## Brian — PS 11 — 2025-03-18 — Solution

EIWL3 Sections 29 and 30

!! HELP — I HAD TROUBLE WITH 30.7 and 30.10 !!

## Exercises from EIWL3 Section 29

```
In[343]:=
       (* 29.1 *) Array[Prime, 100]
Out[343]=
       \{2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79,
        83, 89, 97, 101, 103, 107, 109, 113, 127, 131, 137, 139, 149, 151, 157, 163,
        167, 173, 179, 181, 191, 193, 197, 199, 211, 223, 227, 229, 233, 239, 241, 251,
        257, 263, 269, 271, 277, 281, 283, 293, 307, 311, 313, 317, 331, 337, 347, 349,
        353, 359, 367, 373, 379, 383, 389, 397, 401, 409, 419, 421, 431, 433, 439,
        443, 449, 457, 461, 463, 467, 479, 487, 491, 499, 503, 509, 521, 523, 541}
In[344]:=
       (* 29.2 *) Array[Prime[#] - Prime[# - 1] &, 99, 2]
Out[344]=
       {1, 2, 2, 4, 2, 4, 2, 4, 6, 2, 6, 4, 2, 4, 6, 6, 2, 6, 4, 2, 6, 4, 6, 8, 4, 2,
        4, 2, 4, 14, 4, 6, 2, 10, 2, 6, 6, 4, 6, 6, 2, 10, 2, 4, 2, 12, 12, 4, 2, 4,
        6, 2, 10, 6, 6, 6, 2, 6, 4, 2, 10, 14, 4, 2, 4, 14, 6, 10, 2, 4, 6, 8, 6, 6,
        4, 6, 8, 4, 8, 10, 2, 10, 2, 6, 4, 6, 8, 4, 2, 4, 12, 8, 4, 8, 4, 6, 12, 2, 18
In[345]:=
       (* 29.3*) Array[Plus, {10, 10}] // Grid
Out[345]=
       2 3 4 5 6 7 8 9 10 11
       3 4 5 6 7 8 9 10 11 12
         5 6 7 8 9 10 11 12 13
       5 6 7 8 9 10 11 12 13 14
       6 7 8 9 10 11 12 13 14 15
          8 9 10 11 12 13 14 15 16
       8 9 10 11 12 13 14 15 16 17
       9 10 11 12 13 14 15 16 17 18
       10 11 12 13 14 15 16 17 18 19
      11 12 13 14 15 16 17 18 19 20
In[346]:=
       (* 29.4 *) FoldList[Times, Range[10]]
Out[346]=
       {1, 2, 6, 24, 120, 720, 5040, 40320, 362880, 3628800}
```

```
In[347]:=
       (* 29.5 *) FoldList[Times, Array[Prime, 10]]
Out[347]=
       {2, 6, 30, 210, 2310, 30030, 510510, 9699690, 223092870, 6469693230}
In[348]:=
       (* 29.6 *) FoldList[ImageAdd,
        Graphics /@ Array[{Opacity[0.2], RegularPolygon[#]} &, 6, 3]]
Out[348]=
```

## Exercises from EIWL3 Section 30

```
In[349]:=
           (* 30.1 *) Thread[Alphabet[] → LetterNumber /@ Alphabet[]]
Out[349]=
           \{a \rightarrow 1, b \rightarrow 2, c \rightarrow 3, d \rightarrow 4, e \rightarrow 5, f \rightarrow 6, g \rightarrow 7, h \rightarrow 8,
            i \rightarrow 9, j \rightarrow 10, k \rightarrow 11, l \rightarrow 12, m \rightarrow 13, n \rightarrow 14, o \rightarrow 15, p \rightarrow 16, q \rightarrow 17,
            r \to 18, s \to 19, t \to 20, u \to 21, v \to 22, w \to 23, x \to 24, y \to 25, z \to 26
In[350]:=
           (* 30.2 *) Partition[Alphabet[], 6] // Grid
Out[350]=
          abcdef
          ghijkl
          mnopqr
          stuvwx
```

In[351]:= (\* 30.3 \*) Partition[IntegerDigits[ $2^{1000}$ ], 50] // Grid[#, Frame  $\rightarrow$  All] &

Out[351]=

-	1	0	7	1	5	0	8	6	0	7	1	8	6	2	6	7	3	2	0	9	4	8	4	2	5	0	4	9	0	6	0	0	0	1	8	1	0	5	6	1	4	0	4	8	1	1	7
[3	3	3	6	0	7	4	4	3	7	5	0	3	8	8	3	7	0	3	5	1	0	5	1	1	2	4	9	3	6	1	2	2	4	9	3	1	9	8	3	7	8	8	1	5	6	9	Ę
[:	1	2	7	5	9	4	6	7	2	9	1	7	5	5	3	1	4	6	8	2	5	1	8	7	1	4	5	2	8	5	6	9	2	3	1	4	0	4	3	5	9	8	4	5	7	7	Ę
(	9	8	5	7	4	8	0	3	9	3	4	5	6	7	7	7	4	8	2	4	2	3	0	9	8	5	4	2	1	0	7	4	6	0	5	0	6	2	3	7	1	1	4	1	8	7	7
-	1	8	2	1	5	3	0	4	6	4	7	4	9	8	ω	5	8	1	0	4	1	2	9	7	3	9	8	7	6	7	5	5	9	1	6	5	5	4	ω	0	4	6	0	7	7	0	(
4	4	5	7	1	1	9	6	4	7	7	6	8	6	5	4	2	1	6	7	6	6	0	4	2	9	8	3	1	6	5	2	6	2	4	3	8	6	8	3	7	2	0	5	6	6	8	(

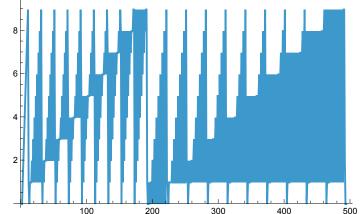
In[352]:=

(\* 30.4 \*)

Partition[Characters[StringTake[WikipediaData["computers"], 400]], 20] // Grid[#, Frame → All] &

Out[352]=

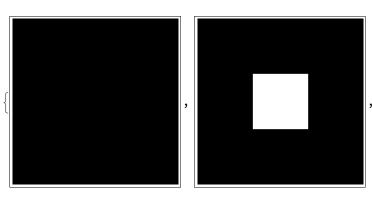
Α		С	0	m	р	u	t	е	r		i	s		а		m	а	С	h
i	n	е		t	h	а	t		С	а	n		b	е		р	r	0	g
r	а	m	m	е	d		t	0		а	u	t	0	m	а	t	i	С	а
l	l	У		С	а	r	r	У		0	u	t		s	е	q	u	е	n
С	е	s		0	f		а	r	i	t	h	m	е	t	i	С		0	r
	l	0	g	i	С	а	ι		0	р	е	r	а	t	i	0	n	S	
(	С	0	m	р	u	t	а	t	i	0	n	)			М	0	d	е	r
n		d	i	g	i	t	а	l		е	ι	е	С	t	r	0	n	i	С
	С	0	m	р	u	t	е	r	s		С	а	n		р	е	r	f	0
r	m		g	е	n	е	r	i	С		s	е	t	s		0	f		0
р	е	r	а	t	i	0	n	s		k	n	0	W	n		а	s		р
r	0	g	r	а	m	s			Т	h	е	s	е		р	r	0	ø	r
а	m	s		е	n	а	b	l	е		С	0	m	р	u	t	е	r	s
	t	0		р	е	r	f	0	r	m		а		W	i	d	е		r
а	n	g	е		0	f		t	а	s	k	s			Т	h	е		t
е	r	m		С	0	m	р	u	t	е	r		s	У	S	t	е	m	
m	а	У		r	е	f	е	r		t	0		а		n	0	m	i	n
а	l	ι	У		С	0	m	р	ι	е	t	е		С	0	m	р	u	t
е	r		t	h	а	t		i	n	С	ι	u	d	е	S		t	h	е
	h	а	r	d	W	а	r	е	,		0	р	е	r	а	t	i	n	g

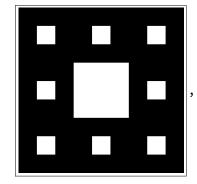


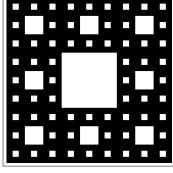
In[354]:=

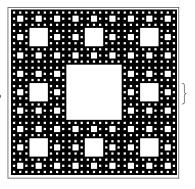
(\* 30.6 \*)

Out[354]=









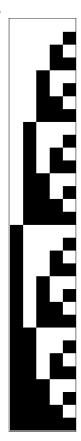
```
In[355]:=
      (* 30.7 *) myList = Array[{\#1, \#2, Sqrt[\#1^2 + \#2^2]} &, {5, 5}]
Out[355]=
      \{\{\{1, 1, \sqrt{2}\}, \{1, 2, \sqrt{5}\}, \{1, 3, \sqrt{10}\}, \{1, 4, \sqrt{17}\}, \{1, 5, \sqrt{26}\}\},\
        \{\{2, 1, \sqrt{5}\}, \{2, 2, 2\sqrt{2}\}, \{2, 3, \sqrt{13}\}, \{2, 4, 2\sqrt{5}\}, \{2, 5, \sqrt{29}\}\},\
        \{\{3, 1, \sqrt{10}\}, \{3, 2, \sqrt{13}\}, \{3, 3, 3, \sqrt{2}\}, \{3, 4, 5\}, \{3, 5, \sqrt{34}\}\},\
        \{\{4, 1, \sqrt{17}\}, \{4, 2, 2\sqrt{5}\}, \{4, 3, 5\}, \{4, 4, 4\sqrt{2}\}, \{4, 5, \sqrt{41}\}\},
        \{\{5, 1, \sqrt{26}\}, \{5, 2, \sqrt{29}\}, \{5, 3, \sqrt{34}\}, \{5, 4, \sqrt{41}\}, \{5, 5, 5, \sqrt{2}\}\}\}
In[356]:=
      Select[myList, IntegerQ[Last[#]] &]
Out[356]=
      { }
In[357]:=
      (* 30.8 *) Array [Length [Last [Sort [Split [Integer Digits [2"]]]]] &, 100]
Out[357]=
      2, 2, 2, 1, 1, 1, 1, 1, 2, 1, 1, 1, 1, 2, 3, 3, 4, 3, 3, 3, 3, 2, 2, 1, 2,
       3, 2, 2, 2, 1, 1, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 1, 1, 1, 1, 1, 2, 2, 2, 3, 3,
       In[358]:=
      (* 30.9 *) Gather[Array[IntegerName, 100],
       First[Characters[#1]] == First[Characters[#2]] &]
Out[358]=
      {{one, one hundred}, {two, three, ten, twelve, thirteen, twenty, twenty-one,
         twenty-two, twenty-three, twenty-four, twenty-five, twenty-six, twenty-seven,
         twenty-eight, twenty-nine, thirty, thirty-one, thirty-two, thirty-three,
         thirty-four, thirty-five, thirty-six, thirty-seven, thirty-eight, thirty-nine},
        {four, five, fourteen, fifteen, forty, forty-one, forty-two, forty-three,
         forty-four, forty-five, forty-six, forty-seven, forty-eight,
         forty-nine, fifty, fifty-one, fifty-two, fifty-three, fifty-four,
         fifty-five, fifty-six, fifty-seven, fifty-eight, fifty-nine},
        {six, seven, sixteen, seventeen, sixty, sixty-one, sixty-two, sixty-three,
         sixty-four, sixty-five, sixty-six, sixty-seven, sixty-eight, sixty-nine,
         seventy, seventy-one, seventy-two, seventy-three, seventy-four,
         seventy-five, seventy-six, seventy-seven, seventy-eight, seventy-nine},
        {eight, eleven, eighteen, eighty, eighty-one, eighty-two, eighty-three,
         eighty-four, eighty-five, eighty-six, eighty-seven, eighty-eight, eighty-nine},
        {nine, nineteen, ninety, ninety-one, ninety-two, ninety-three, ninety-four,
         ninety-five, ninety-six, ninety-seven, ninety-eight, ninety-nine}}
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```
In[359]:=
       (* 30.10 *) Sort[Take[WordList[], 50], Last[Characters[#1]] < Last[Characters[#2]] &]
Out[359]=
       {a, aah, aardvark, aback, abacus, abaft, abalone, abandon, abandoned, abandonment,
        abase, abasement, abash, abashed, abashment, abate, abatement, abattoir,
        abbe, abbess, abbey, abbot, abbreviate, abbreviated, abbreviation, abdicate,
        abdication, abdomen, abdominal, abduct, abducting, abduction, abductor,
        abeam, abed, aberrant, aberration, abet, abettor, abeyance, abhor, abhorrence,
        abhorrent, abidance, abide, abiding, ability, abject, abjection, abjectly}
In[360]:=
        (* 30.11 *)
        Sort[Array[#2 &, 20], First[IntegerDigits[#1]] < First[IntegerDigits[#2]] &]</pre>
Out[360]=
       {196, 169, 144, 121, 100, 16, 1, 289, 256, 225, 25, 361, 324, 36, 400, 49, 4, 64, 81, 9}
In[361]:=
       (* 30.12 *) Sort[Array[IntegerName, 20], StringLength[#1] < StringLength[#2] &]
Out[361]=
       {ten, six, two, one, nine, five, four, eight, seven, three, twenty, twelve,
        eleven, sixteen, fifteen, nineteen, eighteen, fourteen, thirteen, seventeen}
In[362]:=
      (* 30.13 *)
      Gather[RandomChoice[WordList[], 20], StringLength[#1] == StringLength[#2] &]
Out[362]=
       {{shine}, {swelled, stumble, descant}, {assemble, methanol, loveless, strainer},
        {niggle, gossip, untidy, carpel}, {eyeglasses, underskirt},
        {opalescence, propinquity}, {vent}, {simultaneity}, {UFO}, {corollary}}
In[363]:=
       (* 30.14 *) Complement[Alphabet["Russian"], Alphabet["Ukrainian"]]
Out[363]=
       {ъ, ы, э, ё}
In[364]:=
       (* 30.15 *) Intersection[Array[#<sup>2</sup> &, 100], Array[#<sup>3</sup> &, 100]]
Out[364]=
       {1, 64, 729, 4096}
In[365]:=
       (* 30.16 *) Intersection | EntityList | ( Group of 8 COUNTRIES ) | ,
        EntityList | III North Atlantic Treaty Organization COUNTRIES
Out[365]=
        Canada , France , Germany , Italy , United Kingdom ,
```

```
In[366]:=
      (* 30.17 *) Transpose[Permutations[Range[4]]] // Grid
Out[366]=
      1 1 1 1 1 1 2 2 2 2 2 2 3 3 3 3 3 3 4 4 4 4 4 4
      223344113344112244112233
      3 4 2 4 2 3 3 4 1 4 1 3 2 4 1 4 1 2 2 3 1 3 1 2
      4 3 4 2 3 2 4 3 4 1 3 1 4 2 4 1 2 1 3 2 3 1 2 1
In[367]:=
      (* 30.18 *) Permutations[Characters["hello"]]
Out[367]=
      {h, l, l, e, o}, {h, l, l, o, e}, {h, l, o, e, l}, {h, l, o, l, e}, {h, o, e, l, l},
       {h, o, l, e, l}, {h, o, l, l, e}, {e, h, l, l, o}, {e, h, l, o, l}, {e, h, o, l, l},
       {e, l, h, l, o}, {e, l, h, o, l}, {e, l, l, h, o}, {e, l, l, o, h}, {e, l, o, h, l},
       {e, l, o, l, h}, {e, o, h, l, l}, {e, o, l, h, l}, {e, o, l, l, h}, {l, h, e, l, o},
       {l, h, e, o, l}, {l, h, l, e, o}, {l, h, l, o, e}, {l, h, o, e, l}, {l, h, o, l, e},
       {l, e, h, l, o}, {l, e, h, o, l}, {l, e, l, h, o}, {l, e, l, o, h}, {l, e, o, h, l},
       {l, e, o, l, h}, {l, l, h, e, o}, {l, l, h, o, e}, {l, l, e, h, o}, {l, l, e, o, h},
       {l, l, o, h, e}, {l, l, o, e, h}, {l, o, h, e, l}, {l, o, h, l, e}, {l, o, e, h, l},
       {l, o, e, l, h}, {l, o, l, h, e}, {l, o, l, e, h}, {o, h, e, l, l}, {o, h, l, e, l},
       {o, h, l, l, e}, {o, e, h, l, l}, {o, e, l, h, l}, {o, e, l, l, h}, {o, l, h, e, l},
       {o, l, h, l, e}, {o, l, e, h, l}, {o, l, e, l, h}, {o, l, l, h, e}, {o, l, l, e, h}}
```

In[368]:= (\* 30.19 \*)ArrayPlot[Tuples[{0, 1}, 5]]

Out[368]=



```
In[369]:=
        (* 30.20 *) Table[RandomChoice[Alphabet[], 5], 5]
Out[369]=
        \{\{q,\,z,\,r,\,m,\,s\},\,\{e,\,p,\,e,\,y,\,r\},\,\{t,\,t,\,e,\,t,\,f\},\,\{a,\,t,\,x,\,q,\,c\},\,\{b,\,b,\,g,\,s,\,z\}\}
In[370]:=
        (* 30.21 *) Flatten[Array[{#1, #2, #3} &, {2, 2, 2}], 2]
Out[370]=
        \{\{1, 1, 1\}, \{1, 1, 2\}, \{1, 2, 1\}, \{1, 2, 2\}, \{2, 1, 1\}, \{2, 1, 2\}, \{2, 2, 1\}, \{2, 2, 2\}\}
```