

## 2D Histogram Estimator

Accuracy with  $h = 1$ : **42.40%**

Halving the bin size to 0.5 decreased the accuracy by over two-fold (18.14%). Doubling the bin size to 2 increased the accuracy to 56.04%. The maximum attainable accuracy was around 60% with a bin size around 4.

## Naïve Estimator

Accuracy with  $h = 1$ : **41.07%**

Halving the bin size to 0.5 had the same effect that it did with the histogram estimator. The accuracy dropped to 17.70%. Doubling the bin size to 2 also increased the accuracy to 55.59%. The Naïve Estimator was able to attain a marginally greater accuracy than the 2D Histogram Estimator with results above 60.21% when a bin size of 4 was used.

## Kernel Estimator (Gaussian Kernel)

Accuracy with  $h = 1$ : **60.55%**

Halving the  $h$ -value to 0.5 decreased the accuracy to **57.21%** since the data became less smooth. If the data is smoothed out too much the accuracy also decreased. For instance, at  $h=20$ , the accuracy dropped below 60%.

## K-Nearest Neighbor

Accuracy with  $k = 1$ : **52.48%**

An optimal value for  $k$  can be heuristically determined by taking the square root of  $N$ . Since  $N = 1797$  for the test data, an adequate estimate for an optimal  $k$  is 42. This  $k$  values gives an accuracy of **61.49%**.

## 64D Histogram Estimator

*Observation:* The computational time and memory space required to utilize a histogram estimator in the 64-Dimensional hyperspace is exponentially greater than that of 2-Dimensional space. This provides an example of the practical utility of principal component analysis in decreasing the power and time to execute a program. The obtainable accuracy will be higher when using more dimensions, but the trade-off is time and memory. An optimal number of dimensions should be sought out to balance computational time/space and the error.