

# Joint eye-movement and EEG analysis using Hidden semi-Markov Models to identify and characterize reading strategies

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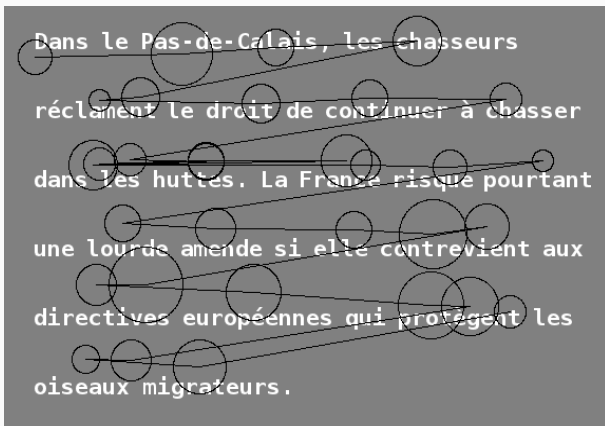
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*Laboratories :* Mistis, Inria / Laboratoire Jean Kuntzmann & Vibs, Gipsa-lab

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# Definitions



**Fixation** (circles): immobilization of visual gaze during few ms.

**Saccade** (lines): brief movement of the eye between two fixation.

**Scanpath**: series of fixations and saccades recorded during a given task.

# Previous studies on reading processes

- Eye-movement contains information in the reading processes
- Precursors analyzed **microprocesses of reading**. e.g. longer fixations with misspelled words / less common words, (Rayner, 1998, Hyrskykari et al. 2000, 2003)
- We focus on reading as a whole mechanism (scanpath) in the context of **information search** tasks involving both **semantic information gathering** and **decision making processes**, (Frey et al. 2013).
- Reading strategies are used as **gears** for different purposes, (Carver, 1990)

# State of the art on data-driven studies and problematic

- Reading strategies discovery in information search task using **Hidden Markov Models** (Simola et al., 2008)
- How to segment scanpaths into interpretable zones, in terms of cognitive phases in information acquisition and processing ?
- Hypothesis: reading strategies changes reflect cognitive steps, expressed indirectly through eye movements regime changes (and Markovian regime changes)

## Issues:

- HMM have non-fitted sojourn distributions for strategies
- Legitimacy of the term "cognitive processes" using eye-movement data only

# Material and Method - Goal and experimental settings

Simulate press review task through binary decision:

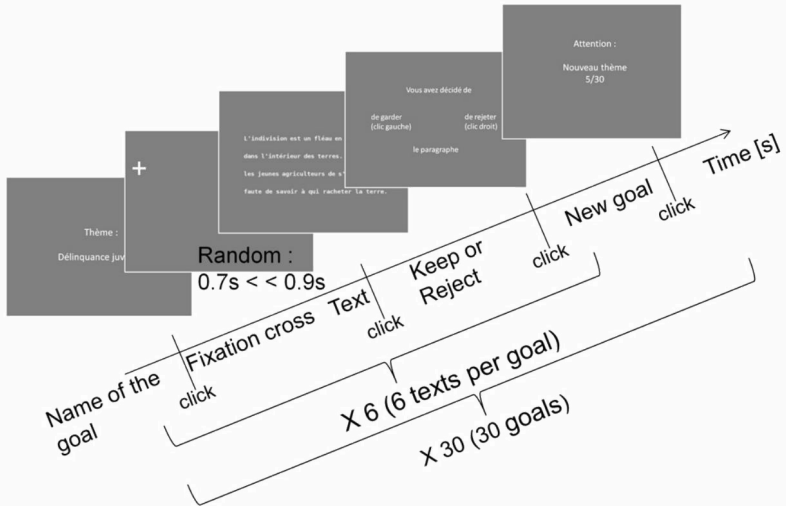
*Is the text related to the topic or not ?*

- positive decision: target words
- negative decision: incongruent words

## Experimental settings

- 15 participants
- 180 texts per participants (Extracted from the french newspaper LeMonde)
- Goal is a nominal phrase. e.g. "modern art"
- 60 Highly / 60 Moderately / 60 Un - related texts to the topic (Latent Semantic Analysis control)

# Material and Method - Experimental Procedure



Frey et al. 2013

Hidden (semi-)Markov Models

Analysis protocol on eye-movements using EEG as covariates

Joint modeling of eye-movements and EEGs

Conclusion & Perspectives

## Quick reminder of a HMM - Model

Let  $\{S_1, \dots, S_T\}$ , a sample of  $T$  R.V. corresponding to a discrete Markov Chain and taking values into a finite state space  $\mathcal{S}$ , with  $\text{Card}(\mathcal{S})=M$ .

Let  $\pi_j \equiv P(S_1 = j)$ , the probability that the first state is  $j$ .  $\pi = \{\pi_j\}$  is a  $1 \times M$  vector denoting **initial distribution**.

Using *Markov property*, let  $a_{ij} \equiv P(S_t = j | S_{t-1} = i)$ , the probabilities to transit from state  $i$  to  $j$  at time  $t$ .  $A = \{a_{ij}\}$  is a  $M \times M$  **transition matrix**.

Consider an output  $\{O_1, \dots, O_T\}$ ,  $\forall t, O_t \in \mathcal{V}$  with  $\text{Card}(\mathcal{V}) = K$ , the observation space.  $O_t$  depends conditionally on  $S_t$ , so we have  $b_j(v_k) \equiv P(O_t = v_k | S_t = j)$ , the **Observation conditional probabilities**.



# Quick reminder of HMM - Inference and Learning

## Inference

**Forward-Backward** algorithm to maintain tractability in inference problems (e.g. probabilities such as  $P(o_1, \dots, o_T | \theta)$ )

## Learning

MLE of  $\hat{\theta}$  via the iterative **Expectation-Maximization** algorithm:

E-step: decomposition of  $E[\ln P(S_{1:T}, O_{1:T} | \theta) | O_{1:T}, \theta^{old}]$  and simplification

M-step: maximize with respect to  $\theta$

## Restoration

Estimation of the most likely state sequence using the **Viterbi** algorithm:

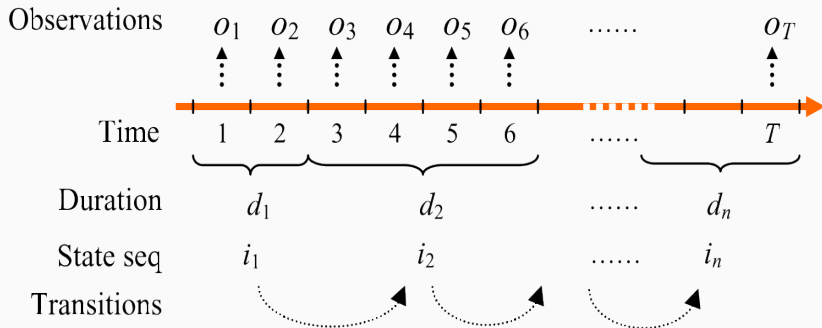
$$\hat{S}_{1:T} = \arg \max_{S_{1:T}} P(S_{1:T} | O_{1:T}, \hat{\theta})$$

## Quick reminder of HMM - Limitations

- State sojourn time are by definition Geometric
- Let  $X \sim G(p)$ ,  $\mathbb{E}[X] = 1/p$ ,  $\mathbb{V}[X] = \frac{1-p}{p^2}$ . Expectation and Variance linked by one single parameter  $p$ .

# Definition of a HSMM

Yu, 2010



State duration  $D \in \mathcal{D} = \{1, \dots, \infty\}$

Sojourn distribution:  $p_j(d) \equiv P(D = d, S_{t+1:t+d} = j, S_{t+d+1} \neq j | S_t = j)$

Model parameters:  $\theta \equiv \{a_{ij}, b_j(v_k), \pi_j, \theta_j\}$

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# Output process construction

## Observed Process: "Readmode"

Categorical variable with 5 levels from long progression to long regression, i.e.  
number of identified words in one saccade  $\in \{> 1, 1, 0, -1, < -1\}$

Time index: fixation onset

## Latent Process

Reading strategies "hidden", observed through the readmode

Number of reading strategies unknown and to be determined

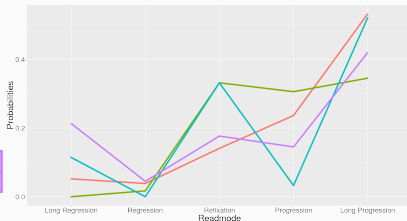
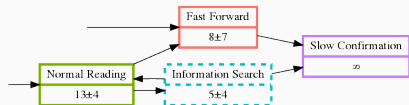
## Strong hypothesis

Scanpaths are independant and identically distributed

## Model covariates

Fixation duration, Saccade amplitude, Textual properties, EEGs

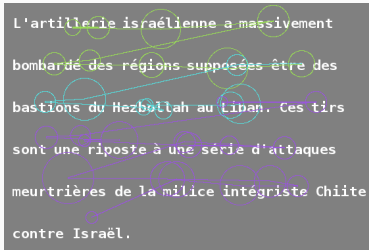
# Estimated model parameters



Each reading strategy is characterized by: a **readmode pattern**, a **sojourn distribution**, **probabilities to transit** to other reading strategies and an **initial probability**

# Scanpath Segmentation (restoration of state sequences)

*"Israeli-Palestinian conflict"*  
(Highly Related)

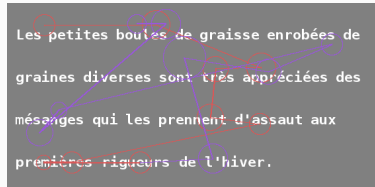


L'artillerie israélienne a massivement bombardé des régions supposées être des bastions du Hezbollah au Liban. Ces tirs sont une riposte à une série d'attaques meurtrières de la milice intégriste Chiite contre Israël.

The image shows a scanpath visualization on a French text snippet. The text is: "L'artillerie israélienne a massivement bombardé des régions supposées être des bastions du Hezbollah au Liban. Ces tirs sont une riposte à une série d'attaques meurtrières de la milice intégriste Chiite contre Israël." The scanpath consists of numerous small circles (fixations) and lines (saccades) connecting them. The path starts at the top left and moves generally downwards and to the right, with several loops and revisits, indicating a complex reading pattern. The circles are colored in shades of green and yellow.

*"Israeli artillery massively bombed areas believed to be Hezbollah strongholds in Lebanon. These shootings are a response to a series of deadly attacks by the fundamentalist Shiite militia of Israel."*

*"Birds hunt" (Moderately Related)*

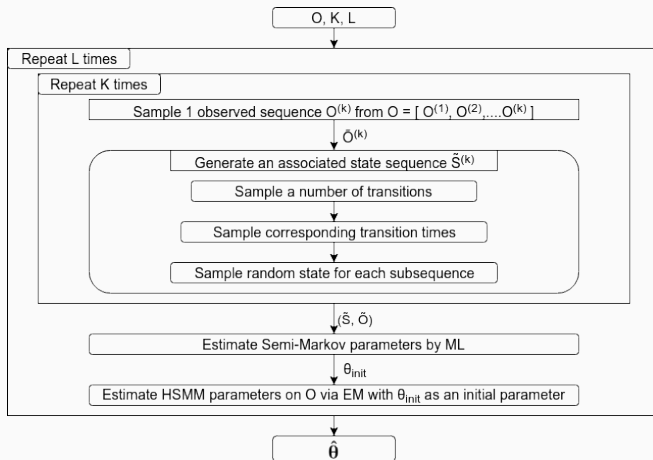


Les petites boules de graisse enrobées de graines diverses sont très appréciées des mésanges qui les prennent d'assaut aux premières rigueurs de l'hiver.

The image shows a scanpath visualization on a French text snippet. The text is: "Les petites boules de graisse enrobées de graines diverses sont très appréciées des mésanges qui les prennent d'assaut aux premières rigueurs de l'hiver." The scanpath consists of numerous small circles (fixations) and lines (saccades) connecting them. The path starts at the top left and moves generally downwards and to the right, with several loops and revisits, indicating a complex reading pattern. The circles are colored in shades of red and purple.

*"Small balls of fat coated with various seeds are much appreciated by the tits that storm them at the first severe winter."*

# Model selection - RandomInit



Algorithm: Random initializations for H(S)MM



## Model selection - Choosing number of Classes

#Classes	LL	BIC	Entropy	ICL*	#Params
3	-50835	-101873	11326	-124525	20
4	-50726	-101814	<b>9753</b>	<b>-121321</b>	26
5	-50645	-101651	11886	-125423	34
6	<b>-50593</b>	<b>-101556</b>	14748	-131054	35

\* Integrated Complete Likelihood is equivalent to BIC with an additional penalty term: the conditional entropy of the hidden variable (Biernacki et al., 2000, Volant et al., 2012)

# Model validation - Several indicators

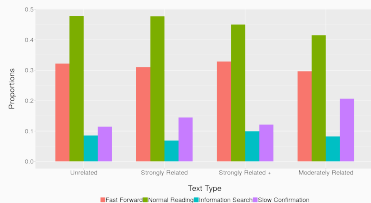
		Normal reading	Fast Forward	Information Search	Slow Confirmation
Fixation duration (ms)		183 ± 68	170 ± 60	190 ± 70	188 ± 68
Saccade amplitude (px)		121 ± 103	150 ± 94	136 ± 103	144 ± 98
Reading speed (wpm)		382	600	436	227
Cumulated cosine*		.33 ± .28	.33 ± .30	.51 ± .23	.47 ± .26
Saccade direction	Backward	.09	.09	.18	.19
	Upward	.01	.02	.04	.10
	Downward	.14	.22	.19	.19
	Forward	.71	.61	.51	.44
	Last	.05	.05	.07	.08

\* Measure of cumulated gathered semantic information

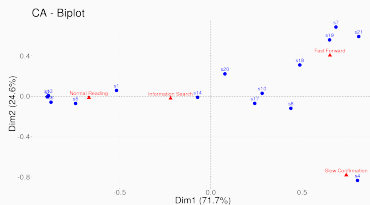
*Speed reading* suggests to be an easy task and therefore shorter fixations - Rayner (1998), Simola et al. (2008)

# Model validation - Understanding the usage

## Strategies usage wrt text types



## Factorial Correspondence Analysis: Strategies and Subjects

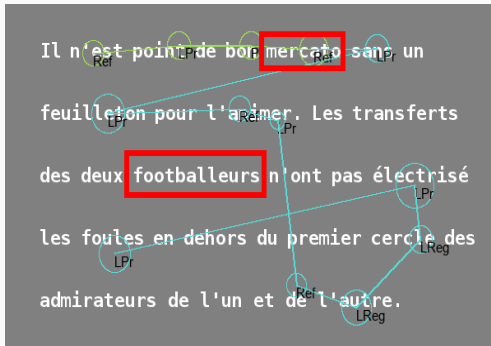


In practise:

- strategies are used differently according to the text type,
- not all strategies are used for every trial or by every subject.

# Model validation - Text - Meta Word Representations

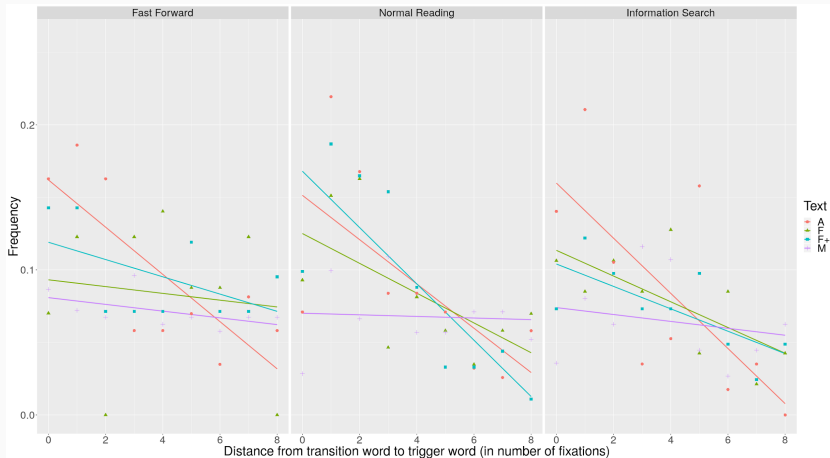
"Russia's chief" - Unrelated



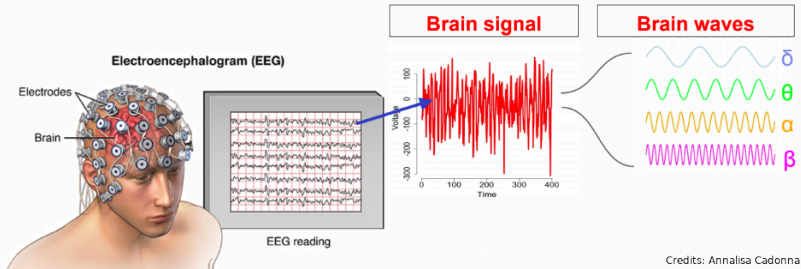
*"There is no good mercato without a soap opera to animate it. The transfers of the two footballers did not electrify the crowds outside the first circle of admirers of the one and the other."*

- Automatic detection of trigger words w.r.t. text names
- We used Facebook's fastText word representations and combined them into a single framework with adjusted cosine similarity measure

# Model validation - Text - distance of target words to transitions

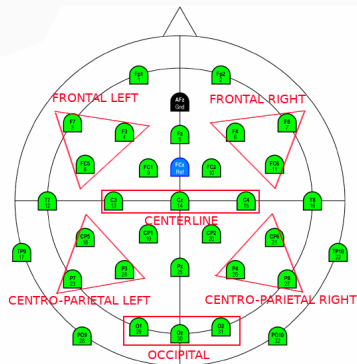
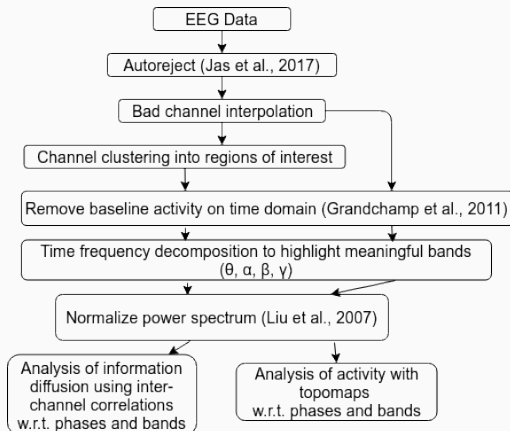


# Model validation - EEGs - Bands, activities, tasks

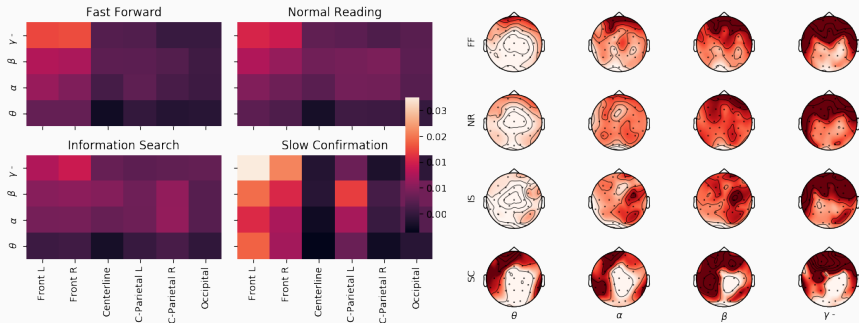


- $\alpha$  and  $\theta$  oscillations reflect memory performances (Klimesch, 1998),
- "Memory is an extremely distributed system with long term memory located primarily in posterior cortices and accessed from prefrontal regions" (Klimesch et al., 2005, 2006, 2011)
- Memory encoding and restitution differences observed in  $\alpha$  band (Seidkhani et al., 2017)

# Model validation - EEGs - Analysis Methodology

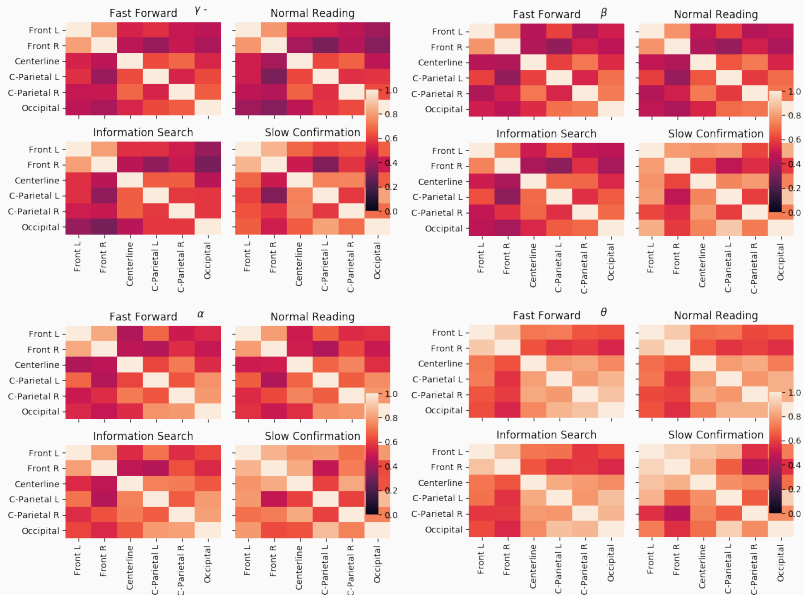


# Model validation - EEGs - Activity





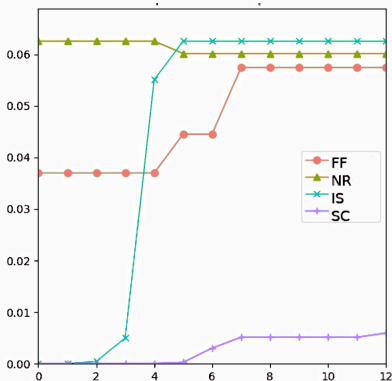
# Model validation - EEGs - Information Diffusion



# Issues - Uncertainty of state sequence restoration

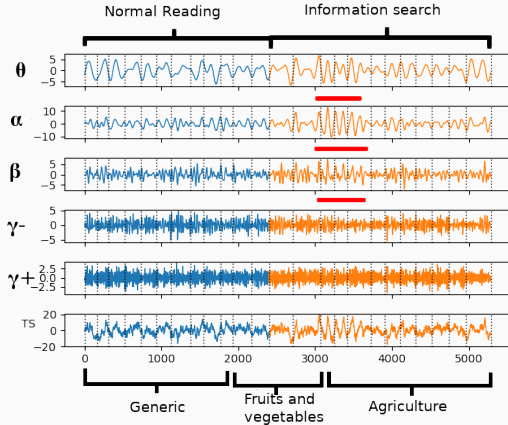
- State Entropy computation (Durand et al. 2012) has shown a high amount of uncertainty.
- Computation of Posterior probabilities of state sequence:

$$s_t^{(k)} = \max_{s_{1:t-1}, s_{t+1:T}} P(s_{1:t-1} = s_{1:t-1}, s_t = k, s_{t+1:T} = s_{t+1:T} | O_{1:T})$$



# Issues - delay in EEGs

"Economic growth" - Unrelated text



- Visible delay between ocular and brain activities
- "Eye movements provide information to the brain which guides the eyes in return.", (Frey et al. 2013)

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Conclusion & Perspectives

# Modeling specifications

## Different sampling rates

- $t \in \{1, \dots, \tau\}$  now denotes a temporal index in ms.
- Let  $N_t$ , the number of fixations from 1 to  $t$ .

## Delayed State

- Let  $\{S_1^{(2)}, \dots, S_T^{(2)}\}$  a discrete latent state taking values in  $\mathcal{S}$  and encoding the first SMC  $\{S_1, \dots, S_{N_T}\}$  at a higher sampling rate, plus a lag.
- We denote the lag  $\{\epsilon_{N_1}, \dots, \epsilon_{N_T}\}$ , with  $\epsilon_{N_t} \in \{1, \dots, \mathcal{L}\}$  in its most general form.
- Hence we have:  $S_{t+\epsilon_{N_t}}^{(2)} = S_{N_t}$
- $\epsilon_{N_t}$  could be deterministic, random, autoregressive, conditional to channels or states.

# Modeling EEG output process

Output process related to EEGs models wavelet coefficients

## Single output process

- $O_t^{(2)}$  is a concatenation of all wavelet coefficients and all channels at time  $t$ .
- $P(O_t^{(2)} | S_t^{(2)} = j) = \mathcal{N}(O, \Sigma_j)$
- Invariant regarding time since it is already encapsulated in  $S_t^{(2)}$
- Sparse covariance matrix

Modeling quite complex and inference algorithm in  $O(T\mathcal{L}M^2D)$  vs  $O(TM^2)$  for HMM...

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Conclusion & Perspectives

- We provided a full statistical analysis methodology for analyzing complex signals,
- we dug deeper in the understanding of reading mechanisms in press review-like tasks,
- we proposed to assemble asynchronous and heterogeneous signals in a single probabilistic model.



- Writing... Paper on the first part and PhD thesis...
- Get first results on simulations for the proposed model to ensure identifiability
- Scaling: new model highly complex + high usage of RAM to store MODWT coefficients of EEGs. Online or preferably minibatch version.

# References I

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-  Yann Guédon, *Estimating Hidden Semi-Markov Chains From Discrete Sequences*, *Journal of Computational and Graphical Statistics* **12** (2003), no. 3, 604–639.
-  Jaana Simola, Jarkko Salojärvi, and Ilpo Kojo, *Using hidden Markov model to uncover processing states from eye movements in information search tasks*, *Cognitive Systems Research* **9** (2008), no. 4, 237–251.
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