Cash Payments and the Penny Policy Debate*

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Abstract

This article quantifies the burden of exchanging currency notes and coins using a model of optimal consumer-merchant exchange of cash payments and consumer payment choice diary data. The model is then applied to analyze a policy debate whether to eliminate the penny coin from circulation. We find that penny elimination would reduce the burden of exchanging cash and will not have any significant inflationary consequences caused by price rounding. Surprisingly, a removal of both the penny and nickel coins from circulation would slightly increase (not decrease) the burden relative to penny elimination only.

Keywords: Optimal currency denominations, cash transactions, burden of exchanging cash, penny elimination.

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1. Introduction

Despite the availability of alternative means of payment, consumers still depend on cash. U.S. consumers in 2019, prior to the COVID pandemic, used cash for 26 percent of all payments and 47 percent of all payments below \$10, see Kim, Kumar, and O'Brien (2020). Coyle, Kim, and O'Brien (2021) found that, amidst the pandemic, this number declined to 19 percent of all payments in 2020. The ECB (2020) finds that in seventeen euro area countries 73 percent by volume (48 percent by value) of all point-of-sale (POS) and person-to-person (P2P) payments were made with cash in 2019. Khiaonarong and Humphrey (2019, 2022) provide estimates and forecasts of cash use in several countries.

Cash payments are two-way exchanges of currency notes and coins. The payer (consumer, buyer) hands in currency notes and coins, then, if needed, receives change from the payee (merchant, seller) in the form of currency notes and coins. The burden of exchanging cash is proportional to the total number of coins and notes required to transact. While the costs of producing a currency denomination are known, the users' exchange costs are not. Consequently, policymakers interested in adjustments to the currency system have incomplete information on the total costs. Given the high frequency of cash usage, rectifying this incomplete information is of the utmost importance. The goal of this article is to quantify the burden of exchanging cash using data from a diary of consumer payment choice. We compute lower and upper bounds on the number of tokens exchanged in each transaction, where a token refers to one unit (coin or note) of a currency denomination. These computations should be useful for policymakers considering adjustments to the currency system.¹

We quantify the burden of exchanging cash by first constructing a repeated game of consumer-merchant interactions. In the model both consumers and merchants are able

¹The burden of exchanging currency notes and coins is shared by both consumers and merchants. Using multicountry panel data, Png and Tan (2021) show that cashier wages increase with retail cash usage. In addition, 8 of 10 cashiers in a large supermarket chain in Singapore preferred card payments to cash payments. The authors explain that by convenience and mental stress of handling cash and view handling cash as a different job attribute which may require additional compensation. The authors also suggest that retailers may pay efficiency wages when cash usage is high to dissuade cashiers from theft.

to pay or give change with any currency denomination except \$2 notes.² They jointly choose, given the dollar amount, which coins and notes to transact with. Using transaction data from consumer payment diary surveys spanning 2015 to 2019, we use the model to compute the burden of cash exchanges for each cash transaction observed. From that, we derive a lower bound distribution of the number of tokens exchanged during the cash transactions. The quantification described represents a lower bound on the burden of exchanging cash because the environment grossly underestimates the true burden. This is because the computations are based on the assumption that consumers and merchants possess all currency and coin denominations in circulation. Therefore, the agents in this environment can transact using the minimum possible number of exchanged tokens in each instance. We view access to all coins and notes as a reasonable assumption for merchants. However, it is likely too strong an assumption for consumers.

We mitigate this issue by considering a second environment where the assumption on consumers is relaxed. In this second environment consumers can only transact using \$20 notes. This assumption represents a consumer first withdrawing cash from an ATM then choosing to transact. We choose to have consumers withdraw \$20 notes because ATMs typically only distribute \$20 notes. Shy (2020) finds significant cash use discontinuities at multiples of \$20 in the U.S. We then re-solve the model and derive a new distribution for the exchange burden which we interpret as an upper bound.

The quantification exercises performed are useful for policymakers because they provide reliable bounds on the burden of exchanging cash with respect to U.S. currency denominations. By reliable we mean that the agents (consumers and merchants) are optimizing with respect to the number of tokens exchanged and that the computations are based on actual transaction diary data in which consumers report the exact dollar amount of each cash payment. Deriving bounds are also useful for the design of optimal currency and coin denominations. Section 2 reviews this literature.

²Greene and Stavins (2020) find that, from 2015 to 2020, consumers rarely had a \$2 note on hand. More precisely, they find that consumers had on average between \$0.00 and \$0.10 dollars in \$2 notes on hand. Moreover, there is no evidence that ATMs dispense \$2 notes.

The second goal of this article is to use the model to analyze counterfactual changes to the currency system by removing low-denomination coins from circulation. In 2013 Canada eliminated the penny from its currency system. In addition, five euro area member states already have rounding rules to the nearest 5-euro cents for cash payments: Belgium, Finland, Ireland, Italy and Netherlands, see EC (2020). To this end, we choose a long-standing policy debate in the United States: whether to drop the one-penny coin from circulation. Beginning in 1989, several bills have been introduced in the U.S. Congress regarding the proposal to drop the one-penny coin from circulation and round prices to their nearest 5¢ value.³ Indeed, the COVID-19 coin shortages in the United States have renewed calls to eliminate the penny. Moreover, our data show that, in both 2019 and 2020, approximately two-thirds of U.S. consumers store coins at their homes or vehicles. The policy is also not without precedent. The one-penny coin was phased out from circulation in Canada on February 4, 2013. Merchants were then instructed to round payment amounts to their nearest multiples of 5¢. For example, payment values \$1.31 and \$1.32 are rounded to \$1.30 whereas \$1.33 and \$1.34 are rounded to \$1.35.⁴

U.S. economy where no pennies are in circulation and merchants have been instructed to round prices to the nearest 5¢. However, it could be the case that, after the policy is implemented, merchants will reset prices and round all prices up. We therefore consider a second counterfactual economy wherein merchants strictly round prices up to the nearest 5¢. We simulate the effects of a hypothetical transition to an economy with no pennies by comparing the burden of exchanging cash in an economy with pennies to the counterfactual economy without pennies. We briefly explore the aggregate price effects of merchant rounding on cash transactions. Importantly, our counterfactual analysis is not restricted to the penny policy. It is general enough to be used by policymakers when analyzing

³See, https://www.congress.gov/bill/101st-congress/house-bill/3761/ (1989), https://www.congress.gov/bill/107th-congress/house-bill/2528 (2001), https://www.congress.gov/bill/109th-congress/house-bill/5818?s=1&r=6 (2006), https://www.congress.gov/bill/115th-congress/senate-bill/759/actions (2017).

⁴See, https://www.canada.ca/en/revenue-agency/programs/about-canada-revenue-agency-cra/phasing-penny.html.

other changes to the currency system.

The paper is organized as follows. Section 2 reviews the literature on currency denominations. Section 3 describes the data and provides descriptive statistics on cash payments. Section 4 derives a model of optimal exchange of currency notes and coins in cash transactions. Using transaction-level data, the model is then used to quantify the burden of exchanging cash. Section 5 provides a counterfactual analysis by computing the effects of transitioning to an economy with no pennies. In particular, Section 6 considers the aggregate price effects from transitioning to a penniless economy. Section 7 analyzes the effects of removing both the 1¢ and the 5¢ coins from circulation. Section 8 concludes. All data and the code used in the article are available at https://github.com/brianprescott/change-burden.

2. Overview of the literature on currency denomination

The literature on the use of cash is surveyed in Shy (Forthcoming). We divide the literature on currency denominations into four subjects: (i) The (mostly theoretical) literature that computes the (user-side) optimal currency denominations for a given distribution of payment amounts. (ii) The (issuer-side) cost of producing and distributing a variety of currency denominations. (iii) An empirical literature that quantifies how existing currency denominations affect consumers' choice of whether to pay cash or with debit and credit cards. (iv) How merchants in some lines of business round prices to facilitate cash transactions.

Cramer (1983) computes optimal currency denominations using the *principle of least ef- fort*. According to this principle, denominations of notes and coins are properly designed so that the settlements of cash transactions minimize the number of tokens (notes and coins) exchanged between the trading parties.

Sumner (1993) and Telser (1995) formulate the problem differently suggesting that the problem of choosing the optimal spacing of currency and coin denominations is related to the problem of spacing units of standard weight measurements (the problem of Bâchet).

For a uniform distribution of transaction amounts, this approach yields denominations that are powers of 3, such as 1, 3, 9, 27, and so on when overpayments and the return of change are allowed. Shallit (2003) solves a different problem by focusing on denominations of coins that minimize the average number of coins needed to hand out change.

Using the principle of the least effort, Van Hove and Heyndels (1996) show that, for a uniform distribution of transaction amounts, the average number of notes and coins exchanged in a transaction is minimized by spacing denominations apart by a factor of two (rather than three), even when allowing for overpayments and the return of change. Van Hove (2001) argues that Bâchet's problem of weights cannot be transposed blindly to the problem of finding optimal currency denominations. The reasons are: (i) Bâchet's problem minimizes the number of standard weights rather than the number of weights used in a typical weighing; and (ii) it is based on the assumption that the set of weights contains only one weight of each size.

Several papers examine the two theories of optimal denominations by comparing the results to denominations in circulation in various countries. Wynne (1997) finds that only five countries have denominations that are either powers or integer multiples of three. Tschoegl (1997) finds that the average ratio of adjacent denominations is 2.6 for coins and 2.62 for notes. Lee (2010) finds that the binary-decimal denomination structure adopted by the eurozone and the U.S. is superior to the decimal-pair structure adopted by Japan and Korea. Denominations of medieval coinage systems are described in Sargent and Velde (1999, 2003).

Franses and Kippers (2007) use data on actual euro cash payments in the Netherlands and find that 39 percent individuals in the sample did not pay efficiently and hence violated the principle of the least effort. Their study is important because the researchers were able to observe the exact denominations of notes and coins that consumers had in their wallet prior to making the purchase. This feature allowed them to refine the definition of efficiency so that the principle of least effort is conditional on what is available in the consumers' wallets.

A second line of research examines issuers' costs of producing a variety of currency denominations. Bouhdaoui, Bounie, and Van Hove (2011) and Bouhdaoui and Van Hove (2017) analyze the cost structure of issuing a variety of currency denominations and show that more efficient currency systems can also be more costly, in particular when denomination-specific fixed production costs are taken into account.

The third line of research examines how currency denominations affect consumers' decisions whether to pay cash. Lee, Wallace, and Zhu (2005) construct a model of random pairwise meetings in which trading parties choose the portfolio of denominations they carry. Lee (2010) studies how different denominations affect the carrying cost of money in a monetary economy and presents welfare estimates of the gains from different denomination structures. Using payment diary data from Canada and the U.S., Chen, Huynh, and Shy (2019), Shy (2020), and Van Hove (2020) show how currency denominations generate discontinuities in the percentage of cash payments.⁵

A fourth line of research examines some markets where sellers set prices to reduce the cost of paying cash. Levy and Young (2004) provide evidence for *convenient prices* reporting that the price of a 6.5-oz Coca-Cola was 5e (a nickel) for 73 years (1886 to 1959). Other examples are local weekday newspapers that during the 1980s were sold for 25e and parking meters that still utilize quarters. In all three examples, sellers utilized low-tech vending machines with no need to provide change. Further empirical support for this behavior is provided in Knotek (2008, 2011) and Bouhdaoui, Bounie, and François (2014).

Our paper contributes to the optimal denominations literature in two ways. First, we formulate a model based on the principle of least effort and apply it to the empirical distribution of cash transactions from 2015 to 2019. Our quantification of the burden of exchanging cash from the empirical distribution of cash payments is, to the best of our knowledge, the first of its kind in the U.S. Furthermore, we demonstrate how the model

⁵Rogoff (2016) argues that large denomination notes should be eliminated since they are mostly used for illegal trading. In contrast, McAndrews (2017) and Hendrickson and Park (2021) argue that eliminating large denominations is sub-optimal for reducing illegal trading and that allowing illegal traders to use large bills with a lower rate of return will produce more seigniorage.

can be used as a framework for policymakers when evaluating counterfactual changes to the currency system. We demonstrate this by using the model to document how the burden of exchanging cash would evolve if the penny were dropped from circulation. This article is related to Boeschoten and Fase (1989) who, using 1984 to 1986 survey data of Dutch households, apply the observed distribution of cash payments and find that, on average, efficient payments involved the use of 3.3 notes and coins per payment. We find that the average burden is 3.14 notes and coins (4.96 notes and coins if consumers are restricted to carrying only \$20 notes before each transaction). Appendix B examines similarities and differences between their study and outs.

Second, we contribute to the literature by studying the price effects resulting from penny elimination. We estimate how merchants' price rounding, as a result of the policy, would impact the distribution of consumer prices. Our results provide valuable information to policymakers considering changes to the U.S. currency system. Importantly, the frameworks presented in this article could be used to study further changes to the currency system beyond penny elimination. We demonstrate this by analyzing the counterfactual effects of eliminating both the penny and the nickel coins.

3. Data and descriptive statistics

The data used throughout this article are taken from the 2015 to 2019 Survey of Consumer Payment Choice (SCPC) and Diary of Consumer Payment Choice (DCPC). The SCPC and DCPC are composed of a representative sample of U.S. consumers age 18 and older taken from the University of Southern California's Understanding America Study.⁶

The SCPC is a recall-based survey where respondents are asked to estimate the number of payments made with a specific type of method during a normal month. The SCPC also collects a wide range of demographic information, which is the information we leverage from it. The DCPC asks respondents to record all of their transactions during three consecutive days in October. The transactions data collected in the DCPC include pur-

⁶See Foster, Greene, and Stavins (2020) for more information on the representativeness of the panel in 2019.

chases, bill payments, p2p payments, ATM withdrawals, deposits, and income receipts. Respondents in the DCPC report how much they paid, the means of payment, and merchant or person they paid on each assigned diary day. Respondents' three-day periods were evenly distributed throughout each day in October from 2015 to 2019.⁷ The data contain weights for all respondents that can be used to produce monthly population estimates of the adult U.S. population for the given year.

The data used for our exchange burden quantification are the 16,906 in-person cash transactions conducted by 3,452 respondents from 2015 to 2019. Figure 1 displays the distribution of transaction amounts for all cash payments not exceeding \$100 (96.6 percent of all cash payments). This distribution achieves its global maximum at \$5 with local maxima at \$1 and then every \$5 interval up until \$60 and then at \$100. This observation is consistent with Shy (2020) who found spikes in the use of cash at \$1, \$5, \$20, and \$40 payment amounts.

The data also provide information on which merchants receive the most cash payments and which consumers make the most cash payments. Table 1 provides all summary statistics of the cash transactions sample. We find that, from 2015 to 2019, retail stores received the most cash payments, 72 percent. They were followed by merchant business service providers (11 percent) and person-to-person (9 percent), respectively. We also know which consumers make the most cash payments. Approximately 40 percent of cash transactions are conducted by consumers with only a high school diploma, while 43 percent are made by those with household income less than \$50,000. The average age of a consumer making a cash transaction was 54, while the most common decade consumers were born in was the 1950s. Now that we know who makes and receives cash payments in our sample, we proceed to characterizing the distribution of the burden of exchanging cash borne by consumers and merchants.

⁷The panel is not balanced as there are many respondents who drop out from one year to the next. See Greene and Stavins (2020) for more information on the panel dimension of the data.

4. Optimal cash transactions and the burden of exchanging cash

This section quantifies the burden of exchanging cash during cash transactions. We construct an analytical model to explain how cash transactions are settled in an economy where payers and payees minimize their exchange burden of cash payments. Similar to Cramer (1983), we say that *a cash transaction is optimal* if, for given currency denominations and for a given payment amount, the chosen currency notes and coins minimize the sum of tokens (currency notes plus coins) that the parties need to exchange. That includes the initial payment and the return of change. For such payments, we say that *the burden of exchanging cash is minimized*.

For example, given the denominations of U.S. currency, there are two potential ways to pay for a 43¢ transaction: (i) to pay with 25¢ + 10¢ + 10¢ coins and receive 1¢ + 1¢ coins as change, or (ii) to pay with a 50¢ coin and receive 5¢ + 1¢ + 1¢ coins as change. We consider the second option to be optimal because it minimizes the number of tokens exchanged between the consumer and the merchant: the first option corresponds to an exchange of 5 coins whereas the second option corresponds to an exchange of 4 coins.

The top panel of Figure 2 displays the optimal burden for transaction amounts between \$4.00 and \$5.00. The figure shows that payment amounts that are multiples of 5¢ have the lowest burdens, while amounts ending in 2¢, 3¢, 7¢, and 8¢ have higher burdens. For example, the top panel of Figure 2 shows that the burden of paying \$4.72 is 5: the buyer pays with a \$5 bill and receives 25¢ + 1¢ + 1¢ + 1¢ coins as change. Similarly, the burden of paying \$4.13 is 6: the buyers pays with a \$5 bill and receives 50¢ + 25¢ + 10¢ + 1¢ + 1¢ coins as change.

4.1 A model of the principle of least effort

Let δ denote the exogenously-given vector of denominations of currency notes and coins in circulation ordered by denomination value. For example, there are currently D=12 denominations circulating in the U.S.: $\delta^{\text{U.S.}}=[0.01,0.05,0.10,0.25,0.50,1,2,5,10,20,50,100].$ We use the term *token* to refer to one unit of one denomination. For example, a token could

be a \$0.01 (1¢) coin or a \$5 note.

Consider a consumer (payer) and a merchant (payee) who engage in a transaction that requires a payment of a, where a is quoted in multiples of some of the denominations listed in δ . For example, in the U.S., cash transaction amounts must be in multiples of \$0.01 (1¢) or higher denominations (but cannot be a fraction of 1¢).

The payment involves a two-way exchange of tokens. First, the consumer pays in the form of a non-negative vector of integers θ^p of multiples of denominations. Second, the merchant returns a non-negative vector of integers θ^r of multiple denominations. Both, θ^p and θ^r are vectors of dimension D which is the number of denominations in circulation. For example, $\theta^p = [2,0,0,0,1,0,0,1,0,0,0,3]$ in the U.S. means that the payer hands in to the merchant two $1\mathfrak{c}$ coins, one $50\mathfrak{c}$ coin, one \$5 bill, and three \$100 bills, which sum up to an initial payment of \$305.52. The vector of returned change θ^r (which could be a vector of zeros) is similarly defined.

For each transaction amount a, the consumer initially pays $\theta^p \cdot \delta \geq a$. That is, the initial payment must be greater than or equal to the transaction amount. Then, in the case of an over-payment $(\theta^p \cdot \delta > a)$, the merchant returns change as a vector θ^r that satisfies $(\theta^p - \theta^r) \cdot \delta = a$. We define the *the burden of exchanging cash* by $b = \sum_{d=1}^D (\theta_d^p + \theta_d^r)$, which is the total number of tokens exchanged between the payer and the payee in both directions.

The consumer and the merchant jointly decide on the exact denominations θ^p and θ^r to be exchanged in both direction to minimize the burden. Formally, for a given transaction amount a and a vector of denominations in circulation δ , they choose non-negative vectors of integers θ^p and θ^r to solve

$$b^{*}(a) = \min_{\theta^{p}, \theta^{r}} \sum_{d=1}^{D} (\theta_{d}^{p} + \theta_{d}^{r})$$

$$\mathbf{s.t.} \quad \theta^{p} \cdot \delta \geq a$$

$$(\theta^{p} - \theta^{r}) \cdot \delta = a.$$

$$(1)$$

Note that a solution for (1), denoted by $b^*(a)$, always exists because the transaction amount

a is quoted in multiples of some denominations in the vector of all denominations δ . However, the solution need not be unique as there may be several combinations to exchange tokens that yield the same minimum burden $b^*(a)$.

4.2 Quantifying the burden of exchanging cash

We now approach the first set of results, which are the derivations of the distribution of the burden of exchanging cash. Recall from Footnote 2 that we exclude the \$2 notes from the set of available denominations. For each cash payment amount a in the DCPC data described in section 3, we use a branch-and-bound algorithm that solves the burden minimization problem defined in (1).⁹ We denote the resulting minimum burden values by $b^*(a)$ for every payment amount a in the data. From these values we compute the distribution of the burden of exchanging cash, b^* , derived from all the 16,906 cash payment amounts a in the DCPC.

The distribution of optimal burdens derived from the cash payment amounts in the data is displayed in the left panel of Figure 3. We find that the optimal burden for approximately one-fifth of cash transactions is $b^* = 2$ and that nearly 45 percent of cash transactions (22.1 + 22.5 percent) result in $b^* \le 2$. The average burden for any given cash transaction is 3.14 coins and notes. Transactions with a > \$100, on average, require approximately 5 tokens and have a median of 8 which is approximately 2.5 times larger than the median for not exceeding \$100. The difference in the highest burden observed for transactions exceeding \$100 and transactions not exceeding \$100 is $b^*(\$6420) - b^*(\$100) = 65 - 9 = 56$.

It is important to re-emphasize that the above results and the derived distribution of burdens displayed on the left panel in Figure 3 constitute only lower bounds of the actual

⁸As pointed out by a reviewer, the formulation of burden b(a) in (1) assumes that the marginal cost of handling an additional token is constant. However, the same solution would be obtained assuming increasing or decreasing marginal cost of an additional token by taking a monotone transformation of b(a). More precisely, the same solution would be obtained by assuming that the burden takes the form of $\hat{b}(a) = \alpha + f[b(a)]$ where the function f satisfies f' > 0 and α is a constant. In this case f'' > 0 (f'' < 0) corresponds to increasing (decreasing) marginal cost of an additional token of change, respectively.

⁹We implement this algorithm via the 1pSolve R-package.

burden of exchanging cash faced by payers and payees. This is because the optimization problem defined in (1) is based on the assumption that the transacting parties possess the exact denominations required to achieve the minimum exchange burden of cash for each particular transaction they are engaged in. If this assumption does not hold for a transaction, then buyers and sellers may have to exchange a larger number of tokens than what is optimal.

To obtain an estimation of the exact burden of exchanging cash, one needs to conduct surveys in which buyers (or sellers) describe the exact denominations that they actually exchange in both directions for each payment they record. Such surveys, particularly those with a sufficiently-large number of observations, are extremely expensive to conduct. However, the distribution of burdens that we compute in this article are still very useful because they provide reliable lower bounds which can form the basis for estimating the true burden of exchanging cash. Nevertheless, we are also interested in computing upper bounds on the these burdens during cash transactions.

4.3 Quantifying the burden of exchanging cash with restricted choice

If the assumption that payers and merchants have access to all denominations does not hold, then they will have to exchange a sub-optimal number of tokens. Thus, in order to provide an upper bound on the exchange burden of cash we impose additional structure on the model. Figure 1 displays significant payment discontinuities at \$20 and other multiples of \$5. With this information in hand, we re-solve the model requiring payers to use \$20 notes, while allowing merchants access to all denominations. This brings the model closer to reality by assuming a payer does not have access to all denominations at the point-of-sale. It also provides an upper bound scenario since it reflects an exchange wherein the payer prefers to use cash yet has none on hand and is therefore restricted to paying with the denomination dispensed by the nearest ATM.

¹⁰Amromin and Chakravorti (2009) classify denominations commonly dispensed by ATMs as ones that are in between large and small denominations. Recent work by Shy (2020) identified a correlation between ATM currency denominations and payment choice.

The resulting distribution of exchange burdens from this simulation is presented in the right panel of Figure 3. In general, we find that restricting payers' choice set shifts the average exchange burden from 3.14 to 4.96 tokens. This 57.8 percent increase in the average exchange burden also includes a 58 percent reduction in the number of cash transactions that require the use of only two tokens (a reduction from 22.5 percent to 9.5 percent). To put these changes into perspective, prior to restricting payers, we found that the share of transactions resulting in $b^* \leq 2$ was approximately 45 percent. However, after restricting payers, the share for these transactions dropped to approximately 15 percent. Finally, the single largest increase in this distribution is observed for the exchange burden of $b^* = 4$ exchanged tokens. The share of this exchange burden increases by 57 percent (from 13 percent to 20.5 percent).

5. Policy counterfactual: Elimination of the penny

An important policy question in the U.S. is whether to cease production and circulation of the penny. As discussed in the introduction, the proposal to eliminate the penny was first submitted to Congress in 1989 and has been resubmitted several times with the last motion occurring in 2017. The debate has received renewed attention due to the COVID-19 coin shortage. Additionally, our data show that approximately two-thirds of U.S. consumers store coins at their homes or vehicles. In light of this, we use the model constructed in Section 4 to simulate how the distribution of the burden of exchanging cash would evolve if the penny were eliminated.

We consider a counterfactual economy wherein the penny has been removed from circulation and all cash transaction amounts are rounded.¹² We consider the counterfactual economy under two rounding policies. The first policy, which we label "symmetric", assumes that merchants round their prices evenly to the nearest 5¢. For example, a trans-

¹¹https://www.nytimes.com/2020/07/29/business/coin-shortage-penny.html

¹²This exercise may seem similar to the restriction of payers' tokens on hand. However, the fact that merchants round their prices in response to the penny being eliminated is what differentiates this from restricting payer choice sets.

action of amount \$1.07 would round to \$1.05, while one valued at \$1.08 would round to \$1.10. This is the same rounding rule used in Canada during their penny elimination, see footnote 4, and also in Belgium, Finland, Ireland, Italy and Netherlands, see EC (2020). However, it might be the case that, without government direction, merchants will reset all prices and round up. Thus, the second policy, labeled "asymmetric", is a rounding rule where merchants round all prices up to the nearest \$0.05. For example, a transaction valued at \$10.01 would round up to \$10.05 rather than down to \$10.00.

Under this counterfactual economy we repeat the exercise of computing the optimal burden of cash exchange for each of the 16,906 cash transactions in the data while assuming that all payment amounts a are rounded according to the symmetric or asymmetric rounding rules. The theoretical implications for the optimal burden of cash exchanges are displayed in the middle panel of Figure 2. This figure shows that the maximum burden for cash payment amounts in the [\$4.01, \$5] interval would decline to 4 tokens in the penniless economy compared with 6 in the current economy. Moreover, the middle panel in Figure 2 shows that there is less variation in the burden over this interval after the penny is removed and prices are rounded.

5.1 Penniless economy with unrestricted choice

We now present the results from eliminating the penny in the economy. Recall that we are quantifying both the lower and upper bound of the burden of cash exchange resulting from penny elimination. We first consider the lower bound of this burden. The lower bound (symmetric) case is represented by the economy wherein both payer and merchant can transact with all tokens (except for \$2 notes). The resulting b_c^* distributions of the burden of cash exchange are displayed in left panels of Figure 4. The top panel reflects the changes when merchants are instructed to round prices symmetrically. The bottom panel shows the changes when merchants are able to round all prices up (asymmetric rounding). Recall that 96.6 percent of all cash payments do not exceed \$100. For these payments, we find that the density for all $b_c^* \geq 7$ drops to about 0.3 percent when pen-

nies are removed and prices are rounded, where subscript "c" stands for counterfactual. Therefore, the new maximum burden b_c^* with density greater than 1 percent would be 6 tokens.

First, we consider the lower bound case under symmetric price rounding (upper-left panel in Figure 4). The share of all cash transactions requiring 3 and 4 tokens each increases by 30 percent, from 18.5 to 24 percent and from 13 to 17 percent, respectively. Importantly, the cumulative share for bins with $b_c^* \leq 4$ increases by 17.2 percent while the share for bins with $b_c^* \geq 5$ decreases by 55 percent. The average burden of cash exchange decreases from 3.14 to 2.729 tokens per transaction, see Table 2. In other words, there is a 13 percent decrease in the average burden per cash transaction.

Next, we analyze the case where merchants engage in asymmetric price rounding (lower-left panel in Figure 4). Under this counterfactual economy, the average burden would decline to 2.727 tokens per cash transaction, see Table 2. Indeed, we find that the differences in the burden under asymmetric price rounding, relative to symmetric, are small. Consider the share of transactions requiring at least 3 tokens. In the symmetric pricing counterfactual this share would be 24 percent, however, in the asymmetric case it is 23.7 percent. Furthermore, looking at the share of all $b_c^* \leq 4$, the asymmetric counterfactual has a share of 89.21 percent while the symmetric counterfactual has a share of 89.18 percent. Thus, we find that merchants rounding prices up has little impact on the lower bound of the burden of cash exchange in a penniless economy when consumers have access to all tokens.

5.2 Penniless economy with restricted consumer choice

We now quantify changes to the upper bound (asymmetric case) of the exchange burden of cash in a penniless economy. This is the economy wherein payers can only transact with \$20 notes while merchants have access to all coins and notes. The results from these counterfactual simulation are displayed in the right panels of Figure 4.

We first look at this counterfactual economy when there is symmetric price rounding

(upper-right panel in Figure 4). Under this counterfactual, the average burden declines by approximately 8 percent (from 4.96 to 4.55), see Table 2. Additionally, the share of cash transactions requiring 4 tokens increases from 20.5 to 25.5 percent. This is in contrast to those requiring $b^* \geq 7$, which declines from 18.1 to 6.5 percent. Interestingly, the share of transactions resulting in $b^* \in \{1, 2\}$ is relatively unchanged when the penny is eliminated.

Finally, looking at the counterfactual under asymmetric price rounding (lower-right panel in Figure 4), we find that the average exchange burden declines from 4.96 to 4.54 tokens per transaction, see Table 2. This 8.4 percent decrease is qualitatively similar to the 8.3 decline under symmetric price rounding. Indeed, much like the results from Section 5.1, we find that the form of price rounding makes little difference in the counterfactual burden of cash exchange.

6. Aggregate price effects of penny elimination

If the penny were eliminated from the U.S. economy then the form of price rounding engaged in by merchants could have inflationary effects. Thus, the potential price effects of penny elimination policies are of interest to policymakers. Therefore, we analyze the price effects of penny elimination. We do so by first estimating the share of transactions in which merchants would have to round prices.

6.1 Symmetric price rounding

First, we look at the price effects under symmetric price rounding. We analyze the effect of penny elimination on the prices by subtracting the counterfactual empirical distribution (after prices are rounded without the penny) from the observed empirical distribution (with the penny). We define a new variable $\Delta^a = a_c - a$ for each observed transaction where a_c is the transaction amount after rounding. Note that, because of the rounding policy, the variable Δ^a is restricted to the set {-\$0.02, -\$0.01, \$0, \$0.01, \$0.02}. That is, since each transaction is rounded to the nearest \$0.05, prices cannot change by more than \$0.02. The effects of price rounding are detailed in Table 3 (Panel A).

We find that, under the symmetric rounding rule, 73 percent of transactions would experience no price change. It is important to note, however, that the lack of price changes may reflect pre-existing price rounding conducted by merchants and respondents. Moreover, the fraction of price decreases (13 percent) and increases (15 percent) approximately offset each other. Nonetheless, given the symmetry of the rounded prices, our findings suggest that, with symmetric price rounding, penny elimination would not have any significant inflationary consequences. These results are consistent with earlier findings by Chande and Fisher (2003) in Canada and Whaples (2007) in the U.S.

6.2 Asymmetric price rounding

We now consider what the price effects would be if, following the penny elimination, all merchants rounded their prices up. This is important because there could be inflationary consequences associated with the penny removal if merchants only rounded prices up. We thus repeat the exercise conducted in Section 6.1 under asymmetric price rounding. Note that, because of the rounding policy, the variable Δ^a for this exercise is restricted to the set $\{\$0,\$0.01,\$0.02,\$0.03,\$0.04\}$. It is important to note that the price increases are bounded above by 4& due to our assumptions on rounding. The effects of price rounding are detailed in Table 3 (Panel A).

We find that, under the asymmetric rounding rule, 73 percent of transactions would experience no price change. However, unlike the symmetric policy, the percentage of price increases is now 27 percent of transactions.

7. Robustness: Elimination of the 1c and the 5c coins from circulation

The results from our main counterfactual have suggested that penny elimination is welfare improving because it lowers the average burden of exchanging cash. If eliminating a token reduces the average burden, then our results suggest that eliminating the nickel, dime, or quarter would also be welfare improving. However, such eliminations present a trade-off because they may be inflationary, especially if merchants only round prices up.

Thus, to explore the potential effects of additional currency system changes, we consider another counterfactual economy wherein both pennies and nickels have been eliminated. In other words, we remove the 0.01 and 0.05 tokens from $\delta^{\text{U.S.}}$ and re-solve the model. The theoretical implications for the optimal burden of cash exchanges are displayed in the bottom panel of Figure 2. It shows that there is less variation in the burden after the penny and the nickel are removed and prices are rounded accordingly.

We conduct the exact same counterfactual exercises as in Sections 5 and 6. The effects on the burden of cash exchange are presented in Figure 5. Furthermore, we examine the implications for aggregate price inflation; results from this exercise are presented in Table 3 (Panel B). We begin our exposition of findings by focusing on the economy where consumers and merchants can use any combination of tokens (unrestricted case). We then proceed to discussing the results when consumers are restricted to using only \$20 notes (restricted case).

In the unrestricted case, we find that, similar to the main counterfactual simulation, removing the penny and nickel simultaneously yields a lower average burden of cash exchange. Specifically, the removal of both tokens results in a 12.1 percent decline in the average burden from 3.14 to 2.76 tokens when prices are rounded symmetrically, see Table 2. When prices are rounded asymmetrically we find that the burden declines by 11.9 percent from 3.14 to 2.77 tokens.

In the restricted case when consumers are restricted to only using \$20 notes and prices are rounded symmetrically, the average burden declines 7.7 percent from 4.96 to 4.576 tokens, see Table 2. If prices were rounded asymmetrically, then the average burden of cash exchange would decline to 4.582 tokens (-7.6 percent change).

Although the removal of both the penny and the nickel reduce average burden, relative to our main counterfactual (elimination of only the penny), eliminating the penny *and* nickel would be sub-optimal since the average burden is higher across all scenarios. For example, as shown in Table 2, the average burden when both the penny and nickel were eliminated and prices are rounded up is 4.582 tokens under the restricted case which is

higher than 4.576 tokens if only the penny were eliminated.

Similar higher burdens occur across all of counterfactual economies because some transactions obtained their minimal burden by combining the nickel with another token. For example, consider a transaction amount of \$10.30. With only penny elimination, this transaction would simply require a \$10 note plus 5¢ and 25¢ coins (3 tokens). However, adding nickel elimination to this transaction would require a \$10 note plus three 10¢ tokens (4 tokens). More generally, transactions which were multiples of 25¢ would require more tokens ex-post. A transaction amount of \$10.25, prior to the nickel elimination, would require 2 tokens (\$10 note and 25¢ coin). However, after nickel elimination, the transaction amount would round up to \$10.30 and require 4 tokens, a 100 percent increase in the burden.

If both the penny and nickel were eliminated, then price inflation would be a greater concern relative to penny elimination alone. This is because, under the new counterfactual, prices would be rounded to the nearest 10e. The implications of this rounding scheme are observed immediately from Table 3 by the share of transactions experiencing no change in price. In our main counterfactual (only penny elimination) this share is 72.69 percent. However, when prices are rounded to the nearest 10e, the share drops to 65.4 percent. We find that this rounding scheme also yields a substantially larger share of price increases when prices are rounded asymmetrically. Specifically, under this rounding scheme, the share of transaction amounts increasing by at least 3ϕ under the elimination of both the penny and the nickel is 3.57 + 3.39 + 7.29 + 2.94 + 8.69 = 25.88 percent, which is higher than 6.81 + 5.90 = 12.31 percent if only the penny were eliminated. It should be noted that under this scenario, the maximum a transaction amount could be rounded would be 9e. Thus, eliminating both the penny and nickel would result in greater price inflation relative to penny elimination alone. However, the aggregate price effects would not be particularly large in either counterfactual economy. The upper bound on price inflation we estimate would be less than 0.07 percent over both main and secondary counterfactual economies.

8. Conclusion

This article quantifies the burden of exchanging cash. We specify a model of optimizing consumers and merchants and then apply it to an empirical distribution of cash payments from transaction survey diary data spanning 2015 to 2019. We then construct the distribution of exchange burden for cash payments observed in the current economy. Furthermore, we use the model to conduct a counterfactual policy simulation wherein the penny is eliminated from the economy. It is also extended to analyze an additional currency system policy, simultaneous penny and nickel elimination.

The baseline results show that, on average, the exchange burden per cash transaction is 3.14 coins and notes, see Table 2. This estimate increases to 4.96 when we assume that consumers can only pay with \$20 notes. The counterfactual simulations suggest that eliminating the penny and rounding prices symmetrically would result in a decrease in the exchange burden of cash. Importantly, this finding is robust to the form of price rounding conducted by merchants. For the baseline model, the average cash exchange burden would decrease from 3.14 to 2.73 coins and notes while it would decline from 4.96 to approximately to 4.55 coins and notes in the model restricting consumer choice sets.

Importantly, we find that eliminating both the penny and nickel would be sub-optimal relative to the main counterfactual (only penny elimination). As shown in Table 2, under such a policy, with symmetric price rounding, the average cash exchange burden given unrestricted (restricted) payers would be 2.76 (4.58) tokens with both penny and nickel eliminated which is slightly higher than 2.73 (4.55) tokens with only the penny eliminated. Moreover, transactions which are multiples of 25ϕ would experience significant increases in the average cash exchange burden if both the penny and nickel were eliminated.

The paper briefly analyzes the aggregate price effects stemming from penny elimination. We find that more than two-thirds of cash transactions will result in no price change. Furthermore, the positive and negative price changes offset each other almost perfectly across all merchant types under symmetric price rounding. If merchants only round prices up to the nearest \$0.05, then we find that the remaining one-third of transactions

would experience evenly distributed price changes in the 1¢ to 5¢ interval. These results suggest that, regardless of the rounding policy, penny elimination would not have any significant inflationary consequences. These results are robust under penny and nickel elimination as well.

Should the 1¢ coin be removed from circulation in the U.S.? First, it should be emphasized that a removal of the penny need not apply to electronic transactions because there is no cost of maintaining the two decimal points in electronic payments. Note that even now, most gas stations in the U.S. continue post gas prices that are fractions of a cent (for example $\$3.87\frac{9}{10}$ per gallon).

The paper focuses only on the demand side for physical cash in the form of notes and coins. However, looking at the supply side, United States Mint (2020) reports that in 2020 the unit production costs were: 1.76c for a penny (1c), 7.42c for a nickel (5c), 3.73c for a dime (10c), and 8.62c for a quarter (25c). In addition, unit costs for both pennies and nickels remained above their face value for fifteen consecutive years. The actual cost is likely to be much higher because the consumers themselves often remove pennies from circulation. The 2020 DCPC finds that only 20.8 percent of consumers keep pennies in their pocket, purse, or wallet. Others store pennies at home (54.9 percent), vehicle (14.1 percent) or leave it at the store (10.2 percent).

On the demand side, a removal of the penny coin would reduce the burden of dealing with small change. Our finding about the small price effects of symmetric and asymmetric rounding will continue to become even less significant in the future because, at the time of writing this paper (2022), inflation rates are rising in many parts of the world. Thus, the rising cost of labor associated with the production of pennies and the rapid decline in the purchasing power of pennies will eventually lead to the removal of the 1¢ coin from circulation. The remaining question is "when?"

¹³EC (2020) reports that the 1- and 2-euro cent coins are not circulating efficiently among economic operators because they are mostly hoarded or get lost. In addition, although retailers (including supermarkets) give them as change to customers, customers do not recirculate the coins (hence, 'one way' use).

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Appendix A A comparison to uniformly distributed cash payments

Figure 1 displays the empirical distribution of cash payment transaction amounts among U.S. consumers from 2015 to 2019. A key feature of this distribution are the jumps observed at multiples of \$5. As mentioned in Section 2, some of the prior work has assumed a uniform distribution of cash payment transaction amounts when analyzing optimal denomination structures. However, reliance on the uniform distribution, by definition, eliminates the potential for the jumps observed in the empirical distribution. Thus, a natural question is how important these jumps are for our calculations of the burden of exchanging cash and the effects of penny elimination.

This appendix analyzes the importance of the empirical distribution relative to a uniform distribution. More specifically, we solve the model described in Section 4, however, we replace the empirical distribution with 20,000 draws from a uniform distribution with minimum value \$0.02 and maximum value of \bar{a} . We consider four values for $\bar{a} \in \{\$9.73, \$24.93, \$60, \$100\}$. The first two values are chosen because, as shown in Table 1, they are they median and mean cash transaction amounts, respectively. The \$60 value is chosen because this is the final major jump in our empirical distribution until \$100 and the latter value for comparability with the analysis provided in Section 4. We then examine the sensitivity of our penny elimination results in Section 5 by replicating the counterfactual simulations using the uniform distribution of cash transaction values.

The results from the baseline model solutions are provided by Table 4. We find that, assuming a uniform distribution with $\bar{a}=\$9.73$, the average burden is 4.64 tokens. If we additionally assume that payers are restricted to only using \$20 notes, then the average burden increases to 6.40 tokens. In our remaining simulations, since we assume a uniform distribution, the average burdens increases with the upper bound. Hence, when the upper bound value is \$100, the average burden is 5.75 tokens if payers are unrestricted and 7.94 tokens if payers are restricted.

The results from counterfactual simulations solved using a uniform distribution are provided by Table 5. For the sake of simplicity, we only consider two of the upper bounds

for the simulations. Namely, we simulate the the counterfactual economy with an upper bound value of $\overline{a} \in \{24.93, 100\}$. We find that if $\overline{a} = 24.93$ and consumers are unrestricted, then the average burden declines by approximately 24 percent (3.8440/5.04-1). Similarly, if $\overline{a} = 100$, then the average burden declines by 21 percent (4.546/5.75-1). These findings are in contrast to the counterfactual simulations under the empirical distribution. Those results, provided by Table 2, find that the average burden under unrestricted consumer choice declines by 13 percent. Moreover, as seen in Table 4, we find similar results when consumer choice is restricted to \$20 notes. These findings are consistent with the notion that jumps in the empirical distribution are critical. The jumps, particularly those at \$5, \$10, and \$20, being currency denomination values, require significantly fewer tokens to transact. Additionally, they are not impacted by coin elimination of any type. Hence, removing density from these transaction values mechanically increases the average burden and overestimates the gains from coin elimination.

These results provide evidence that the empirical distribution is superior to the uniform distribution when estimating the burden of exchanging cash. If the researcher wants the uniform distribution estimates to match the estimates provided by the empirical distribution, they would be required to make strong assumptions on the upper bound of cash payment transaction amounts. When using the empirical distribution the researcher is not required to make any such assumption. However, we do acknowledge that the empirical distribution does sacrifice the analytic tractability which the uniform distribution affords. Nevertheless, we view the empirical distribution as necessary for estimating reliable bounds on the burden of exchanging cash.

Appendix B A comparison with Boeschoten and Fase (1989)

Boeschoten and Fase (1989) estimate the burden of cash transactions using data on payments in the Netherlands during 1984–1986. Their study uses a similar method for estimating the burden of cash exchange, which is computed as the most efficient way that would minimize the number of exchanged tokens (the sum of notes and coins) for each

payment value. However, unlike Boeschoten and Fase (1989) who perform some additional simulations with changing the range of note denominations, our study focuses on counterfactual scenarios of removing the lowest denomination coins from circulation.

In general it is hard to compare the two studies for the following reasons: (i) As we show below, the two studies use different currency denomination structures, and (ii) rely on different empirical distributions of cash payments. (iii) The studies rely on different populations; for example, the Dutch survey included age 12 and older whereas the diary survey included adults only (18 years and older). This is in addition to the fact that people in different countries may purchase different consumption bundles due to cultural differences and also due to changes in consumer expenditures that took place from the 1980s to 2019. (iv) Since 1986, there has been a sharp decline in the fraction of payments made with cash. Boeschoten and Fase (1989) report that 80 percent of the payments were made in cash in the Netherlands and 36 percent in the United States. In the United States, this fraction dropped to 26 percent in 2019, see Kim, Kumar, and O'Brien (2020).

Table 6 displays the Dutch guilder denominations used in Boeschoten and Fase (1989) and their USD value in 2019. Using the March 1986 exchange rate of 2.565 guilders for one USD, some guilder denominations turn out to be similar to today's USD denominations. For example, in 2019, one 1986 guilder was equal to 0.91 USD and 10 guilders to 9.12 USD. However, these denomination comparisons are sensitive to the fluctuating exchange rate that went down from 3.755 guilders for one USD in March 1985 and from 2.936 guilders per one USD in March 1984 to 2.565 guilders for one USD in 1986.

Despite the similarities between the 1986 Dutch guilder and the 2019 USD denominations, Table 6 shows that the guilder did not have the equivalent of today's 1¢ and 50¢ U.S. coins and that the U.S. does not have an equivalent of the 2.5 guilder coin and the 250 and the 1000 guilder notes. However, even with these denominational differences, the estimated average burdens are quite similar: 3.3 tokens in Boeschoten and Fase (1989) versus 3.14 in the unrestricted case in our study.

Table 1: Summary statistics of cash transactions sample from 2015 to 2019

-	Mean/Fraction	Std. Dev.	Median	Min	Max
Numeric demographic variables					
Age	53.69	14.26	55	18	101
Household size	2.56	1.30	2	1	11
Discrete demographic variables					
$\frac{1}{\text{Income}} < \$25k$	0.19	0.39	_	_	_
Income $\in [\$25k, \$50k)$	0.24	0.43	_	_	_
Income $\in [\$50k, \$75k]$	0.19	0.40	_	_	_
Income $\in [\$75k, \$100k)$	0.14	0.35	_	_	_
Income $\geq $100k$	0.23	0.42	_	_	_
Education: Less than high school	0.03	0.17	_	_	_
Education: High school diploma	0.41	0.49	_	_	_
Education: Associate's degree	0.15	0.36	_	_	_
Education: Bachelor's degree	0.23	0.42	_	_	_
Education: Graduate degree	0.17	0.38	_	_	_
Birth decade: Before 1950s	0.17	0.37	_	_	_
Birth decade: 1950s	0.27	0.44	_	_	_
Birth decade: 1960s	0.23	0.42	_	_	_
Birth decade: 1970s	0.18	0.38	_	_	_
Birth decade: 1980s	0.11	0.32	_	_	_
Birth decade: After 1980s	0.04	0.19	_	_	_
Ethnicity: Latinx	0.06	0.24	_	_	_
Race: Asian	0.02	0.14	_	_	_
Race: Black	0.09	0.28	_	_	_
Race: Other	0.04	0.18	_	_	_
Race: White	0.86	0.34	_	_	_
Unbanked	0.06	0.24	_	_	_
Employed	0.60	0.49	_	_	_
Male	0.89	0.71	_	_	_
Married	0.59	0.49	_	_	_
<u>Transaction variables</u>					
Amount (a)	\$24.93	\$91.42	\$9.73	\$0.02	\$6420.00
Merchant: Hospital, doctor or dentist	0.01	0.09	_	_	_
Merchant: Nonprofit, charity or religion	0.04	0.19	_	_	_
Merchant: Government	0.02	0.14	_	_	_
Merchant: Retail store	0.72	0.45	_	_	_
Merchant: A person	0.09	0.29	_	_	_
Merchant: Business that primarily sells services	0.11	0.31	_	_	_
Merchant: Education provider	0.01	0.09	_	_	_
Merchant: Financial services provider	0.01	0.07	_	_	_

Number of consumers = 3,452 Number of transactions = 16,906

Notes: The discrete demographic variables report the fraction of cash transactions conducted by each demographic group. The discrete merchant variables report the fraction of all cash transactions occurring at that merchant type. The median value is not calculated for discrete variables.

Source: Diary of Consumer Payment Choice, 2015 to 2019.

Table 2: Average burden of exchanging cash

Coin elimination type	Unrestricted	Restricted (\$20 only)		
	Symmetric rounding			
No elimination	3.14	4.96		
Penny elimination	2.729	4.55		
Penny and nickel elimination	2.76	4.576		
	Asymmetric rounding			
No elimination	3.14	4.96		
Penny elimination	2.727	4.54		
Penny and nickel elimination	2.77	4.582		

Notes: There is no rounding before the eliminations. Symmetric rounding refers to when prices are rounded positively and negatively symmetrically. Asymmetric rounding refers to prices being rounded positively only to the next nearest coin multiple in circulation. Unrestricted refers to payees who possess the optimal combination of notes and coins for each transaction. Restricted refers to payments made by payees who have only \$20 bills.

Source: Diary of Consumer Payment Choice, 2015 to 2019; authors' calculations.

Table 3: Percentage share of price changes stemming from currency elimination

Panel A: Penny elimination												
Δ^a	-4¢	-3¢	-2ϕ	-1¢	0¢	1¢	2¢	3¢	4¢	5¢	6¢ ≥	7¢
Symmetric rounding	_	_	6.81	5.90	72.69	7.55	7.04	_	_	_		
Asymmetric rounding	_	_	_	_	72.69	7.55	7.04	6.81	5.90	-		_
Panel B: Penny and nickel elimination												
Δ^a	-4ϕ	-3ϕ	-2ϕ	-1ϕ	0¢	1ϕ	2ϕ	3ϕ	4ϕ	5¢	6¢	≥ 7 ¢
Symmetric rounding	2.94	2.94	3.24	2.51	65.40	4.61	4.11	3.57	3.39	7.29	_	
Asymmetric rounding	_	_	_	_	65.40	4.61	4.11	3.57	3.39	7.29	2.94	8.69

Notes: Symmetric rounding refers to when prices are rounded positively and negatively symmetrically. Asymmetric rounding refers to prices being rounded positively only to the next nearest coin multiple in circulation. For example, under penny elimination with asymmetric rounding, the price \$5.01 would round to \$5.05.

Source: Authors' calculations from the Diary of Consumer Payment Choice, 2015 to 2019.

Table 4: Average burden of cash exchange under a uniform distribution

Distribution	Unrestricted	Restricted (\$20 only)
Uniform(\$0.02, \$9.73)	4.64	6.40
Uniform(\$0.02, \$24.93)	5.04	6.24
Uniform(\$0.02, \$60)	5.52	6.97
Uniform(\$0.02, \$100)	5.75	7.94
Empirical	3.14	4.96

Notes: Unrestricted refers to payees who possess the optimal combination of notes and coins for each transaction. Restricted refers to payments made by payees who have only \$20 bills. The thresholds for the uniform were chosen as follows: \$9.73 is the median cash transaction value in the empirical distribution while \$24.93 is the mean value. The value \$60 is chosen because it is the last major jump in the empirical distribution prior to \$100 while the latter was chosen for optimal comparability with the analysis in Section 4.

Source: Diary of Consumer Payment Choice, 2015 to 2019; authors' calculations.

Table 5: Counterfactual average burden of exchanging cash under uniform distribution

	$\overline{a} = \$2$	4.93	\overline{a} = \$100				
Coin elimination type	Unrestricted	Restricted	Unrestricted	Restricted			
	Symmetric rounding						
No elimination	5.04	6.24	5.75	7.94			
Penny elimination	3.8440	5.037	4.546	6.737			
	Asymmetric rounding						
No elimination	5.04	6.24	5.75	7.94			
Penny elimination	3.8439	5.038	4.545	6.735			

Notes: There is no rounding before the eliminations. Symmetric rounding refers to when prices are rounded positively and negatively symmetrically. Asymmetric rounding refers to prices being rounded positively only to the next nearest coin multiple in circulation. Unrestricted refers to payees who possess the optimal combination of notes and coins for each transaction. Restricted refers to payments made by payees who have only \$20 bills.

Source: Diary of Consumer Payment Choice, 2015 to 2019; authors' calculations.

Table 6: Dutch guilder denominations in 1986

Guilder coin denomination	0.05	0.10	0.25	1.00	2.50		
Guilder coin in 1986 USD	0.02	0.04	0.10	0.39	0.97		
Guilder coin in 2019 USD	0.05	0.09	0.23	0.91	2.28		
Guilder note denomination	5.00	10.00	25.00	50.00	100.00	250.00	1000.00
Guilder note in 1986 USD	1.95	3.90	9.75	19.49	38.99	97.47	389.86
Guilder note in 2019 USD	4.56	9.12	22.81	45.61	91.23	228.07	912.28

Note: Dutch guilder denominations correspond to Table 7 in Boeschoten and Fase (1989). Calculations are based on a March 1986 exchange rate of 2.565 Dutch guilder for 1 USD which was worthing \$2.34 in March 2019.

Source: "Treasury Reporting Rates of Exchange 1986" downloaded from www.govinfo.gov. CPI inflation calculator posted on www.bls.gov.

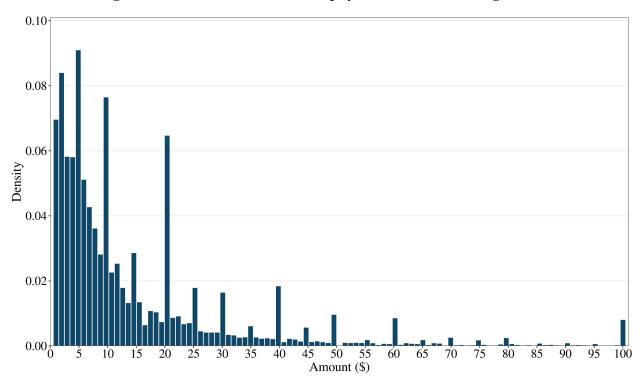
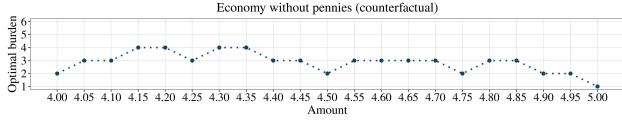


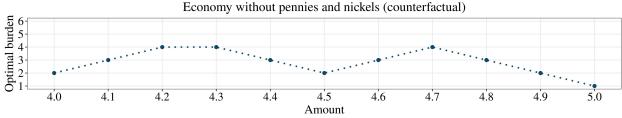
Figure 1: Distribution of all cash payments not exceeding \$100.

Notes: The distribution is constructed using the 16,342 cash payments not exceeding \$100 (96.6 percent of all cash payments). The histogram bins are evenly spaced along \$1 intervals. *Source*: Authors' calculations from the 2015 to 2019 Diary of Consumer Payment Choice.

Economy with pennies (current) Optimal burden 4.00 4.05 4.10 4.15 4.20 4.25 4.30 4.35 4.40 4.45 4.50 4.55 4.60 4.65 4.70 4.75 4.80 4.85 4.90 4.95 5.00

Figure 2: The burden for a cash payment valued between \$4 and \$5.





Notes: *Top*: Optimal burden by cash payment amount before the penny is eliminated. *Middle*: Optimal burden after the penny has been eliminated. Bottom: Optimal burden after the penny and the nickel have been eliminated. All computations are based on the assumption that \$2 bills are not used for payment purposes.

Source: Authors' calculations.

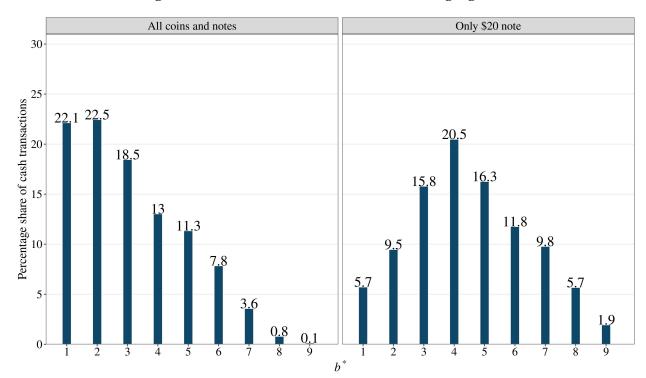
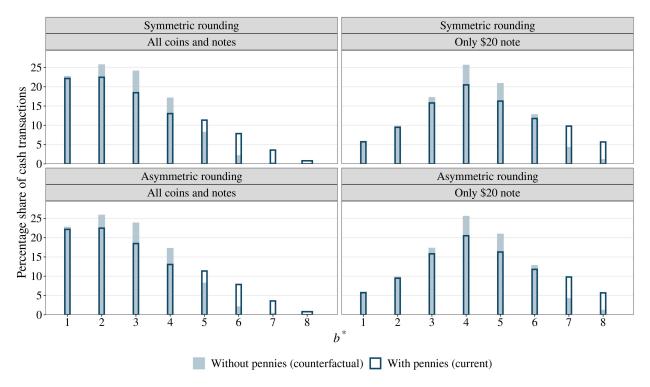


Figure 3: Distribution of burdens of exchanging cash

Note: Both panels of Figure 3 are derived from all the 16,906 cash payments in the data. However, we do not present histogram values beyond burden of 9 because they are too small. *Left*: Distribution of optimal burdens of cash payments for 16,906 cash payments assuming that consumers possess all denominations (except for \$2 bills). *Right*: Distribution of optimal burdens of cash payments assuming that consumers pay with \$20 currency notes. *Source*: Authors' calculations from the 2015 to 2019 Diary of Consumer Payment Choice.

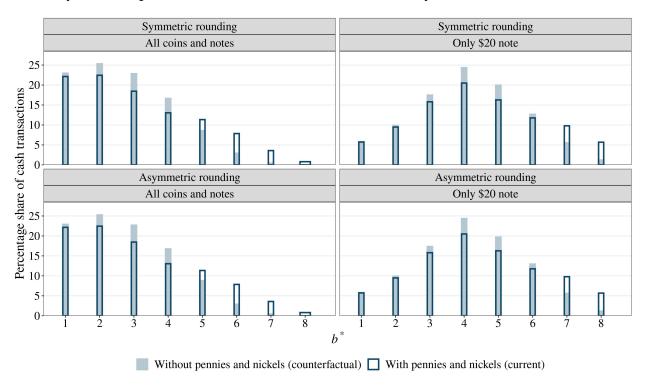
Figure 4: A comparison of distribution of burden of cash exchange in the counterfactual penniless economy to current economy with pennies.



Note: Results are derived from all the 16,906 cash payments in the data. However, we do not present histogram values beyond burden of 9 because they are too small. The percentage shares are calculated using the volume of transactions, not value. *Left*: Distribution of optimal burdens of cash exchange using all denominations. *Right*: Distribution of optimal burdens of cash exchange assuming that consumers pay with \$20 currency notes. All panels display burden of the counterfactual economy (without the penny) in solid blue bins and for the current economy (with pennies included) in unfilled bins.

Source: Authors' calculations from the 2015 to 2019 Diary of Consumer Payment Choice.

Figure 5: A comparison of distribution of burden of cash exchange in the counterfactual economy without pennies or nickels to the current economy.



Note: Results are derived from all the 16,906 cash payments in the data. However, we do not present histogram values beyond burden of 9 because they are too small. The percentage shares are calculated using the volume of transactions, not value. *Left*: Distribution of optimal burdens of cash exchange using all denominations. *Right*: Distribution of optimal burdens of cash exchange assuming that consumers pay with \$20 currency notes. All panels display burden of the counterfactual economy (without the penny and nickel) in solid blue bins and for the current economy (with pennies and nickels included) in unfilled bins.

Source: Authors' calculations from the 2015 to 2019 Diary of Consumer Payment Choice.