Brian — PS 12 — 2025-03-21 — Solution

EIWL3 Sections 31 and 32

Exercises from EIWL3 Section 31

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In[1]:= (* 31.1 *) Take [Integer Digits [2<sup>1000</sup>], -5]
 Out[1]= \{6, 9, 3, 7, 6\}
 in[2]:= (* 31.2 *) Alphabet[] [[10;; 20]]
 Out[2] = {j, k, l, m, n, o, p, q, r, s, t}
       (* 31.3 *) Alphabet[] [2 Range[13]]
       (* I don't like the fact that I have hard-coded 13 *)
 Out[4] = \{b, d, f, h, j, l, n, p, r, t, v, x, z\}
 In[10]:= (* 31.4 *) ListLinePlot[IntegerDigits[12<sup>#</sup>][-2] & /@ Range[100]]
Out[10]=
In[14]:= (* 31.5 *) TakeSmallest[Join[Array[#<sup>2</sup> &, 20], Array[#<sup>3</sup> &, 20]], 10]
Out[14]=
       {1, 1, 4, 8, 9, 16, 25, 27, 36, 49}
 In[18]:= (* 31.6 *) Position[TextWords[WikipediaData["computers"]], "software"]
Out[18]=
       \{\{62\}, \{6124\}, \{6218\}, \{6240\}, \{6980\}, \{7002\},
         \{7005\}, \{7009\}, \{7023\}, \{8226\}, \{8327\}, \{8334\}, \{8342\}, \{8364\}\}
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In[20]:= (* The above is marked wrong by Mathematica's exercise checker,
      and that is because *)
       (* Position returns each position in
       its own little list. So you need a Flatten[]. *)
      Flatten[Position[TextWords[WikipediaData["computers"]], "software"]]
Out[20]=
       {62, 6124, 6218, 6240, 6980, 7002, 7005, 7009, 7023, 8226, 8327, 8334, 8342, 8364}
In[26]:= (* 31.7 *) Histogram[Position[Characters[#] & /@ WordList[], "e"] [[All, 2]]]
Out[26]=
      6000
      5000
      4000
      3000
      2000
      1000
                                            15
                                                       20
In[32]:= (* 31.8 *) If[IntegerQ[Sqrt[#]], Red, #] & /@ Array[#3 &, 100]
Out[32]=
       {■, 8, 27, ■, 125, 216, 343, 512, ■, 1000, 1331, 1728, 2197, 2744, 3375, ■, 4913, 5832,
       6859, 8000, 9261, 10648, 12167, 13824, \blacksquare, 17576, 19683, 21952, 24389, 27000,
       29791, 32768, 35937, 39304, 42875, , 50653, 54872, 59319, 64000, 68921,
       74 088, 79 507, 85 184, 91 125, 97 336, 103 823, 110 592, ■, 125 000, 132 651, 140 608,
        148 877, 157 464, 166 375, 175 616, 185 193, 195 112, 205 379, 216 000, 226 981,
        238 328, 250 047, , , 274 625, 287 496, 300 763, 314 432, 328 509, 343 000, 357 911,
       373 248, 389 017, 405 224, 421 875, 438 976, 456 533, 474 552, 493 039, 512 000,
       551 368, 571 787, 592 704, 614 125, 636 056, 658 503, 681 472, 704 969, 729 000,
       753571, 778688, 804357, 830584, 857375, 884736, 912673, 941192, 970299, \blacksquare
In[34]:= (* 31.9 *) If[First[IntegerDigits[#]] < 5, Nothing, #] & /@ Array[Prime, 100]</pre>
Out[34]=
       {5, 7, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97, 503, 509, 521, 523, 541}
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In[40]:= (* 31.10 *) NestList[Drop[#, {RandomInteger[{1, Length[#]}]}] &, Range[10], 9] // Grid
Out[40]=
      12345678910
      1 3 4 5 6 7 8 9 10
      134678 9 10
      3 4 6 7 8 9 10
      346789
      3 4 6 7 9
      3 4 6 9
      3 4 9
      3 9
      9
      (* 31.11 *) TakeLargestBy[WordList[], StringLength, 10]
Out[44]=
      {electroencephalographic, electroencephalograph,
       buckminsterfullerene, compartmentalization,
       counterrevolutionary, electroencephalogram, internationalization,
       magnetohydrodynamics, uncharacteristically, counterintelligence}
      (* 31.12 *) TakeLargestBy[Array[IntegerName, 100], StringLength, 10]
Out[45]=
      {seventy-three, seventy-seven, seventy-eight, twenty-three, twenty-seven,
       twenty-eight, thirty-three, thirty-seven, thirty-eight, seventy-four}
In[47]:= Position[Characters["banana"], "a"]
Out[47]=
      \{\{2\}, \{4\}, \{6\}\}
In[49]:= (* 31.13 *) TakeLargestBy[Array[IntegerName, 100],
       Length[Position[Characters[#], "e"]] &, 5]
Out[49]=
      {seventeen, seventy-three, seventy-seven, eleven, eighteen}
```

Exercises from EIWL3 Section 32

```
In[55]:= (* 32.1 *) Cases[IntegerDigits[Range[1000]], {1, __, 9}]
       (* Technically, you should use __ not _, but it doesn't *)
       (* actually matter because the range wasn't large enough. *)
Out[55]=
       \{\{1, 0, 9\}, \{1, 1, 9\}, \{1, 2, 9\}, \{1, 3, 9\},
        \{1, 4, 9\}, \{1, 5, 9\}, \{1, 6, 9\}, \{1, 7, 9\}, \{1, 8, 9\}, \{1, 9, 9\}\}
In[56]:= (* 32.2 *) Cases[IntegerDigits[Range[1000]], {x_, x_, x_}]
Out[56]=
       \{\{1, 1, 1\}, \{2, 2, 2\}, \{3, 3, 3\}, \{4, 4, 4\},
        \{5, 5, 5\}, \{6, 6, 6\}, \{7, 7, 7\}, \{8, 8, 8\}, \{9, 9, 9\}\}
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ln[57] = (* 32.3 *) Cases[IntegerDigits[Range[1000]^2], {9, , 0 | 1}]
Out[57]=
                \{\{9,0,0\},\{9,6,1\},\{9,8,0,1\},\{9,0,0,0,0\},
                  \{9, 0, 6, 0, 1\}, \{9, 5, 4, 8, 1\}, \{9, 6, 1, 0, 0\}, \{9, 6, 7, 2, 1\},
                  \{9, 0, 0, 6, 0, 1\}, \{9, 0, 2, 5, 0, 0\}, \{9, 0, 4, 4, 0, 1\}, \{9, 1, 9, 6, 8, 1\},
                  \{9, 2, 1, 6, 0, 0\}, \{9, 2, 3, 5, 2, 1\}, \{9, 3, 8, 9, 6, 1\}, \{9, 4, 0, 9, 0, 0\},
                  \{9, 4, 2, 8, 4, 1\}, \{9, 5, 8, 4, 4, 1\}, \{9, 6, 0, 4, 0, 0\}, \{9, 6, 2, 3, 6, 1\},
                  \{9, 7, 8, 1, 2, 1\}, \{9, 8, 0, 1, 0, 0\}, \{9, 8, 2, 0, 8, 1\}, \{9, 9, 8, 0, 0, 1\}\}
  ln[60]:= (* 32.4 *) IntegerDigits[Range[100]] /. { 0 \rightarrow Gray, 9 \rightarrow Orange}
Out[60]=
               \{\{1\}, \{2\}, \{3\}, \{4\}, \{5\}, \{6\}, \{7\}, \{8\}, \{\blacksquare\}, \{1, \blacksquare\}, \{1, 1\}, \{1, 2\}, \{1, 3\}, \{1, 1\}, \{1, 2\}, \{1, 3\}, \{1, 1\}, \{1, 2\}, \{1, 3\}, \{1, 1\}, \{1, 2\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}, \{1, 3\}
                  \{1, 4\}, \{1, 5\}, \{1, 6\}, \{1, 7\}, \{1, 8\}, \{1, \blacksquare\}, \{2, \blacksquare\}, \{2, 1\}, \{2, 2\},
                  \{2,3\},\{2,4\},\{2,5\},\{2,6\},\{2,7\},\{2,8\},\{2,\blacksquare\},\{3,\blacksquare\},\{3,1\},\{3,2\},
                  \{3,3\},\{3,4\},\{3,5\},\{3,6\},\{3,7\},\{3,8\},\{3,\blacksquare\},\{4,\blacksquare\},\{4,1\},\{4,2\},
                  \{4, 3\}, \{4, 4\}, \{4, 5\}, \{4, 6\}, \{4, 7\}, \{4, 8\}, \{4, \blacksquare\}, \{5, \blacksquare\}, \{5, 1\}, \{5, 2\},
                  \{5, 3\}, \{5, 4\}, \{5, 5\}, \{5, 6\}, \{5, 7\}, \{5, 8\}, \{5, \blacksquare\}, \{6, \blacksquare\}, \{6, 1\}, \{6, 2\},
                  \{6,3\},\{6,4\},\{6,5\},\{6,6\},\{6,7\},\{6,8\},\{6,\blacksquare\},\{7,\blacksquare\},\{7,1\},\{7,2\},
                  \{7, 3\}, \{7, 4\}, \{7, 5\}, \{7, 6\}, \{7, 7\}, \{7, 8\}, \{7, \blacksquare\}, \{8, \blacksquare\}, \{8, 1\}, \{8, 2\},
                  \{8,3\}, \{8,4\}, \{8,5\}, \{8,6\}, \{8,7\}, \{8,8\}, \{8,\blacksquare\}, \{\blacksquare,\blacksquare\}, \{\blacksquare,1\},
                  \{\blacksquare, 2\}, \{\blacksquare, 3\}, \{\blacksquare, 4\}, \{\blacksquare, 5\}, \{\blacksquare, 6\}, \{\blacksquare, 7\}, \{\blacksquare, 8\}, \{\blacksquare, \blacksquare\}, \{1, \blacksquare, \blacksquare\}\}
                (* 32.5 *) IntegerDigits [2^{1000}] /. 0 \rightarrow \text{Red}
Out[61]=
                \{1, \blacksquare, 7, 1, 5, \blacksquare, 8, 6, \blacksquare, 7, 1, 8, 6, 2, 6, 7, 3, 2, \blacksquare, 9, 4, 8, 4, 2, 5, \blacksquare, 4, 9,
                 \blacksquare, 6, \blacksquare, \blacksquare, \blacksquare, 1, 8, 1, \blacksquare, 5, 6, 1, 4, \blacksquare, 4, 8, 1, 1, 7, \blacksquare, 5, 5, 3, 3, 6, \blacksquare,
                  7, 4, 4, 3, 7, 5, \blacksquare, 3, 8, 8, 3, 7, \blacksquare, 3, 5, 1, \blacksquare, 5, 1, 1, 2, 4, 9, 3, 6, 1, 2,
                  2, 4, 9, 3, 1, 9, 8, 3, 7, 8, 8, 1, 5, 6, 9, 5, 8, 5, 8, 1, 2, 7, 5, 9, 4, 6, 7, 2,
                  9, 1, 7, 5, 5, 3, 1, 4, 6, 8, 2, 5, 1, 8, 7, 1, 4, 5, 2, 8, 5, 6, 9, 2, 3, 1, 4, \blacksquare
                  4, 3, 5, 9, 8, 4, 5, 7, 7, 5, 7, 4, 6, 9, 8, 5, 7, 4, 8, 1, 3, 9, 3, 4, 5, 6, 7, 7,
                  7, 4, 8, 2, 4, 2, 3, \blacksquare, 9, 8, 5, 4, 2, 1, \blacksquare, 7, 4, 6, \blacksquare, 5, \blacksquare, 6, 2, 3, 7, 1, 1,
                  4, 1, 8, 7, 7, 9, 5, 4, 1, 8, 2, 1, 5, 3, 1, 4, 6, 4, 7, 4, 9, 8, 3, 5, 8, 1, 9, 4,
                  1, 2, 6, 7, 3, 9, 8, 7, 6, 7, 5, 5, 9, 1, 6, 5, 5, 4, 3, 9, 4, 6, \blacksquare, 7, 7, \blacksquare, 6,
                  2, 9, 1, 4, 5, 7, 1, 1, 9, 6, 4, 7, 7, 6, 8, 6, 5, 4, 2, 1, 6, 7, 6, 6, 1, 4, 2, 9,
                  8, 3, 1, 6, 5, 2, 6, 2, 4, 3, 8, 6, 8, 3, 7, 2, \blacksquare, 5, 6, 6, 8, \blacksquare, 6, 9, 3, 7, 6
  In[65]:= (* 32.6 *) Characters["The Wolfram Language"] /. "a" | "e" | "i" | "o" | "u" → Nothing
Out[65]=
               \{T, h, , W, l, f, r, m, , L, n, g, g\}
 In[67]:= (* 32.7 *) Cases[IntegerDigits[2<sup>1000</sup>], 0 | 1]
Out[67]=
               1, 1, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 1, 1, 0, 1, 0, 0
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In[69]:= (* 32.8 *) Cases[IntegerDigits[Range[100, 999]], {x_, _, x_}] Out[69]= $\{\{1, 0, 1\}, \{1, 1, 1\}, \{1, 2, 1\}, \{1, 3, 1\}, \{1, 4, 1\}, \{1, 5, 1\}, \{1, 6, 1\}, \{1, 7, 1\},$ $\{1, 8, 1\}, \{1, 9, 1\}, \{2, 0, 2\}, \{2, 1, 2\}, \{2, 2, 2\}, \{2, 3, 2\}, \{2, 4, 2\}, \{2, 5, 2\},$ $\{2, 6, 2\}, \{2, 7, 2\}, \{2, 8, 2\}, \{2, 9, 2\}, \{3, 0, 3\}, \{3, 1, 3\}, \{3, 2, 3\}, \{3, 3, 3\},$ $\{3, 4, 3\}, \{3, 5, 3\}, \{3, 6, 3\}, \{3, 7, 3\}, \{3, 8, 3\}, \{3, 9, 3\}, \{4, 0, 4\}, \{4, 1, 4\},$ $\{4, 2, 4\}, \{4, 3, 4\}, \{4, 4, 4\}, \{4, 5, 4\}, \{4, 6, 4\}, \{4, 7, 4\}, \{4, 8, 4\}, \{4, 9, 4\},$ $\{5, 0, 5\}, \{5, 1, 5\}, \{5, 2, 5\}, \{5, 3, 5\}, \{5, 4, 5\}, \{5, 5, 5\}, \{5, 6, 5\}, \{5, 7, 5\},$ $\{5, 8, 5\}, \{5, 9, 5\}, \{6, 0, 6\}, \{6, 1, 6\}, \{6, 2, 6\}, \{6, 3, 6\}, \{6, 4, 6\},$ $\{6, 5, 6\}, \{6, 6, 6\}, \{6, 7, 6\}, \{6, 8, 6\}, \{6, 9, 6\}, \{7, 0, 7\}, \{7, 1, 7\},$ $\{7, 2, 7\}, \{7, 3, 7\}, \{7, 4, 7\}, \{7, 5, 7\}, \{7, 6, 7\}, \{7, 7, 7\}, \{7, 8, 7\},$ $\{7, 9, 7\}, \{8, 0, 8\}, \{8, 1, 8\}, \{8, 2, 8\}, \{8, 3, 8\}, \{8, 4, 8\}, \{8, 5, 8\},$ $\{8, 6, 8\}, \{8, 7, 8\}, \{8, 8, 8\}, \{8, 9, 8\}, \{9, 0, 9\}, \{9, 1, 9\}, \{9, 2, 9\},$

 $\{9, 3, 9\}, \{9, 4, 9\}, \{9, 5, 9\}, \{9, 6, 9\}, \{9, 7, 9\}, \{9, 8, 9\}, \{9, 9, 9\}\}$