n, i, j, k	Index variables for meta-lists
num	Numeric literals
hex	Bit vector literal, specified by C-style hex number
bin	Bit vector literal, specified by C-style binary number
string	String literals
regexp	Regular expresions, as a string literal
x, y, z	Variables
ix	Variables

l	::=		Source locations
	|		
$x^l,\ y^l,\ z^l,\ name$	::=		Location-annotated names
	|	$x\ l$	
	|	$(ix)l$	Remove infix status
ix^l	::=		Location-annotated infix names
	|	$ix\ l$	
	|	$`x`l$	Add infix status
α	::=		Type variables
	|	$'x$	
α^l	::=		Location-annotated type variables
	|	$\alpha\ l$	
N	::=		numeric variables
	|	$''x$	
N^l	::=		Location-annotated numeric variables
	|	$N\ l$	
id	::=		Long identifers
	|	$x_1^l .. x_n^l . x^l\ l$	
tnv	::=		Union of type variables and Nexp type variables, without loca
	|	α	
	|	N	
$tnvar^l$	::=		Union of type variables and Nexp type variables, with location
	|	α^l	
	|	N^l	
$tnvs$	::=		Type variable lists
	|	$tnv_1 .. tnv_n$	
$tnvars^l$	::=		Type variable lists
	|	$tnvar_1^l .. tnvar_n^l$	
$Nexp\_aux$	::=		Numerical expressions for specifying vector lengths and indexe
	|	N	
	|	num	
	|	$Nexp_1 * Nexp_2$	
	|	$Nexp_1 + Nexp_2$	
	|	$(Nexp)$	

Nexp	::=		Location-annotated vector lengths
	|	*Nexp_aux l*	
Nexp_constraint	::=		Whether a vector is bounded or fixed size
	|	*Nexp*	
	|	$\geq$ *Nexp*	
typ_aux	::=		Types
	|	_	Unspecified type
	|	α^l	Type variables
	|	$typ_1 \rightarrow typ_2$	Function types
	|	$typ_1 * .... * typ_n$	Tuple types
	|	*Nexp*	As a typ to permit applications over Nexps, otherwise no
	|	*id* typ_1 .. typ_n	Type applications
	|	(*typ*)	
typ	::=		Location-annotated types
	|	*typ_aux l*	
lit_aux	::=		Literal constants
	|	**true**	
	|	**false**	
	|	*num*	
	|	*hex*	hex and bin are constant bit vectors, entered as C-style l
	|	*bin*	
	|	*string*	
	|	()	
	|	**bitzero**	bitzero and bitone are constant bits, if commonly used w
	|	**bitone**	
lit	::=		
	|	*lit_aux l*	Location-annotated literal constants
$;^?$	::=		Optional semi-colons
	|		
	|	;	
pat_aux	::=		Patterns
	|	_	Wildcards
	|	(*pat* **as** x^l)	Named patterns
	|	(*pat* : *typ*)	Typed patterns
	|	*id* pat_1 .. pat_n	Single variable and constructor patterns
	|	$\langle\|fpat_1; ...; fpat_n ;^?\|\rangle$	Record patterns
	|	$[\|pat_1; ..; pat_n ;^?\|]$	Vector patterns
	|	$[\|pat_1 .. pat_n\|]$	Concatenated vector patterns
	|	$(pat_1, ..., pat_n)$	Tuple patterns
	|	$[pat_1; ..; pat_n ;^?]$	List patterns

	|	(pat)	
	|	$pat_1 :: pat_2$	Cons patterns
	|	$x^l + num$	constant addition patterns
	|	lit	Literal constant patterns
pat	::=		Location-annotated patterns
	|	$pat\_aux\ l$	
$fpat$	::=		Field patterns
	|	$id = pat\ l$	
$\|^?$	::=		Optional bars
	|		
	|	|	
exp_aux	::=		Expressions
	|	id	Identifiers
	|	N	Nexp var, has type num
	|	**fun** $psexp$	Curried functions
	|	**function** $\|^?\ pexp_1 \| \ldots \| pexp_n$ **end**	Functions with pattern matching
	|	$exp_1\ exp_2$	Function applications
	|	$exp_1\ ix^l\ exp_2$	Infix applications
	|	$\langle \| fexps \| \rangle$	Records
	|	$\langle \| exp$ **with** $fexps \| \rangle$	Functional update for records
	|	$exp.id$	Field projection for records
	|	$[\| exp_1;\ ..\ ;\ exp_n\ ;^? \|]$	Vector instantiation
	|	$exp.(Nexp)$	Vector access
	|	$exp.(Nexp_1..Nexp_2)$	Subvector extraction
	|	**match** exp **with** $\|^?\ pexp_1 \| \ldots \| pexp_n\ l$ **end**	Pattern matching expressions
	|	$(exp : typ)$	Type-annotated expressions
	|	**let** $letbind$ **in** exp	Let expressions
	|	$(exp_1,\ ....\ , exp_n)$	Tuples
	|	$[exp_1;\ ..\ ;\ exp_n\ ;^?]$	Lists
	|	(exp)	
	|	**begin** exp **end**	Alternate syntax for (exp)
	|	**if** exp_1 **then** exp_2 **else** exp_3	Conditionals
	|	$exp_1 :: exp_2$	Cons expressions
	|	lit	Literal constants
	|	$\{exp_1 \| exp_2\}$	Set comprehensions
	|	$\{exp_1 \|$ **forall** $qbind_1\ ..\ qbind_n \| exp_2\}$	Set comprehensions with explicit binding
	|	$\{exp_1;\ ..\ ;\ exp_n\ ;^?\}$	Sets
	|	$q\ qbind_1\ ...\ qbind_n.exp$	Logical quantifications
	|	$[exp_1 \|$ **forall** $qbind_1\ ..\ qbind_n \| exp_2]$	List comprehensions (all binders must be qua
exp	::=		Location-annotated expressions
	|	$exp\_aux\ l$	

q	::=		Quantifiers
	|	**forall**	
	|	**exists**	
$qbind$	::=		Bindings for quantifiers
	|	x^l	
	|	$(pat\ \mathbf{IN}\ exp)$	Restricted quantifications over sets
	|	$(pat\ \mathbf{MEM}\ exp)$	Restricted quantifications over lists
$fexp$	::=		Field-expressions
	|	$id = exp\ l$	
$fexps$	::=		Field-expression lists
	|	$fexp_1; \ldots; fexp_n\ ;^?\ l$	
$pexp$	::=		Pattern matches
	|	$pat \rightarrow exp\ l$	
$psexp$	::=		Multi-pattern matches
	|	$pat_1 \ldots pat_n \rightarrow exp\ l$	
$tannot^?$	::=		Optional type annotations
	|		
	|	$: typ$	
$funcl\_aux$	::=		Function clauses
	|	$x^l\ pat_1 \ldots pat_n\ tannot^?\ = exp$	
$letbind\_aux$	::=		Let bindings
	|	$pat\ tannot^?\ = exp$	Value bindings
	|	$funcl\_aux$	Function bindings
$letbind$	::=		Location-annotated let bindings
	|	$letbind\_aux\ l$	
$funcl$	::=		Location-annotated function clauses
	|	$funcl\_aux\ l$	
$id^?$	::=		Optional name for inductively defined relatio
	|		
	|	$x^l :$	
$rule\_aux$	::=		Inductively defined relation clauses
	|	$id^?\ \mathbf{forall}\ x_1^l .. x_n^l . exp \Longrightarrow x^l\ exp_1 .. exp_i$	
$rule$	::=		Location-annotated inductively defined relati
	|	$rule\_aux\ l$	

typs	::=		Type lists
	|	$typ_1 * ... * typ_n$	
ctor_def	::=		Datatype definition clauses
	|	x^l **of** *typs*	
	|	x^l	S Constant constructors
texp	::=		Type definition bodies
	|	*typ*	Type abbreviations
	|	$\langle \vert x_1^l : typ_1; ... ; x_n^l : typ_n \;;^? \vert \rangle$	Record types
	|	$\vert^? ctor\_def_1 \vert ... \vert ctor\_def_n$	Variant types
$name^?$	::=		Optional name specification for variables of defined type
	|		
	|	$[name = regexp]$	
td	::=		Type definitions
	|	$x^l\, tnvars^l\, name^? = texp$	
	|	$x^l\, tnvars^l\, name^?$	Definitions of opaque types
c	::=		Typeclass constraints
	|	$id\, tnvar^l$	
cs	::=		Typeclass constraint lists
	|		
	|	$c_1, .., c_i \Rightarrow$	Must have > 0 constraints
c_pre	::=		Type and instance scheme prefixes
	|		
	|	$\textbf{forall}\, tnvar_1^l .. tnvar_n^l . cs$	Must have > 0 type variables
typschm	::=		Type schemes
	|	*c_pre typ*	
instschm	::=		Instance schemes
	|	$c\_pre(id\ typ)$	
target	::=		Backend target names
	|	**hol**	
	|	**isabelle**	
	|	**ocaml**	
	|	**coq**	
	|	**tex**	
	|	**html**	
τ	::=		Backend target name lists
	|	$\{target_1; ..; target_n\}$	

$\tau^?$	::=		Optional targets
	|		
	|	τ	
val_def	::=		Value definitions
	|	**let** $\tau^?$ *letbind*	Non-recursive value definitions
	|	**let rec** $\tau^?$ $funcl_1$ **and** ... **and** $funcl_n$	Recursive function definitions
	|	**let inline** $\tau^?$ *letbind*	Function definitions to be inlined
val_spec	::=		Value type specifications
	|	**val** x^l : *typschm*	
def_aux	::=		Top-level definitions
	|	**type** td_1 **and** ... **and** td_n	Type definitions
	|	*val_def*	Value definitions
	|	**rename** $\tau^?$ *id* $= x^l$	Rename constant or type
	|	**module** $x^l =$ **struct** *defs* **end**	Module definitions
	|	**module** $x^l =$ *id*	Module renamings
	|	**open** *id*	Opening modules
	|	**indreln** $\tau^?$ $rule_1$ **and** ... **and** $rule_n$	Inductively defined relations
	|	*val_spec*	Top-level type constraints
	|	**class** $(x^l\ tnvar^l)$ **val** x_1^l : typ_1 l_1 ... **val** x_n^l : typ_n l_n **end**	Typeclass definitions
	|	**instance** *instschm* val_def_1 l_1 ... val_def_n l_n **end**	Typeclass instantiations
def	::=		Location-annotated definitions
	|	*def_aux* l	
$;;^?$	::=		Optional double-semi-colon
	|		
	|	;;	
defs	::=		Definition sequences
	|	$def_1\ ;;_1^?\ ..\ def_n\ ;;_n^?$	
p	::=		Unique paths
	|	$x_1 .. x_n.x$	
	|	**__list**	
	|	**__bool**	
	|	**__num**	
	|	**__set**	
	|	**__string**	
	|	**__unit**	
	|	**__bit**	
	|	**__vector**	
σ	::=		Type variable substitutions
	|	$\{tnv_1 \mapsto t_1\ ..\ tnv_n \mapsto t_n\}$	

$t,\ u$	::=			Internal types
	|	α		
	|	$t_1 \rightarrow t_2$		
	|	$t_1 * .... * t_n$		
	|	$p\ t\_args$		
	|	ne		
	|	$\sigma(t)$	M	Multiple substitutions
	|	$\sigma(tnv)$	M	Single variable substitution
	|	**curry** (t_multi, t)	M	Curried, multiple argument functions
ne	::=			internal numeric expressions
	|	N		
	|	num		
	|	$num * ne$		
	|	$ne_1 + ne_2$		
	|	$(-ne)$		
	|	**normalize** (ne)	M	
	|	$ne_1 + \ ... \ + ne_n$	M	
	|	**bitlength** (bin)	M	
	|	**bitlength** (hex)	M	
	|	**length** $(pat_1 ... pat_n)$	M	
	|	**length** $(exp_1 ... exp_n)$	M	
t_args	::=			Lists of types
	|	$t_1 .. t_n$		
	|	$\sigma(t\_args)$	M	Multiple substitutions
t_multi	::=			Lists of types
	|	$(t_1 * .. * t_n)$		
	|	$\sigma(t\_multi)$	M	Multiple substitutions
nec	::=			Numeric expression constraints
	|	$ne \langle nec$		
	|	$ne = nec$		
	|	$ne <= nec$		
	|	ne		
$names$	::=			Sets of names
	|	$\{x_1, .., x_n\}$		
$\mathcal{C}$	::=			Typeclass constraint lists
	|	$(p_1\ tnv_1) .. (p_n\ tnv_n)$		
env_tag	::=			Tags for the (non-constructor) value descriptions
	|	**method**		Bound to a method
	|	**val**		Specified with val
	|	**let**		Defined with let or indreln

v_desc	::=		Value descriptions
	|	$\langle \textbf{forall}\ tnvs.t\_multi \to p, (x\ \textbf{of}\ names)\rangle$	Constructors
	|	$\langle \textbf{forall}\ tnvs.\mathcal{C} \Rightarrow t, env\_tag\rangle$	Values
f_desc	::=		
	|	$\langle \textbf{forall}\ tnvs.p \to t, (x\ \textbf{of}\ names)\rangle$	Fields
$\Sigma^{\mathcal{C}}$	::=		Typeclass constraints
	|	$\{(p_1\ t_1), .., (p_n\ t_n)\}$	
	|	${\Sigma^{\mathcal{C}}}_1 \cup .. \cup {\Sigma^{\mathcal{C}}}_n$	M
$\Sigma^{\mathcal{N}}$	::=		Nexp constraint lists
	|	$\{nec_1, .., nec_n\}$	
	|	${\Sigma^{\mathcal{N}}}_1 \cup .. \cup {\Sigma^{\mathcal{N}}}_n$	M
E	::=		Environments
	|	$\langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}}\rangle$	
	|	$E_1 \uplus E_2$	M
	|	ϵ	M
E^{X}	::=		Value environments
	|	$\{x_1 \mapsto v\_desc_1, .., x_n \mapsto v\_desc_n\}$	
	|	$E^{\mathrm{X}}_1 \uplus .. \uplus E^{\mathrm{X}}_n$	M
E^{F}	::=		Field environments
	|	$\{x_1 \mapsto f\_desc_1, .., x_n \mapsto f\_desc_n\}$	
	|	$E^{\mathrm{F}}_1 \uplus .. \uplus E^{\mathrm{F}}_n$	M
E^{M}	::=		Module environments
	|	$\{x_1 \mapsto E_1, .., x_n \mapsto E_n\}$	
E^{P}	::=		Path environments
	|	$\{x_1 \mapsto p_1, .., x_n \mapsto p_n\}$	
	|	$E^{\mathrm{P}}_1 \uplus .. \uplus E^{\mathrm{P}}_n$	M
E^{L}	::=		Lexical bindings
	|	$\{x_1 \mapsto t_1, .., x_n \mapsto t_n\}$	
	|	$E^{\mathrm{L}}_1 \uplus .. \uplus E^{\mathrm{L}}_n$	M
tc_abbrev	::=		Type abbreviations
	|	$.t$	
	|		
tc_def	::=		Type and class constructor definitions
	|	$tnvs\ tc\_abbrev$	Type constructors
Δ	::=		Type constructor definitions

	$\mid$	$\{p_1 \mapsto tc\_def_1, .., p_n \mapsto tc\_def_n\}$	
	$\mid$	$\Delta_1 \uplus \Delta_2$	M

δ	::=		Typeclass definitions
	$\mid$	$\{p_1 \mapsto xs_1, .., p_n \mapsto xs_n\}$	
	$\mid$	$\delta_1 \uplus \delta_2$	M

inst	::=		A typeclass instance, t must not contain nested typ
	$\mid$	$\mathcal{C} \Rightarrow (p\ t)$	

I	::=		Global instances
	$\mid$	$\{inst_1, .., inst_n\}$	
	$\mid$	$I_1 \cup I_2$	M

D	::=		Global type definition store
	$\mid$	$\langle \Delta, \delta, I \rangle$	
	$\mid$	$D_1 \uplus D_2$	M
	$\mid$	ϵ	M

xs	::=	
	$\mid$	$x_1 .. x_n$

terminals	::=		
	$\mid$	$\geq$	>=
	$\mid$	$\rightarrow$	->
	$\mid$	$\Longrightarrow$	==>
	$\mid$	$\langle\mid$	<|
	$\mid$	$\mid\rangle$	|>
	$\mid$	$\cap$	
	$\mid$	$\cup$	
	$\mid$	$\uplus$	
	$\mid$	$\notin$	
	$\mid$	$\subset$	
	$\mid$	$\neq$	
	$\mid$	$\emptyset$	
	$\mid$	$\langle$	
	$\mid$	$\rangle$	
	$\mid$	$\vdash$	
	$\mid$	,	
	$\mid$	$\mapsto$	
	$\mid$	$\triangleright$	
	$\mid$	$\rightsquigarrow$	
	$\mid$	$\Rightarrow$	
	$\mid$	$\_$	
	$\mid$	ϵ	

formula	::=	

	$judgement$	
	$formula_1 \quad .. \quad formula_n$	
	$E^{\mathrm{M}}(x) \triangleright E$	Module lookup
	$E^{\mathrm{P}}(x) \triangleright p$	Path lookup
	$E^{\mathrm{F}}(x) \triangleright f\_desc$	Field lookup
	$E^{\mathrm{X}}(x) \triangleright v\_desc$	Value lookup
	$E^{\mathrm{L}}(x) \triangleright t$	Lexical binding lookup
	$\Delta(p) \triangleright tc\_def$	Type constructor lookup
	$\delta(p) \triangleright xs$	Type constructor lookup
	$\mathbf{dom}\,(E_1^{\mathrm{M}}) \cap \mathbf{dom}\,(E_2^{\mathrm{M}}) = \emptyset$	
	$\mathbf{dom}\,(E_1^{\mathrm{X}}) \cap \mathbf{dom}\,(E_2^{\mathrm{X}}) = \emptyset$	
	$\mathbf{dom}\,(E_1^{\mathrm{F}}) \cap \mathbf{dom}\,(E_2^{\mathrm{F}}) = \emptyset$	
	$\mathbf{dom}\,(E_1^{\mathrm{P}}) \cap \mathbf{dom}\,(E_2^{\mathrm{P}}) = \emptyset$	
	$\mathbf{disjoint\,doms}\,(E_1^{\mathrm{L}}, \ldots., E_n^{\mathrm{L}})$	Pairwise disjoint domains
	$\mathbf{disjoint\,doms}\,(E_1^{\mathrm{X}}, \ldots., E_n^{\mathrm{X}})$	Pairwise disjoint domains
	$\mathbf{compatible\,overlap}\,(x_1 \mapsto t_1, .., x_n \mapsto t_n)$	$(x_i = x_j) \Longrightarrow (t_i = t_j)$
	$\mathbf{duplicates}\,(tnvs) = \emptyset$	
	$\mathbf{duplicates}\,(x_1, .., x_n) = \emptyset$	
	$x \notin \mathbf{dom}\,(E^{\mathrm{L}})$	
	$x \notin \mathbf{dom}\,(E^{\mathrm{X}})$	
	$x \notin \mathbf{dom}\,(E^{\mathrm{F}})$	
	$p \notin \mathbf{dom}\,(\delta)$	
	$p \notin \mathbf{dom}\,(\Delta)$	
	$\mathbf{FV}\,(t) \subset tnvs$	Free type variables
	$\mathbf{FV}\,(t\_multi) \subset tnvs$	Free type variables
	$\mathbf{FV}\,(\mathcal{C}) \subset tnvs$	Free type variables
	$inst\,\mathbf{IN}\,I$	
	$(p\ t) \notin I$	
	$E_1^{\mathrm{L}} = E_2^{\mathrm{L}}$	
	$E_1^{\mathrm{X}} = E_2^{\mathrm{X}}$	
	$E_1^{\mathrm{F}} = E_2^{\mathrm{F}}$	
	$E_1 = E_2$	
	$\Delta_1 = \Delta_2$	
	$\delta_1 = \delta_2$	
	$I_1 = I_2$	
	$names_1 = names_2$	
	$t_1 = t_2$	
	$\sigma_1 = \sigma_2$	
	$p_1 = p_2$	
	$xs_1 = xs_2$	
	$tnvs_1 = tnvs_2$	

$convert\_tnvars$	::=	
	$tnvars^l \rightsquigarrow tnvs$	
	$tnvar^l \rightsquigarrow tnv$	

look_m	::=		
	|	$E_1(x_1^l \,..\, x_n^l) \triangleright E_2$	Name path lookup
look_m_id	::=		
	|	$E_1(id) \triangleright E_2$	Module identifier lookup
look_tc	::=		
	|	$E(id) \triangleright p$	Path identifier lookup
check_t	::=		
	|	$\Delta \vdash t\ \mathbf{ok}$	Well-formed types
	|	$\Delta, tnv \vdash t\ \mathbf{ok}$	Well-formed type/Nexps ma
teq	::=		
	|	$\Delta \vdash t_1 = t_2$	Type equality
convert_typ	::=		
	|	$\Delta, E \vdash typ \rightsquigarrow t$	Convert source types to int
	|	$\vdash Nexp \rightsquigarrow ne$	Convert and normalize num
convert_typs	::=		
	|	$\Delta, E \vdash typs \rightsquigarrow t\_multi$	
check_lit	::=		
	|	$\vdash lit : t$	Typing literal constants
inst_field	::=		
	|	$\Delta, E \vdash \mathbf{field}\ id : p\ t\_args \to t \triangleright (x\ \mathbf{of}\ names)$	Field typing (also returns c
inst_ctor	::=		
	|	$\Delta, E \vdash \mathbf{ctor}\ id : t\_multi \to p\ t\_args \triangleright (x\ \mathbf{of}\ names)$	Data constructor typing (al
inst_val	::=		
	|	$\Delta, E \vdash \mathbf{val}\ id : t \triangleright \Sigma^{\mathcal{C}}$	Typing top-level bindings, c
not_ctor	::=		
	|	$E, E^{\mathrm{L}} \vdash x\ \mathbf{not\ ctor}$	v is not bound to a data co
not_shadowed	::=		
	|	$E^{\mathrm{L}} \vdash id\ \mathbf{not\ shadowed}$	id is not lexically shadowed
check_pat	::=		
	|	$\Delta, E, E_1^{\mathrm{L}} \vdash pat : t \triangleright E_2^{\mathrm{L}}$	Typing patterns, building t
	|	$\Delta, E, E_1^{\mathrm{L}} \vdash pat\_aux : t \triangleright E_2^{\mathrm{L}}$	Typing patterns, building t
id_field	::=		
	|	$E \vdash id\ \mathbf{field}$	Check that the identifier is

id_value	::=		
	|	$E \vdash id\ \mathbf{value}$	Check that the identifier is a
check_exp	::=		
	|	$\Delta, E, E^{\mathrm{L}} \vdash exp : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}$	Typing expressions, collecting
	|	$\Delta, E, E^{\mathrm{L}} \vdash exp\_aux : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}$	Typing expressions, collecting
	|	$\Delta, E, E_1^{\mathrm{L}} \vdash qbind_1 \,..\, qbind_n \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}$	Build the environment for qua
	|	$\Delta, E, E_1^{\mathrm{L}} \vdash \mathbf{list}\ qbind_1 \,..\, qbind_n \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}$	Build the environment for qua
	|	$\Delta, E, E^{\mathrm{L}} \vdash funcl \triangleright \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}$	Build the environment for a fu
	|	$\Delta, E, E_1^{\mathrm{L}} \vdash letbind \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}$	Build the environment for a le
check_rule	::=		
	|	$\Delta, E, E^{\mathrm{L}} \vdash rule \triangleright \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}$	Build the environment for an
check_texp_tc	::=		
	|	$xs, \Delta_1, E \vdash \mathbf{tc}\ td \triangleright \Delta_2, E^{\mathrm{P}}$	Extract the type constructor i
check_texps_tc	::=		
	|	$xs, \Delta_1, E \vdash \mathbf{tc}\ td_1 \,..\, td_i \triangleright \Delta_2, E^{\mathrm{P}}$	Extract the type constructor i
check_texp	::=		
	|	$\Delta, E \vdash tnvs\ p = texp \triangleright \langle E^{\mathrm{F}}, E^{\mathrm{X}} \rangle$	Check a type definition, with
check_texps	::=		
	|	$xs, \Delta, E \vdash td_1 \,..\, td_n \triangleright \langle E^{\mathrm{F}}, E^{\mathrm{X}} \rangle$	
convert_class	::=		
	|	$\delta, E \vdash id \rightsquigarrow p$	Lookup a type class
solve_class_constraint	::=		
	|	$I \vdash (p\ t)\ \mathbf{IN}\ \mathcal{C}$	Solve class constraint
solve_class_constraints	::=		
	|	$I \vdash \Sigma^{\mathcal{C}} \triangleright \mathcal{C}$	Solve class constraints
check_val_def	::=		
	|	$\Delta, I, E \vdash val\_def \triangleright E^{\mathrm{X}}$	Check a value definition
check_t_instance	::=		
	|	$\Delta, (\alpha_1, .., \alpha_n) \vdash t\ \mathbf{instance}$	Check that t be a typeclass in
check_defs	::=		
	|	$\overline{z_j}^{\,j}, D_1, E_1 \vdash def \triangleright D_2, E_2$	Check a definition
	|	$\overline{z_j}^{\,j}, D_1, E_1 \vdash defs \triangleright D_2, E_2$	Check definitions, given modu
judgement	::=		
	|	*convert_tnvars*	

| *look_m*
| *look_m_id*
| *look_tc*
| *check_t*
| *teq*
| *convert_typ*
| *convert_typs*
| *check_lit*
| *inst_field*
| *inst_ctor*
| *inst_val*
| *not_ctor*
| *not_shadowed*
| *check_pat*
| *id_field*
| *id_value*
| *check_exp*
| *check_rule*
| *check_texp_tc*
| *check_texps_tc*
| *check_texp*
| *check_texps*
| *convert_class*
| *solve_class_constraint*
| *solve_class_constraints*
| *check_val_def*
| *check_t_instance*
| *check_defs*

user_syntax ::=
| n
| *num*
| *hex*
| *bin*
| *string*
| *regexp*
| x
| ix
| l
| x^l
| ix^l
| α
| α^l
| N
| N^l
| *id*

| tnv
| $tnvar^{l}$
| $tnvs$
| $tnvars^{l}$
| $Nexp\_aux$
| $Nexp$
| $Nexp\_constraint$
| typ_aux
| typ
| lit_aux
| lit
| $;^{?}$
| pat_aux
| pat
| $fpat$
| $|^{?}$
| exp_aux
| exp
| q
| $qbind$
| $fexp$
| $fexps$
| $pexp$
| $psexp$
| $tannot^{?}$
| $funcl\_aux$
| $letbind\_aux$
| $letbind$
| $funcl$
| $id^{?}$
| $rule\_aux$
| $rule$
| $typs$
| $ctor\_def$
| $texp$
| $name^{?}$
| td
| c
| cs
| c_pre
| $typschm$
| $instschm$
| $target$
| τ
| $\tau^{?}$
| val_def

| val_spec
| def_aux
| def
| $;;^?$
| $defs$
| p
| σ
| t
| ne
| t_args
| t_multi
| nec
| $names$
| $\mathcal{C}$
| env_tag
| v_desc
| f_desc
| $\Sigma^{\mathcal{C}}$
| $\Sigma^{\mathcal{N}}$
| E
| E^{X}
| E^{F}
| E^{M}
| E^{P}
| E^{L}
| tc_abbrev
| tc_def
| Δ
| δ
| $inst$
| I
| D
| xs
| $terminals$
| $formula$

$\boxed{tnvars^{l} \rightsquigarrow tnvs}$

$$\frac{tnvar_1^{l} \rightsquigarrow tnv_1 \quad .. \quad tnvar_n^{l} \rightsquigarrow tnv_n}{tnvar_1^{l} \,..\, tnvar_n^{l} \rightsquigarrow tnv_1 \,..\, tnv_n} \quad \text{CONVERT\_TNVARS\_NONE}$$

$\boxed{tnvar^{l} \rightsquigarrow tnv}$

$$\frac{}{\alpha\, l \rightsquigarrow \alpha} \quad \text{CONVERT\_TNVAR\_A}$$

$$\frac{}{N\, l \rightsquigarrow N} \quad \text{CONVERT\_TNVAR\_N}$$

$\boxed{E_1(x_1^{l} \,..\, x_n^{l}) \triangleright E_2}$ Name path lookup

$$\frac{}{E(\,) \triangleright E} \quad \text{LOOK\_M\_NONE}$$

$$\frac{E^{\mathrm{M}}(x) \triangleright E_1 \quad E_1(\overline{y_i^l}^{\,i}) \triangleright E_2}{\langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}}\rangle (x\ l\ \overline{y_i^l}^{\,i}) \triangleright E_2}\ \textsc{look\_m\_some}$$

$\boxed{E_1(id) \triangleright E_2}$ Module identifier lookup

$$\frac{E_1(\overline{y_i^l}^{\,i}\ x\ l_1) \triangleright E_2}{E_1(\overline{y_i^l.}^{\,i}\ x\ l_1\ l_2) \triangleright E_2}\ \textsc{look\_m\_id\_all}$$

$\boxed{E(id) \triangleright p}$ Path identifier lookup

$$\frac{E(\overline{y_i^l}^{\,i}) \triangleright \langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}}\rangle \quad E^{\mathrm{P}}(x) \triangleright p}{E(\overline{y_i^l.}^{\,i}\ x\ l_1\ l_2) \triangleright p}\ \textsc{look\_tc\_all}$$

$\boxed{\Delta \vdash t\ \mathbf{ok}}$ Well-formed types

$$\frac{}{\Delta \vdash \alpha\ \mathbf{ok}}\ \textsc{check\_t\_var}$$

$$\frac{\Delta \vdash t_1\ \mathbf{ok} \quad \Delta \vdash t_2\ \mathbf{ok}}{\Delta \vdash t_1 \to t_2\ \mathbf{ok}}\ \textsc{check\_t\_fn}$$

$$\frac{\Delta \vdash t_1\ \mathbf{ok} \quad .... \quad \Delta \vdash t_n\ \mathbf{ok}}{\Delta \vdash t_1 * .... * t_n\ \mathbf{ok}}\ \textsc{check\_t\_tup}$$

$$\frac{\Delta(p) \triangleright tnv_1 .. tnv_n\ tc\_abbrev \quad \Delta, tnv_1 \vdash t_1\ \mathbf{ok} \quad .. \quad \Delta, tnv_n \vdash t_n\ \mathbf{ok}}{\Delta \vdash p\ t_1 .. t_n\ \mathbf{ok}}\ \textsc{check\_t\_app}$$

$\boxed{\Delta, tnv \vdash t\ \mathbf{ok}}$ Well-formed type/Nexps matching the application type variable

$$\frac{\Delta \vdash t\ \mathbf{ok}}{\Delta, \alpha \vdash t\ \mathbf{ok}}\ \textsc{check\_tlen\_t}$$

$$\frac{}{\Delta, N \vdash ne\ \mathbf{ok}}\ \textsc{check\_tlen\_len}$$

$\boxed{\Delta \vdash t_1 = t_2}$ Type equality

$$\frac{\Delta \vdash t\ \mathbf{ok}}{\Delta \vdash t = t}\ \textsc{teq\_refl}$$

$$\frac{\Delta \vdash t_2 = t_1}{\Delta \vdash t_1 = t_2}\ \textsc{teq\_sym}$$

$$\frac{\Delta \vdash t_1 = t_2 \quad \Delta \vdash t_2 = t_3}{\Delta \vdash t_1 = t_3}\ \textsc{teq\_trans}$$

$$\frac{\Delta \vdash t_1 = t_3 \quad \Delta \vdash t_2 = t_4}{\Delta \vdash t_1 \to t_2 = t_3 \to t_4}\ \textsc{teq\_arrow}$$

$$\frac{\Delta \vdash t_1 = u_1 \quad .... \quad \Delta \vdash t_n = u_n}{\Delta \vdash t_1 * .... * t_n = u_1 * .... * u_n}\ \textsc{teq\_tup}$$

$$\frac{\begin{array}{c}\Delta(p) \triangleright \alpha_1 .. \alpha_n \\ \Delta \vdash t_1 = u_1 \quad .. \quad \Delta \vdash t_n = u_n\end{array}}{\Delta \vdash p\ t_1 .. t_n = p\ u_1 .. u_n}\ \text{TEQ\_APP}$$

$$\frac{\Delta(p) \triangleright \alpha_1 .. \alpha_n .u}{\Delta \vdash p\ t_1 .. t_n = \{\alpha_1 \mapsto t_1 .. \alpha_n \mapsto t_n\}(u)}\ \text{TEQ\_EXPAND}$$

$$\frac{ne = \mathbf{normalize}\,(ne')}{\Delta \vdash ne = ne'}\ \text{TEQ\_NEXP}$$

$\boxed{\Delta, E \vdash typ \rightsquigarrow t}$ Convert source types to internal types

$$\frac{}{\Delta, E \vdash \alpha\ l'\ l \rightsquigarrow \alpha}\ \text{CONVERT\_TYP\_VAR}$$

$$\frac{\begin{array}{c}\Delta, E \vdash typ_1 \rightsquigarrow t_1 \\ \Delta, E \vdash typ_2 \rightsquigarrow t_2\end{array}}{\Delta, E \vdash typ_1 \to typ_2\ l \rightsquigarrow t_1 \to t_2}\ \text{CONVERT\_TYP\_FN}$$

$$\frac{\Delta, E \vdash typ_1 \rightsquigarrow t_1 \quad .... \quad \Delta, E \vdash typ_n \rightsquigarrow t_n}{\Delta, E \vdash typ_1 * .... * typ_n\ l \rightsquigarrow t_1 * .... * t_n}\ \text{CONVERT\_TYP\_TUP}$$

$$\frac{\begin{array}{l}\Delta, E \vdash typ_1 \rightsquigarrow t_1 \quad .. \quad \Delta, E \vdash typ_n \rightsquigarrow t_n \\ E(id) \triangleright p \\ \Delta(p) \triangleright \alpha_1 .. \alpha_n\ tc\_abbrev\end{array}}{\Delta, E \vdash id\ typ_1 .. typ_n\ l \rightsquigarrow p\ t_1 .. t_n}\ \text{CONVERT\_TYP\_APP}$$

$$\frac{\vdash Nexp \rightsquigarrow ne}{\Delta, E \vdash Nexp\ \rightsquigarrow ne}\ \text{CONVERT\_TYP\_NEXP}$$

$$\frac{\Delta, E \vdash typ \rightsquigarrow t}{\Delta, E \vdash (typ)\ l \rightsquigarrow t}\ \text{CONVERT\_TYP\_PAREN}$$

$$\frac{\begin{array}{c}\Delta, E \vdash typ \rightsquigarrow t_1 \\ \Delta \vdash t_1 = t_2\end{array}}{\Delta, E \vdash typ \rightsquigarrow t_2}\ \text{CONVERT\_TYP\_EQ}$$

$\boxed{\vdash Nexp \rightsquigarrow ne}$ Convert and normalize numeric expressions

$$\frac{}{\vdash N\ l \rightsquigarrow N}\ \text{CONVERT\_NEXP\_VAR}$$

$$\frac{}{\vdash num\ \rightsquigarrow num}\ \text{CONVERT\_NEXP\_NUM}$$

$$\frac{}{\vdash num\ * N\ \rightsquigarrow num * N}\ \text{CONVERT\_NEXP\_MULT}$$

$$\frac{\begin{array}{c}\vdash Nexp_1 \rightsquigarrow ne_1 \\ \vdash Nexp_2 \rightsquigarrow ne_2\end{array}}{\vdash Nexp_1 + Nexp_2\ \rightsquigarrow ne_1 + ne_2}\ \text{CONVERT\_NEXP\_ADD}$$

$\boxed{\Delta, E \vdash typs \rightsquigarrow t\_multi}$

$$\frac{\Delta, E \vdash typ_1 \rightsquigarrow t_1 \quad .. \quad \Delta, E \vdash typ_n \rightsquigarrow t_n}{\Delta, E \vdash typ_1 * .. * typ_n \rightsquigarrow (t_1 * .. * t_n)}\ \text{CONVERT\_TYPS\_ALL}$$

$\boxed{\vdash lit : t}$ Typing literal constants

$$\frac{}{\vdash \mathbf{true}\ l : \_\_\mathbf{bool}}\ \text{CHECK\_LIT\_TRUE}$$

$$\frac{}{\vdash \mathbf{false}\ l : \_\_\mathbf{bool}}\ \text{CHECK\_LIT\_FALSE}$$

$$\frac{}{\vdash num\ l : \_\_\mathbf{num}}\ \text{CHECK\_LIT\_NUM}$$

$$\frac{num = \mathbf{bitlength}\ (hex)}{\vdash hex\ l : \_\_\mathbf{vector}\ num\ \_\_\mathbf{bit}}\ \text{CHECK\_LIT\_HEX}$$

$$\frac{num = \mathbf{bitlength}\ (bin)}{\vdash bin\ l : \_\_\mathbf{vector}\ num\ \_\_\mathbf{bit}}\ \text{CHECK\_LIT\_BIN}$$

$$\frac{}{\vdash string\ l : \_\_\mathbf{string}}\ \text{CHECK\_LIT\_STRING}$$

$$\frac{}{\vdash ()\ l : \_\_\mathbf{unit}}\ \text{CHECK\_LIT\_UNIT}$$

$$\frac{}{\vdash \mathbf{bitzero}\ l : \_\_\mathbf{bit}}\ \text{CHECK\_LIT\_BITZERO}$$

$$\frac{}{\vdash \mathbf{bitone}\ l : \_\_\mathbf{bit}}\ \text{CHECK\_LIT\_BITONE}$$

$\boxed{\Delta, E \vdash\ \mathbf{field}\ id : p\ t\_args \to t \triangleright (x\ \mathbf{of}\ names)}$ Field typing (also returns canonical field names)

$$\frac{\begin{array}{l} E(\overline{x_i^l}^{\,i}) \triangleright \langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \\ E^{\mathrm{F}}(y) \triangleright \langle\, \mathbf{forall}\ tnv_1\ ..\ tnv_n.p \to t, (z\ \mathbf{of}\ names) \rangle \\ \Delta \vdash t_1\ \mathbf{ok} \quad .. \quad \Delta \vdash t_n\ \mathbf{ok} \end{array}}{\Delta, E \vdash\ \mathbf{field}\ \overline{x_i^l}^{\,i}\ y\ l_1\ l_2 : p\ t_1\ ..\ t_n \to \{tnv_1 \mapsto t_1\ ..\ tnv_n \mapsto t_n\}(t) \triangleright (z\ \mathbf{of}\ names)}\ \text{INST\_FIELD\_ALL}$$

$\boxed{\Delta, E \vdash\ \mathbf{ctor}\ id : t\_multi \to p\ t\_args \triangleright (x\ \mathbf{of}\ names)}$ Data constructor typing (also returns canonical constru

$$\frac{\begin{array}{l} E(\overline{x_i^l}^{\,i}) \triangleright \langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \\ E^{\mathrm{X}}(y) \triangleright \langle\, \mathbf{forall}\ tnv_1\ ..\ tnv_n.t\_multi \to p, (z\ \mathbf{of}\ names) \rangle \\ \Delta \vdash t_1\ \mathbf{ok} \quad .. \quad \Delta \vdash t_n\ \mathbf{ok} \end{array}}{\Delta, E \vdash\ \mathbf{ctor}\ \overline{x_i^l}^{\,i}\ y\ l_1\ l_2 : \{tnv_1 \mapsto t_1\ ..\ tnv_n \mapsto t_n\}(t\_multi) \to p\ t_1\ ..\ t_n \triangleright (z\ \mathbf{of}\ names)}\ \text{INST\_CTOR\_ALL}$$

$\boxed{\Delta, E \vdash\ \mathbf{val}\ id : t \triangleright \Sigma^{\mathcal{C}}}$ Typing top-level bindings, collecting typeclass constraints

$$\frac{\begin{array}{l} E(\overline{x_i^l}^{\,i}) \triangleright \langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \\ E^{\mathrm{X}}(y) \triangleright \langle\, \mathbf{forall}\ tnv_1\ ..\ tnv_n.(p_1\ tnv_1')\ ..\ (p_i\ tnv_i') \Rightarrow t, env\_tag \rangle \\ \Delta \vdash t_1\ \mathbf{ok} \quad .. \quad \Delta \vdash t_n\ \mathbf{ok} \\ \sigma = \{tnv_1 \mapsto t_1\ ..\ tnv_n \mapsto t_n\} \end{array}}{\Delta, E \vdash\ \mathbf{val}\ \overline{x_i^l}^{\,i}\ y\ l_1\ l_2 : \sigma(t) \triangleright \{(p_1\ \sigma(tnv_1')),\ ..\ ,(p_i\ \sigma(tnv_i'))\}}\ \text{INST\_VAL\_ALL}$$

$\boxed{E, E^{\mathrm{L}} \vdash x\ \mathbf{not\ ctor}}$ v is not bound to a data constructor

$$\frac{E^{\mathrm{L}}(x) \triangleright t}{E, E^{\mathrm{L}} \vdash x\ \mathbf{not\ ctor}}\ \text{NOT\_CTOR\_VAL}$$

$$\frac{x \notin \mathbf{dom}\ (E^{\mathrm{X}})}{\langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle, E^{\mathrm{L}} \vdash x\ \mathbf{not\ ctor}}\ \text{NOT\_CTOR\_UNBOUND}$$

$$\frac{E^{\mathrm{X}}(x) \triangleright \langle\, \mathbf{forall}\ tnv_1\ ..\ tnv_n.(p_1\ tnv_1')\ ..\ (p_i\ tnv_i') \Rightarrow t, env\_tag \rangle}{\langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle, E^{\mathrm{L}} \vdash x\ \mathbf{not\ ctor}}\ \text{NOT\_CTOR\_BOUND}$$

$\boxed{E^{\mathrm{L}} \vdash id\ \mathbf{not\ shadowed}}$ id is not lexically shadowed

$$\frac{x \notin \mathbf{dom}\ (E^{\mathrm{L}})}{E^{\mathrm{L}} \vdash\ x\ l_1\ l_2\ \mathbf{not\ shadowed}}\ \text{NOT\_SHADOWED\_SING}$$

$$\frac{}{E^{\mathrm{L}} \vdash x_1^l \ldots x_n^l.y^l.z^l\ l\ \mathbf{not\ shadowed}}\ \text{NOT\_SHADOWED\_MULTI}$$

$\boxed{\Delta, E, E_1^{\mathrm{L}} \vdash pat : t \triangleright E_2^{\mathrm{L}}}$ Typing patterns, building their binding environment

$$\frac{\Delta, E, E_1^{\mathrm{L}} \vdash pat\_aux : t \triangleright E_2^{\mathrm{L}}}{\Delta, E, E_1^{\mathrm{L}} \vdash pat\_aux\ l : t \triangleright E_2^{\mathrm{L}}}\ \text{CHECK\_PAT\_ALL}$$

$\boxed{\Delta, E, E_1^{\mathrm{L}} \vdash pat\_aux : t \triangleright E_2^{\mathrm{L}}}$ Typing patterns, building their binding environment

$$\frac{\Delta \vdash t\ \mathbf{ok}}{\Delta, E, E^{\mathrm{L}} \vdash \_ : t \triangleright \{\,\}}\ \text{CHECK\_PAT\_AUX\_WILD}$$

$$\frac{\begin{array}{l}\Delta, E, E_1^{\mathrm{L}} \vdash pat : t \triangleright E_2^{\mathrm{L}} \\ x \notin \mathbf{dom}\,(E_2^{\mathrm{L}})\end{array}}{\Delta, E, E_1^{\mathrm{L}} \vdash (pat\ \mathbf{as}\ x\ l) : t \triangleright E_2^{\mathrm{L}} \uplus \{x \mapsto t\}}\ \text{CHECK\_PAT\_AUX\_AS}$$

$$\frac{\begin{array}{l}\Delta, E, E_1^{\mathrm{L}} \vdash pat : t \triangleright E_2^{\mathrm{L}} \\ \Delta, E \vdash typ \rightsquigarrow t\end{array}}{\Delta, E, E_1^{\mathrm{L}} \vdash (pat : typ) : t \triangleright E_2^{\mathrm{L}}}\ \text{CHECK\_PAT\_AUX\_TYP}$$

$$\frac{\begin{array}{l}\Delta, E \vdash \mathbf{ctor}\ id : (t_1 * .. * t_n) \to p\ t\_args \triangleright (x\ \mathbf{of}\ names) \\ E^{\mathrm{L}} \vdash id\ \mathbf{not\ shadowed} \\ \Delta, E, E^{\mathrm{L}} \vdash pat_1 : t_1 \triangleright E_1^{\mathrm{L}} \quad .. \quad \Delta, E, E^{\mathrm{L}} \vdash pat_n : t_n \triangleright E_n^{\mathrm{L}} \\ \mathbf{disjoint\ doms}\,(E_1^{\mathrm{L}}, .., E_n^{\mathrm{L}})\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash id\ pat_1 .. pat_n : p\ t\_args \triangleright E_1^{\mathrm{L}} \uplus .. \uplus E_n^{\mathrm{L}}}\ \text{CHECK\_PAT\_AUX\_IDENT\_CONSTR}$$

$$\frac{\begin{array}{l}\Delta \vdash t\ \mathbf{ok} \\ E, E^{\mathrm{L}} \vdash x\ \mathbf{not\ ctor}\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash\ x\ l_1\ l_2\ : t \triangleright \{x \mapsto t\}}\ \text{CHECK\_PAT\_AUX\_VAR}$$

$$\frac{\begin{array}{l}\overline{\Delta, E \vdash \mathbf{field}\ id_i : p\ t\_args \to t_i \triangleright (x_i\ \mathbf{of}\ names)}^{\,i} \\ \overline{\Delta, E, E^{\mathrm{L}} \vdash pat_i : t_i \triangleright E_i^{\mathrm{L}}}^{\,i} \\ \mathbf{disjoint\ doms}\,(\overline{E_i^{\mathrm{L}}}^{\,i}) \\ \mathbf{duplicates}\,(\overline{x_i}^{\,i}) = \emptyset\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash \langle|\ \overline{id_i = pat_i\ l_i}^{\,i}\ ;^?|\rangle : p\ t\_args \triangleright \uplus\, \overline{E_i^{\mathrm{L}}}^{\,i}}\ \text{CHECK\_PAT\_AUX\_RECORD}$$

$$\frac{\begin{array}{l}\Delta, E, E^{\mathrm{L}} \vdash pat_1 : t \triangleright E_1^{\mathrm{L}} \quad ... \quad \Delta, E, E^{\mathrm{L}} \vdash pat_n : t \triangleright E_n^{\mathrm{L}} \\ \mathbf{disjoint\ doms}\,(E_1^{\mathrm{L}}, ..., E_n^{\mathrm{L}}) \\ \mathbf{length}\,(pat_1 ... pat_n) = num\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash [|pat_1; ...; pat_n|] : \_\_\mathbf{vector}\ num\ t \triangleright E_1^{\mathrm{L}} \uplus ... \uplus E_n^{\mathrm{L}}}\ \text{CHECK\_PAT\_AUX\_VECTOR}$$

$$\frac{\begin{array}{l}\Delta, E, E^{\mathrm{L}} \vdash pat_1 : \_\_\mathbf{vector}\ ne_1\ t \triangleright E_1^{\mathrm{L}} \quad ... \quad \Delta, E, E^{\mathrm{L}} \vdash pat_n : \_\_\mathbf{vector}\ ne_n\ t \triangleright E_n^{\mathrm{L}} \\ \mathbf{disjoint\ doms}\,(E_1^{\mathrm{L}}, ..., E_n^{\mathrm{L}}) \\ ne' = ne_1 + ... + ne_n\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash [|pat_1 ... pat_n|] : \_\_\mathbf{vector}\ ne'\ t \triangleright E_1^{\mathrm{L}} \uplus ... \uplus E_n^{\mathrm{L}}}\ \text{CHECK\_PAT\_AUX\_VECTOR(}$$

$$\frac{\begin{array}{l}\Delta, E, E^{\mathrm{L}} \vdash pat_1 : t_1 \triangleright E_1^{\mathrm{L}} \quad .... \quad \Delta, E, E^{\mathrm{L}} \vdash pat_n : t_n \triangleright E_n^{\mathrm{L}} \\ \mathbf{disjoint\ doms}\,(E_1^{\mathrm{L}}, ..., E_n^{\mathrm{L}})\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash (pat_1, ..., pat_n) : t_1 * .... * t_n \triangleright E_1^{\mathrm{L}} \uplus .... \uplus E_n^{\mathrm{L}}}\ \text{CHECK\_PAT\_AUX\_TUP}$$

$$\frac{\begin{array}{l}\Delta \vdash t\ \mathbf{ok} \\ \Delta, E, E^{\mathrm{L}} \vdash pat_1 : t \triangleright E_1^{\mathrm{L}} \quad .. \quad \Delta, E, E^{\mathrm{L}} \vdash pat_n : t \triangleright E_n^{\mathrm{L}} \\ \mathbf{disjoint\ doms}\,(E_1^{\mathrm{L}}, .., E_n^{\mathrm{L}})\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash [pat_1; ..; pat_n\ ;^?] : \_\_\mathbf{list}\ t \triangleright E_1^{\mathrm{L}} \uplus .. \uplus E_n^{\mathrm{L}}}\ \text{CHECK\_PAT\_AUX\_LIST}$$

$$\frac{\Delta, E, E_1^{\mathrm{L}} \vdash pat : t \triangleright E_2^{\mathrm{L}}}{\Delta, E, E_1^{\mathrm{L}} \vdash (pat) : t \triangleright E_2^{\mathrm{L}}} \quad \text{CHECK\_PAT\_AUX\_PAREN}$$

$$\frac{\begin{array}{l}\Delta, E, E_1^{\mathrm{L}} \vdash pat_1 : t \triangleright E_2^{\mathrm{L}} \\ \Delta, E, E_1^{\mathrm{L}} \vdash pat_2 : \_\_\mathbf{list}\ t \triangleright E_3^{\mathrm{L}} \\ \mathbf{disjoint\ doms}\ (E_2^{\mathrm{L}}, E_3^{\mathrm{L}})\end{array}}{\Delta, E, E_1^{\mathrm{L}} \vdash pat_1 :: pat_2 : \_\_\mathbf{list}\ t \triangleright E_2^{\mathrm{L}} \uplus E_3^{\mathrm{L}}} \quad \text{CHECK\_PAT\_AUX\_CONS}$$

$$\frac{\vdash lit : t}{\Delta, E, E^{\mathrm{L}} \vdash lit : t \triangleright \{\,\}} \quad \text{CHECK\_PAT\_AUX\_LIT}$$

$$\frac{E, E^{\mathrm{L}} \vdash x\ \mathbf{not\ ctor}}{\Delta, E, E^{\mathrm{L}} \vdash x\ l + num : \_\_\mathbf{num}\ \triangleright \{x \mapsto \_\_\mathbf{num}\ \}} \quad \text{CHECK\_PAT\_AUX\_NUM\_ADD}$$

$\boxed{E \vdash id\ \mathbf{field}}$ Check that the identifier is a permissible field identifier

$$\frac{E^{\mathrm{F}}(x) \triangleright f\_desc}{\langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \vdash x\ l_1\ l_2\ \mathbf{field}} \quad \text{ID\_FIELD\_EMPTY}$$

$$\frac{\begin{array}{l}E^{\mathrm{M}}(x) \triangleright E \\ x \notin \mathbf{dom}\,(E^{\mathrm{F}}) \\ E \vdash \overline{y_i^l.}^{\,i}\ z^l\ l_2\ \mathbf{field}\end{array}}{\langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \vdash x\ l_1.\ \overline{y_i^l.}^{\,i}\ z^l\ l_2\ \mathbf{field}} \quad \text{ID\_FIELD\_CONS}$$

$\boxed{E \vdash id\ \mathbf{value}}$ Check that the identifier is a permissible value identifier

$$\frac{E^{\mathrm{X}}(x) \triangleright v\_desc}{\langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \vdash x\ l_1\ l_2\ \mathbf{value}} \quad \text{ID\_VALUE\_EMPTY}$$

$$\frac{\begin{array}{l}E^{\mathrm{M}}(x) \triangleright E \\ x \notin \mathbf{dom}\,(E^{\mathrm{X}}) \\ E \vdash \overline{y_i^l.}^{\,i}\ z^l\ l_2\ \mathbf{value}\end{array}}{\langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \vdash x\ l_1.\ \overline{y_i^l.}^{\,i}\ z^l\ l_2\ \mathbf{value}} \quad \text{ID\_VALUE\_CONS}$$

$\boxed{\Delta, E, E^{\mathrm{L}} \vdash exp : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}$ Typing expressions, collecting typeclass and index constraints

$$\frac{\Delta, E, E^{\mathrm{L}} \vdash exp\_aux : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}{\Delta, E, E^{\mathrm{L}} \vdash exp\_aux\ l : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}} \quad \text{CHECK\_EXP\_ALL}$$

$\boxed{\Delta, E, E^{\mathrm{L}} \vdash exp\_aux : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}$ Typing expressions, collecting typeclass and index constraints

$$\frac{E^{\mathrm{L}}(x) \triangleright t}{\Delta, E, E^{\mathrm{L}} \vdash x\ l_1\ l_2 : t \triangleright \{\,\}, \{\,\}} \quad \text{CHECK\_EXP\_AUX\_VAR}$$

$$\frac{}{\Delta, E, E^{\mathrm{L}} \vdash N : num \triangleright \{\,\}, \{\,\}} \quad \text{CHECK\_EXP\_AUX\_NVAR}$$

$$\frac{\begin{array}{l}E^{\mathrm{L}} \vdash id\ \mathbf{not\ shadowed} \\ E \vdash id\ \mathbf{value} \\ \Delta, E \vdash\ \mathbf{ctor}\ id : t\_multi \to p\ t\_args \triangleright (x\ \mathbf{of}\ names)\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash id : \mathbf{curry}\ (t\_multi, p\ t\_args) \triangleright \{\,\}, \{\,\}} \quad \text{CHECK\_EXP\_AUX\_CTOR}$$

$$\frac{\begin{array}{l}E^{\mathrm{L}} \vdash id\ \mathbf{not\ shadowed} \\ E \vdash id\ \mathbf{value} \\ \Delta, E \vdash\ \mathbf{val}\ id : t \triangleright \Sigma^{\mathcal{C}}\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash id : t \triangleright \Sigma^{\mathcal{C}}, \{\,\}} \quad \text{CHECK\_EXP\_AUX\_VAL}$$

$$\frac{\begin{array}{l}\Delta, E, E^{\mathrm{L}} \vdash pat_1 : t_1 \triangleright E_1^{\mathrm{L}} \quad ... \quad \Delta, E, E^{\mathrm{L}} \vdash pat_n : t_n \triangleright E_n^{\mathrm{L}} \\ \Delta, E, E^{\mathrm{L}} \uplus E_1^{\mathrm{L}} \uplus ... \uplus E_n^{\mathrm{L}} \vdash exp : u \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \\ \mathbf{disjoint\ doms}\,(E_1^{\mathrm{L}}, ..., E_n^{\mathrm{L}})\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash \mathbf{fun}\, pat_1 \,...\, pat_n \rightarrow exp\ l : \mathbf{curry}\,((t_1 * ... * t_n), u) \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}\ \text{CHECK\_EXP\_AUX\_FN}$$

$$\frac{\begin{array}{l}\overline{\Delta, E, E^{\mathrm{L}} \vdash pat_i : t \triangleright E_i^{\mathrm{L}}}^{\,i} \\ \overline{\Delta, E, E^{\mathrm{L}} \uplus E_i^{\mathrm{L}} \vdash exp_i : u \triangleright \Sigma^{\mathcal{C}}{}_i, \Sigma^{\mathcal{N}}{}_i}^{\,i}\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash \mathbf{function}\,|^?\, \overline{pat_i \rightarrow exp_i\ l_i}^{\,i}\, \mathbf{end} : t \rightarrow u \triangleright \overline{\Sigma^{\mathcal{C}}{}_i}^{\,i}, \overline{\Sigma^{\mathcal{N}}{}_i}^{\,i}}\ \text{CHECK\_EXP\_AUX\_FUNCTION}$$

$$\frac{\begin{array}{l}\Delta, E, E^{\mathrm{L}} \vdash exp_1 : t_1 \rightarrow t_2 \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \\ \Delta, E, E^{\mathrm{L}} \vdash exp_2 : t_1 \triangleright \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash exp_1\ exp_2 : t_2 \triangleright \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_1 \cup \Sigma^{\mathcal{N}}{}_2}\ \text{CHECK\_EXP\_AUX\_APP}$$

$$\frac{\begin{array}{l}\Delta, E, E^{\mathrm{L}} \vdash (ix) : t_1 \rightarrow t_2 \rightarrow t_3 \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \\ \Delta, E, E^{\mathrm{L}} \vdash exp_1 : t_1 \triangleright \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2 \\ \Delta, E, E^{\mathrm{L}} \vdash exp_2 : t_2 \triangleright \Sigma^{\mathcal{C}}{}_3, \Sigma^{\mathcal{N}}{}_3\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash exp_1\ ix\ l\ exp_2 : t_3 \triangleright \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2 \cup \Sigma^{\mathcal{C}}{}_3, \Sigma^{\mathcal{N}}{}_1 \cup \Sigma^{\mathcal{N}}{}_2 \cup \Sigma^{\mathcal{N}}{}_3}\ \text{CHECK\_EXP\_AUX\_INFIX\_APP1}$$

$$\frac{\begin{array}{l}\Delta, E, E^{\mathrm{L}} \vdash\ x\ : t_1 \rightarrow t_2 \rightarrow t_3 \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \\ \Delta, E, E^{\mathrm{L}} \vdash exp_1 : t_1 \triangleright \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2 \\ \Delta, E, E^{\mathrm{L}} \vdash exp_2 : t_2 \triangleright \Sigma^{\mathcal{C}}{}_3, \Sigma^{\mathcal{N}}{}_3\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash exp_1\ `x`\ l\ exp_2 : t_3 \triangleright \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2 \cup \Sigma^{\mathcal{C}}{}_3, \Sigma^{\mathcal{N}}{}_1 \cup \Sigma^{\mathcal{N}}{}_2 \cup \Sigma^{\mathcal{N}}{}_3}\ \text{CHECK\_EXP\_AUX\_INFIX\_APP2}$$

$$\frac{\begin{array}{l}\overline{\Delta, E \vdash\ \mathbf{field}\ id_i : p\ t\_args \rightarrow t_i \triangleright (x_i\ \mathbf{of}\ names)}^{\,i} \\ \overline{\Delta, E, E^{\mathrm{L}} \vdash exp_i : t_i \triangleright \Sigma^{\mathcal{C}}{}_i, \Sigma^{\mathcal{N}}{}_i}^{\,i} \\ \mathbf{duplicates}\,(\,\overline{x_i}^{\,i}\,) = \emptyset \\ names = \{\,\overline{x_i}^{\,i}\,\}\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash \langle|\overline{id_i = exp_i\ l_i}^{\,i}\ ;^?\ l|\rangle : p\ t\_args \triangleright \overline{\Sigma^{\mathcal{C}}{}_i}^{\,i}, \overline{\Sigma^{\mathcal{N}}{}_i}^{\,i}}\ \text{CHECK\_EXP\_AUX\_RECORD}$$

$$\frac{\begin{array}{l}\overline{\Delta, E \vdash\ \mathbf{field}\ id_i : p\ t\_args \rightarrow t_i \triangleright (x_i\ \mathbf{of}\ names)}^{\,i} \\ \overline{\Delta, E, E^{\mathrm{L}} \vdash exp_i : t_i \triangleright \Sigma^{\mathcal{C}}{}_i, \Sigma^{\mathcal{N}}{}_i}^{\,i} \\ \mathbf{duplicates}\,(\,\overline{x_i}^{\,i}\,) = \emptyset \\ \Delta, E, E^{\mathrm{L}} \vdash exp : p\ t\_args \triangleright \Sigma^{\mathcal{C}\prime}, \Sigma^{\mathcal{N}\prime}\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash \langle|exp\ \mathbf{with}\ \overline{id_i = exp_i\ l_i}^{\,i}\ ;^?\ l|\rangle : p\ t\_args \triangleright \Sigma^{\mathcal{C}\prime} \cup \overline{\Sigma^{\mathcal{C}}{}_i}^{\,i}, \Sigma^{\mathcal{N}\prime} \cup \overline{\Sigma^{\mathcal{N}}{}_i}^{\,i}}\ \text{CHECK\_EXP\_AUX\_RECUP}$$

$$\frac{\begin{array}{l}\Delta, E, E^{\mathrm{L}} \vdash exp_1 : t \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad ... \quad \Delta, E, E^{\mathrm{L}} \vdash exp_n : t \triangleright \Sigma^{\mathcal{C}}{}_n, \Sigma^{\mathcal{N}}{}_n \\ \mathbf{length}\,(exp_1 \,...\, exp_n) = num\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash [|exp_1; \,...\,; exp_n\,|] : \_\_\mathbf{vector}\ num\ t \triangleright \Sigma^{\mathcal{C}}{}_1 \cup ... \cup \Sigma^{\mathcal{C}}{}_n, \Sigma^{\mathcal{N}}{}_1 \cup ... \cup \Sigma^{\mathcal{N}}{}_n}\ \text{CHECK\_EXP\_AUX\_VECTOR}$$

$$\frac{\begin{array}{l}\Delta, E, E^{\mathrm{L}} \vdash exp : \_\_\mathbf{vector}\ ne'\ t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \\ \vdash Nexp \rightsquigarrow ne\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash exp.(Nexp) : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \cup \{ne\langle ne'\}}\ \text{CHECK\_EXP\_AUX\_VECTORGET}$$

$$\frac{\begin{array}{l}\Delta, E, E^{\mathrm{L}} \vdash exp : \_\_\mathbf{vector}\ ne'\ t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \\ \vdash Nexp_1 \rightsquigarrow ne_1 \\ \vdash Nexp_2 \rightsquigarrow ne_2 \\ ne = ne_2 + (-ne_1)\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash exp.(Nexp_1..Nexp_2) : \_\_\mathbf{vector}\ ne\ t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \cup \{ne_1\langle ne_2\langle ne'\}}\ \text{CHECK\_EXP\_AUX\_VECTORSUB}$$

$$\frac{\begin{array}{l}E \vdash id\ \mathbf{field} \\ \Delta, E \vdash\ \mathbf{field}\ id : p\ t\_args \rightarrow t \triangleright (x\ \mathbf{of}\ names) \\ \Delta, E, E^{\mathrm{L}} \vdash exp : p\ t\_args \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash exp.id : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}\ \text{CHECK\_EXP\_AUX\_FIELD}$$

$$\frac{\overline{\Delta, E, E^{\mathrm{L}} \vdash pat_i : t \triangleright E_i^{\mathrm{L}}}^{\,i} \quad \overline{\Delta, E, E^{\mathrm{L}} \uplus E_i^{\mathrm{L}} \vdash exp_i : u \triangleright \Sigma^{\mathcal{C}}{}_i, \Sigma^{\mathcal{N}}{}_i}^{\,i} \quad \Delta, E, E^{\mathrm{L}} \vdash exp : t \triangleright \Sigma^{\mathcal{C}\prime}, \Sigma^{\mathcal{N}\prime}}{\Delta, E, E^{\mathrm{L}} \vdash \mathbf{match}\ exp\ \mathbf{with}\ |^{?}\ \overline{pat_i \rightarrow exp_i\ l_i}^{\,i}\ l\ \mathbf{end} : u \triangleright \Sigma^{\mathcal{C}\prime} \cup \overline{\Sigma^{\mathcal{C}}{}_i}^{\,i}, \Sigma^{\mathcal{N}\prime} \cup \overline{\Sigma^{\mathcal{N}}{}_i}^{\,i}}\ \text{CHECK\_EXP\_AUX\_CASE}$$

$$\frac{\Delta, E, E^{\mathrm{L}} \vdash exp : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \quad \Delta, E \vdash typ \rightsquigarrow t}{\Delta, E, E^{\mathrm{L}} \vdash (exp : typ) : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}\ \text{CHECK\_EXP\_AUX\_TYPED}$$

$$\frac{\Delta, E, E_1^{\mathrm{L}} \vdash letbind \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad \Delta, E, E_1^{\mathrm{L}} \uplus E_2^{\mathrm{L}} \vdash exp : t \triangleright \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2}{\Delta, E, E^{\mathrm{L}} \vdash \mathbf{let}\ letbind\ \mathbf{in}\ exp : t \triangleright \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_1 \cup \Sigma^{\mathcal{N}}{}_2}\ \text{CHECK\_EXP\_AUX\_LET}$$

$$\frac{\Delta, E, E^{\mathrm{L}} \vdash exp_1 : t_1 \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad .... \quad \Delta, E, E^{\mathrm{L}} \vdash exp_n : t_n \triangleright \Sigma^{\mathcal{C}}{}_n, \Sigma^{\mathcal{N}}{}_n}{\Delta, E, E^{\mathrm{L}} \vdash (exp_1, \ldots., exp_n) : t_1 * .... * t_n \triangleright \Sigma^{\mathcal{C}}{}_1 \cup .... \cup \Sigma^{\mathcal{C}}{}_n, \Sigma^{\mathcal{N}}{}_1 \cup .... \cup \Sigma^{\mathcal{N}}{}_n}\ \text{CHECK\_EXP\_AUX\_TUP}$$

$$\frac{\Delta \vdash t\ \mathbf{ok} \quad \Delta, E, E^{\mathrm{L}} \vdash exp_1 : t \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad .. \quad \Delta, E, E^{\mathrm{L}} \vdash exp_n : t \triangleright \Sigma^{\mathcal{C}}{}_n, \Sigma^{\mathcal{N}}{}_n}{\Delta, E, E^{\mathrm{L}} \vdash [exp_1; \ldots; exp_n\ ;^{?}] : \_\_\mathbf{list}\ t \triangleright \Sigma^{\mathcal{C}}{}_1 \cup .. \cup \Sigma^{\mathcal{C}}{}_n, \Sigma^{\mathcal{N}}{}_1 \cup .. \cup \Sigma^{\mathcal{N}}{}_n}\ \text{CHECK\_EXP\_AUX\_LIST}$$

$$\frac{\Delta, E, E^{\mathrm{L}} \vdash exp : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}{\Delta, E, E^{\mathrm{L}} \vdash (exp) : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}\ \text{CHECK\_EXP\_AUX\_PAREN}$$

$$\frac{\Delta, E, E^{\mathrm{L}} \vdash exp : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}{\Delta, E, E^{\mathrm{L}} \vdash \mathbf{begin}\ exp\ \mathbf{end} : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}\ \text{CHECK\_EXP\_AUX\_BEGIN}$$

$$\frac{\Delta, E, E^{\mathrm{L}} \vdash exp_1 : \_\_\mathbf{bool} \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad \Delta, E, E^{\mathrm{L}} \vdash exp_2 : t \triangleright \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2 \quad \Delta, E, E^{\mathrm{L}} \vdash exp_3 : t \triangleright \Sigma^{\mathcal{C}}{}_3, \Sigma^{\mathcal{N}}{}_3}{\Delta, E, E^{\mathrm{L}} \vdash \mathbf{if}\ exp_1\ \mathbf{then}\ exp_2\ \mathbf{else}\ exp_3 : t \triangleright \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2 \cup \Sigma^{\mathcal{C}}{}_3, \Sigma^{\mathcal{N}}{}_1 \cup \Sigma^{\mathcal{N}}{}_2 \cup \Sigma^{\mathcal{N}}{}_3}\ \text{CHECK\_EXP\_AUX\_IF}$$

$$\frac{\Delta, E, E^{\mathrm{L}} \vdash exp_1 : t \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad \Delta, E, E^{\mathrm{L}} \vdash exp_2 : \_\_\mathbf{list}\ t \triangleright \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2}{\Delta, E, E^{\mathrm{L}} \vdash exp_1 :: exp_2 : \_\_\mathbf{list}\ t \triangleright \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_1 \cup \Sigma^{\mathcal{N}}{}_2}\ \text{CHECK\_EXP\_AUX\_CONS}$$

$$\frac{\vdash lit : t}{\Delta, E, E^{\mathrm{L}} \vdash lit : t \triangleright \{\,\}, \{\,\}}\ \text{CHECK\_EXP\_AUX\_LIT}$$

$$\frac{\begin{array}{l}\overline{\Delta \vdash t_i\ \mathbf{ok}}^{\,i} \\ \Delta, E, E^{\mathrm{L}} \uplus \{\,\overline{x_i \mapsto t_i}^{\,i}\,\} \vdash exp_1 : t \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \\ \Delta, E, E^{\mathrm{L}} \uplus \{\,\overline{x_i \mapsto t_i}^{\,i}\,\} \vdash exp_2 : \_\_\mathbf{bool} \triangleright \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2 \\ \mathbf{disjoint}\ \mathbf{doms}\,(E^{\mathrm{L}}, \{\,\overline{x_i \mapsto t_i}^{\,i}\,\}) \\ E = \langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \\ \overline{x_i \notin \mathbf{dom}\,(E^{\mathrm{X}})}^{\,i}\end{array}}{\Delta, E, E^{\mathrm{L}} \vdash \{exp_1 | exp_2\} : \_\_\mathbf{set}\ t \triangleright \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_1 \cup \Sigma^{\mathcal{N}}{}_2}\ \text{CHECK\_EXP\_AUX\_SET\_COMP}$$

$$\frac{\Delta, E, E_1^{\mathrm{L}} \vdash \overline{qbind_i}^{\,i} \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_1 \quad \Delta, E, E_1^{\mathrm{L}} \uplus E_2^{\mathrm{L}} \vdash exp_1 : t \triangleright \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2 \quad \Delta, E, E_1^{\mathrm{L}} \uplus E_2^{\mathrm{L}} \vdash exp_2 : \_\_\mathbf{bool} \triangleright \Sigma^{\mathcal{C}}{}_3, \Sigma^{\mathcal{N}}{}_3}{\Delta, E, E_1^{\mathrm{L}} \vdash \{exp_1 | \mathbf{forall}\ \overline{qbind_i}^{\,i} | exp_2\} : \_\_\mathbf{set}\ t \triangleright \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2 \cup \Sigma^{\mathcal{C}}{}_3, \Sigma^{\mathcal{N}}{}_2 \cup \Sigma^{\mathcal{N}}{}_3}\ \text{CHECK\_EXP\_AUX\_SET\_COMP\_}$$

$$\frac{\Delta \vdash t\ \mathbf{ok} \quad \Delta, E, E^{\mathrm{L}} \vdash exp_1 : t \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad .. \quad \Delta, E, E^{\mathrm{L}} \vdash exp_n : t \triangleright \Sigma^{\mathcal{C}}{}_n, \Sigma^{\mathcal{N}}{}_n}{\Delta, E, E^{\mathrm{L}} \vdash \{exp_1; \ldots; exp_n\ ;^{?}\} : \_\_\mathbf{set}\ t \triangleright \Sigma^{\mathcal{C}}{}_1 \cup .. \cup \Sigma^{\mathcal{C}}{}_n, \Sigma^{\mathcal{N}}{}_1 \cup .. \cup \Sigma^{\mathcal{N}}{}_n}\ \text{CHECK\_EXP\_AUX\_SET}$$

$$\frac{\Delta, E, E_1^{\mathrm{L}} \vdash \overline{qbind_i}^{\,i} \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_1 \quad \Delta, E, E_1^{\mathrm{L}} \uplus E_2^{\mathrm{L}} \vdash exp : \_\_\mathbf{bool} \triangleright \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2}{\Delta, E, E_1^{\mathrm{L}} \vdash q\ \overline{qbind_i}^{\,i}\ .exp : \_\_\mathbf{bool} \triangleright \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2}\ \text{CHECK\_EXP\_AUX\_QUANT}$$

$$\frac{\Delta, E, E_1^{\mathrm{L}} \vdash \mathbf{list}\ \overline{qbind_i}^{\,i} \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_1 \quad \Delta, E, E_1^{\mathrm{L}} \uplus E_2^{\mathrm{L}} \vdash exp_1 : t \triangleright \Sigma^{\mathcal{C}}{}_2, \Sigma^{\mathcal{N}}{}_2 \quad \Delta, E, E_1^{\mathrm{L}} \uplus E_2^{\mathrm{L}} \vdash exp_2 : \_\_\mathbf{bool} \triangleright \Sigma^{\mathcal{C}}{}_3, \Sigma^{\mathcal{N}}{}_3}{\Delta, E, E_1^{\mathrm{L}} \vdash [exp_1 |\, \mathbf{forall}\ \overline{qbind_i}^{\,i}\ | exp_2] : \_\_\mathbf{list}\ t \triangleright \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2 \cup \Sigma^{\mathcal{C}}{}_3, \Sigma^{\mathcal{N}}{}_2 \cup \Sigma^{\mathcal{N}}{}_3}\ \text{CHECK\_EXP\_AUX\_LIST\_COMP\_}$$

$\boxed{\Delta, E, E_1^{\mathrm{L}} \vdash qbind_1 \,..\, qbind_n \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}}$ Build the environment for quantifier bindings, collecting typeclass cons

$$\frac{}{\Delta, E, E^{\mathrm{L}} \vdash \triangleright \{\,\}, \{\,\}}\ \text{CHECK\_LISTQUANT\_BINDING\_EMPTY}$$

$$\frac{\Delta \vdash t\ \mathbf{ok} \quad \Delta, E, E_1^{\mathrm{L}} \uplus \{x \mapsto t\} \vdash \overline{qbind_i}^{\,i} \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_1 \quad \mathbf{disjoint\ doms}\,(\{x \mapsto t\}, E_2^{\mathrm{L}})}{\Delta, E, E_1^{\mathrm{L}} \vdash x\ l\ \overline{qbind_i}^{\,i} \triangleright \{x \mapsto t\} \uplus E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_1}\ \text{CHECK\_LISTQUANT\_BINDING\_VAR}$$

$$\frac{\Delta, E, E_1^{\mathrm{L}} \vdash pat : t \triangleright E_3^{\mathrm{L}} \quad \Delta, E, E_1^{\mathrm{L}} \vdash exp : \_\_\mathbf{set}\ t \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad \Delta, E, E_1^{\mathrm{L}} \uplus E_3^{\mathrm{L}} \vdash \overline{qbind_i}^{\,i} \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_2 \quad \mathbf{disjoint\ doms}\,(E_3^{\mathrm{L}}, E_2^{\mathrm{L}})}{\Delta, E, E_1^{\mathrm{L}} \vdash (pat\ \mathbf{IN}\ exp)\ \overline{qbind_i}^{\,i} \triangleright E_2^{\mathrm{L}} \uplus E_3^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2}\ \text{CHECK\_LISTQUANT\_BINDING\_RESTR}$$

$$\frac{\Delta, E, E_1^{\mathrm{L}} \vdash pat : t \triangleright E_3^{\mathrm{L}} \quad \Delta, E, E_1^{\mathrm{L}} \vdash exp : \_\_\mathbf{list}\ t \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad \Delta, E, E_1^{\mathrm{L}} \uplus E_3^{\mathrm{L}} \vdash \overline{qbind_i}^{\,i} \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_2 \quad \mathbf{disjoint\ doms}\,(E_3^{\mathrm{L}}, E_2^{\mathrm{L}})}{\Delta, E, E_1^{\mathrm{L}} \vdash (pat\ \mathbf{MEM}\ exp)\ \overline{qbind_i}^{\,i} \triangleright E_2^{\mathrm{L}} \uplus E_3^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2}\ \text{CHECK\_LISTQUANT\_BINDING\_LIST\_RESTR}$$

$\boxed{\Delta, E, E_1^{\mathrm{L}} \vdash \mathbf{list}\ qbind_1 \,..\, qbind_n \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}}$ Build the environment for quantifier bindings, collecting typeclass

$$\frac{}{\Delta, E, E^{\mathrm{L}} \vdash \mathbf{list} \triangleright \{\,\}, \{\,\}}\ \text{CHECK\_QUANT\_BINDING\_EMPTY}$$

$$\frac{\Delta, E, E_1^{\mathrm{L}} \vdash pat : t \triangleright E_3^{\mathrm{L}} \quad \Delta, E, E_1^{\mathrm{L}} \vdash exp : \_\_\mathbf{list}\ t \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad \Delta, E, E_1^{\mathrm{L}} \uplus E_3^{\mathrm{L}} \vdash \overline{qbind_i}^{\,i} \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_2 \quad \mathbf{disjoint\ doms}\,(E_3^{\mathrm{L}}, E_2^{\mathrm{L}})}{\Delta, E, E_1^{\mathrm{L}} \vdash \mathbf{list}\ (pat\ \mathbf{MEM}\ exp)\ \overline{qbind_i}^{\,i} \triangleright E_2^{\mathrm{L}} \uplus E_3^{\mathrm{L}}, \Sigma^{\mathcal{C}}{}_1 \cup \Sigma^{\mathcal{C}}{}_2}\ \text{CHECK\_QUANT\_BINDING\_RESTR}$$

$\boxed{\Delta, E, E^{\mathrm{L}} \vdash funcl \triangleright \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}$ Build the environment for a function definition clause, collecting typecl

$$\frac{\Delta, E, E^{\mathrm{L}} \vdash pat_1 : t_1 \triangleright E_1^{\mathrm{L}} \quad ... \quad \Delta, E, E^{\mathrm{L}} \vdash pat_n : t_n \triangleright E_n^{\mathrm{L}} \quad \Delta, E, E^{\mathrm{L}} \uplus E_1^{\mathrm{L}} \uplus \,...\, \uplus E_n^{\mathrm{L}} \vdash exp : u \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \quad \mathbf{disjoint\ doms}\,(E_1^{\mathrm{L}}, \,...\,, E_n^{\mathrm{L}}) \quad \Delta, E \vdash typ \rightsquigarrow u}{\Delta, E, E^{\mathrm{L}} \vdash x\ l_1\ pat_1 \,...\, pat_n\ : typ = exp\ l_2 \triangleright \{x \mapsto \mathbf{curry}\,((t_1 * \,...\, * t_n), u)\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}\ \text{CHECK\_FUNCL\_ANNOT}$$

$$\frac{\Delta, E, E^{\mathrm{L}} \vdash pat_1 : t_1 \triangleright E_1^{\mathrm{L}} \quad ... \quad \Delta, E, E^{\mathrm{L}} \vdash pat_n : t_n \triangleright E_n^{\mathrm{L}} \quad \Delta, E, E^{\mathrm{L}} \uplus E_1^{\mathrm{L}} \uplus \,...\, \uplus E_n^{\mathrm{L}} \vdash exp : u \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \quad \mathbf{disjoint\ doms}\,(E_1^{\mathrm{L}}, \,...\,, E_n^{\mathrm{L}})}{\Delta, E, E^{\mathrm{L}} \vdash x\ l_1\ pat_1 \,...\, pat_n\ = exp\ l_2 \triangleright \{x \mapsto \mathbf{curry}\,((t_1 * \,...\, * t_n), u)\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}\ \text{CHECK\_FUNCL\_NOANNOT}$$

$\boxed{\Delta, E, E_1^{\mathrm{L}} \vdash \mathit{letbind} \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}$ Build the environment for a let binding, collecting typeclass and index con

$$\frac{\begin{array}{l}\Delta, E, E_1^{\mathrm{L}} \vdash \mathit{pat} : t \triangleright E_2^{\mathrm{L}} \\ \Delta, E, E_1^{\mathrm{L}} \vdash \mathit{exp} : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \\ \Delta, E \vdash \mathit{typ} \rightsquigarrow t\end{array}}{\Delta, E, E_1^{\mathrm{L}} \vdash \mathit{pat} \ : \mathit{typ} = \mathit{exp}\ l \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}} \quad \text{CHECK\_LETBIND\_VAL\_ANNOT}$$

$$\frac{\begin{array}{l}\Delta, E, E_1^{\mathrm{L}} \vdash \mathit{pat} : t \triangleright E_2^{\mathrm{L}} \\ \Delta, E, E_1^{\mathrm{L}} \vdash \mathit{exp} : t \triangleright \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}\end{array}}{\Delta, E, E_1^{\mathrm{L}} \vdash \mathit{pat}\ = \mathit{exp}\ l \triangleright E_2^{\mathrm{L}}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}} \quad \text{CHECK\_LETBIND\_VAL\_NOANNOT}$$

$$\frac{\Delta, E, E_1^{\mathrm{L}} \vdash \mathit{funcl\_aux}\ l \triangleright \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}{\Delta, E, E_1^{\mathrm{L}} \vdash \mathit{funcl\_aux}\ l \triangleright \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}} \quad \text{CHECK\_LETBIND\_FN}$$

$\boxed{\Delta, E, E^{\mathrm{L}} \vdash \mathit{rule} \triangleright \{x \mapsto t\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}}}$ Build the environment for an inductive relation clause, collecting typecl

$$\frac{\begin{array}{l}\overline{\Delta \vdash t_i\ \mathbf{ok}}^{\,i} \\ E_2^{\mathrm{L}} = \{\ \overline{y_i \mapsto t_i}^{\,i}\ \} \\ \Delta, E, E_1^{\mathrm{L}} \uplus E_2^{\mathrm{L}} \vdash \mathit{exp}' : \_\_\mathbf{bool}\ \triangleright \Sigma^{\mathcal{C}\prime}, \Sigma^{\mathcal{N}\prime} \\ \Delta, E, E_1^{\mathrm{L}} \uplus E_2^{\mathrm{L}} \vdash \mathit{exp}_1 : u_1 \triangleright \Sigma^{\mathcal{C}}{}_1, \Sigma^{\mathcal{N}}{}_1 \quad .. \quad \Delta, E, E_1^{\mathrm{L}} \uplus E_2^{\mathrm{L}} \vdash \mathit{exp}_n : u_n \triangleright \Sigma^{\mathcal{C}}{}_n, \Sigma^{\mathcal{N}}{}_n\end{array}}{\Delta, E, E_1^{\mathrm{L}} \vdash \mathit{id}^{?}\ \mathbf{forall}\ \overline{y_i\ l_i}^{\,i}\ .\mathit{exp}' \Longrightarrow x\ l\ \mathit{exp}_1\ ..\ \mathit{exp}_n\ l' \triangleright \{x \mapsto \mathbf{curry}\ ((u_1 * .. * u_n), \_\_\mathbf{bool}\ )\}, \Sigma^{\mathcal{C}\prime} \cup \Sigma^{\mathcal{C}}{}_1 \cup .. \cup \Sigma}$$

$\boxed{xs, \Delta_1, E \vdash\ \mathbf{tc}\ td \triangleright \Delta_2, E^{\mathrm{P}}}$ Extract the type constructor information

$$\frac{\begin{array}{l}\mathit{tnvars}^{l} \rightsquigarrow \mathit{tnvs} \\ \Delta, E \vdash \mathit{typ} \rightsquigarrow t \\ \mathbf{duplicates}\,(\mathit{tnvs}) = \emptyset \\ \mathbf{FV}\,(t) \subset \mathit{tnvs} \\ \overline{y_i.}^{\,i}\ x \notin \mathbf{dom}\,(\Delta)\end{array}}{\overline{y_i}^{\,i}, \Delta, E \vdash\ \mathbf{tc}\ x\ l\ \mathit{tnvars}^{l} = \mathit{typ} \triangleright \{\overline{y_i.}^{\,i}\ x \mapsto \mathit{tnvs}\ .t\}, \{x \mapsto \overline{y_i.}^{\,i}\ x\}} \quad \text{CHECK\_TEXP\_TC\_ABBREV}$$

$$\frac{\begin{array}{l}\mathit{tnvars}^{l} \rightsquigarrow \mathit{tnvs} \\ \mathbf{duplicates}\,(\mathit{tnvs}) = \emptyset \\ \overline{y_i.}^{\,i}\ x \notin \mathbf{dom}\,(\Delta)\end{array}}{\overline{y_i}^{\,i}, \Delta, E_1 \vdash\ \mathbf{tc}\ x\ l\ \mathit{tnvars}^{l} \triangleright \{\overline{y_i.}^{\,i}\ x \mapsto \mathit{tnvs}\ \}, \{x \mapsto \overline{y_i.}^{\,i}\ x\}} \quad \text{CHECK\_TEXP\_TC\_ABSTRACT}$$

$$\frac{\begin{array}{l}\mathit{tnvars}^{l} \rightsquigarrow \mathit{tnvs} \\ \mathbf{duplicates}\,(\mathit{tnvs}) = \emptyset \\ \overline{y_i.}^{\,i}\ x \notin \mathbf{dom}\,(\Delta)\end{array}}{\overline{y_i}^{\,i}, \Delta_1, E \vdash\ \mathbf{tc}\ x\ l\ \mathit{tnvars}^{l} = \langle | x_1^{l} : \mathit{typ}_1; \ ...\ ; x_j^{l} : \mathit{typ}_j\ ;^{?} | \rangle \triangleright \{\overline{y_i.}^{\,i}\ x \mapsto \mathit{tnvs}\ \}, \{x \mapsto \overline{y_i.}^{\,i}\ x\}} \quad \text{CHECK\_TEXP\_TC\_REC}$$

$$\frac{\begin{array}{l}\mathit{tnvars}^{l} \rightsquigarrow \mathit{tnvs} \\ \mathbf{duplicates}\,(\mathit{tnvs}) = \emptyset \\ \overline{y_i.}^{\,i}\ x \notin \mathbf{dom}\,(\Delta)\end{array}}{\overline{y_i}^{\,i}, \Delta_1, E \vdash\ \mathbf{tc}\ x\ l\ \mathit{tnvars}^{l} = |^{?}\ \mathit{ctor\_def}_1 | \ ... \ | \mathit{ctor\_def}_j \triangleright \{\overline{y_i.}^{\,i}\ x \mapsto \mathit{tnvs}\ \}, \{x \mapsto \overline{y_i.}^{\,i}\ x\}} \quad \text{CHECK\_TEXP\_TC\_VAR}$$

$\boxed{xs, \Delta_1, E \vdash\ \mathbf{tc}\ td_1\ ..\ td_i \triangleright \Delta_2, E^{\mathrm{P}}}$ Extract the type constructor information

$$\frac{}{xs, \Delta, E \vdash\ \mathbf{tc} \triangleright \{\ \}, \{\ \}} \quad \text{CHECK\_TEXPS\_TC\_EMPTY}$$

$$\frac{\begin{array}{l}xs, \Delta_1, E \vdash\ \mathbf{tc}\ td \triangleright \Delta_2, E_2^{\mathrm{P}} \\ xs, \Delta_1 \uplus \Delta_2, E \uplus \langle \{\ \}, E_2^{\mathrm{P}}, \{\ \}, \{\ \} \rangle \vdash\ \mathbf{tc}\ \overline{td_i}^{\,i} \triangleright \Delta_3, E_3^{\mathrm{P}} \\ \mathbf{dom}\,(E_2^{\mathrm{P}}) \cap \mathbf{dom}\,(E_3^{\mathrm{P}}) = \emptyset\end{array}}{xs, \Delta_1, E \vdash\ \mathbf{tc}\ td\ \overline{td_i}^{\,i} \triangleright \Delta_2 \uplus \Delta_3, E_2^{\mathrm{P}} \uplus E_3^{\mathrm{P}}} \quad \text{CHECK\_TEXPS\_TC\_ABBREV}$$

$\boxed{\Delta, E \vdash tnvs\ p = texp \triangleright \langle E^{\mathrm{F}}, E^{\mathrm{X}} \rangle}$ Check a type definition, with its path already resolved

$$\frac{}{\Delta, E \vdash tnvs\ p = typ \triangleright \langle \{\,\}, \{\,\} \rangle}\ \textsc{check\_texp\_abbrev}$$

$$\frac{\begin{array}{l}\overline{\Delta, E \vdash typ_i \rightsquigarrow t_i}^{\,i} \\ names = \{\,\overline{x_i}^{\,i}\,\} \\ \mathbf{duplicates}\,(\,\overline{x_i}^{\,i}\,) = \emptyset \\ \overline{\mathbf{FV}\,(t_i) \subset tnvs}^{\,i} \\ E^{\mathrm{F}} = \{\,\overline{x_i \mapsto \langle\, \mathbf{forall}\, tnvs.p \to t_i, (x_i\ \mathbf{of}\ names) \rangle}^{\,i}\,\}\end{array}}{\Delta, E \vdash tnvs\ p = \langle |\,\overline{x_i^l : typ_i}^{\,i}\ ;^{?}\, | \rangle \triangleright \langle E^{\mathrm{F}}, \{\,\} \rangle}\ \textsc{check\_texp\_rec}$$

$$\frac{\begin{array}{l}\overline{\Delta, E \vdash typs_i \rightsquigarrow t\_multi_i}^{\,i} \\ names = \{\,\overline{x_i}^{\,i}\,\} \\ \mathbf{duplicates}\,(\,\overline{x_i}^{\,i}\,) = \emptyset \\ \overline{\mathbf{FV}\,(t\_multi_i) \subset tnvs}^{\,i} \\ E^{\mathrm{X}} = \{\,\overline{x_i \mapsto \langle\, \mathbf{forall}\, tnvs.t\_multi_i \to p, (x_i\ \mathbf{of}\ names) \rangle}^{\,i}\,\}\end{array}}{\Delta, E \vdash tnvs\ p = |^{?}\,\overline{x_i^l\ \mathbf{of}\ typs_i}^{\,i} \triangleright \langle \{\,\}, E^{\mathrm{X}} \rangle}\ \textsc{check\_texp\_var}$$

$\boxed{xs, \Delta, E \vdash td_1\ ..\ td_n \triangleright \langle E^{\mathrm{F}}, E^{\mathrm{X}} \rangle}$

$$\frac{}{\overline{y_i}^{\,i}, \Delta, E \vdash \triangleright \langle \{\,\}, \{\,\} \rangle}\ \textsc{check\_texps\_empty}$$

$$\frac{\begin{array}{l}tnvars^l \rightsquigarrow tnvs \\ \Delta, E_1 \vdash tnvs\ \overline{y_i.}^{\,i}\ x = texp \triangleright \langle E_1^{\mathrm{F}}, E_1^{\mathrm{X}} \rangle \\ \overline{y_i}^{\,i}, \Delta, E \vdash \overline{td_j}^{\,j} \triangleright \langle E_2^{\mathrm{F}}, E_2^{\mathrm{X}} \rangle \\ \mathbf{dom}\,(E_1^{\mathrm{X}}) \cap \mathbf{dom}\,(E_2^{\mathrm{X}}) = \emptyset \\ \mathbf{dom}\,(E_1^{\mathrm{F}}) \cap \mathbf{dom}\,(E_2^{\mathrm{F}}) = \emptyset\end{array}}{\overline{y_i}^{\,i}, \Delta, E \vdash x\ l\ tnvars^l\ = texp\ \overline{td_j}^{\,j} \triangleright \langle E_1^{\mathrm{F}} \uplus E_2^{\mathrm{F}}, E_1^{\mathrm{X}} \uplus E_2^{\mathrm{X}} \rangle}\ \textsc{check\_texps\_cons\_concrete}$$

$$\frac{\overline{y_i}^{\,i}, \Delta, E \vdash \overline{td_j}^{\,j} \triangleright \langle E^{\mathrm{F}}, E^{\mathrm{X}} \rangle}{\overline{y_i}^{\,i}, \Delta, E \vdash x\ l\ tnvars^l\ \overline{td_j}^{\,j} \triangleright \langle E^{\mathrm{F}}, E^{\mathrm{X}} \rangle}\ \textsc{check\_texps\_cons\_abstract}$$

$\boxed{\delta, E \vdash id \rightsquigarrow p}$ Lookup a type class

$$\frac{\begin{array}{c}E(id) \triangleright p \\ \delta(p) \triangleright xs\end{array}}{\delta, E \vdash id \rightsquigarrow p}\ \textsc{convert\_class\_all}$$

$\boxed{I \vdash (p\ t)\ \mathbf{IN}\ \mathcal{C}}$ Solve class constraint

$$\frac{}{I \vdash (p\ \alpha)\ \mathbf{IN}\ (p_1\ tnv_1)\ ..\ (p_i\ tnv_i)(p\ \alpha)(p_1'\ tnv_1')\ ..\ (p_j'\ tnv_j')}\ \textsc{solve\_class\_constraint\_immediate}$$

$$\frac{\begin{array}{l}(p_1\ tnv_1)\ ..\ (p_n\ tnv_n) \Rightarrow (p\ t)\ \mathbf{IN}\ I \\ I \vdash (p_1\ \sigma(tnv_1))\ \mathbf{IN}\ \mathcal{C} \quad .. \quad I \vdash (p_n\ \sigma(tnv_n))\ \mathbf{IN}\ \mathcal{C}\end{array}}{I \vdash (p\ \sigma(t))\ \mathbf{IN}\ \mathcal{C}}\ \textsc{solve\_class\_constraint\_chain}$$

$\boxed{I \vdash \Sigma^{\mathcal{C}} \triangleright \mathcal{C}}$ Solve class constraints

$$\frac{I \vdash (p_1\ t_1)\ \mathbf{IN}\ \mathcal{C} \quad .. \quad I \vdash (p_n\ t_n)\ \mathbf{IN}\ \mathcal{C}}{I \vdash \{(p_1\ t_1),\ ..,\ (p_n\ t_n)\} \triangleright \mathcal{C}}\ \textsc{solve\_class\_constraints\_all}$$

$\boxed{\Delta, I, E \vdash \mathit{val\_def} \triangleright E^{\mathrm{X}}}$ Check a value definition

$$\frac{\begin{array}{l}\Delta, E, \{\,\} \vdash \mathit{letbind} \triangleright \{\,\overline{x_i \mapsto t_i}^{\,i}\,\}, \Sigma^{\mathcal{C}}, \Sigma^{\mathcal{N}} \\ I \vdash \Sigma^{\mathcal{C}} \triangleright \mathcal{C} \\ \overline{\mathbf{FV}\,(t_i) \subset \mathit{tnvs}}^{\,i} \\ \mathbf{FV}\,(\mathcal{C}) \subset \mathit{tnvs}\end{array}}{\Delta, I, E_1 \vdash \mathbf{let}\,\tau^{?}\,\mathit{letbind} \triangleright \{\,\overline{x_i \mapsto \langle\,\mathbf{forall}\,\mathit{tnvs}.\mathcal{C} \Rightarrow t_i, \mathbf{let}\rangle}^{\,i}\,\}} \quad \text{CHECK\_VAL\_DEF\_VAL}$$

$$\frac{\begin{array}{l}\overline{\Delta, E, E^{\mathrm{L}} \vdash \mathit{funcl}_i \triangleright \{x_i \mapsto t_i\}, {\Sigma^{\mathcal{C}}}_i, {\Sigma^{\mathcal{N}}}_i}^{\,i} \\ I \vdash \Sigma^{\mathcal{C}} \triangleright \mathcal{C} \\ \overline{\mathbf{FV}\,(t_i) \subset \mathit{tnvs}}^{\,i} \\ \mathbf{FV}\,(\mathcal{C}) \subset \mathit{tnvs} \\ \mathbf{compatible\,overlap}\,(\,\overline{x_i \mapsto t_i}^{\,i}\,) \\ E^{\mathrm{L}} = \{\,\overline{x_i \mapsto t_i}^{\,i}\,\}\end{array}}{\Delta, I, E \vdash \mathbf{let\,rec}\,\tau^{?}\,\overline{\mathit{funcl}_i}^{\,i} \triangleright \{\,\overline{x_i \mapsto \langle\,\mathbf{forall}\,\mathit{tnvs}.\mathcal{C} \Rightarrow t_i, \mathbf{let}\rangle}^{\,i}\,\}} \quad \text{CHECK\_VAL\_DEF\_RECFUN}$$

$\boxed{\Delta, (\alpha_1, .., \alpha_n) \vdash t\,\mathbf{instance}}$ Check that t be a typeclass instance

$$\frac{}{\Delta, (\alpha) \vdash \alpha\,\mathbf{instance}} \quad \text{CHECK\_T\_INSTANCE\_VAR}$$

$$\frac{}{\Delta, (\alpha_1, \ldots., \alpha_n) \vdash \alpha_1 * \ldots. * \alpha_n\,\mathbf{instance}} \quad \text{CHECK\_T\_INSTANCE\_TUP}$$

$$\frac{}{\Delta, (\alpha_1, \alpha_2) \vdash \alpha_1 \to \alpha_n\,\mathbf{instance}} \quad \text{CHECK\_T\_INSTANCE\_FN}$$

$$\frac{\Delta(p) \triangleright \alpha'_1 .. \alpha'_n}{\Delta, (\alpha_1, .., \alpha_n) \vdash p\,\alpha_1 .. \alpha_n\,\mathbf{instance}} \quad \text{CHECK\_T\_INSTANCE\_TC}$$

$\boxed{\overline{z_j}^{\,j}, D_1, E_1 \vdash \mathit{def} \triangleright D_2, E_2}$ Check a definition

$$\frac{\begin{array}{l}\overline{z_j}^{\,j}, \Delta_1, E \vdash \mathbf{tc}\,\overline{td_i}^{\,i} \triangleright \Delta_2, E^{\mathrm{P}} \\ \overline{z_j}^{\,j}, \Delta_1 \uplus \Delta_2, E \uplus \langle\{\,\}, E^{\mathrm{P}}, \{\,\}, \{\,\}\rangle \vdash \overline{td_i}^{\,i} \triangleright \langle E^{\mathrm{F}}, E^{\mathrm{X}}\rangle\end{array}}{\overline{z_j}^{\,j}, \langle\Delta_1, \delta, I\rangle, E \vdash \mathbf{type}\,\overline{td_i}^{\,i}\,l \triangleright \langle\Delta_2, \{\,\}, \{\,\}\rangle, \langle\{\,\}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}}\rangle} \quad \text{CHECK\_DEF\_TYPE}$$

$$\frac{\Delta, I, E \vdash \mathit{val\_def} \triangleright E^{\mathrm{X}}}{\overline{z_j}^{\,j}, \langle\Delta, \delta, I\rangle, E \vdash \mathit{val\_def}\,l \triangleright \epsilon, \langle\{\,\}, \{\,\}, \{\,\}, E^{\mathrm{X}}\rangle} \quad \text{CHECK\_DEF\_VAL\_DEF}$$

$$\frac{\begin{array}{l}\overline{\Delta, E_1, E^{\mathrm{L}} \vdash \mathit{rule}_i \triangleright \{x_i \mapsto t_i\}, {\Sigma^{\mathcal{C}}}_i, {\Sigma^{\mathcal{N}}}_i}^{\,i} \\ I \vdash \overline{{\Sigma^{\mathcal{C}}}_i}^{\,i} \triangleright \mathcal{C} \\ \overline{\mathbf{FV}\,(t_i) \subset \mathit{tnvs}}^{\,i} \\ \mathbf{FV}\,(\mathcal{C}) \subset \mathit{tnvs} \\ \mathbf{compatible\,overlap}\,(\,\overline{x_i \mapsto t_i}^{\,i}\,) \\ E^{\mathrm{L}} = \{\,\overline{x_i \mapsto t_i}^{\,i}\,\} \\ E_2 = \langle\{\,\}, \{\,\}, \{\,\}, \{\,\overline{x_i \mapsto \langle\,\mathbf{forall}\,\mathit{tnvs}.\mathcal{C} \Rightarrow t_i, \mathbf{let}\rangle}^{\,i}\,\}\rangle\end{array}}{\overline{z_j}^{\,j}, \langle\Delta, \delta, I\rangle, E_1 \vdash \mathbf{indreln}\,\tau^{?}\,\overline{\mathit{rule}_i}^{\,i}\,l \triangleright \epsilon, E_2} \quad \text{CHECK\_DEF\_INDRELN}$$

$$\frac{\overline{z_j}^{\,j}\,x, D_1, E_1 \vdash \mathit{defs} \triangleright D_2, E_2}{\overline{z_j}^{\,j}, D_1, E_1 \vdash \mathbf{module}\,x\,l_1 = \mathbf{struct}\,\mathit{defs}\,\mathbf{end}\,l_2 \triangleright D_2, \langle\{x \mapsto E_2\}, \{\,\}, \{\,\}, \{\,\}\rangle} \quad \text{CHECK\_DEF\_MODULE}$$

$$\frac{E_1(\mathit{id}) \triangleright E_2}{\overline{z_j}^{\,j}, D, E_1 \vdash \mathbf{module}\,x\,l_1 = \mathit{id}\,l_2 \triangleright \epsilon, \langle\{x \mapsto E_2\}, \{\,\}, \{\,\}, \{\,\}\rangle} \quad \text{CHECK\_DEF\_MODULE\_RENAME}$$

$$\frac{\begin{array}{l}\Delta, E \vdash typ \rightsquigarrow t \\ \mathbf{FV}\,(t) \subset \overline{\alpha_i}^{\,i} \\ \mathbf{FV}\,(\overline{\alpha'_k}^{\,k}) \subset \overline{\alpha_i}^{\,i} \\ \overline{\delta, E \vdash id_k \rightsquigarrow p_k}^{\,k} \\ E' = \langle \{\,\}, \{\,\}, \{\,\}, \{x \mapsto \langle\, \mathbf{forall}\, \overline{\alpha_i}^{\,i}.\overline{(p_k\, \alpha'_k)}^{\,k} \Rightarrow t, \mathbf{val} \rangle\} \rangle\end{array}}{\overline{z_j}^{\,j}, \langle \Delta, \delta, I \rangle, E \vdash \mathbf{val}\, x\, l_1 : \mathbf{forall}\, \overline{\alpha_i\, l''_i}^{\,i}.\overline{id_k\, \alpha'_k\, l''_k}^{\,k} \Rightarrow typ\, l_2 \triangleright \epsilon, E'}\ \text{CHECK\_DEF\_SPEC}$$

$$\frac{\begin{array}{l}\overline{\Delta, E_1 \vdash typ_i \rightsquigarrow t_i}^{\,i} \\ \overline{\mathbf{FV}\,(t_i) \subset \alpha}^{\,i} \\ p = \overline{z_j}.^{j}\, x \\ E_2 = \langle \{\,\}, \{x \mapsto p\}, \{\,\}, \{\, \overline{y_i \mapsto \langle\, \mathbf{forall}\, \alpha.(p\, \alpha) \Rightarrow t_i, \mathbf{method} \rangle}^{\,i}\, \} \rangle \\ \delta_2 = \{p \mapsto \overline{y_i}^{\,i}\} \\ p \notin \mathbf{dom}\,(\delta_1)\end{array}}{\overline{z_j}^{\,j}, \langle \Delta, \delta_1, I \rangle, E_1 \vdash \mathbf{class}\,(x\, l\, \alpha\, l'')\, \overline{\mathbf{val}\, y_i\, l_i : typ_i\, l_i}^{\,i}\, \mathbf{end}\, l' \triangleright \langle \{\,\}, \delta_2, \{\,\} \rangle, E_2}\ \text{CHECK\_DEF\_CLASS}$$

$$\frac{\begin{array}{l}E = \langle E^{\mathrm{M}}, E^{\mathrm{P}}, E^{\mathrm{F}}, E^{\mathrm{X}} \rangle \\ \Delta, E \vdash typ' \rightsquigarrow t' \\ \Delta, (\,\overline{\alpha_i}^{\,i}\,) \vdash t'\, \mathbf{instance} \\ tnvs = \overline{\alpha_i}^{\,i} \\ \mathbf{duplicates}\,(tnvs) = \emptyset \\ \overline{\delta, E \vdash id_k \rightsquigarrow p_k}^{\,k} \\ \mathbf{FV}\,(\overline{\alpha'_k}^{\,k}) \subset tnvs \\ E(id) \triangleright p \\ \delta(p) \triangleright \overline{z_j}^{\,j} \\ I_2 = \{\, \overline{\Rightarrow (p_k\, \alpha'_k)}^{\,k}\, \} \\ \overline{\Delta, I \cup I_2, E \vdash val\_def_n \triangleright E^{\mathrm{X}}_n}^{\,n} \\ \mathbf{disjoint\ doms}\,(\,\overline{E^{\mathrm{X}}_n}^{\,n}\,) \\ \overline{E^{\mathrm{X}}(x_k) \triangleright \langle\, \mathbf{forall}\, \alpha''.(p\, \alpha'') \Rightarrow t_k, \mathbf{method} \rangle}^{\,k} \\ \{\, \overline{x_k \mapsto \langle\, \mathbf{forall}\, tnvs.\ \Rightarrow \{\alpha'' \mapsto t'\}(t_k), \mathbf{let} \rangle}^{\,k}\, \} = \overline{E^{\mathrm{X}}_n}^{\,n} \\ \overline{x_k}^{\,k} = \overline{z_j}^{\,j} \\ I_3 = \{\, \overline{(p_k\, \alpha'_k) \Rightarrow (p\, t')}^{\,k}\, \} \\ (p\, \{\, \overline{\alpha_i \mapsto \alpha'''_i}^{\,i}\, \}(t')) \notin I\end{array}}{\overline{z_j}^{\,j}, \langle \Delta, \delta, I \rangle, E \vdash \mathbf{instance}\, \mathbf{forall}\, \overline{\alpha_i\, l'_i}^{\,i}.\overline{id_k\, \alpha'_k\, l''_k}^{\,k} \Rightarrow (id\, typ')\, \overline{val\_def_n\, l_n}^{\,n}\, \mathbf{end}\, l' \triangleright \langle \{\,\}, \{\,\}, I_3 \rangle, \epsilon}\ \text{CHECK\_DEF\_}$$

$\boxed{\overline{z_j}^{\,j}, D_1, E_1 \vdash defs \triangleright D_2, E_2}$ Check definitions, given module path, definitions and environment

$$\frac{}{\overline{z_j}^{\,j}, D, E \vdash\ \triangleright \epsilon, \epsilon}\ \text{CHECK\_DEFS\_EMPTY}$$

$$\frac{\begin{array}{l}\overline{z_j}^{\,j}, D_1, E_1 \vdash def \triangleright D_2, E_2 \\ \overline{z_j}^{\,j}, D_1 \uplus D_2, E_1 \uplus E_2 \vdash \overline{def_i\ ;;^?_i}^{\,i} \triangleright D_3, E_3\end{array}}{\overline{z_j}^{\,j}, D_1, E_1 \vdash def\ ;;^? \overline{def_i\ ;;^?_i}^{\,i} \triangleright D_2 \uplus D_3, E_2 \uplus E_3}\ \text{CHECK\_DEFS\_RELEVANT\_DEF}$$

$$\frac{\begin{array}{l}E_1(id) \triangleright E_2 \\ \overline{z_j}^{\,j}, D_1, E_1 \uplus E_2 \vdash \overline{def_i\ ;;^?_i}^{\,i} \triangleright D_3, E_3\end{array}}{\overline{z_j}^{\,j}, D_1, E_1 \vdash \mathbf{open}\, id\, l\ ;;^? \overline{def_i\ ;;^?_i}^{\,i} \triangleright D_3, E_3}\ \text{CHECK\_DEFS\_OPEN}$$

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Definition rules:         145 good    0 bad
Definition rule clauses:  437 good    0 bad
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