Jeremy — PS 11 — 2025-03-18

EIWL3 Sections 29 and 30

In[371]:=

```
Array[Prime, 100]
```

Out[371]=

{2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79,
 83, 89, 97, 101, 103, 107, 109, 113, 127, 131, 137, 139, 149, 151, 157, 163,
 167, 173, 179, 181, 191, 193, 197, 199, 211, 223, 227, 229, 233, 239, 241, 251,
 257, 263, 269, 271, 277, 281, 283, 293, 307, 311, 313, 317, 331, 337, 347, 349,
 353, 359, 367, 373, 379, 383, 389, 397, 401, 409, 419, 421, 431, 433, 439,
 443, 449, 457, 461, 463, 467, 479, 487, 491, 499, 503, 509, 521, 523, 541}

In[372]:=

```
Array[Prime[# + 1] - Prime[#] &, 100]
```

Out[372]=

{1, 2, 2, 4, 2, 4, 2, 4, 6, 2, 6, 4, 2, 4, 6, 6, 2, 6, 4, 2, 6, 4, 6, 8, 4, 2,
 4, 2, 4, 14, 4, 6, 2, 10, 2, 6, 6, 4, 6, 6, 2, 10, 2, 4, 2, 12, 12, 4, 2, 4,
 6, 2, 10, 6, 6, 6, 2, 6, 4, 2, 10, 14, 4, 2, 4, 14, 6, 10, 2, 4, 6, 8, 6, 6, 4,
 6, 8, 4, 8, 10, 2, 10, 2, 6, 4, 6, 8, 4, 2, 4, 12, 8, 4, 8, 4, 6, 12, 2, 18, 6}

In[373]:=

```
Array[#1 + #2 &, {10, 10}] // Grid
```

Out[373]=

```
 2  3  4  5  6  7  8  9 10 11
 3  4  5  6  7  8  9 10 11 12
 4  5  6  7  8  9 10 11 12 13
 5  6  7  8  9 10 11 12 13 14
 6  7  8  9 10 11 12 13 14 15
 7  8  9 10 11 12 13 14 15 16
 8  9 10 11 12 13 14 15 16 17
 9 10 11 12 13 14 15 16 17 18
10 11 12 13 14 15 16 17 18 19
11 12 13 14 15 16 17 18 19 20
```

In[374]:=

```
FoldList[#1 * #2 &, 1, Range[10]]
```

Out[374]=

{1, 1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800}

In[375]:=

```
FoldList[#1 * #2 &, 1, Array[Prime, 10]]
```
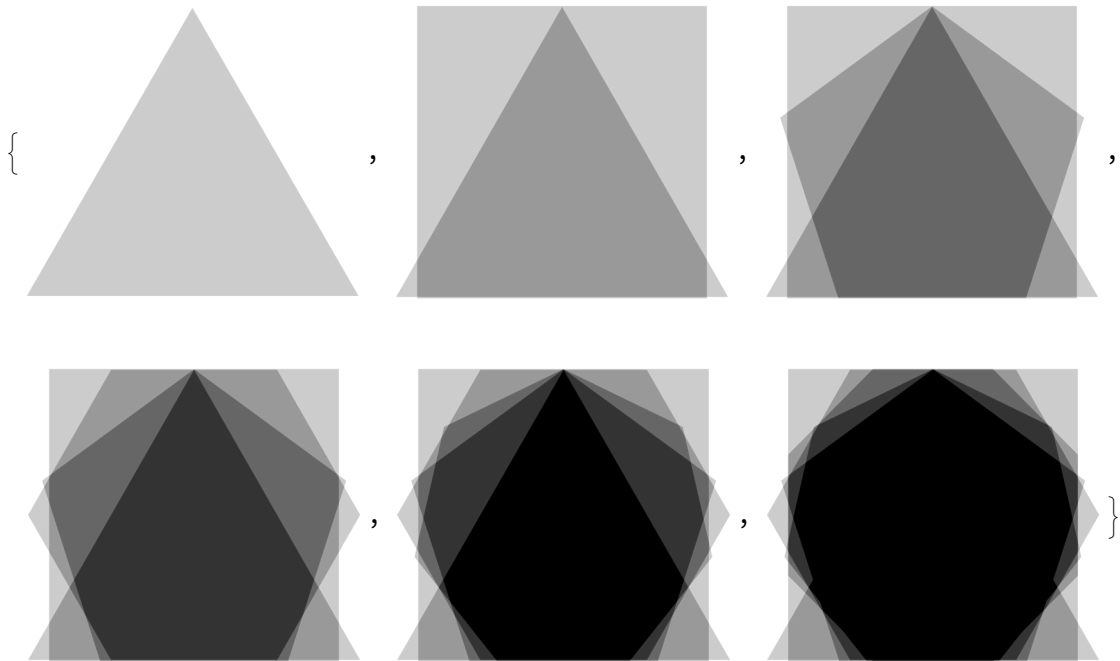
Out[375]=

{1, 2, 6, 30, 210, 2310, 30030, 510510, 9699690, 223092870, 6469693230}

In[376]:=

```
FoldList[ImageAdd,
  Table[Graphics[Style[RegularPolygon[n], Opacity[0.2]]], {n, 3, 8}]]
```

Out[376]=

In[377]:=

```
Thread[Alphabet[] → Range[26]]
```

Out[377]=

{a → 1, b → 2, c → 3, d → 4, e → 5, f → 6, g → 7, h → 8,
 i → 9, j → 10, k → 11, l → 12, m → 13, n → 14, o → 15, p → 16, q → 17,
 r → 18, s → 19, t → 20, u → 21, v → 22, w → 23, x → 24, y → 25, z → 26}

In[378]:=

```
Grid[Partition[Take[Alphabet[], 24], 6]]
```

Out[378]=

a b c d e f
g h i j k l
m n o p q r
s t u v w x

In[379]:=

```
Grid[Partition[IntegerDigits[2^1000], 50], Frame → All]
```

Out[379]=

1	0	7	1	5	0	8	6	0	7	1	8	6	2	6	7	3	2	0	9	4	8	4	2	5	0	4	9	0	6	0	0	0	1	8	1	0	5	6	1	4	0	4	8	1	1	7
3	3	6	0	7	4	4	3	7	5	0	3	8	8	3	7	0	3	5	1	0	5	1	1	2	4	9	3	6	1	2	2	4	9	3	1	9	8	3	7	8	8	1	5	6	9	5
1	2	7	5	9	4	6	7	2	9	1	7	5	5	3	1	4	6	8	2	5	1	8	7	1	4	5	2	8	5	6	9	2	3	1	4	0	4	3	5	9	8	4	5	7	7	5
9	8	5	7	4	8	0	3	9	3	4	5	6	7	7	7	4	8	2	4	2	3	0	9	8	5	4	2	1	0	7	4	6	0	5	0	6	2	3	7	1	1	4	1	8	7	7
1	8	2	1	5	3	0	4	6	4	7	4	9	8	3	5	8	1	9	4	1	2	6	7	3	9	8	7	6	7	5	5	9	1	6	5	5	4	3	9	4	6	0	7	7	0	6
4	5	7	1	1	9	6	4	7	7	6	8	6	5	4	2	1	6	7	6	6	0	4	2	9	8	3	1	6	5	2	6	2	4	3	8	6	8	3	7	2	0	5	6	6	8	0

In[380]:=

```
Grid[Partition[Take[Characters[WikipediaData["computers"]], 400], 20], Frame → All]
```
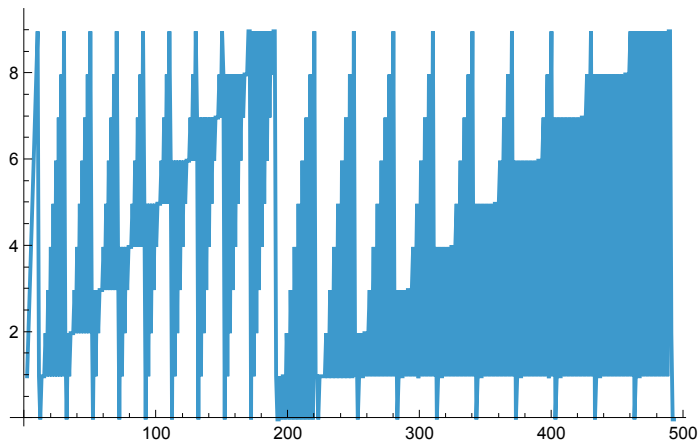
Out[380]=

A		c	o	m	p	u	t	e	r		i	s		a		m	a	c	h
i	n	e		t	h	a	t		c	a	n		b	e		p	r	o	g
r	a	m	m	e	d		t	o		a	u	t	o	m	a	t	i	c	a
l	l	y		c	a	r	r	y		o	u	t		s	e	q	u	e	n
c	e	s		o	f		a	r	i	t	h	m	e	t	i	c		o	r
	l	o	g	i	c	a	l		o	p	e	r	a	t	i	o	n	s	
(	c	o	m	p	u	t	a	t	i	o	n	)	.		M	o	d	e	r
n		d	i	g	i	t	a	l		e	l	e	c	t	r	o	n	i	c
	c	o	m	p	u	t	e	r	s		c	a	n		p	e	r	f	o
r	m		g	e	n	e	r	i	c		s	e	t	s		o	f		o
p	e	r	a	t	i	o	n	s		k	n	o	w	n		a	s		p
r	o	g	r	a	m	s	.		T	h	e	s	e		p	r	o	g	r
a	m	s		e	n	a	b	l	e		c	o	m	p	u	t	e	r	s
	t	o		p	e	r	f	o	r	m		a		w	i	d	e		r
a	n	g	e		o	f		t	a	s	k	s	.		T	h	e		t
e	r	m		c	o	m	p	u	t	e	r		s	y	s	t	e	m	
m	a	y		r	e	f	e	r		t	o		a		n	o	m	i	n
a	l	l	y		c	o	m	p	l	e	t	e		c	o	m	p	u	t
e	r		t	h	a	t		i	n	c	l	u	d	e	s		t	h	e
	h	a	r	d	w	a	r	e	,		o	p	e	r	a	t	i	n	g

In[381]:=

```
ListLinePlot[Flatten[IntegerDigits /@ Range[200]]]
```
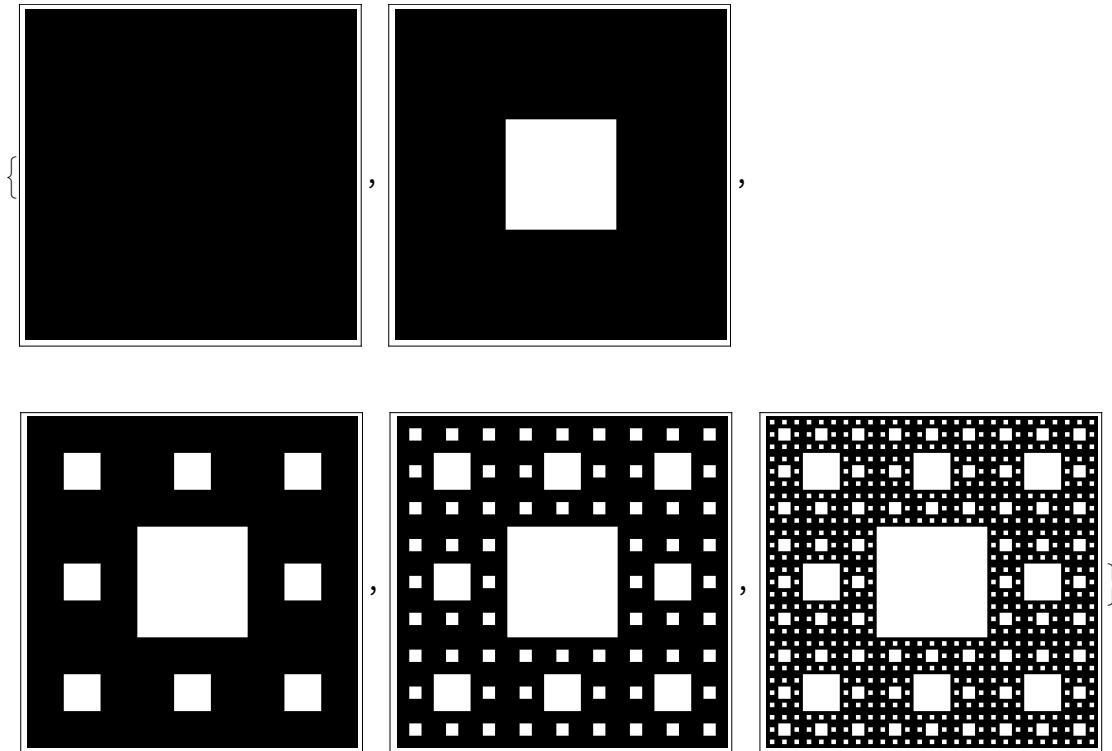
Out[381]=

In[382]:=
```
ArrayPlot /@ NestList[ArrayFlatten[{{#, #, #}, {#, 0, #}, {#, #, #}}] &, {{1}}, 4]
```

Out[382]=

In[383]:=
```
Select[Flatten[Table[{x, y, Sqrt[x^2 + y^2]}, {x, 20}, {y, 20}], 1],
 IntegerQ[Last[#]] &]
```

Out[383]=
```
{{3, 4, 5}, {4, 3, 5}, {5, 12, 13}, {6, 8, 10},
 {8, 6, 10}, {8, 15, 17}, {9, 12, 15}, {12, 5, 13}, {12, 9, 15},
 {12, 16, 20}, {15, 8, 17}, {15, 20, 25}, {16, 12, 20}, {20, 15, 25}}
```

In[384]:=
```
Table[Length[Last[SortBy[Split[IntegerDigits[2^n]], Length]]], {n, 100}]
```

Out[384]=
```
{1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 2, 1, 2, 2, 1, 1, 1, 2, 3,
 2, 2, 2, 1, 1, 1, 1, 1, 2, 1, 1, 1, 1, 2, 3, 3, 4, 3, 3, 3, 3, 2, 2, 1, 2,
 3, 2, 2, 2, 1, 1, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 1, 1, 1, 1, 2, 2, 2, 3, 3,
 3, 3, 3, 2, 2, 1, 2, 2, 3, 2, 2, 2, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2}
```

In[385]:=
```
GatherBy[Table[IntegerName[n], {n, 100}], First[Characters[#]] &]
```

Out[385]=
```
{{one, one hundred}, {two, three, ten, twelve, thirteen, twenty, twenty-one,
  twenty-two, twenty-three, twenty-four, twenty-five, twenty-six, twenty-seven,
  twenty-eight, twenty-nine, thirty, thirty-one, thirty-two, thirty-three,
  thirty-four, thirty-five, thirty-six, thirty-seven, thirty-eight, thirty-nine},
 {four, five, fourteen, fifteen, forty, forty-one, forty-two, forty-three,
  forty-four, forty-five, forty-six, forty-seven, forty-eight,
  forty-nine, fifty, fifty-one, fifty-two, fifty-three, fifty-four,
  fifty-five, fifty-six, fifty-seven, fifty-eight, fifty-nine},
 {six, seven, sixteen, seventeen, sixty, sixty-one, sixty-two, sixty-three,
  sixty-four, sixty-five, sixty-six, sixty-seven, sixty-eight, sixty-nine,
  seventy, seventy-one, seventy-two, seventy-three, seventy-four,
  seventy-five, seventy-six, seventy-seven, seventy-eight, seventy-nine},
 {eight, eleven, eighteen, eighty, eighty-one, eighty-two, eighty-three,
  eighty-four, eighty-five, eighty-six, eighty-seven, eighty-eight, eighty-nine},
 {nine, nineteen, ninety, ninety-one, ninety-two, ninety-three, ninety-four,
  ninety-five, ninety-six, ninety-seven, ninety-eight, ninety-nine}}
```

In[386]:=
```
SortBy[Take[WordList[], 50], Last[Characters[#]] &]
```

Out[386]=
```
{a, abandoned, abashed, abbreviated, abed, abalone, abase, abate, abbe, abbreviate,
 abdicate, abeyance, abhorrence, abidance, abide, abducting, abiding, aah,
 abash, aardvark, aback, abdominal, abeam, abandon, abbreviation, abdication,
 abdomen, abduction, aberration, abjection, abattoir, abductor, abettor,
 abhor, abacus, abbess, abaft, abandonment, abasement, abashment, abatement,
 abbot, abduct, aberrant, abet, abhorrent, abject, abbey, ability, abjectly}
```

In[387]:=
```
SortBy[Array[#^2 &, 20], First[IntegerDigits[#]] &]
```

Out[387]=
```
{1, 16, 100, 121, 144, 169, 196, 25, 225, 256, 289, 36, 324, 361, 4, 49, 400, 64, 81, 9}
```

In[388]:=
```
SortBy[Range[20], StringLength[IntegerName[#]] &]
```

Out[388]=
```
{1, 2, 6, 10, 4, 5, 9, 3, 7, 8, 11, 12, 20, 15, 16, 13, 14, 18, 19, 17}
```

In[389]:=
```
GatherBy[RandomSample[WordList[], 20], StringLength[#] &]
```

Out[389]=
```
{{sculptor, unbolted},
 {seaworthy, dyspepsia, shipwreck, squinting, predicate, upholster, squalidly},
 {ceding, canvas}, {newspaperwoman}, {schizophrenia, magniloquence},
 {cheddar, mindset, netting}, {squad}, {assertively}, {arrogation}}
```

In[390]:=
```
Complement[Alphabet["Ukrainian"], Alphabet["Russian"]]
```

Out[390]=
{є, і, ї, ґ}

In[391]:=
```
Intersection[Array[#^2 &, 100], Array[#^3 &, 100]]
```

Out[391]=
{1, 64, 729, 4096}

In[392]:=
```
Intersection[EntityList[ ⊞ Group of 8  COUNTRIES ✓ ],
  EntityList[ ⊞ North Atlantic Treaty Organization  COUNTRIES ⋯ ✓ ]]
```

Out[392]=
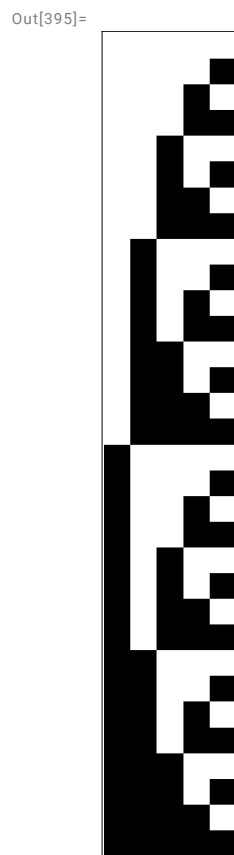{ Canada , France , Germany , Italy , United Kingdom , United States }

In[393]:=
```
Grid[Transpose[Permutations[Range[4]]]]
```

Out[393]=
```
1 1 1 1 1 1 2 2 2 2 2 2 3 3 3 3 3 3 4 4 4 4 4 4
2 2 3 3 4 4 1 1 3 3 4 4 1 1 2 2 4 4 1 1 2 2 3 3
3 4 2 4 2 3 3 4 1 4 1 3 2 4 1 4 1 2 2 3 1 3 1 2
4 3 4 2 3 2 4 3 4 1 3 1 4 2 4 1 2 1 3 2 3 1 2 1
```

In[394]:=
```
StringJoin /@ Permutations[Characters["hello"]]
```

Out[394]=
{hello, helol, heoll, hlelo, hleol, hlleo, hlloe, hloel, hlole, hoell, holel, holle,
 ehllo, ehlol, eholl, elhlo, elhol, ellho, elloh, elohl, elolh, eohll, eolhl, eollh,
 lhelo, lheol, lhleo, lhloe, lhoel, lhole, lehlo, lehol, lelho, leloh, leohl, leolh,
 llheo, llhoe, lleho, lleoh, llohe, lloeh, lohel, lohle, loehl, loelh, lolhe, loleh,
 ohell, ohlel, ohlle, oehll, oelhl, oellh, olhel, olhle, olehl, olelh, ollhe, olleh}

In[395]:=
```mathematica
ArrayPlot[Tuples[{0, 1}, 5]]
```

Out[395]=

In[396]:=
```mathematica
Table[StringJoin[RandomChoice[Alphabet[], 5]], 10]
```

Out[396]=

{nocqy, wvlhj, oxrso, bksye, imdxj, ydyjb, oioto, jgphy, kbmtt, yqazk}

In[397]:=
```mathematica
Tuples[{1, 2}, 3]
```

Out[397]=

{{1, 1, 1}, {1, 1, 2}, {1, 2, 1}, {1, 2, 2}, {2, 1, 1}, {2, 1, 2}, {2, 2, 1}, {2, 2, 2}}