# Eli — Waves Exam 3

## April 29, 2025

This exam tests your fluency with the core of the Wolfram Language, as it was presented in *An Elementary Introduction to the Wolfram Language, 3rd Edition (EIWL3)*, Sections 25-34 and 38-41. There is one problem with two or three parts corresponding to each section. *Tip: all of them are meant to be quick. If you get bogged down, move on.* 

#### **Directions:**

After downloading this notebook, rename it with your first name in the filename. E.g., Eli-Exam3.nb, Harper-Exam3.nb, Hexi-Exam3.nb, Jeremy-Exam3.nb, Rania-Exam3.nb, Tahm-Exam3.nb, or Walker-Exam3.nb.

Then disconnect from the wifi and work the exam. Save your notebook early and often so that you don't lose work in progress.

Your answers always go into the Wolfram Language Input cells that begin with a comment, e.g.,

```
(* 1a *) foobar /@ Plus[Array]
```

All your answers should execute and re-execute without warnings or error messages.

You may refer to your downloaded copies of EIWL3, and anything else we developed in the course (like your cheat sheets!), but not to any web resources.

When you are done, save your notebook one last time, re-join the wifi, and then email it to me.

This exam was designed to require about 45 minutes, but if you need a full hour, that is ok. Everyone will stop at the one-hour mark.

### 1. Applying Functions (EIWL3 Section 25)

(a)

Use Map with a *levelspec* to put a frame around each individual number in the array Array [Plus, {10,10}] (we don't want frames around already-framed things — just one level of frames around the individual numbers).

In[225]:=

(\* 1a \*) Framed /@ Flatten[Array[Plus,{10,10}]]

Out[225]=

10, 16, 

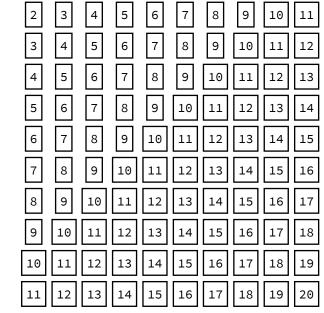
(b)

Copy what you did in (a), but for this part, also turn the result into a grid using **Grid** and the "as an afterthought" syntax:

In[226]:=

(\* 1b \*) Partition[Framed /@ Flatten[Array[Plus, {10,10}]], 10] // Grid

Out[226]=



### 2. Pure Anonymous Functions (EIWL3 Section 26)

(a)

Use the # and & notation to create an anonymous function that cubes whatever is given it, and then use @ to apply it to every member of the list  $\{1,2,3,4,5\}$ .

```
In[227]:=
        (* 2a *) #^3 & /@ Range [5]
Out[227]=
        {1, 8, 27, 64, 125}
```

#### (b)

Use the #1, #2, and & notation to create an anonymous function that divides its first argument by its second argument. Combine this with Apply and a levelspec to apply the function to  $\{\{1,2\},\{2,3\},\{3,4\},\{4,5\}\}$ . Once you have this right, you will get  $\{\frac{1}{2},\frac{2}{3},\frac{3}{4},\frac{4}{5}\}$ .

In[228]:= (\* 2b \*)#1/#2 &@@Transpose[{{1,2},{2,3},{3,4},{4,5}}] Out[228]=  $\left\{\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}\right\}$ 

In[229]:=

Apply

Out[229]=

Apply

#### 3. Applying Functions Repeatedly (EIWL3 Section 27)

#### (a)

Use **Nest** to apply **Factorial** twice to {1,2,3,4}. If you have this right, 620,448,401,733,239,439,360,000 will be one of the elements of your answer.

In[230]:= (\* 3a \*) Nest[Factorial, {1, 2, 3, 4}, 2] Out[230]= {1, 2, 720, 620 448 401 733 239 439 360 000}

#### (b)

Use **NestList** to apply **Factorial** three times to {1,2,3}, as well as showing the results of doing it 0, 1, and 2 times. If you have this right, you will have an insanely large result at the third step. Do not go any higher, or I do not know what will happen to your computer.

```
In[231]:=
                     (* 3b *) NestList[Factorial, {1, 2, 3}, 3]
Out[231]=
                     \{\{1, 2, 3\}, \{1, 2, 6\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2, 720\}, \{1, 2,
                            2\,601\,218\,943\,565\,795\,100\,204\,903\,227\,081\,043\,611\,191\,521\,875\,016\,945\,785\,727\,541\,837\,850\,835\,\%
                                631\ 156\ 947\ 382\ 240\ 678\ 577\ 958\ 130\ 457\ 082\ 619\ 920\ 575\ 892\ 247\ 259\ 536\ 641\ 565\ 162\ 052\ 015\ \times 100
                                873\,791\,984\,587\,740\,832\,529\,105\,244\,690\,388\,811\,884\,123\,764\,341\,191\,951\,045\,505\,346\,658\,616
                                783 758 997 420 676 784 016 967 207 846 280 629 229 032 107 161 669 867 260 548 988 445 514
                                257 193 985 499 448 939 594 496 064 045 132 362 140 265 986 193 073 249 369 770 477 606 067
                                680\,670\,176\,491\,669\,403\,034\,819\,961\,881\,455\,625\,195\,592\,566\,918\,830\,825\,514\,942\,947\,596\,537\,\%
                                274\,845\,624\,628\,824\,234\,526\,597\,789\,737\,740\,896\,466\,553\,992\,435\,928\,786\,212\,515\,967\,483\,220\,\%
                                976 029 505 696 699 927 284 670 563 747 137 533 019 248 313 587 076 125 412 683 415 860 129
                                447\,566\,011\,455\,420\,749\,589\,952\,563\,543\,068\,288\,634\,631\,084\,965\,650\,682\,771\,552\,996\,256\,790\,
                                845\,235\,702\,552\,186\,222\,358\,130\,016\,700\,834\,523\,443\,236\,821\,935\,793\,184\,701\,956\,510\,729\,781\,\%
                                804 354 173 890 560 727 428 048 583 995 919 729 021 726 612 291 298 420 516 067 579 036 232
                                337\,699\,453\,964\,191\,475\,175\,567\,557\,695\,392\,233\,803\,056\,825\,308\,599\,977\,441\,675\,784\,352\,815 :
                                913 461 340 394 604 901 269 542 028 838 347 101 363 733 824 484 506 660 093 348 484 440 711
                                931\ 292\ 537\ 694\ 657\ 354\ 337\ 375\ 724\ 772\ 230\ 181\ 534\ 032\ 647\ 177\ 531\ 984\ 537\ 341\ 478\ 674\ 327\ 537\ 547
                                048\,457\,983\,786\,618\,703\,257\,405\,938\,924\,215\,709\,695\,994\,630\,557\,521\,063\,203\,263\,493\,209\,220\,
                                738\,320\,923\,356\,309\,923\,267\,504\,401\,701\,760\,572\,026\,010\,829\,288\,042\,335\,606\,643\,089\,888\,710\,\times 10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1}\,10^{-1
                                297 380 797 578 013 056 049 576 342 838 683 057 190 662 205 291 174 822 510 536 697 756 603
                                029\,574\,043\,387\,983\,471\,518\,552\,602\,805\,333\,866\,357\,139\,101\,046\,336\,419\,769\,097\,397\,432\,285\,\%
                                994 219 837 046 979 109 956 303 389 604 675 889 865 795 711 176 566 670 039 156 748 153 115
                                943\,980\,043\,625\,399\,399\,731\,203\,066\,490\,601\,325\,311\,304\,719\,028\,898\,491\,856\,203\,766\,669\,164\,\%
                                468\,791\,125\,249\,193\,754\,425\,845\,895\,000\,311\,561\,682\,974\,304\,641\,142\,538\,074\,897\,281\,723\,375\,\%
```

#### 4. Tests and Conditionals (EIWL3 Section 28)

000 000 000 000 000 000 000 } }

(a)

Use **PrimeQ** and /@ to generate a **True** or **False** list that is twenty elements long expressing which numbers in **Range** [20] are prime.

(b)

Combine PrimeQ with Select to only list the numbers in Range [20] that are prime.

```
In[233]:=
       (* 4b *) Select[Range[20], PrimeQ]
Out[233]=
       {2, 3, 5, 7, 11, 13, 17, 19}
```

#### 5. More About Pure Functions (*EIWL3* Section 29)

(a)

Accomplish exactly the same thing as **Table**  $[n*(n-1)/2, \{n,6\}]$  using **Array** and a pure function.

```
In[234]:=
        (* 5a *) Array[#*(#-1) &, 6]
Out[234]=
        \{0, 2, 6, 12, 20, 30\}
```

(b)

Make some modifications to FoldList[Plus, {1,2,3,4,5}] so that it produces a list of the first 10 factorials. Instead of hand-coding the list up to 10, begin by first changing {1,2,3,4,5} to Range [10].

```
In[235]:=
       (* 5b *) FoldList[Times,Range[10]]
Out[235]=
       {1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800}
```

### 6. Rearranging Lists (EIWL3 Section 30)

(a)

```
Use Transpose and one of the levelspec options to turn
      {{{1,uno},{2,dos},{3,tres}}},{{4,cuatro},{5,cinco},{6,seis}}} into
      {{{1,2,3},{uno,dos,tres}},{{4,5,6},{cuatro,cinco,seis}}}
In[236]:=
      (* 6a *)
      Flatten /@ {{{1,uno},{2,dos},{3,tres}},{4,cuatro},{5,cinco},{6,seis}}} (*NW*)
Out[236]=
      {{1, uno, 2, dos, 3, tres}, {4, cuatro, 5, cinco, 6, seis}}
```

(b)

```
Use Flatten and a levelspec option to turn
      {{{1,uno},{2,dos},{3,tres}}},{{4,cuatro},{5,cinco},{6,seis}}} into
      {{1,uno},{2,dos},{3,tres},{4,cuatro},{5,cinco},{6,seis}}
In[237]:=
      (*6b*)
      Partition[Flatten[{{{1,uno},{2,dos},{3,tres}},{{4,cuatro},{5,cinco},{6,seis}}}], 2]
Out[237]=
      {{1, uno}, {2, dos}, {3, tres}, {4, cuatro}, {5, cinco}, {6, seis}}
```

#### 7. Parts of Lists (EIWL3 Section 31)

(a)

```
Use the magical All position (you will need to use All more than once) to turn
      {{{Eli, Lerner},{Harper,Yonago},{Hexi,Jin}},{{Jeremy,Choy},{Rania,Zaki}
      ,{Tahm,Loyd},{Walker,Harris}}}into
      {{Eli, Harper, Hexi}, {Jeremy, Rania, Tahm, Walker}}
In[238]:=
      (* 7a *) {{{Eli, Lerner},{Harper,Yonago},{Hexi,Jin}},
        {{Jeremy,Choy},{Rania,Zaki},{Tahm,Loyd},{Walker,Harris}}}[All,All,1]
Out[238]=
      {{Eli, Harper, Hexi}, {Jeremy, Rania, Tahm, Walker}}
```

(b)

Use a magical negative positional argument to extract { Jeremy, Rania, Tahm, Walker} from {{Eli, Harper, Hexi}, {Jeremy, Rania, Tahm, Walker}} and combine that with Take with a different magical *negative* argument to extract { Tahm, Walker }.

```
In[239]:=
       (* 7b *) Take[{{Eli,Harper,Hexi},{Jeremy,Rania,Tahm,Walker}}[-1],-2]
Out[239]=
       {Tahm, Walker}
```

### 8. Patterns (EIWL3 Section 32)

(a)

Use Cases to choose the lists that begin and end with the same letter in this list of lists (but look ahead to part (b) before you solve part (a)):

```
{"a", "l", "u", "l", "a"},
{"a", "l", "o", "h", "a"},
```

```
{"a", "r", "a", "r", "a"},
       {"b", "o", "n", "u", "s"},
       {"c", "i", "v", "i", "c"},
       {"d", "e", "b", "e", "d"},
       {"e", "l", "b", "o", "w"},
       {"z", "a"},
       {"z", "z"}
      }
In[240]:=
      (* 8a *) Cases[{{"a", "l", "u", "l", "a"},
       {"a", "l", "o", "h", "a"},
       {"a", "r", "a", "r", "a"},
       {"b", "o", "n", "u", "s"},
       {"c", "i", "v", "i", "c"},
       {"d", "e", "b", "e", "d"},
       {"e", "l", "b", "o", "w"},
       {"z", "a"},
       {"z", "z"}}, {x_, __, x_}]
Out[240]=
      {{a, l, u, l, a}, {a, l, o, h, a}, {a, r, a, r, a}, {c, i, v, i, c}, {d, e, b, e, d}}
```

(b)

The pattern **BlankNullSequence** has the shorthand . Use to improve the pattern you used in Part (a) so that the two-letter list {z,z} is also included in your result.

```
In[241]:=
      (* 8b *) Cases[{{"a", "l", "u", "l", "a"}.
       {"a", "l", "o", "h", "a"},
       {"a", "r", "a", "r", "a"},
       {"b", "o", "n", "u", "s"},
       {"c", "i", "v", "i", "c"},
       {"d", "e", "b", "e", "d"},
       {"e", "l", "b", "o", "w"},
       {"z", "a"},
       {"z", "z"}}, {x_, ___, x_}]
Out[241]=
       {{a, l, u, l, a}, {a, l, o, h, a}, {a, r, a, r, a}, {c, i, v, i, c}, {d, e, b, e, d}, {z, z}}
```

### 9. Assigning Names to Things (EIWL3 Section 38)

(a)

Use Module to compute x=Factorial[10], and then produce  $\{x,x^2,x^3\}$ .

{3628800, 13168189440000, 47784725839872000000}

(b)

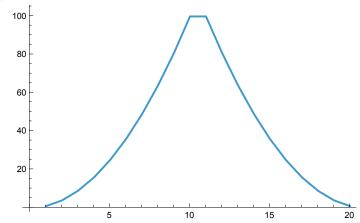
Inside Module, let rangeSquared=Range[10]^2, and then produce a list line plot of rangeSquared joined with Reverse[rangeSquared].

In[243]:=

Out[242]=

(\* 9b \*) Module[{rangeSquared=Range[10]^2},
ListLinePlot[Join[rangeSquared, Reverse[rangeSquared]]]]





### 10. Immediate and Delayed Values (EIWL3 Section 39)

(a)

Make a one-character change to this expression,

Module [ $\{x := RandomInteger[10]\}, \{x, x^2, x^3, x^4\}$ ], so that it produces four different powers of the same random number instead of four different powers of different random numbers.

In[244]:=
 (\* 10a \*) Module[{x=RandomInteger[10]},{x,x²,x³,x⁴}]
Out[244]=
 {0, 0, 0, 0}

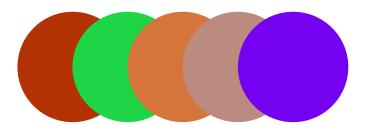
(b)

Make a one-character change to this expression,

Module[{color=RandomColor[]},Graphics[Table[Style[Disk[{i,0}],color],{i
,5}]]], so that it produces five different-color disks.

```
In[245]:=
      (* 10b *) Module[{color:=RandomColor[]},
       Graphics[Table[Style[Disk[{i,0}],color],{i,5}]]]
```

Out[245]=



#### 11. Defining Your Own Functions (EIWL3 Section 40)

(a)

Define a function f that takes a list of three elements and out of them makes a list of lists that contains all six possible orderings. Using **Permutations** will make this easy.

```
Include a test of your function as f[1,2,3] and make sure it gets
       \{\{1,2,3\},\{1,3,2\},\{2,1,3\},\{2,3,1\},\{3,1,2\},\{3,2,1\}\}.
In[246]:=
       (* 11a *) f[x_, y_, z_] := Permutations[{x, y, z}]
In[247]:=
       f[1, 2, 3]
```

 $\{\{1, 2, 3\}, \{1, 3, 2\}, \{2, 1, 3\}, \{2, 3, 1\}, \{3, 1, 2\}, \{3, 2, 1\}\}$ 

(b)

Out[247]=

Define a function g that gives 1 for g[0], and gives n\*g[n-1] for any integer n greater than 0, but don't use an If statement! Include a test of your function as g[6] and make sure it gets 720.

```
In[248]:=
       (* 11b *)g[x_] := 1/; x == 0
       g[x_{-}] := x * (g[x-1]) /; x > 0
       g[5] (*for some reason, I am reaching my recursion limit at 5*)
Out[250]=
       120
```

### 12. More About Patterns (EIWL3 Section 41)

(a)

Use the replacement rule notation — e.g.,  $/ \cdot$  and -> — to exchange the first and last element in any list containing two or more elements and test your replacement using the list

```
{alpha, beta, gamma, delta, epsilon}.
In[251]:=
      (* 12a *) listFunction[l List]:= l /. First[l]→Last[l]& Last[l]→First[l]
In[252]:=
      listFunction[{alpha, beta, gamma, delta, epsilon}]
Out[252]=
      epsilon ({alpha, beta, gamma, delta, epsilon} /.
            First[{alpha, beta, gamma, delta, epsilon}] →
             Last[{alpha, beta, gamma, delta, epsilon}] &) → alpha
      (b)
      Starting with Characters/@RomanNumeral [Range [100], select all the sequences correspond-
      ing to the Roman numerals that have XXX in them.
In[253]:=
      (* 12b *) Cases[Characters /@ RomanNumeral[Range[100]], {___, "X", "X", "X", ___}]
Out[253]=
      {{X, X, X}, {X, X, X, I}, {X, X, X, I, I}, {X, X, X, I, I, I}, {X, X, X, I, V},
       {X, X, X, V}, {X, X, X, V, I}, {X, X, X, V, I, I}, {X, X, X, V, I, I, I},
       \{X, X, X, I, X\}, \{L, X, X, X\}, \{L, X, X, X, I\}, \{L, X, X, X, I, I\},\
       {L, X, X, X, I, I, I}, {L, X, X, X, I, V}, {L, X, X, X, V}, {L, X, X, X, V, I},
       {L, X, X, X, V, I, I}, {L, X, X, X, V, I, I, I}, {L, X, X, I, X}}
      (c)
      Use StringJoin to turn what you got in 12(b) into
      ,LXXXII,LXXXIII,LXXXIV,LXXXV,LXXXVI,LXXXVII,LXXXVIII,LXXXIX}.
In[254]:=
      (* 12c *)
      StringJoin /@ Cases[Characters /@ RomanNumeral[Range[100]], {___, "X", "X", "X", ___}]
Out[254]=
      {XXX, XXXI, XXXII, XXXIII, XXXIV, XXXV, XXXVI, XXXVII, XXXVIII, XXXIX, LXXX,
       LXXXI, LXXXII, LXXXIII, LXXXIV, LXXXV, LXXXVI, LXXXVII, LXXXVIII, LXXXIX}
In[255]:=
In[256]:=
      Replace
Out[256]=
      Replace
```