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Exercise 4: Task 6
1)
       F(4,v) = \mathcal{F}\{f(x,y)\}
        F{f(x,y) ej2T(uox/M+voy/N)} =
         \sum_{x=0}^{M+1} \sum_{y=0}^{N-1} f(x,y) e^{j2\pi(u_0x/M + u_0y/N)} e^{-j2\pi(u_x/M + u_0y/N)} =
        \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f(x,y) e^{-j2\pi [(u-u_0)x/M + (v-v_0)y/N]} =
      [F(u-u, v-vo)]
         F = { F(u,v) e-j2 T(xou/M + you/N) } =
         \frac{1}{MN} \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} F(u,v) e^{-j2\pi(x_0u/M + y_0v/N)} e^{j2\pi(ux/M + vy/N)} =
         \frac{1}{MN} \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} F(u,v) e^{j2\pi [(x-x_0)u/M + (y-y_0)v/N]} =
      f (x-x0, y-y0)
2)
         x = rcos \theta
                                 u = \omega \cos \phi
            y = r \sin \theta
                                      V = \omega \sin \phi
       -> define rotated coordinates (x', y') in terms
            of x, y, and \hat{\theta}_o
            D'= Dr O.
            x = r \cos(\theta' - \theta_0)
            x = r cos O'cos Oo + r sin O' sin Oo
            x = x' \cos \theta_0 + y' \sin \theta_0
            y = r sin (0'-00)
            y = r \sin \theta' \cos \theta_0 - r \cos \theta' \sin \theta_0

y = y' \cos \theta_0 - x' \sin \theta_0
       -> find the 2D DFT of f(x', y')
            F { f(x, y')} =
            \sum_{x'}\sum_{y'}^{1}f(x',y')e^{-j2\pi(\frac{ux}{M}+\frac{vn}{N})}=
           \sum_{y'} \int_{y'}^{y'} f(x', y') e^{-i2\pi \left[\frac{M}{M}(x'\cos\theta_0 + y'\sin\theta_0) + \frac{M}{M}(y'\cos\theta_0 - x'\sin\theta_0)\right]} =
           \sum_{x'} \sum_{y'} f(x',y') e^{-j2\pi \left[\frac{x'}{m} \left(u\cos\theta_{o} - v\sin\theta_{o}\right) + \frac{y'}{N} \left(v\cos\theta_{o} + u\sin\theta_{o}\right)\right]}
       -> Recognize rotated coordinates (u', v')
                   u' = u \cos \theta_0 - v \sin \theta_0 = r \cos (\phi + \theta_0)
                  V' = V \cos \theta_0 + u \sin \theta_0 = r \sin (\phi + \theta_0)
         \sum_{x'} \sum_{y'} f(x', y') e^{-j^2 \pi} \left( \frac{x'u'}{m} + \frac{y'v'}{n'} \right) =
        \int F(u',v'), s.T. (u',v') are the coordinates \int (u,v) rotated by \Theta_0
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