

Introduction to Digital Design

Week 3: Switches, Transistors, Logic Gates

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Overview

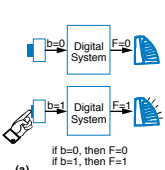
- Combinational circuit
 - Circuit outputs depend solely on the present combination of the circuit inputs.
- Switches
 - Electronic switches are the basis of binary digital circuits.
 - Three parts: source, output, and control.
- CMOS Transistors
 - Miniaturized switches.
 - NMOS, PMOS.
- Boolean Logic Gates
 - Boolean algebra primer: Boolean expression
 - Basic logic gates: NOT, AND, OR

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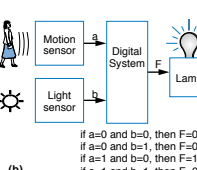
Introduction

2.1

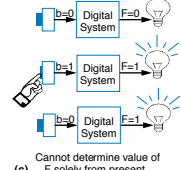
- Let's learn to design digital circuits, starting with a simple form of circuit:
 - **Combinational circuit**
 - Outputs depend solely on the present combination of the circuit inputs' values
 - Vs. sequential circuit: Has "memory" that impacts outputs too



(a)



(b)



(c)

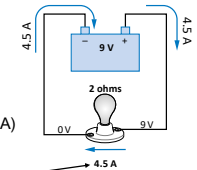
Note: Slides with animation are denoted with a small red "A" near the animated items

2.1

Switches

2.2

- Electronic switches are the basis of binary digital circuits
 - Electrical terminology
 - **Voltage:** Difference in electric potential between two points (volts, V)
 - Analogous to water pressure
 - **Resistance:** Tendency of wire to resist current flow (ohms, Ω)
 - Analogous to water pipe diameter
 - **Current:** Flow of charged particles (amps, A)
 - Analogous to water flow
 - $V = I * R$ (Ohm's Law)
 - $9V = I * 2\text{ ohms}$
 - $I = 4.5A$

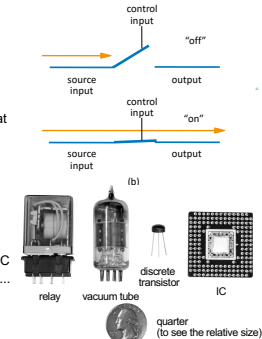


If a 9V potential difference is applied across a 2 ohm resistor, then 4.5 A of current will flow.

2.2

Switches

- A switch has three parts
 - Source input, and output
 - Current tries to flow from source input to output
 - Control input
 - Voltage that controls whether that current can flow
- The amazing shrinking switch
 - 1930s: Relays
 - 1940s: Vacuum tubes
 - 1950s: Discrete transistor
 - 1960s: Integrated circuits (ICs)
 - Initially just a few transistors on IC
 - Then tens, hundreds, thousands...




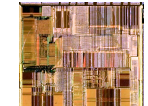
relay vacuum tube discrete transistor IC

quarter (to see the relative size)

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Moore's Law

- IC capacity doubling about every 18 months for several decades
 - Known as "Moore's Law" after Gordon Moore, co-founder of Intel
 - Predicted in 1965 predicted that components per IC would double roughly every year or so
 - Book cover depicts related phenomena
 - For a particular number of transistors, the IC area shrinks by half every 18 months
 - Consider how much shrinking occurs in just 10 years (try drawing it)
 - Enables incredibly powerful computation in incredibly tiny devices
 - Today's ICs hold *billions* of transistors
 - The first Pentium processor (early 1990s) needed only 3 million

An Intel Pentium processor IC having millions of transistors

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The CMOS Transistor

2.3

- CMOS transistor
 - Basic switch in modern ICs

A positive voltage here... attracts electrons here, turning the channel between the source and drain into a conductor

Silicon -- not quite a conductor or insulator: *Semiconductor*

gate

source

drain

IC package

IC

gate

1

0

conducts

does not conduct

does not conduct

conducts

7

CMOS Transistor Analogy

source

gate

drain

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Boolean Logic Gates

Building Blocks for Digital Circuits

(Because Switches are Hard to Work With)

2.4

These blocks... ..are hard to work with.

Transistors are hard to work with

The right building blocks... ..enable greater designs.

The logic gates that we'll soon introduce enable greater designs

- "Logic gates" are better digital circuit building blocks than switches (transistors)
 - Why?...

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Boolean Algebra and its Relation to Digital Circuits

- To understand the benefits of "logic gates" vs. switches, we should first understand Boolean algebra
- "Traditional" algebra
 - Variables represent real numbers (x, y)
 - Operators operate on variables, return real numbers ($2.5 \cdot x + y - 3$)
- Boolean Algebra**
 - Variables represent 0 or 1 only
 - Operators return 0 or 1 only
 - Basic operators
 - AND: $a \text{ AND } b$ returns 1 only when both $a=1$ and $b=1$
 - OR: $a \text{ OR } b$ returns 1 if either (or both) $a=1$ or $b=1$
 - NOT: $\text{NOT } a$ returns the opposite of a (1 if $a=0$, 0 if $a=1$)

a	b	AND
0	0	0
0	1	0
1	0	0
1	1	1

a	b	OR
0	0	0
0	1	1
1	0	1
1	1	1

a	NOT
0	1
1	0

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Boolean Algebra and its Relation to Digital Circuits

- Developed mid-1800's by George Boole to formalize human thought
 - Ex: "I'll go to lunch if Mary goes OR John goes, AND Sally does not go."
 - Let F represent my going to lunch (1 means I go, 0 I don't go)
 - Likewise, m for Mary going, j for John, and s for Sally
 - Then $F = (m \text{ OR } j) \text{ AND NOT}(s)$
- Nice features
 - Formally evaluate
 - $m=1, j=0, s=1 \rightarrow F = (1 \text{ OR } 0) \text{ AND NOT}(1) = 1 \text{ AND } 0 = 0$
 - Formally transform
 - $F = (m \text{ AND NOT}(s)) \text{ OR } (j \text{ AND NOT}(s))$
 - Looks different, but same function
 - We'll show transformation techniques soon
 - Formally prove
 - Prove that if Sally goes to lunch ($s=1$), then I don't go ($F=0$)
 - $F = (m \text{ OR } j) \text{ AND NOT}(1) = (m \text{ OR } j) \text{ AND } 0 = 0$

a	b	AND
0	0	0
0	1	0
1	0	0
1	1	1

a	b	OR
0	0	0
0	1	1
1	0	1
1	1	1

a	NOT
0	1
1	0

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Evaluating Boolean Equations

- Evaluate the Boolean equation $F = (a \text{ AND } b) \text{ OR } (c \text{ AND } d)$ for the given values of variables a, b, c , and d :
 - Q1: $a=1, b=1, c=1, d=0$.
 - Answer: $F = (1 \text{ AND } 1) \text{ OR } (1 \text{ AND } 0) = 1 \text{ OR } 0 = 1$.
 - Q2: $a=0, b=1, c=0, d=1$.
 - Answer: $F = (0 \text{ AND } 1) \text{ OR } (0 \text{ AND } 1) = 0 \text{ OR } 0 = 0$.
 - Q3: $a=1, b=1, c=1, d=1$.
 - Answer: $F = (1 \text{ AND } 1) \text{ OR } (1 \text{ AND } 1) = 1 \text{ OR } 1 = 1$.

a	b	AND
0	0	0
0	1	0
1	0	0
1	1	1

a	b	OR
0	0	0
0	1	1
1	0	1
1	1	1

a	NOT
0	1
1	0

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Converting to Boolean Equations

- Convert the following English statements to a Boolean equation
 - Q1. a is 1 and b is 1.
 - Answer: $F = a \text{ AND } b$
 - Q2. either of a or b is 1.
 - Answer: $F = a \text{ OR } b$
 - Q3. a is 1 and b is 0.
 - Answer: $F = a \text{ AND NOT}(b)$
 - Q4. a is not 0.
 - Answer:
 - (a) Option 1: $F = \text{NOT}(\text{NOT}(a))$
 - (b) Option 2: $F = a$

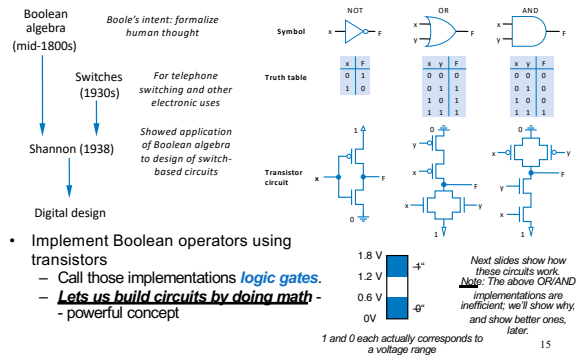
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Converting to Boolean Equations

- Q1. A fire sprinkler system should spray water if high heat is sensed and the system is set to enabled.
 - Answer: Let Boolean variable h represent "high heat is sensed," e represent "enabled," and F represent "spraying water." Then an equation is: $F = h \text{ AND } e$.
- Q2. A car alarm should sound if the alarm is enabled, and either the car is shaken or the door is opened.
 - Answer: Let a represent "alarm is enabled," s represent "car is shaken," d represent "door is opened," and F represent "alarm sounds." Then an equation is: $F = a \text{ AND } (s \text{ OR } d)$.
 - (a) Alternatively, assuming that our door sensor d represents "door is closed" instead of open (meaning d=1 when the door is closed, 0 when open), we obtain the following equation: $F = a \text{ AND } (s \text{ OR NOT}(d))$.

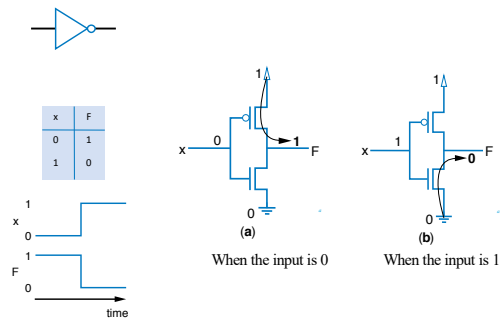
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Relating Boolean Algebra to Digital Design



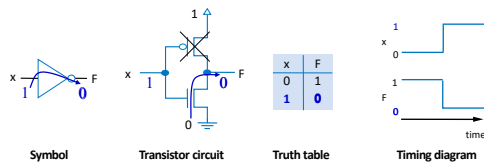
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NOT gate



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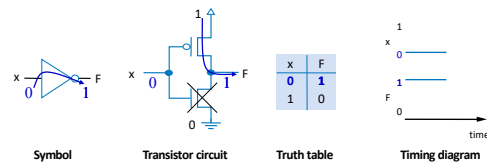
Relating a Logic Gate Symbol, Circuit, Truth Table, and Timing Diagram



Setting x to 1 causes F to be 0

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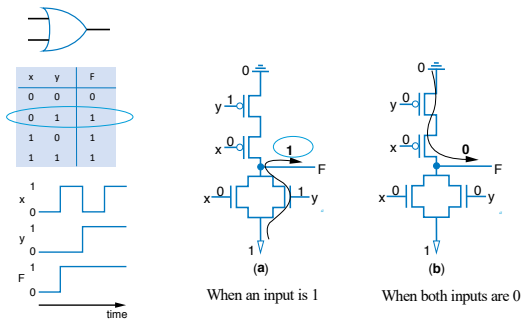
Relating a Logic Gate Symbol, Circuit, Truth Table, and Timing Diagram



Setting x to 0 causes F to be 1

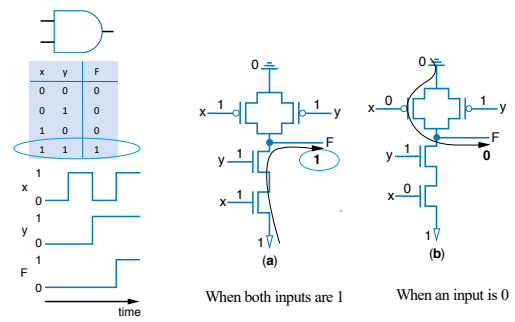
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OR gate



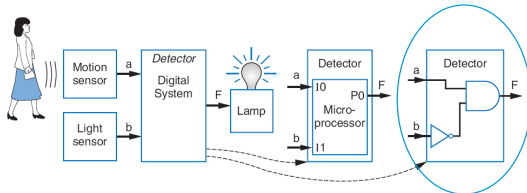
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AND gate



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Building Circuits Using Gates



- Recall Chapter 1 motion-in-dark example
 - Turn on lamp ($F=1$) when motion sensed ($a=1$) and no light ($b=0$)
 - $F = a \text{ AND NOT}(b)$
 - Build using logic gates, AND and NOT, as shown
 - We just built our first digital circuit!

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Example: Converting a Boolean Equation to a Circuit of Logic Gates

Start from the output, work back towards the inputs

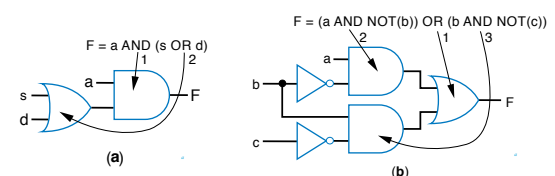
- Q: Convert the following equation to logic gates:
 $F = a \text{ AND NOT}(b \text{ OR NOT}(c))$



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Example: Converting a Boolean Equation to a Circuit of Logic Gates

[Video](#)



Start from the output, work back towards the inputs

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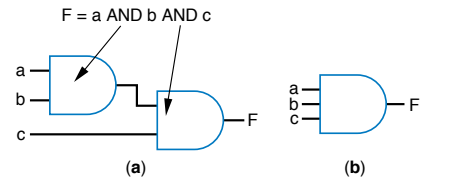
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More examples

[Video](#)

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Using gates with more than 2 inputs



Can think of as $\text{AND}(a,b,c)$

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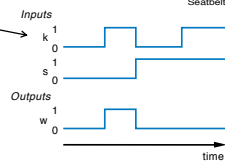
Example: Seat Belt Warning Light System

- Design circuit for warning light
- Sensors
 - $s=1$: seat belt fastened
 - $k=1$: key inserted

- Capture Boolean equation
 - seat belt not fastened, and key inserted
- Convert equation to circuit

$$w = \text{NOT}(s) \text{ AND } k$$

- Timing diagram illustrates circuit behavior
 - We set inputs to any values
 - Output set according to circuit



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Example: Seat Belt Warning Light System

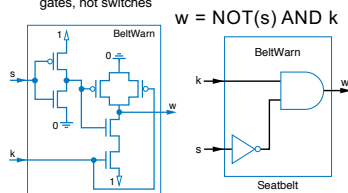
[Video](#)

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Gates vs. switches

Notice

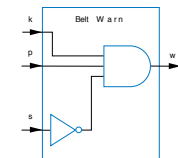
- Boolean algebra enables easy capture as equation and conversion to circuit
 - How design with switches?
 - Of course, logic gates are built from switches, but we think at level of logic gates, not switches



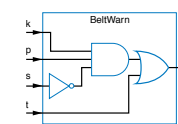
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More examples: Seat belt warning light extensions

- Only illuminate warning light if person is in the seat ($p=1$), and seat belt not fastened and key inserted
- $w = p \text{ AND } \text{NOT}(s) \text{ AND } k$

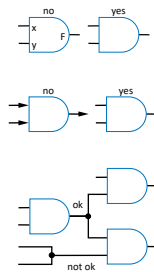


- Given $t=1$ for 5 seconds after key inserted. Turn on warning light when $t=1$ (to check that warning lights are working)
- $w = (p \text{ AND } \text{NOT}(s) \text{ AND } k) \text{ OR } t$



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Some Gate-Based Circuit Drawing Conventions



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Summary

- Combinational circuit
 - Circuit outputs depend solely on the present combination of the circuit inputs.
- Switches
 - Electronic switches are the basis of binary digital circuits.
 - Three parts: source, output, and control.
- CMOS Transistors
 - Miniaturized switches.
 - NMOS, PMOS.
- Boolean Logic Gates
 - Boolean algebra primer: Boolean expression
 - Basic logic gates: NOT, AND, OR

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