1 multiplication

All from nine and the last from ten

Theorem 1.1 Suppose a,b are positive integers. We will compute ab. Let 10^n be the power of 10 closed to a and b. Let $\bar{a}=a-10^n$ and $\bar{b}=b-10^n$ Then we can multiply

$$\begin{array}{c|cccc} & number & complement \\ & a & \bar{a} \\ & \times & b & \bar{b} \\ \hline & 10^{2n} + \bar{a} + b & \bar{a}b \\ \end{array}$$

Proof.

$$ab = (10^n + \bar{a})(10^n + \bar{b}) = 10^{2n} + 10^n(\bar{a} + \bar{b}) + \bar{a}\bar{b}$$

Example 1.2 (9×7)

$$\begin{array}{c|cc} number & complement \\ 9 & -1 \\ \times & 7 & -3 \\ \hline & 6 & 3 \\ \end{array}$$