

# Eli — Waves Exam 3

April 29, 2025

TOTAL SCORE / 25

Comments and Scores for Each Problem Are on Last Page

This exam tests your fluency with the core of the Wolfram Language, as it was presented in *An Elementary Introduction to the Wolfram Language, 3rd Edition (EIWL3)*, Sections 25-34 and 38-41. There is one problem with two or three parts corresponding to each section. **Tip: all of them are meant to be quick. If you get bogged down, move on.**

## Directions:

After downloading this notebook, rename it with your first name in the filename. E.g., *Eli-Exam3.nb*, *Harper-Exam3.nb*, *Hexi-Exam3.nb*, *Jeremy-Exam3.nb*, *Rania-Exam3.nb*, *Tahm-Exam3.nb*, or *Walker-Exam3.nb*.

Then disconnect from the wifi and work the exam. Save your notebook early and often so that you don't lose work in progress.

**Your answers always go into the Wolfram Language Input cells that begin with a comment, e.g.,**

```
(* 1a *) foobar /@ Plus[Array]
```

**All your answers should execute and re-execute without warnings or error messages.**

You may refer to your downloaded copies of *EIWL3*, and anything else we developed in the course (like your cheat sheets!), but not to any web resources.

When you are done, save your notebook one last time, re-join the wifi, and then email it to me.

This exam was designed to require about 45 minutes, but if you need a full hour, that is ok. Everyone will stop at the one-hour mark.

## 1. Applying Functions (*EIWL3* Section 25)

(a)

Use **Map** with a *levelspec* to put a frame around each individual number in the array **Array[Plus, {10, 10}]** (we don't want frames around already-framed things — just one level of frames around the individual numbers).

In[225]:=

```
(* 1a *) Framed /@ Flatten[Array[Plus, {10, 10}]]
```

Out[225]=

```
{2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 3, 4, 5, 6, 7, 8, 9, 10, 11,
12, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 5, 6, 7, 8, 9, 10, 11,
12, 13, 14, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 7, 8, 9, 10,
11, 12, 13, 14, 15, 16, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17,
9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 10, 11, 12, 13, 14,
15, 16, 17, 18, 19, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20}
```

(b)

Copy what you did in (a), but for this part, also turn the result into a grid using **Grid** and the “as an afterthought” syntax:

In[226]:=

```
(* 1b *) Partition[Framed /@ Flatten[Array[Plus, {10, 10}]], 10] // Grid
```

Out[226]=

2	3	4	5	6	7	8	9	10	11
3	4	5	6	7	8	9	10	11	12
4	5	6	7	8	9	10	11	12	13
5	6	7	8	9	10	11	12	13	14
6	7	8	9	10	11	12	13	14	15
7	8	9	10	11	12	13	14	15	16
8	9	10	11	12	13	14	15	16	17
9	10	11	12	13	14	15	16	17	18
10	11	12	13	14	15	16	17	18	19
11	12	13	14	15	16	17	18	19	20

## 2. Pure Anonymous Functions (EIWL3 Section 26)

(a)

Use the **#** and **&** notation to create an anonymous function that cubes whatever is given it, and then use **/@** to apply it to every member of the list **{1, 2, 3, 4, 5}**.

```
In[227]:= (* 2a *) #^3 & /@ Range[5]
```

```
Out[227]= {1, 8, 27, 64, 125}
```

(b)

Use the **#1**, **#2**, and **&** notation to create an anonymous function that divides its first argument by its second argument. Combine this with **Apply** and a *levelspec* to apply the function to **{{1,2},{2,3},{3,4},{4,5}}**. Once you have this right, you will get  $\{\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}\}$ .

```
In[228]:= (* 2b *) #1 / #2 & @@ Transpose[{{1,2},{2,3},{3,4},{4,5}}]
```

```
Out[228]= {1/2, 2/3, 3/4, 4/5}
```

```
In[229]:= Apply
```

```
Out[229]= Apply
```

### 3. Applying Functions Repeatedly (EIWL3 Section 27)

(a)

Use **Nest** to apply **Factorial** twice to **{1,2,3,4}**. If you have this right, 620,448,401,733,239,439,360,000 will be one of the elements of your answer.

```
In[230]:= (* 3a *) Nest[Factorial, {1, 2, 3, 4}, 2]
```

```
Out[230]= {1, 2, 720, 620 448 401 733 239 439 360 000}
```

(b)

Use **NestList** to apply **Factorial** three times to **{1,2,3}**, as well as showing the results of doing it 0, 1, and 2 times. If you have this right, you will have an insanely large result at the third step. Do not go any higher, or I do not know what will happen to your computer.

```
{False, True, True, False, True, False, True, False, False, False,
 True, False, True, False, False, False, True, False, True, False}
```

(b)

Combine **PrimeQ** with **Select** to only list the numbers in **Range[20]** that are prime.

```
In[233]:=
(* 4b *) Select[Range[20], PrimeQ]

Out[233]=
{2, 3, 5, 7, 11, 13, 17, 19}
```

## 5. More About Pure Functions (EIWL3 Section 29)

(a)

Accomplish exactly the same thing as **Table[n\*(n-1)/2, {n,6}]** using **Array** and a pure function.

```
In[234]:=
(* 5a *) Array[#*(#-1)&, 6]

Out[234]=
{0, 2, 6, 12, 20, 30}
```

(b)

Make some modifications to **FoldList[Plus, {1,2,3,4,5}]** so that it produces a list of the first 10 factorials. Instead of hand-coding the list up to 10, begin by first changing **{1,2,3,4,5}** to **Range[10]**.

```
In[235]:=
(* 5b *) FoldList[Times, Range[10]]

Out[235]=
{1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800}
```

## 6. Rearranging Lists (EIWL3 Section 30)

(a)

Use **Transpose** and one of the *level/spec* options to turn  
**{{{1,uno},{2,dos},{3,tres}},{{4,cuatro},{5,cinco},{6,seis}}}** into  
**{{{1,2,3},{uno,dos,tres}},{{4,5,6},{cuatro,cinco,seis}}}**

```
In[236]:=
(* 6a *)
Flatten/@{{{1,uno},{2,dos},{3,tres}},{{4,cuatro},{5,cinco},{6,seis}}} (*NW*)

Out[236]=
{{1, uno, 2, dos, 3, tres}, {4, cuatro, 5, cinco, 6, seis}}
```

(b)

Use **Flatten** and a *levelspec* option to turn

`{{{1,uno},{2,dos},{3,tres}},{{4,cuatro},{5,cinco},{6,seis}}}` into  
`{{1,uno},{2,dos},{3,tres},{4,cuatro},{5,cinco},{6,seis}}`

In[237]:=

```
(* 6b *)
```

```
Partition[Flatten[{{{1,uno},{2,dos},{3,tres}},{{4,cuatro},{5,cinco},{6,seis}}}], 2]
```

Out[237]=

```
{{1, uno}, {2, dos}, {3, tres}, {4, cuatro}, {5, cinco}, {6, seis}}
```

## 7. Parts of Lists (EIWL3 Section 31)

(a)

Use the magical **All** position (you will need to use **All** more than once) to turn

`{{{Eli, Lerner},{Harper,Yonago},{Hexi,Jin}},{{Jeremy,Choy},{Rania,Zaki},{Tahm,Loyd},{Walker,Harris}}}` into  
`{{Eli,Harper,Hexi},{Jeremy,Rania,Tahm,Walker}}`

In[238]:=

```
(* 7a *) {{{Eli, Lerner},{Harper,Yonago},{Hexi,Jin}},
```

```
{{Jeremy,Choy},{Rania,Zaki},{Tahm,Loyd},{Walker,Harris}}}][All,All,1]
```

Out[238]=

```
{{Eli, Harper, Hexi}, {Jeremy, Rania, Tahm, Walker}}
```

(b)

Use a magical *negative positional argument* to extract `{Jeremy,Rania,Tahm,Walker}` from

`{{Eli,Harper,Hexi},{Jeremy,Rania,Tahm,Walker}}` and combine that with **Take** with a different magical *negative* argument to extract `{Tahm,Walker}`.

In[239]:=

```
(* 7b *) Take[{{Eli,Harper,Hexi},{Jeremy,Rania,Tahm,Walker}}][[-1],-2]
```

Out[239]=

```
{Tahm, Walker}
```

## 8. Patterns (EIWL3 Section 32)

(a)

Use **Cases** to choose the lists that begin and end with the same letter in this list of lists (but look ahead to part (b) before you solve part (a)):

```
{
  {"a", "l", "u", "l", "a"},
  {"a", "l", "o", "h", "a"},
}
```

```
{“a”, “r”, “a”, “r”, “a”},
{“b”, “o”, “n”, “u”, “s”},
{“c”, “i”, “v”, “i”, “c”},
{“d”, “e”, “b”, “e”, “d”},
{“e”, “l”, “b”, “o”, “w”},
{“z”, “a”},
{“z”, “z”}
}
```

In[240]:=

```
(* 8a *) Cases[{{"a", "l", "u", "l", "a"},
{"a", "l", "o", "h", "a"},
{"a", "r", "a", "r", "a"},
{"b", "o", "n", "u", "s"},
{"c", "i", "v", "i", "c"},
{"d", "e", "b", "e", "d"},
{"e", "l", "b", "o", "w"},
{"z", "a"},
{"z", "z"}}, {x_, __, x_}]
```

Out[240]=

```
{{a, l, u, l, a}, {a, l, o, h, a}, {a, r, a, r, a}, {c, i, v, i, c}, {d, e, b, e, d}}
```

(b)

The pattern **BlankNullSequence** has the shorthand `___`. Use `___` to improve the pattern you used in Part (a) so that the two-letter list `{z, z}` is also included in your result.

In[241]:=

```
(* 8b *) Cases[{{"a", "l", "u", "l", "a"},
{"a", "l", "o", "h", "a"},
{"a", "r", "a", "r", "a"},
{"b", "o", "n", "u", "s"},
{"c", "i", "v", "i", "c"},
{"d", "e", "b", "e", "d"},
{"e", "l", "b", "o", "w"},
{"z", "a"},
{"z", "z"}}, {x_, ___, x_}]
```

Out[241]=

```
{{a, l, u, l, a}, {a, l, o, h, a}, {a, r, a, r, a}, {c, i, v, i, c}, {d, e, b, e, d}, {z, z}}
```

## 9. Assigning Names to Things (EIWL3 Section 38)

(a)

Use **Module** to compute `x=Factorial[10]`, and then produce `{x,x^2,x^3}`.

In[242]:=

```
(* 9a *) Module[{x=Factorial[10]}, {x,x^2,x^3}]
```

Out[242]=

```
{3 628 800, 13 168 189 440 000, 47 784 725 839 872 000 000}
```

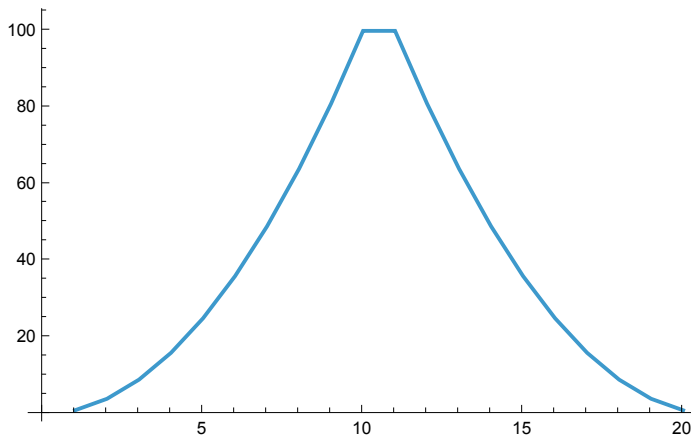
(b)

Inside **Module**, let **rangeSquared=Range[10]^2**, and then produce a list line plot of **rangeSquared** joined with **Reverse[rangeSquared]**.

In[243]:=

```
(* 9b *) Module[{rangeSquared=Range[10]^2},  
  ListLinePlot[Join[rangeSquared, Reverse[rangeSquared]]]]
```

Out[243]=



## 10. Immediate and Delayed Values (EIWL3 Section 39)

(a)

Make a *one-character change* to this expression,

**Module[{x:=RandomInteger[10]}, {x,x^2,x^3,x^4}]**, so that it produces four different powers of the same random number instead of four different powers of different random numbers.

In[244]:=

```
(* 10a *) Module[{x=RandomInteger[10]}, {x,x^2,x^3,x^4}]
```

Out[244]=

```
{0, 0, 0, 0}
```

(b)

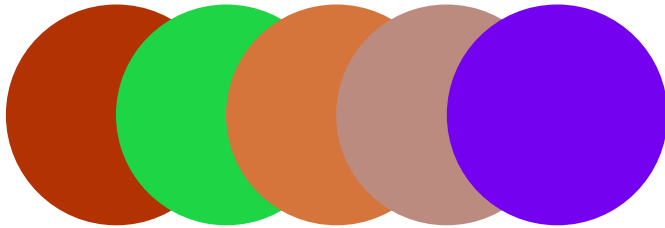
Make a *one-character change* to this expression,

**Module[{color=RandomColor[]}, Graphics[Table[Style[Disk[{i,0}],color],{i,5}]]]**, so that it produces five different-color disks.



```
In[245]:=
(* 10b *) Module[{color:=RandomColor[]},
  Graphics[Table[Style[Disk[{i,0}],color],{i,5}]]]
```

```
Out[245]=
```



## 11. Defining Your Own Functions (EIWL3 Section 40)

(a)

Define a function **f** that takes a list of three elements and out of them makes a list of lists that contains all six possible orderings. Using **Permutations** will make this easy.

Include a test of your function as **f[1,2,3]** and make sure it gets **{{1,2,3},{1,3,2},{2,1,3},{2,3,1},{3,1,2},{3,2,1}}**.

```
In[246]:=
```

```
(* 11a *) f[x_, y_, z_] := Permutations[{x, y, z}]
```

```
In[247]:=
```

```
f[1, 2, 3]
```

```
Out[247]=
```

```
{{1, 2, 3}, {1, 3, 2}, {2, 1, 3}, {2, 3, 1}, {3, 1, 2}, {3, 2, 1}}
```

(b)

Define a function **g** that gives **1** for **g[0]**, and gives **n\*g[n-1]** for any integer **n** greater than **0**, *but don't use an If statement!* Include a test of your function as **g[6]** and make sure it gets **720**.

```
In[248]:=
```

```
(* 11b *) g[x_] := 1 /; x == 0
g[x_] := x * (g[x - 1]) /; x > 0
g[5] (*for some reason, I am reaching my recursion limit at 5*)
```

```
Out[250]=
```

```
120
```

## 12. More About Patterns (EIWL3 Section 41)

(a)

Use the replacement rule notation — e.g., **/.** and **->** — to exchange the first and last element in any list containing two or more elements and test your replacement using the list

```
{alpha, beta, gamma, delta, epsilon}.
```

```
In[251]:=
```

```
(* 12a *) listFunction[l_List]:= l /. First[l]→Last[l]& Last[l]→First[l]
```

```
In[252]:=
```

```
listFunction[{alpha, beta, gamma, delta, epsilon}]
```

```
Out[252]=
```

```
epsilon ({alpha, beta, gamma, delta, epsilon} /.  
  First[{alpha, beta, gamma, delta, epsilon}] →  
  Last[{alpha, beta, gamma, delta, epsilon}] &) → alpha
```

(b)

Starting with `Characters/@RomanNumeral[Range[100]]`, select all the sequences corresponding to the Roman numerals that have XXX in them.

```
In[253]:=
```

```
(* 12b *) Cases[Characters /@ RomanNumeral[Range[100]], {___, "X", "X", "X", ___}]
```

```
Out[253]=
```

```
{{X, X, X}, {X, X, X, I}, {X, X, X, I, I}, {X, X, X, I, I, I}, {X, X, X, I, V},  
 {X, X, X, V}, {X, X, X, V, I}, {X, X, X, V, I, I}, {X, X, X, V, I, I, I},  
 {X, X, X, I, X}, {L, X, X, X}, {L, X, X, X, I}, {L, X, X, X, I, I},  
 {L, X, X, X, I, I, I}, {L, X, X, X, I, V}, {L, X, X, X, V}, {L, X, X, X, V, I},  
 {L, X, X, X, V, I, I}, {L, X, X, X, V, I, I, I}, {L, X, X, X, I, X}}
```

(c)

Use `StringJoin` to turn what you got in 12(b) into

```
{XXX,XXXI,XXXII,XXXIII,XXXIV,XXXV,XXXVI,XXXVII,XXXVIII,XXXIX,LXXX,LXXXI,  
LXXXII,LXXXIII,LXXXIV,LXXXV,LXXXVI,LXXXVII,LXXXVIII,LXXXIX}.
```

```
In[254]:=
```

```
(* 12c *)
```

```
StringJoin /@ Cases[Characters /@ RomanNumeral[Range[100]], {___, "X", "X", "X", ___}]
```

```
Out[254]=
```

```
{XXX, XXXI, XXXII, XXXIII, XXXIV, XXXV, XXXVI, XXXVII, XXXVIII, XXXIX, LXXX,  
LXXXI, LXXXII, LXXXIII, LXXXIV, LXXXV, LXXXVI, LXXXVII, LXXXVIII, LXXXIX}
```

```
In[255]:=
```

```
In[256]:=
```

```
Replace
```

```
Out[256]=
```

```
Replace
```

1. Applying Functions 1.5 / 2

Use of Flatten and Partition is clumsy :( . Directions were to use Map with a levelspec ...

2. Pure Anonymous Functions 1.5 / 2

2(a) great. In 2(b) , directions were to use a levelspec, which is cleaner, although Transpose got it done.

3. Applying Functions Repeatedly 2 / 2

Perfect.

4. Tests and Conditionals 2 / 2

Very nice.

5. More About Pure Functions \_\_\_\_ / 2

6. Rearranging Lists \_\_\_\_ / 2

7. Parts of Lists \_\_\_\_ / 2

8. Patterns \_\_\_\_ / 2

9. Assigning Names to Things \_\_\_\_ / 2

10. Immediate and Delayed Values \_\_\_\_ / 2

11. Defining Your Own Functions \_\_\_\_ / 2

12. More About Patterns \_\_\_\_ / 3