512]:=
      Grid[Array[#1 + #2 &, {10, 10}]]
Out[512]=
       2 3 4 5 6 7 8 9 10 11
       3 4 5 6 7 8 9 10 11 12
       4 5 6 7 8 9 10 11 12 13
          6 7
               8 9 10 11 12 13 14
       6 7 8 9 10 11 12 13 14 15
       7 8 9 10 11 12 13 14 15 16
       8 9 10 11 12 13 14 15 16 17
       9 10 11 12 13 14 15 16 17 18
      10 11 12 13 14 15 16 17 18 19
      11 12 13 14 15 16 17 18 19 20
In[513]:=
       FoldList[Times, 1, Range[10]]
Out[513]=
       {1, 1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800}
In[514]:=
      FoldList[Times, Array[Prime[#] &, 10]]
Out[514]=
       {2, 6, 30, 210, 2310, 30030, 510510, 9699690, 223092870, 6469693230}
```





## Section 30

In[518]:=

```
 \begin{array}{l} \text{In} [516] \coloneqq \\ & \text{Thread} \big[ \text{FromLetterNumber} \big[ \text{Range} \big[ 26 \big] \big] \rightarrow \text{Range} \big[ 26 \big] \big] \\ \text{Out} [516] \coloneqq \\ & \{ a \rightarrow 1, \ b \rightarrow 2, \ c \rightarrow 3, \ d \rightarrow 4, \ e \rightarrow 5, \ f \rightarrow 6, \ g \rightarrow 7, \ h \rightarrow 8, \\ & i \rightarrow 9, \ j \rightarrow 10, \ k \rightarrow 11, \ l \rightarrow 12, \ m \rightarrow 13, \ n \rightarrow 14, \ o \rightarrow 15, \ p \rightarrow 16, \ q \rightarrow 17, \\ & r \rightarrow 18, \ s \rightarrow 19, \ t \rightarrow 20, \ u \rightarrow 21, \ v \rightarrow 22, \ w \rightarrow 23, \ x \rightarrow 24, \ y \rightarrow 25, \ z \rightarrow 26 \} \\ \\ & \text{In} [517] \coloneqq \\ & \text{Grid} \big[ \text{Partition} \big[ \text{FromLetterNumber} \big[ \text{Range} \big[ 24 \big] \big], \ 6 \big] \big] \\ \\ \text{Out} [517] \coloneqq \\ & \text{a b c d e f} \\ & \text{g h i j k l} \\ & \text{m n o p q r} \\ & \text{s t u v w x} \\ \end{array}
```

#### Grid[Partition[IntegerDigits[2^1000], 50], Frame → All]

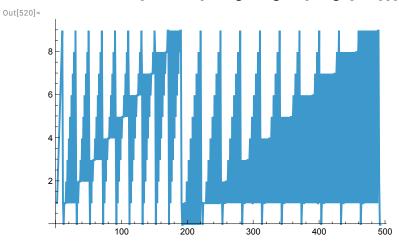
| Out[518]= |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|-----------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
|           | 1 | 0 | 7 | 1 | 5 | 0 | 8 | 6 | 0 | 7 | 1 | 8 | 6 | 2 | 6 | 7 | 3 | 2 | 0 | 9 | 4 | 8 | 4 | 2 | 5 | 0 | 4 | 9 | 0 | 6 | 0 | 0 | 0 | 1 | 8 | 1 | 0 | 5 | 6 | 1 | 4 | 0 | 4 | 8 | 1 | 1 | 7 |
|           | 3 | 3 | 6 | 0 | 7 | 4 | 4 | 3 | 7 | 5 | 0 | 3 | 8 | 8 | 3 | 7 | 0 | 3 | 5 | 1 | 0 | 5 | 1 | 1 | 2 | 4 | 9 | 3 | 6 | 1 | 2 | 2 | 4 | 9 | 3 | 1 | 9 | 8 | 3 | 7 | 8 | 8 | 1 | 5 | 6 | 9 | Ę |
|           | 1 | 2 | 7 | 5 | 9 | 4 | 6 | 7 | 2 | 9 | 1 | 7 | 5 | 5 | 3 | 1 | 4 | 6 | 8 | 2 | 5 | 1 | 8 | 7 | 1 | 4 | 5 | 2 | 8 | 5 | 6 | 9 | 2 | 3 | 1 | 4 | 0 | 4 | 3 | 5 | 9 | 8 | 4 | 5 | 7 | 7 | Ę |
|           | 9 | 8 | 5 | 7 | 4 | 8 | 0 | 3 | 9 | 3 | 4 | 5 | 6 | 7 | 7 | 7 | 4 | 8 | 2 | 4 | 2 | 3 | 0 | 9 | 8 | 5 | 4 | 2 | 1 | 0 | 7 | 4 | 6 | 0 | 5 | 0 | 6 | 2 | 3 | 7 | 1 | 1 | 4 | 1 | 8 | 7 | 7 |
|           | 1 | 8 | 2 | 1 | 5 | 3 | 0 | 4 | 6 | 4 | 7 | 4 | 9 | 8 | ω | 5 | 8 | 1 | 9 | 4 | 1 | 2 | 6 | 7 | 3 | 0 | 8 | 7 | 6 | 7 | 5 | 5 | 9 | 1 | 6 | 5 | 5 | 4 | 3 | 9 | 4 | 6 | 0 | 7 | 7 | 0 | ( |
|           | 4 | 5 | 7 | 1 | 1 | 9 | 6 | 4 | 7 | 7 | 6 | 8 | 6 | 5 | 4 | 2 | 1 | 6 | 7 | 6 | 6 | 0 | 4 | 2 | 9 | 8 | 3 | 1 | 6 | 5 | 2 | 6 | 2 | 4 | 3 | 8 | 6 | 8 | 3 | 7 | 2 | 0 | 5 | 6 | 6 | 8 | ( |

In[519]:=  $\label{lem:computers} {\tt Grid[Partition[Take[Characters[WikipediaData["Computers"]], 400], 20], Frame \rightarrow {\tt All}]}$ 

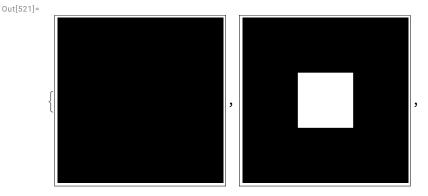
Out[519]=

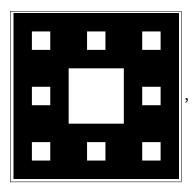
| _ |   |   |   |   |   |   |   |   |   |   | - |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| Α |   | С | 0 | m | р | u | t | е | r |   | i | s |   | а |   | m | а | С | h |
| i | n | υ |   | t | h | а | t |   | C | а | n |   | b | υ |   | р | r | 0 | g |
| r | а | m | m | Ψ | а |   | ۲ | 0 |   | а | ٦ | ť | 0 | m | а | t | ï | U | а |
| l | l | У |   | С | а | r | r | У |   | 0 | u | t |   | S | Ф | q | u | е | n |
| С | е | s |   | 0 | f |   | а | r | i | t | h | m | е | t | i | С |   | 0 | r |
|   | l | 0 | g | i | С | а | ι |   | 0 | р | е | r | а | t | i | 0 | n | s |   |
| ( | С | 0 | m | р | u | t | а | t | i | 0 | n | ) |   |   | М | 0 | d | е | r |
| n |   | d | i | g | i | t | а | ι |   | е | ι | е | С | t | r | 0 | n | i | С |
|   | С | 0 | m | р | u | t | е | r | s |   | С | а | n |   | р | е | r | f | 0 |
| r | m |   | g | е | n | е | r | i | С |   | s | е | t | s |   | 0 | f |   | 0 |
| р | е | r | а | t | i | 0 | n | s |   | k | n | 0 | w | n |   | а | s |   | р |
| r | 0 | g | r | а | m | s |   |   | Т | h | е | s | е |   | р | r | 0 | g | r |
| а | m | s |   | е | n | а | b | ι | е |   | С | 0 | m | р | u | t | е | r | s |
|   | t | 0 |   | р | е | r | f | 0 | r | m |   | а |   | W | i | d | е |   | r |
| а | n | g | е |   | 0 | f |   | t | а | s | k | s |   |   | Т | h | е |   | t |
| е | r | m |   | С | 0 | m | р | u | t | е | r |   | s | У | s | t | е | m |   |
| m | а | У |   | r | е | f | е | r |   | t | 0 |   | а |   | n | 0 | m | i | n |
| а | l | ι | У |   | С | 0 | m | р | ι | е | t | е |   | С | 0 | m | р | u | t |
| е | r |   | t | h | а | t |   | i | n | С | ι | u | d | е | s |   | t | h | е |
|   | h | а | r | а | W | а | r | Φ | , |   | 0 | р | Φ | r | а | t | i | n | g |

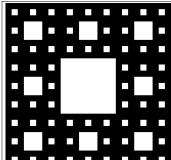
In[520]:= ListLinePlot[Flatten[IntegerDigits[Range[200]]]]

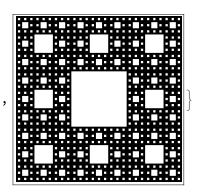


In[521]:= ArrayPlot /@ NestList[ArrayFlatten[{{#, #, #}, {#, 0, #}, {#, #, #}}] &, {{1}}, 4]









In[522]:=

Select[Flatten[Table[ $\{x, y, Sqrt[x^2 + y^2]\}, \{x, 20\}, \{y, 20\}], 1],$ IntegerQ[Last[#]] &]

Out[522]=

```
\{\{3, 4, 5\}, \{4, 3, 5\}, \{5, 12, 13\}, \{6, 8, 10\},\
 \{8, 6, 10\}, \{8, 15, 17\}, \{9, 12, 15\}, \{12, 5, 13\}, \{12, 9, 15\},
 \{12, 16, 20\}, \{15, 8, 17\}, \{15, 20, 25\}, \{16, 12, 20\}, \{20, 15, 25\}\}\
```

In[523]:=

Table[Max[Length[Gather[IntegerDigits[2^n]]]], {n, 100}]

Out[523]=

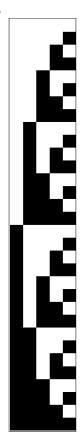
```
{1, 1, 1, 2, 2, 2, 3, 3, 3, 4, 4, 4, 4, 5, 5, 3, 5, 4, 4, 7, 6, 5, 4, 4, 4, 6,
6, 6, 9, 7, 7, 5, 6, 6, 7, 7, 8, 7, 7, 7, 6, 8, 7, 9, 8, 7, 8, 9, 7, 8, 9, 8,
7, 7, 8, 8, 7, 9, 8, 9, 9, 9, 9, 9, 9, 8, 9, 10, 9, 10, 7, 9, 8, 9, 9, 9, 8, 9,
 10, 9, 9, 10, 9, 10, 9, 9, 10, 10, 10, 9, 8, 9, 9, 10, 10, 10, 10, 10, 9, 10}
```

```
In[524]:=
      GatherBy[Array[IntegerName, 100], StringTake[#, 1] &]
Out[524]=
      {{one, one hundred}, {two, three, ten, twelve, thirteen, twenty, twenty-one,
        twenty-two, twenty-three, twenty-four, twenty-five, twenty-six, twenty-seven,
        twenty-eight, twenty-nine, thirty, thirty-one, thirty-two, thirty-three,
        thirty-four, thirty-five, thirty-six, thirty-seven, thirty-eight, thirty-nine},
       {four, five, fourteen, fifteen, forty, forty-one, forty-two, forty-three,
         forty-four, forty-five, forty-six, forty-seven, forty-eight,
         forty-nine, fifty, fifty-one, fifty-two, fifty-three, fifty-four,
        fifty-five, fifty-six, fifty-seven, fifty-eight, fifty-nine},
       {six, seven, sixteen, seventeen, sixty, sixty-one, sixty-two, sixty-three,
        sixty-four, sixty-five, sixty-six, sixty-seven, sixty-eight, sixty-nine,
        seventy, seventy-one, seventy-two, seventy-three, seventy-four,
        seventy-five, seventy-six, seventy-seven, seventy-eight, seventy-nine},
       {eight, eleven, eighteen, eighty, eighty-one, eighty-two, eighty-three,
        eighty-four, eighty-five, eighty-six, eighty-seven, eighty-eight, eighty-nine},
       {nine, nineteen, ninety, ninety-one, ninety-two, ninety-three, ninety-four,
        ninety-five, ninety-six, ninety-seven, ninety-eight, ninety-nine}}
In[525]:=
      SortBy[Take[WordList[], 50], StringTake[StringReverse[#], 1] &]
Out[525]=
      {a, abandoned, abashed, abbreviated, abed, abalone, abase, abate, abbe, abbreviate,
       abdicate, abeyance, abhorrence, abidance, abide, abducting, abiding, aah,
       abash, aardvark, aback, abdominal, abeam, abandon, abbreviation, abdication,
       abdomen, abduction, aberration, abjection, abattoir, abductor, abettor,
       abhor, abacus, abbess, abaft, abandonment, abasement, abashment, abatement,
       abbot, abduct, aberrant, abet, abhorrent, abject, abbey, ability, abjectly}
In[526]:=
      SortBy[Table[n^2, {n, 20}], First[IntegerDigits[#]] &]
Out[526]=
      {1, 16, 100, 121, 144, 169, 196, 25, 225, 256, 289, 36, 324, 361, 4, 49, 400, 64, 81, 9}
In[527]:=
      SortBy[Range[20], Length[Characters[IntegerName[#]]] &]
Out[527]=
      \{1, 2, 6, 10, 4, 5, 9, 3, 7, 8, 11, 12, 20, 15, 16, 13, 14, 18, 19, 17\}
In[528]:=
      GatherBy[RandomSample[WordList[], 20], StringLength]
Out[528]=
      {{topple, enough, tanned, sorbet},
       {amuse}, {brushwork, ruination, socialist, frivolous},
       {transmogrification}, {fortuneteller}, {valuable, unproved},
       {exaggerated, coeducation, kitchenware}, {curt, oops}, {karaoke}, {salutation}}
```

```
In[529]:=
                   Complement[Alphabet["Ukrainian"], Alphabet["Russian"]]
Out[529]=
                    \{\varepsilon, i, i, \ell\}
In[530]:=
                   Intersection[Table[n^2, {n, 100}], Table[n^3, {n, 100}]]
Out[530]=
                   {1, 64, 729, 4096}
                   Intersection EntityList | Worth Atlantic Treaty Organization COUNTRIES |
                      EntityList ☐ Group of 8 COUNTRIES ✓
Out[531]=
                                                   France,
                                                                             Germany, Italy,
                                                                                                                                United Kingdom ),
In[532]:=
                   Grid[Transpose[Permutations[Range[4]]]]
Out[532]=
                   1 1 1 1 1 1 2 2 2 2 2 2 3 3 3 3 3 3 4 4 4 4 4 4
                   2 2 3 3 4 4 1 1 3 3 4 4 1 1 2 2 4 4 1 1 2 2 3 3
                  3 4 2 4 2 3 3 4 1 4 1 3 2 4 1 4 1 2 2 3 1 3 1 2
                  4 3 4 2 3 2 4 3 4 1 3 1 4 2 4 1 2 1 3 2 3 1 2 1
In[533]:=
                   StringJoin /@ Permutations[Characters["hello"]]
Out[533]=
                    {hello, helol, heoll, hlelo, hleol, hlleo, hlloe, hloel, hlole, hoell, holel, holle,
                      ehllo, ehlol, eholl, elhlo, elhol, ellho, elloh, elohl, eohll, eolhl, eolhl,
                      lhelo, lheol, lhleo, lhloe, lhoel, lhole, lehlo, lelho, leloh, leohl, leolh,
                      llheo, llhoe, lleho, lleoh, llohe, lloeh, lohle, loehl, loelh, lolhe, loleh,
                       ohell, ohlel, ohlle, oehll, oelhl, oellh, olhel, olhle, olehl, olehh, ollhe, olleh}
```

#### In[534]:= ArrayPlot[Tuples[{0, 1}, 5]]

Out[534]=



```
In[535]:=
       Table[StringJoin[RandomSample[FromLetterNumber[Range[26]], 5]], 10]
Out[535]=
       {gilwe, kynjh, btdsv, hwkxp, lofap, zbdtx, xcsrf, xecam, jwybz, wqzfe}
In[536]:=
       Tuples[{1, 2}, 3]
Out[536]=
       \{\{1, 1, 1\}, \{1, 1, 2\}, \{1, 2, 1\}, \{1, 2, 2\}, \{2, 1, 1\}, \{2, 1, 2\}, \{2, 2, 1\}, \{2, 2, 2\}\}
In[537]:=
```