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# Week 5:

## Tradeoffs Step of PrOACT

**Instructor:** Brielle K Thompson

**Course:** NAT\_R 8001 Decision Analysis for Research and  
Management of Natural Resources

# Review of last week

- Discussed the Alternatives and Consequences step of SDM

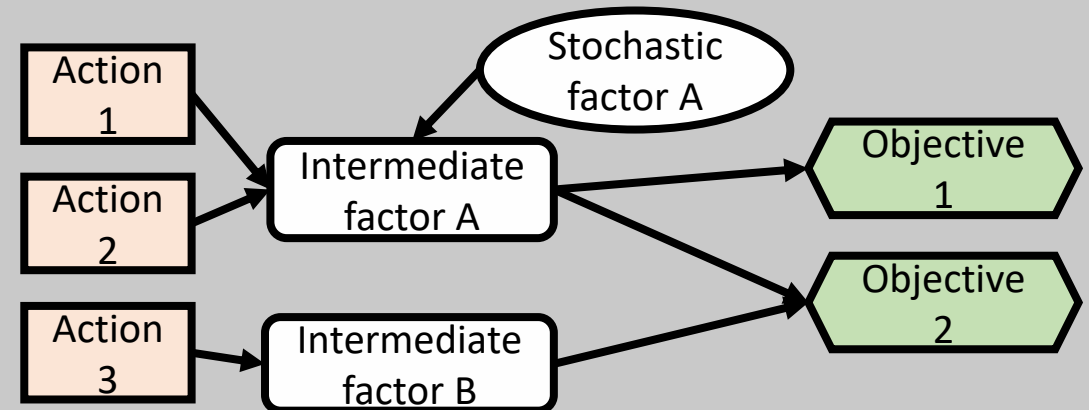
## Identifying Alternatives:

1. Focus on fundamental objectives & address conflicting objectives
2. Challenge constraints
3. Create groups of alternatives (portfolios/strategies)
4. Revisit objectives

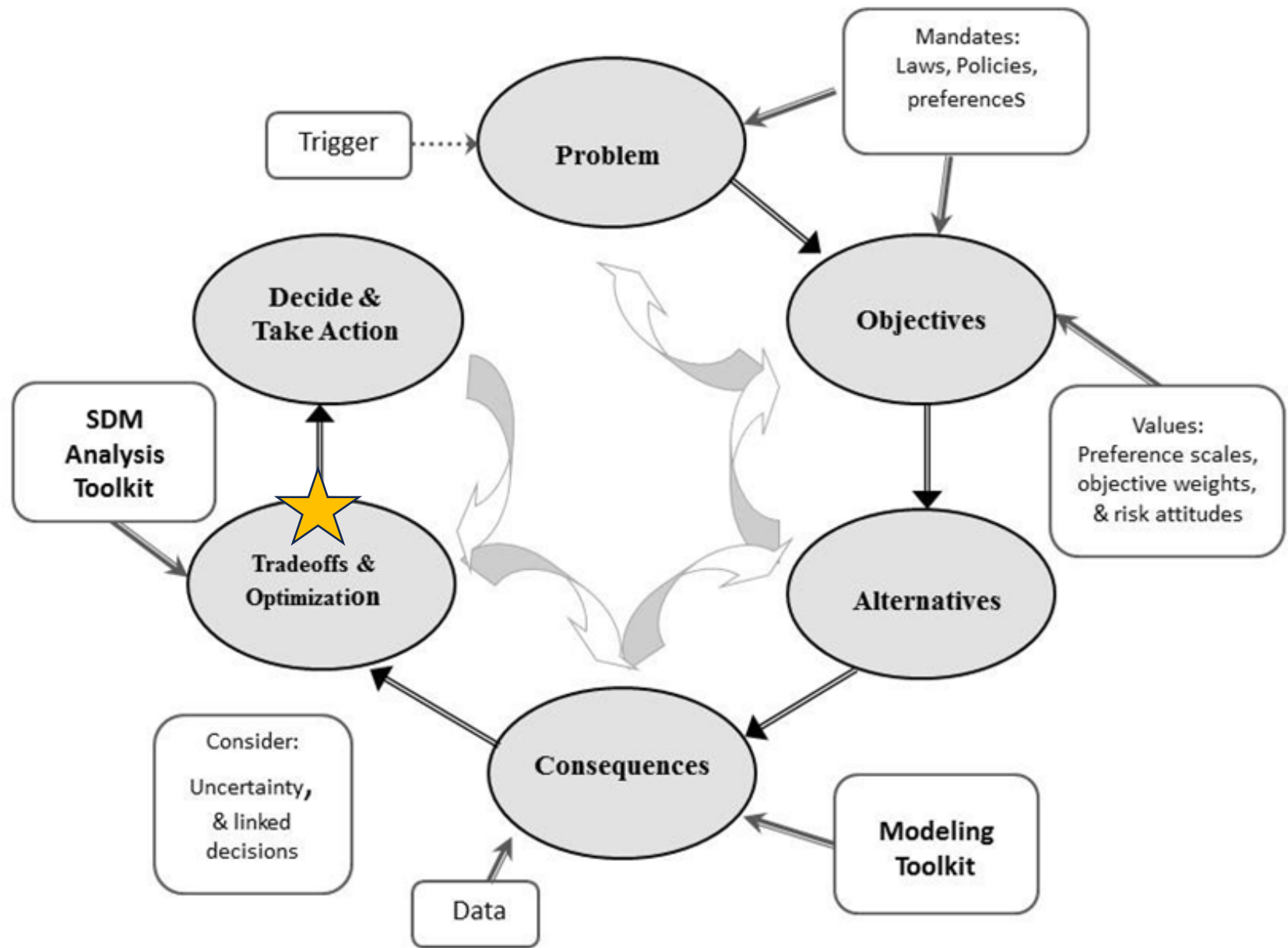


## Tips for evaluating consequences:

- Build an influence diagram to help create models
- Identify model type (population model, economic model, expert elicitation, etc.)
- Organize outcomes in a consequence table



Today:  
Learn about  
the Tradeoffs  
step



Source: Jean Fitts Cochrane



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# Tradeoffs

“How much you would give up on one objective in order to achieve gains on another objective”

- Gregory et al. 2012

# Role of analytical methods in tradeoff analysis

- Identify “best” (optimal) solution
  - Ties together alternatives, objectives, and predicted consequences
  - How do you integrate all the components?
- Easiest with a single objective
- Easiest without uncertainty
- Solution method depends on the structure of the problem

# Analytical approaches

	Approach
<b>Single Objective</b>	<ul style="list-style-type: none"><li>• Deterministic optimization</li></ul>
<b>Multiple Objectives</b>	<ul style="list-style-type: none"><li>• Multiple Attribute Utility</li><li>• Simplification</li><li>• SMART</li><li>• Pareto frontier analysis</li></ul>
	Negotiate among most efficient alternatives

↓  
Increased  
complexity



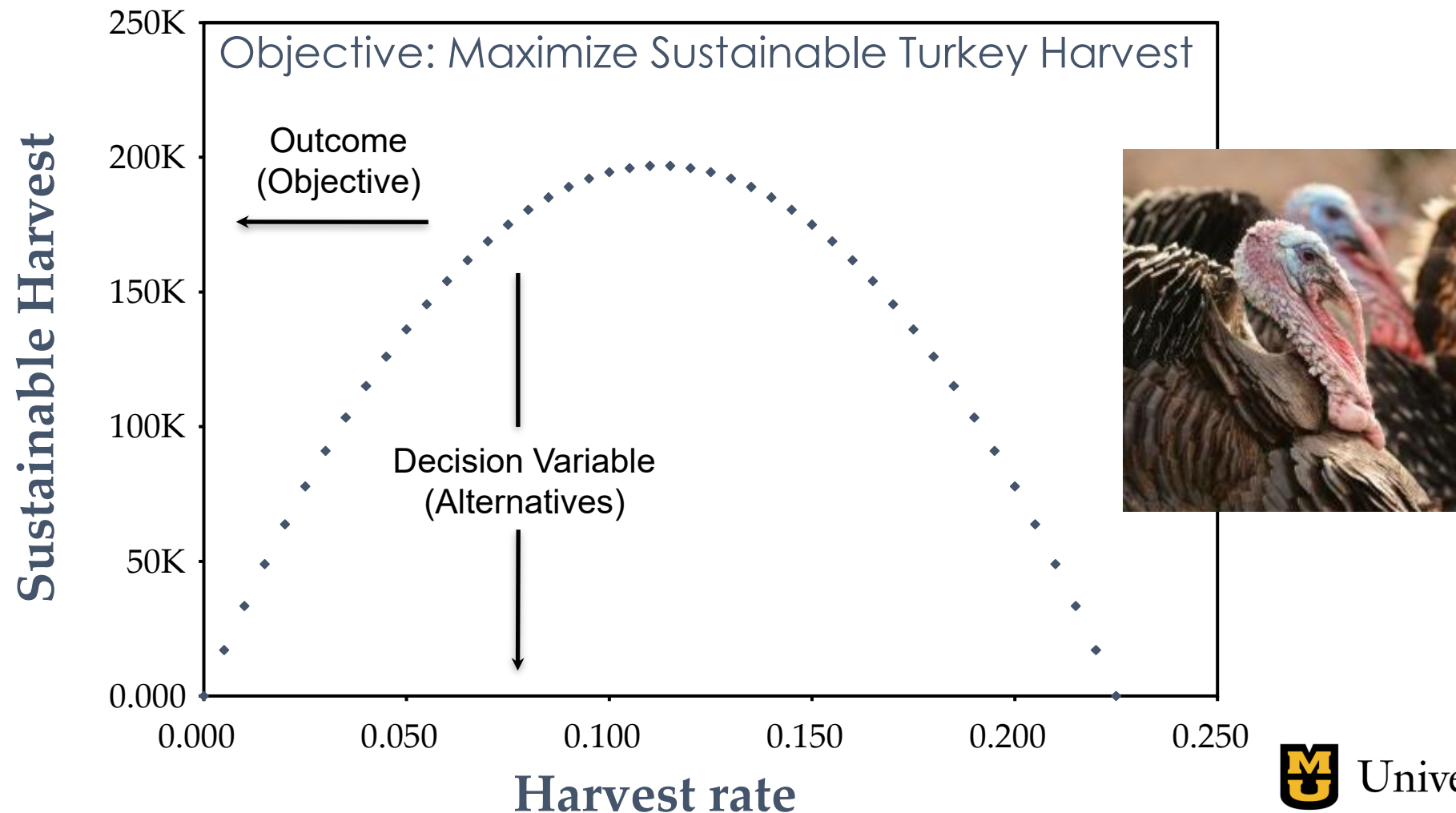
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# Single objective approach:

- Used when we have a single continuous decision variable (i.e., alternatives)
  - e.g., harvest rate, amount of herbicide to apply, size of biocontrol release, etc.
- Predict outcomes (i.e., objective) are a function of the decision variable
- Optimization solution methods:
  - Graphical
  - Closed-formed solutions (calculus/differentiation)
  - Numerical solutions (mathematical search methods)
  - Constrained optimization (mathematical solution)

# Single objective approach:

- Graphical optimization:





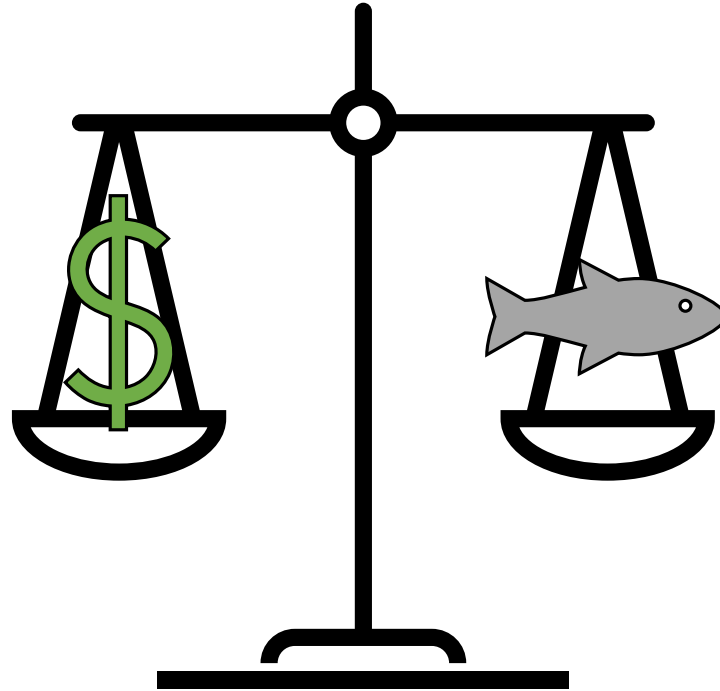
# Single objective approach:

Question: Can you think of an example of a single objective problem?

- Not very common in natural resource management.
- Single objectives are easier to optimize, so we may want to reduce multiple objective problems to make them easier to solve.

# Multiple objective tools

- Nearly all natural resource management problems are multiple-objective problems



# Multiple objective tools

A. Simplify the problem as much as possible

1. Remove dominated alternatives
2. Remove irrelevant objectives
3. Make even swaps

B. Reduce to a single objective if possible

C. Negotiate a solution from a set of best compromises

D. Evaluate trade-offs explicitly

# A. Simplify the problem

## **1. Remove dominated alternatives:**

- i.e., another alternative performs the same or better on all objectives

# A. Simplify the problem (EXAMPLE)

**1. Remove dominated alternatives** (another alternative performs the same or better on all objectives)

Objectives	Direction	Alternatives			
		Status quo	Minor repair	Major repair	Re-build
Cost (\$M)	Min				
Environmental Benefit (0-10)	Max				
Disturbance (0-10)	Min				
Silt runoff (k ft <sup>3</sup> )	Min				
Water Retention (MG)	Max				

# A. Simplify the problem (EXAMPLE)

**1. Remove dominated alternatives** (another alternative performs the same or better on all objectives)

Objectives	Direction	Alternatives			
		Status quo	Minor repair	Major repair	Re-build
Cost (\$M)	Min	0	2	12	20
Environmental Benefit (0-10)	Max	1	3	10	10
Disturbance (0-10)	Min	0	1	7	10
Silt runoff (k ft <sup>3</sup> )	Min	5	1	3	3
Water Retention (MG)	Max	41	41	41	39

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**1. Remove dominated alternatives** (another alternative performs the same or better on all objectives)

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# A. Simplify the problem

## 1. Remove dominated alternatives:

- i.e., another alternative performs the same or better on all objectives

## 2. Remove irrelevant objectives:

- i.e., performance measures of that objective does not vary over alternatives
- This isn't to say the objective isn't important to you, just that it doesn't help discern among the alternatives currently considered.



# A. Simplify the problem (EXAMPLE)

## 2. Remove irrelevant objective

Objectives	Direction	Alternatives			
		Status quo	Minor repair	Major repair	Re-build
Cost (\$M)	Min	0	2	12	20
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Dominated Alternative

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Dominated Alternative

Irrelevant Objective

# A. Simplify the problem (EXAMPLE)

- **Simplified problem:**

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		Status quo	Minor repair	Major repair
Cost (\$M)	Min	0	2	12
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Silt runoff (k ft <sup>3</sup> )	Min	5	1	3



# A. Simplify the problem

## 1. Remove dominated alternatives:

- i.e., another alternative performs the same or better on all objectives

## 2. Remove irrelevant objectives:

- i.e., performance measures of that objective does not vary over alternatives
- This isn't to say the objective isn't important to you, just that it doesn't help discern among the alternatives currently considered.

## 3. Make even swaps:

- If two objectives are in the same unit, then combine outcomes

# A. Simplify the problem (EXAMPLE)

## 3. Even swaps

Convert silt runoff to cost @ \$0.5M / k ft<sup>3</sup>

Objectives	Direction	Alternatives		
		Status quo	Minor repair	Major repair
Cost (\$M)	Min	0	2	12
Environmental Benefit (0-10)	Max	1	3	10
Disturbance (0-10)	Min	0	1	7
Silt runoff (k ft <sup>3</sup> )	Min	5	1	3



# A. Simplify the problem (EXAMPLE)

## 3. Even swaps

Convert silt runoff to cost @ \$0.5M / k ft<sup>3</sup>

Objectives	Direction	Alternatives		
		Status quo	Minor repair	Major repair
Cost (\$M)	Min	0	2	12
Environmental Benefit (0-10)	Max	1	3	10
Disturbance (0-10)	Min	0	1	7
Silt runoff (k ft <sup>3</sup> )	Min	<del>5</del> 2.5 M	<del>4</del> 0.5 M	<del>3</del> 1.5 M



# A. Simplify the problem (EXAMPLE)

## 3. Even swaps

Convert silt runoff to cost @ \$0.5M / k ft<sup>3</sup>

Objectives	Direction	Alternatives		
		Status quo	Minor repair	Major repair
Cost (\$M)	Min	0 + 2.5	2 + 0.5	12 + 1.5
Environmental Benefit (0-10)	Max	1	3	10
Disturbance (0-10)	Min	0	1	7
Silt runoff (k ft <sup>3</sup> )				



## B. Reduce to a single objective

- Tip: Convert all objectives but one to constraints
  - Example: don't spend more than \$2.5M
  - Keep disturbance at or below 3
  - Then take the maximum environmental benefit

Objectives	Direction	Alternatives		
		Status quo	Minor repair	Major repair
Cost (\$M)	Min	2.5	2.5	13.5
Environmental Benefit (0-10)	Max	1	3	10
Disturbance (0-10)	Min	0	1	7





# Activity: Evaluate tradeoffs

Hint: Are there any irrelevant objectives, dominated outcomes, even swaps?

**Objective** [measurable attribute] {Direction}

	<b>Alternative</b>	<b>Respect Life</b>	<b>HBC Recovery</b>	<b>Wilderness Disturbance</b>	<b>Cost</b>
		[0-10 scale]	[P(N>6000)]	[User-days]	[M\$/5-yr]
		{Max}	{Max}	{Min}	{Min}
<b>A</b>	<b>No action</b>	<b>6</b>	<b>0.2</b>	<b>0</b>	<b>0</b>
<b>B</b>	<b>Alternative B</b>	<b>7</b>	<b>0.3</b>	<b>30</b>	<b>2.5</b>
<b>C</b>	<b>Alternative C</b>	<b>6</b>	<b>0.3</b>	<b>40</b>	<b>3</b>
<b>D</b>	<b>Alternative D</b>	<b>9.5</b>	<b>0.3</b>	<b>50</b>	<b>4.5</b>
<b>E</b>	<b>Alternative E</b>	<b>9</b>	<b>0.25</b>	<b>60</b>	<b>2</b>

The consequence table was inspired by Runge et al. 2011  
but the values in the table were altered for simplicity



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## C. Negotiate a solution from a set of best compromises

With  $\geq$  two objectives  
we can do **pareto  
frontier analysis**

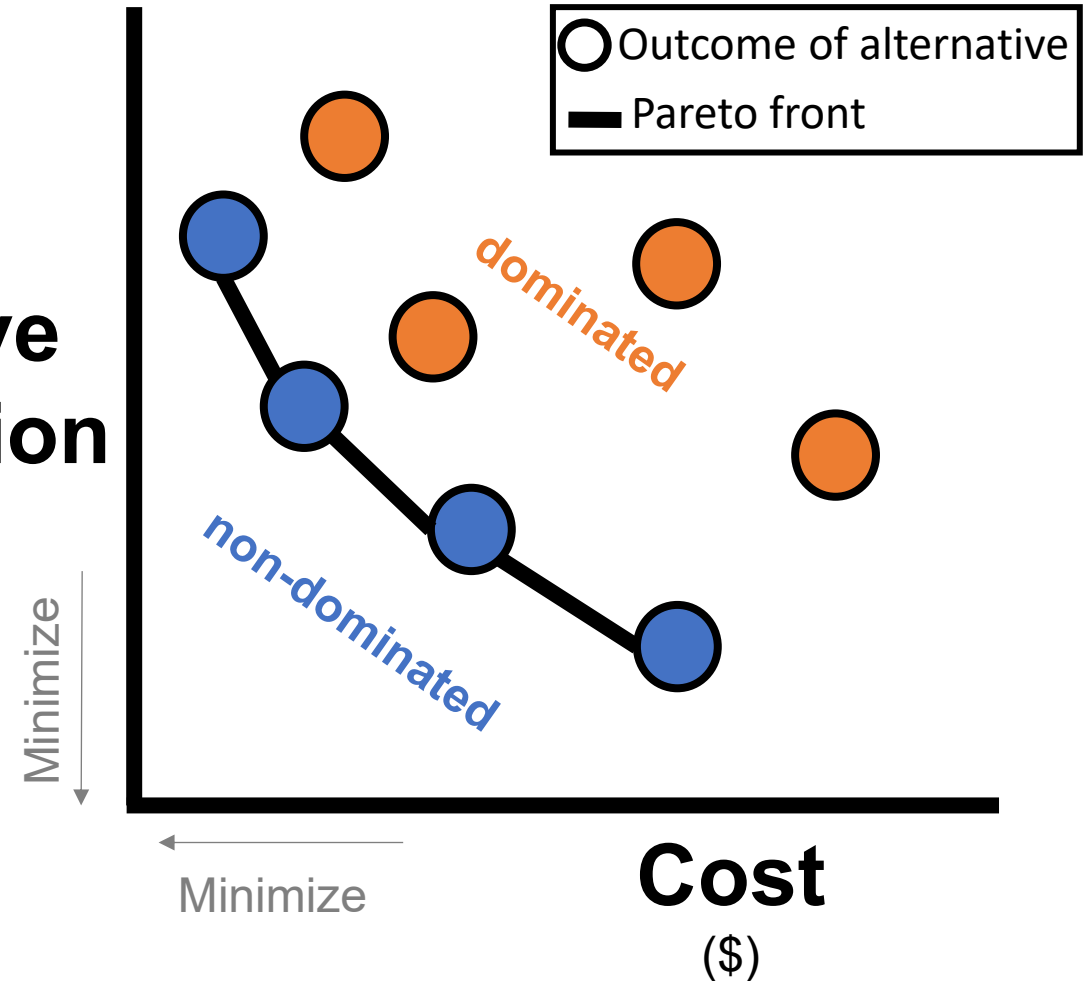
**Pareto optimal alternative**  
(non-dominated or 'efficient')

outcome on one objective  
cannot be improved without a  
reduction in another objective

**Pareto inefficient alternative**  
(dominated alternative or 'not efficient')

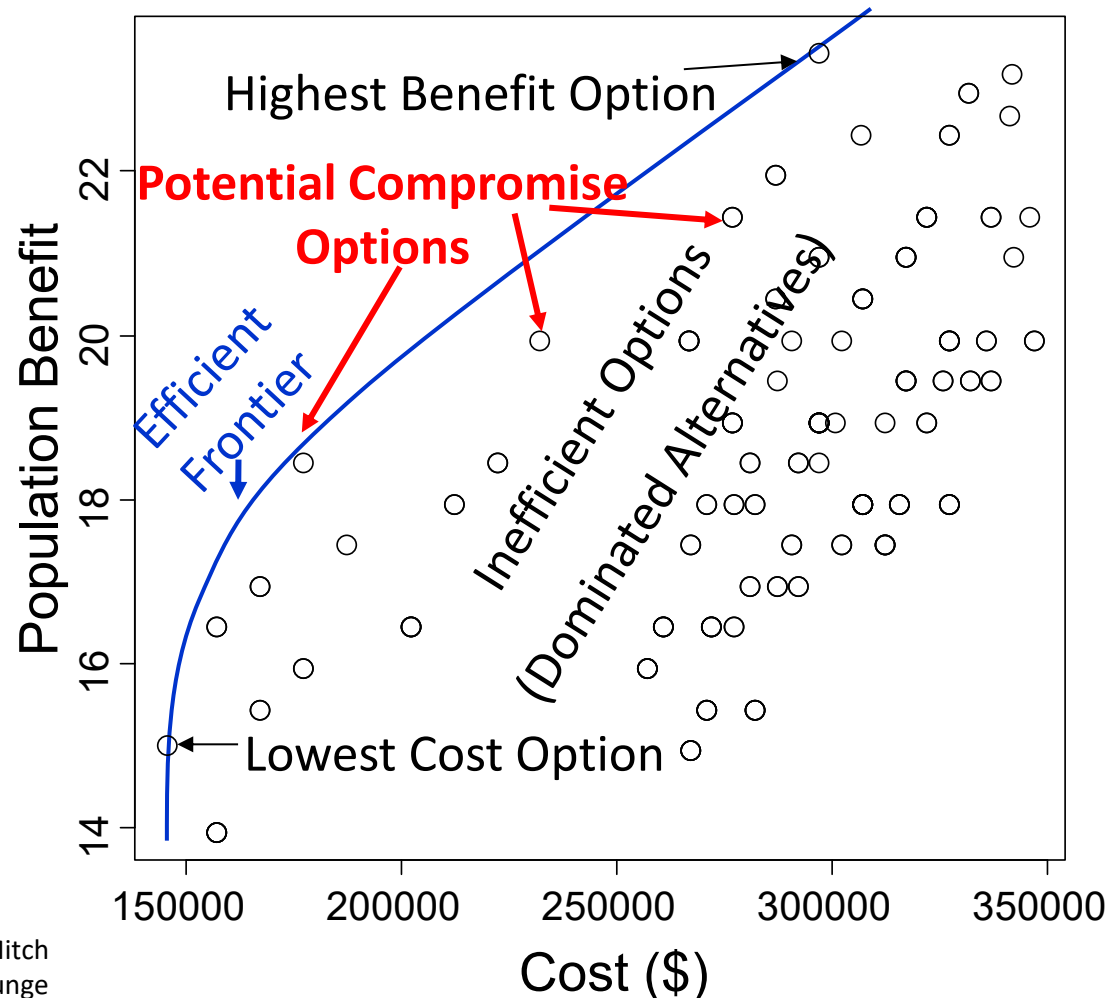
Another alternative performs at least as  
well on all objectives and performs strictly  
better on at least one

**Invasive  
population**  
(#)



# C. Negotiate a solution from a set of best compromises

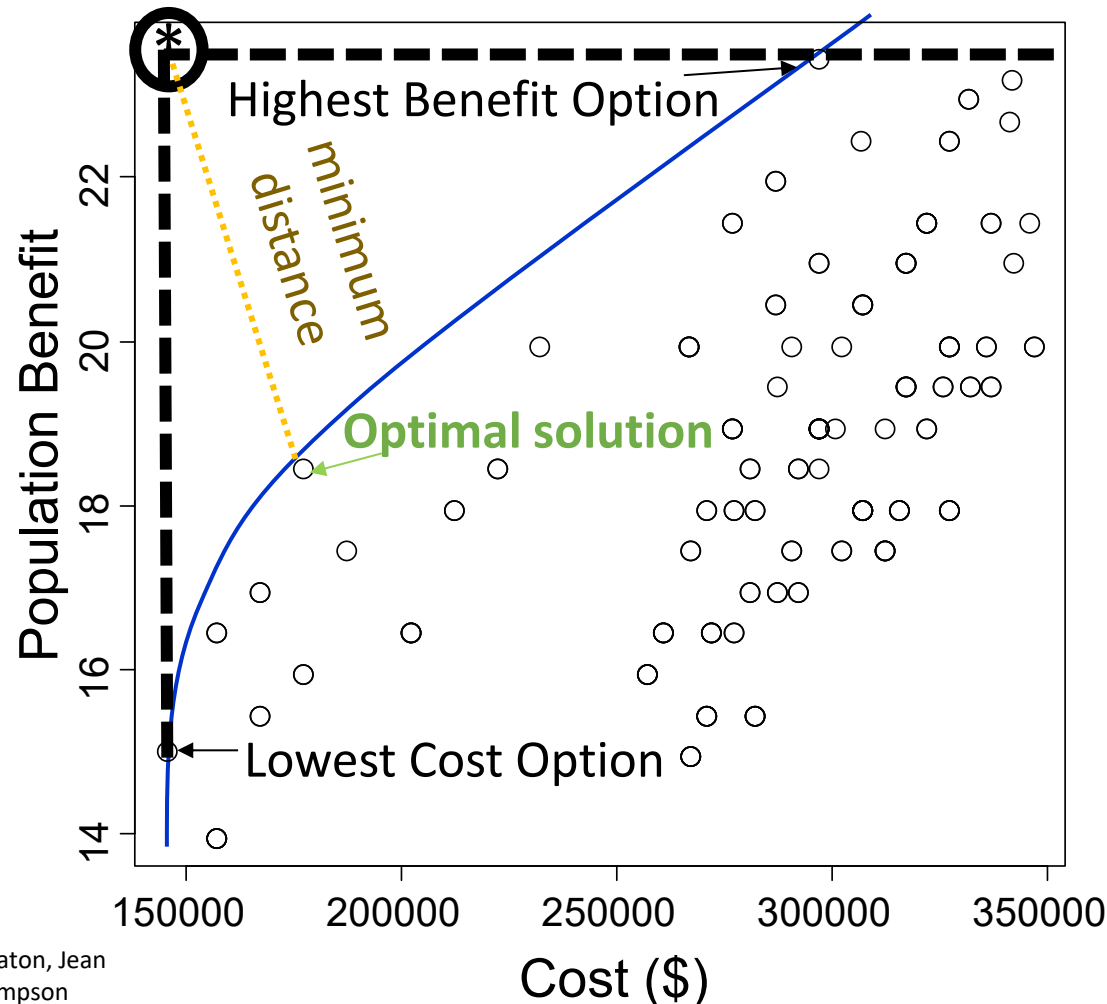
## Example: Cost vs Population Benefit



○ = outcome of each alternative

# C. Negotiate a solution from a set of best compromises

## Example: Cost vs Population Benefit



○ = outcome of each alternative

If cost and population benefit are deemed equal, we can find the **optimal solution** as the minimum distance between the ideal point (\*)






# Example: Consequence table + tradeoffs

Alternative management strategy, no. segments of removal effort	Objective (expected value)			Dominated by X Alternative
	Suppression (in millions)	Containment (%)	Prevention (in millions)	
No removals, 0	21.13 M	90.3%	1.15 M	None
Abundance, 1	<b>20.52 M</b>	90.2%	1.15 M	None
Growth, 1	20.83 M	<b>89.7%</b>	1.15 M	None
Edges, 1	20.68 M	90.0%	0.83 M	None
Downstream, 1	20.81 M	90.1%	<b>0.48 M</b>	None
Random, 1	20.61 M	90.0%	1.10 M	None
Abundance, 4	<b>18.82 M</b>	89.6%	1.14 M	None
Growth, 4	20.05 M	87.2%	1.01 M	Downstream, 4
Edges, 4	19.24 M	88.1%	0.48 M	None
Downstream, 4	19.37 M	<b>86.2%</b>	<b>0.18 M</b>	None
Random, 4	19.00 M	88.6%	0.96 M	None
Abundance, 8	<b>16.67 M</b>	85.7%	1.02 M	None
Growth, 8	18.34 M	83.1%	0.58 M	Downstream, 8
Edges, 8	17.92 M	85.1%	0.31 M	Downstream, 8
Downstream, 8	17.32 M	<b>81.4%</b>	<b>0.15 M</b>	None
Random, 8	16.93 M	85.7%	0.83 M	None
Abundance, 16	<b>11.81 M</b>	74.1%	0.67 M	None
Growth, 16	14.25 M	72.9%	0.22 M	Edges, 16
Edges, 16	14.24 M	<b>71.4%</b>	0.22 M	None
Downstream, 16	13.17 M	73.7%	<b>0.15 M</b>	None
Random, 16	12.78 M	78.3%	0.56 M	None

# Example: Consequence table + tradeoffs

**Subset of the table:** management alternatives to control invasive rusty crayfish

4 alternatives  
to compare

Alternative management strategy, no. segments of removal effort	Objective (expected value)			Dominated by X Alternative
	Suppression (in millions)	Containment (%)	Prevention (in millions)	
Abundance, 8 	16.67 M	85.7%	1.02 M	None
Growth, 8 	18.34 M	83.1%	0.58 M	Downstream, 8
Edges, 8 	17.92 M	85.1%	0.31 M	Downstream, 8
Downstream, 8 	17.32 M	81.4%	0.15 M	None
Random, 8 	16.93 M	85.7%	0.83 M	None

Best in having low  
# of crayfish  
(*suppression objective*)

\*But worse than  
Downstream, 8 in the  
other 2 objectives

Best alternative in having low  
% coverage of crayfish & low  
# of crayfish entering an  
important area (*Containment  
& Prevention objectives*)

\*But worse than Abundance,  
8 in the first objective

“Middle ground  
outcome”

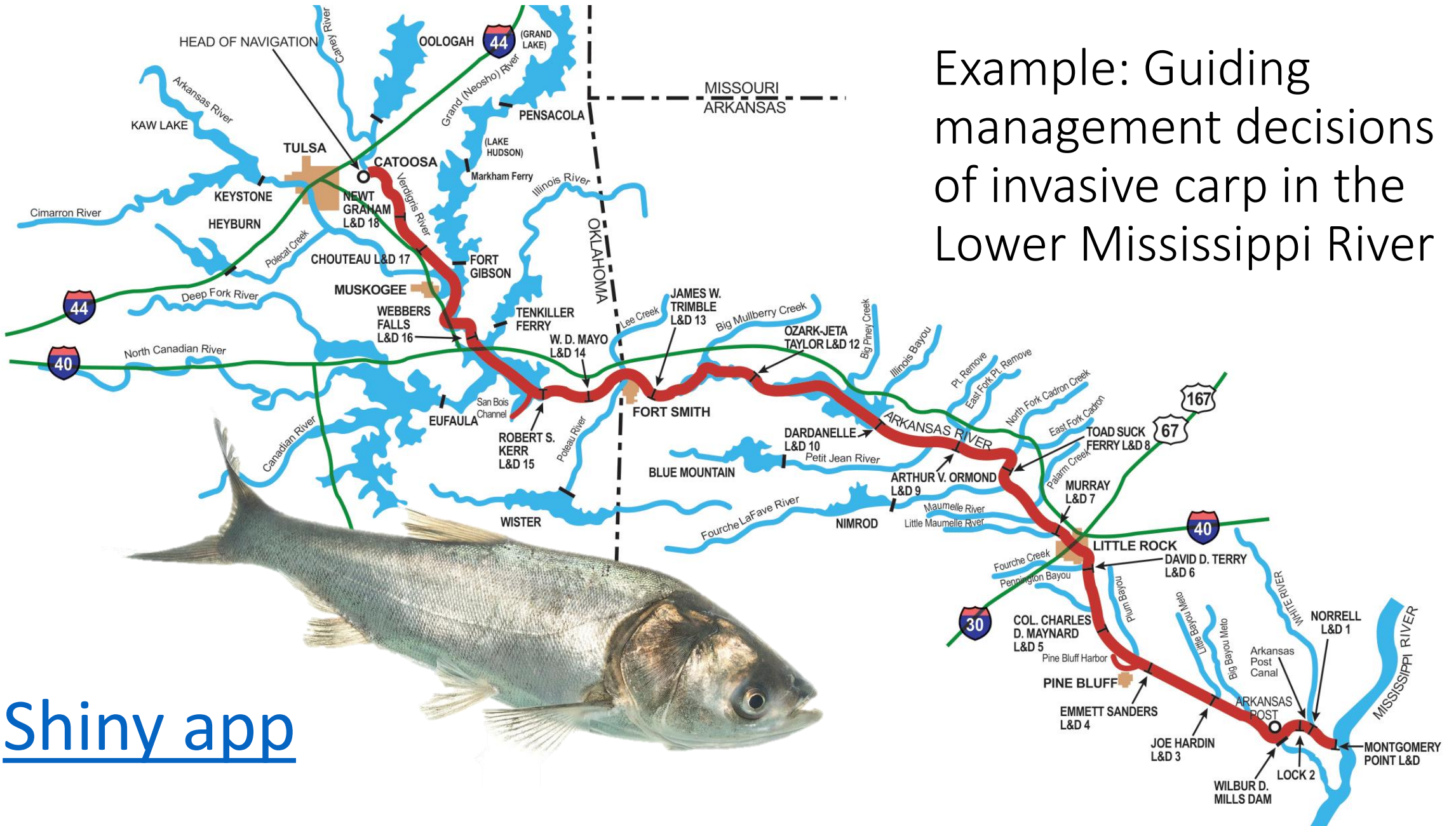
Better than  
Abundance, 8 in  
Prevention & better  
than Downstream, 8  
in Suppression

Means we  
should not  
conduct  
Growth, 8 or  
Edges, 8





Example: Guiding management decisions of invasive carp in the Lower Mississippi River



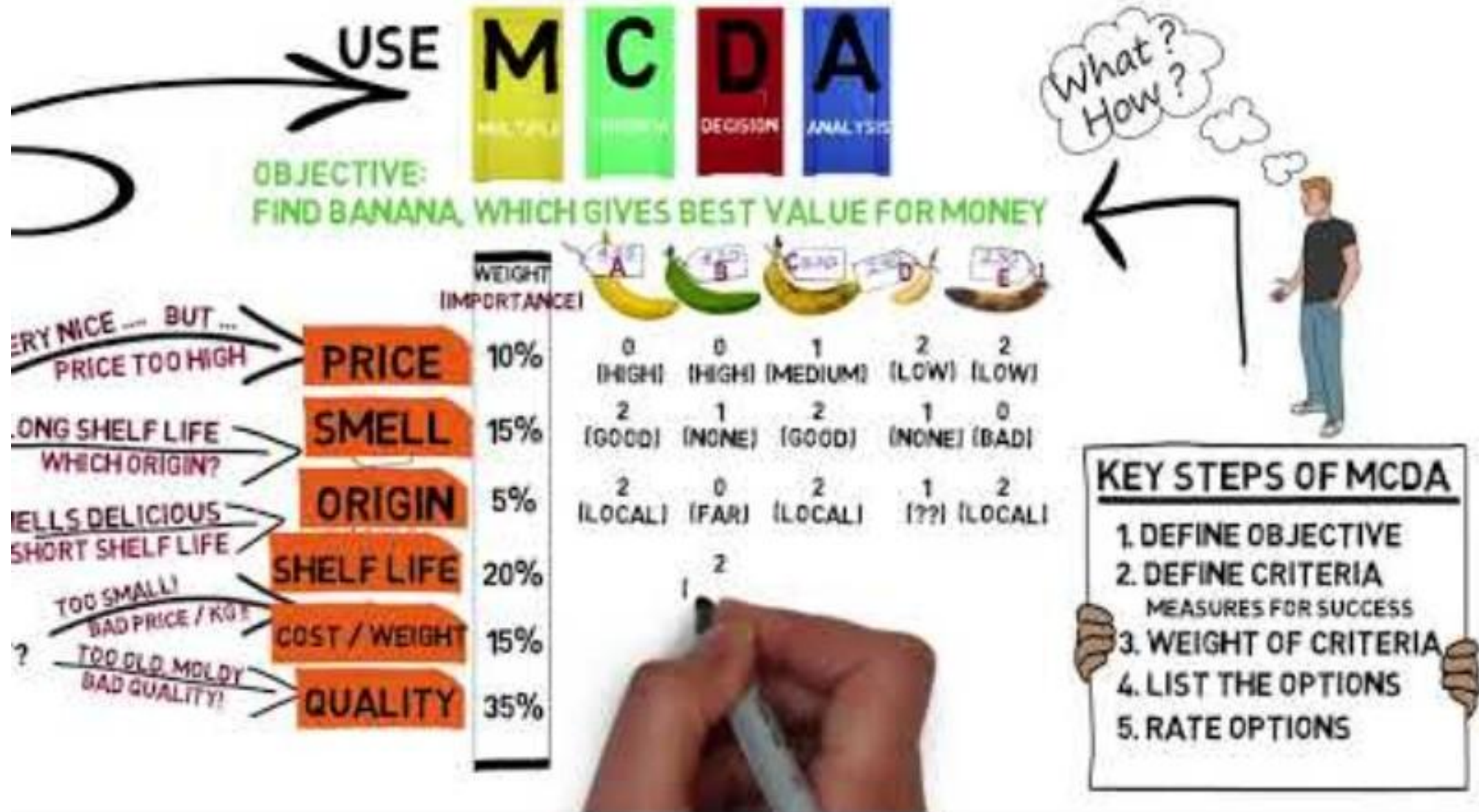
Shiny app

## D. Evaluate trade-offs explicitly

- Multicriteria decision analysis:
  - Offers tools to evaluate multiple objective problems
- A variety of tools exist (beyond the scope of this workshop)
  - Outranking methods
  - Analytic Hierarchy Process
  - Multi-attribute value/utility theory
  - SMART (simple multi-attribute rating technique)
- *See this week's reading for more examples*



# 3-minute intro to MCDA



# SMART (simple multi-attribute rating technique)

## 1. Normalize all attributes to 0-1 scale within each objective

For Goal to Maximize the attribute:

$$(x - \text{minimum}) / (\text{maximum} - \text{minimum})$$

For Goal to Minimize the attribute:

$$1 - (x - \text{minimum}) / (\text{maximum} - \text{minimum})$$

## 2. Assign weights to each fundamental objective

## 3. Calculate weighted sum of scores for each alternative

## 4. Recommend alternative with highest weighted score

## 5. Sensitivity analysis! (Is the recommendation sensitive to the weights and predictions?)

# Activity: SMART Practice

## EXCEL LINK

- Given our simplified impoundment repair problem (see consequence table), solve it using SMART for two different sets of weights:
  - Weights for cost/environmental benefit/disturbance are: 0.6, 0.3, 0.1
  - Weights for cost/environmental benefit/disturbance are: 0.2, 0.6, 0.2
- What if my weights are 0.6, 0.3, 0.1, but I am uncertain about the environmental benefit of the minor repair? It could be as small as 1 or as large as 5. Is my decision sensitive to this uncertainty?



# Where do objective weights come from?

- Represent relative *values* of a decision maker
- Some methods
  - Direct elicitation- importance weights
  - Swing weighting
  - Pairwise weighting (AHP)
- Weights are context-dependent
  - If you change the range of predictions for an attribute, its weight may need to change



# Importance weights

- These reflect the **relative importance** of each criterion in a decision-making process and are used in SMART
- Example:

	Weight	Translocations	Habitat Restoration
Maximize Pr (persistence)	0.9	0.5	0.9
Minimize cost	0.1	\$1,000,000	\$100,000,000

This is a common weighting scheme we see from the level of biologists- not as worried about the costs as the biological outcome.

# Importance weights

- These reflect the **relative importance** of each criterion in a decision-making process and are used in SMART
- Example:

	Weight	Translocations	Habitat Restoration
Maximize Pr (persistence)	0.9	0.5	<del>0.9</del> 0.51
Minimize cost	0.1	\$1,000,000	\$100,000,000

But what if this is the new outcome? Should we update the weights?

# Importance weights

- These reflect the **relative importance** of each criterion in a decision-making process and are used in SMART
- Example:

	Weight	Translocations	Habitat Restoration
Maximize Pr (persistence)	0.9	0	1
Minimize cost	0.1	1	0

How about now when we standardize outcomes?

***We may want a new method to assign weights that considers the absolute range of the predicted values***



# Swing weighting

- Summing normalized scores (i.e., using SMART) with direct importance weights can be misleading.
- Swing weights consider the particular values available (range of actual alternatives).
  - Preferences are context specific, not abstract.
- Use the 'swing' or range from worst to best values across the alternatives.





# Swing weighting – Buying a car example



Displays possible outcomes for each objective

Objective				Range	
	Description	Attribute	Goal	Worst	Best
A	Life span	years	max	6	12
B	Price	\$(1,000)	min	24	8
C	Color	natural	max	yellow	red

# Swing weighting – Buying a car example



Objective				Range		Hypothetical Alternatives (car)			
	Description	Attribute	Goal	Worst	Best	Bench mark	1	2	3
A	Life span	years	max	6	12	6			
B	Price	\$(1,000)	min	24	8	24			
C	Color	natural	max	yellow	red	Yellow			

Write down  
worst-case  
alternative

# Swing weighting – Buying a car example



Objective				Range		Hypothetical Alternatives (car)			
	Description	Attribute	Goal	Worst	Best	Bench mark	1	2	3
A	Life span	years	max	6	12	6	12	6	6
B	Price	\$(1,000)	min	24	8	24	24	8	24
C	Color	natural	max	yellow	red	Yellow	Yellow	Yellow	Red

These alternatives have outcomes that are the worst for each objective except one

# Swing weighting – Buying a car example



Objective				Range		Hypothetical Alternatives (car)			
	Description	Attribute	Goal	Worst	Best	Bench mark	1	2	3
A	Life span	years	max	6	12	6	12	6	6
B	Price	\$(1,000)	min	24	8	24	24	8	24
C	Color	natural	max	yellow	red	Yellow	Yellow	Yellow	Red
Rank		(1 is best; 4 is worst)				4	2	1	3

Next, rank each of the 4 alternatives (including worst-case benchmark) from 1 to 4

# Swing weighting – Buying a car example



Objective				Range		Hypothetical Alternatives (car)			
	Description	Attribute	Goal	Worst	Best	Bench mark	1	2	3
A	Life span	years	max	6	12	6 24 Yellow	12	6	6
B	Price	\$(1,000)	min	24	8		24	8	24
C	Color	natural	max	yellow	red		Yellow	Yellow	Red
Rank		(1 is best; 4 is worst)				4	2	1	3
Score		(100 is best; 0 is worst)				0	70	100	5

Using the ranks, score the alternatives from 0 to 100  
(we rank then score for some cognitive help!)



# Swing weighting – Buying a car example



Objective				Range		Hypothetical Alternatives (car)			
	Description	Attribute	Goal	Worst	Best	Bench mark	1	2	3
A	Life span	years	max	6	12	6 24 Yellow	12	6	6
B	Price	\$(1,000)	min	24	8		24	8	24
C	Color	natural	max	yellow	red		Yellow	Yellow	Red
	Rank	(1 is best; 4 is worst)				4	2	1	3
	Score	(100 is best; 0 is worst)				0	70	100	5
	Weight	score/(sum of scores)				0	0.40	0.57	0.03

Calculate your weights!



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# Swing weighting – Buying a car example



Objective				Range		Hypothetical Alternatives (car)			
	Description	Attribute	Goal	Worst	Best	Bench mark	1	2	3
A	Life span	years	max	6	12	6 24 Yellow	12	6	6
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C	Color	natural	max	yellow	red		Yellow	Yellow	Red
	Rank	(1 is best; 4 is worst)				4	2	1	3
	Score	(100 is best; 0 is worst)				0	70	100	5
	Weight	score/(sum of scores)				0	0.40	0.57	0.03

**These are your weights for objective A,B,C!!!!**



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# Swing weighting activity

**SEE EXAMPLE**

**EXCEL LINK**



# Skills Check

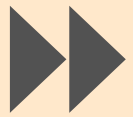
**SEE SKILLS CHECK**

**EXCEL LINK**

# Activity: think about your decision problem

- For your final project presentation, you will provide a slide of your Tradeoffs
- Some hints:
  - Review your consequence table from last week (or make one now)
  - Do you have any irrelevant objectives? Dominated alternatives? Can you make even swaps?
  - Can you use smart or swing weighting to help make your decision?
- **Feel free to go back to your problem framing, objectives, alternatives, and consequences steps!**

# Looking ahead:



**Next week:** I step of PrOACTI



**Weekly:** Work through a step of the PrOACT process/  
learn extra tools

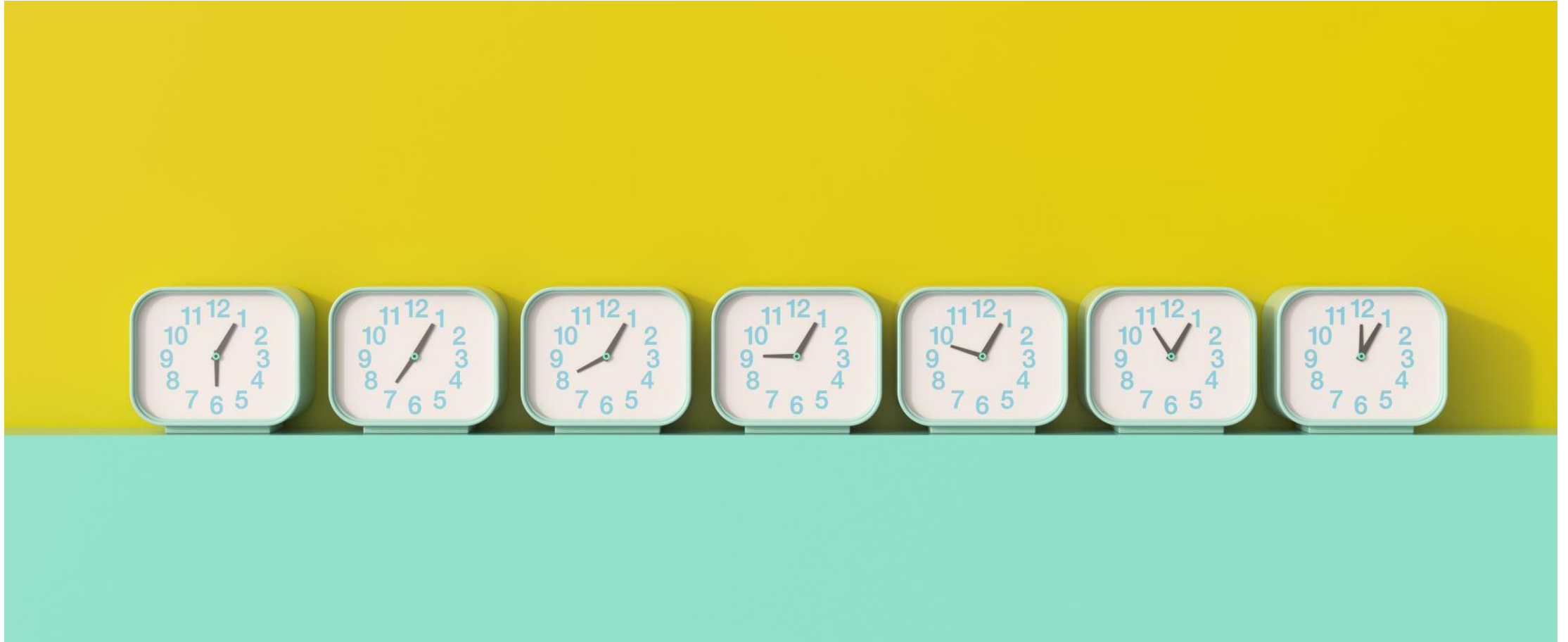


**Last week of class:**

Elevator pitch of your research project in  
terms of SDM/PrOACT

Note: Abridged PrOACT story slides with a star on the upper right  
are good examples to use for your presentation

# Extra time activities:



Reading discussion: Runge et al. 2020 Chapter 5 (Converse)

- Why do you think multi-criteria decision analysis is useful?
- Compare the pros/cons of structured discussions over quantitative techniques to examine trade-offs
- What are some pitfalls of MCDA?
- What happens if we miss an objective?