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PLOT for 3

gauss.m code:

```
function A = gauss(A)

s = size(A);

s = s(1);

U = A;

L = eye(s);

for i = 1:s-1
```

```
10<sup>-14</sup>
10<sup>-15</sup>
10<sup>-16</sup>
10<sup>-17</sup>
10<sup>-18</sup>
10<sup>-20</sup>
10<sup>-21</sup>
-2 -1.5 -1 -0.5 0 0.5 1 1.5 2
×10<sup>-5</sup>
```

```
gauss_p.m code:
function [A I] = gauss_p(A)
  s = size(A);
  s = s(1);
```

U = A;

A1 = A;

scal = max(abs(U),[],2); %make scale

%index array

I = 1:1:s;

check = abs(A1(:,i))./scal;

[~,piv] = max(check()); %index to swap

ind = find(I == piv);

l([ind i]) = l([i ind]); %swap

for j = i+1:s %%%%%%%row reduce%%%%%%%%

ni = I(i);

nj = l(j); %% use l as hash table

a = -U(nj,i);

b = U(ni,i);

$$fact = a/b;$$

$$U(nj,:) = fact*U(ni,:) + U(nj,:);$$

```
L(nj,i) = -fact;
      end
    end
  end
  P = zeros(s);
  cnt = 1;
  for i = I
    P(cnt,i) = 1;
    cnt = cnt + 1;
  end
  %%L = P+L;
  %%L = P*L;
  %%U = P*U;
  A = L + U;
end
backward code:
function x = backward(A,b,I)
  s = size(A);
  s = s(1);
  for k = 1:s-1
    for i = k+1:s
      ni = l(i);
      nk = I(k);
      b(ni) = b(ni) - A(ni,k)*b(nk);
    end
  end
```

```
ns = I(s);
  x(s) = b(ns)/A(ns,s);
  for i = s-1:-1:1
    ni = I(i);
    sum = b(ni);
    for j = i+1:s
      sum = sum - A(ni,j)*x(j);
    end
    x(i) = sum/A(ni,i);
  end
end
main.m code:
function main()
  fprintf('n\t\tAb\t\t\tno piv\t\t\tno piv\t\t\cond(A)\n');
  for s = 2:20
    H = hilb(s);
    b = sum(H,2);
    x = ones(s,1);
    A = gauss(H);
    I = 1:1:s;
    [Ap lp] = gauss_p(H);
    xn = backward(A,b,I)';
    xp = backward(Ap,b,lp)';
```

```
Ab = norm(H \setminus b - x)/norm(x);
    err = norm(xn - x)/norm(x);
    errp = norm(xp - x)/norm(x);
    con = cond(H);
    fprintf('%d\t%e\t%e\t%e\n', s,Ab,err,errp,con);
  end
end
main2.m code:
function main2()
 fprintf('n\t\tAb\t\t\t piv\t\t\t\t);
 fprintf('-----\n');
 for s = 1:5
   A = rand(500);
    b = sum(A,2);
   x = ones(500,1);
   A = gauss(A);
   I = 1:1:500;
    [Ap lp] = gauss_p(A);
   xn = backward(A,b,I)';
    xp = backward(Ap,b,lp)';
    Ab = norm(A \setminus b - x)/norm(x);
```

```
err = norm(xn - x)/norm(x);
errp = norm(xp - x)/norm(x);
con = cond(A);

fprintf('%d\t%e\t%e\t%e\t%e\n', 500,Ab,err,errp,con);
end
```

end