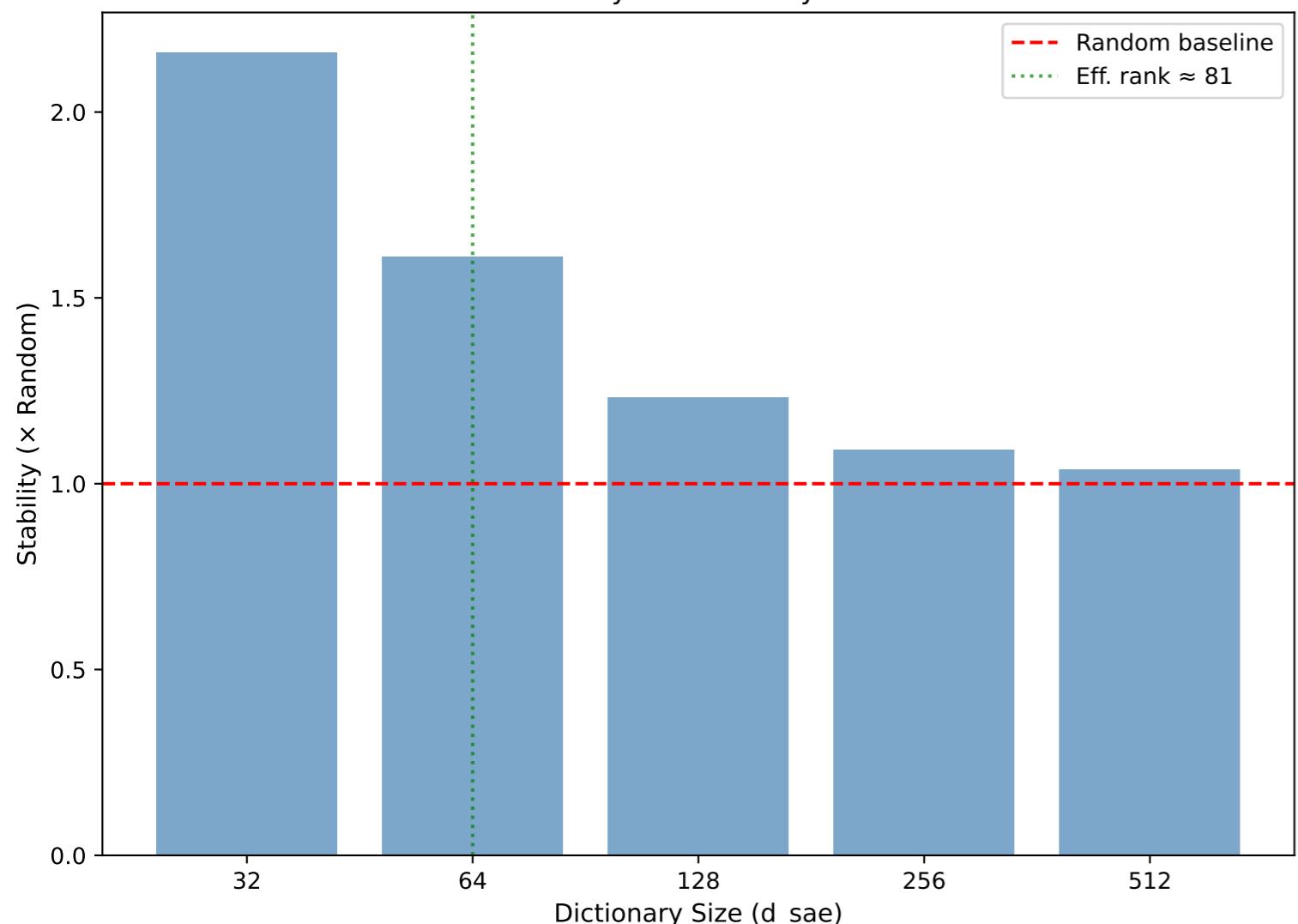
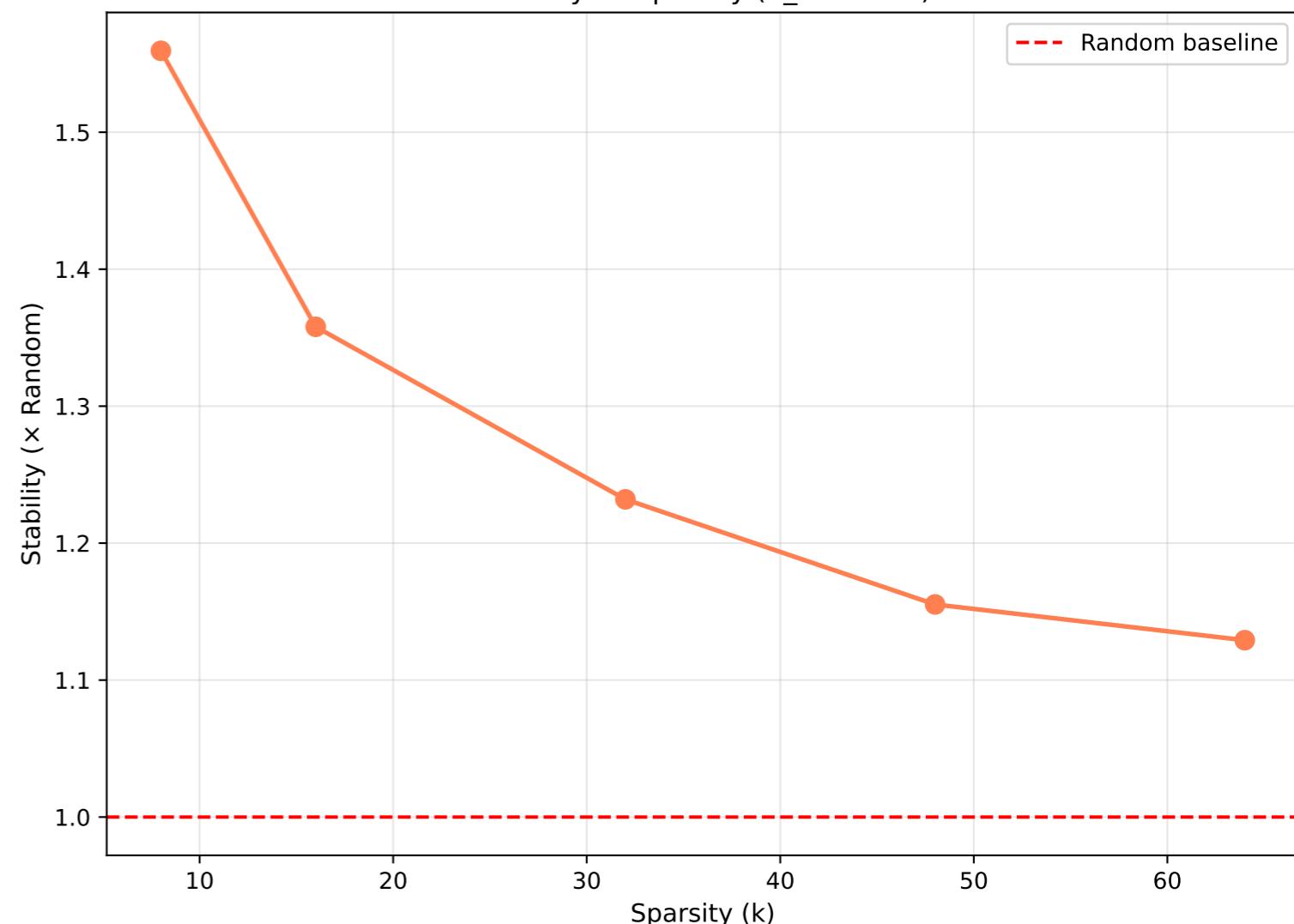
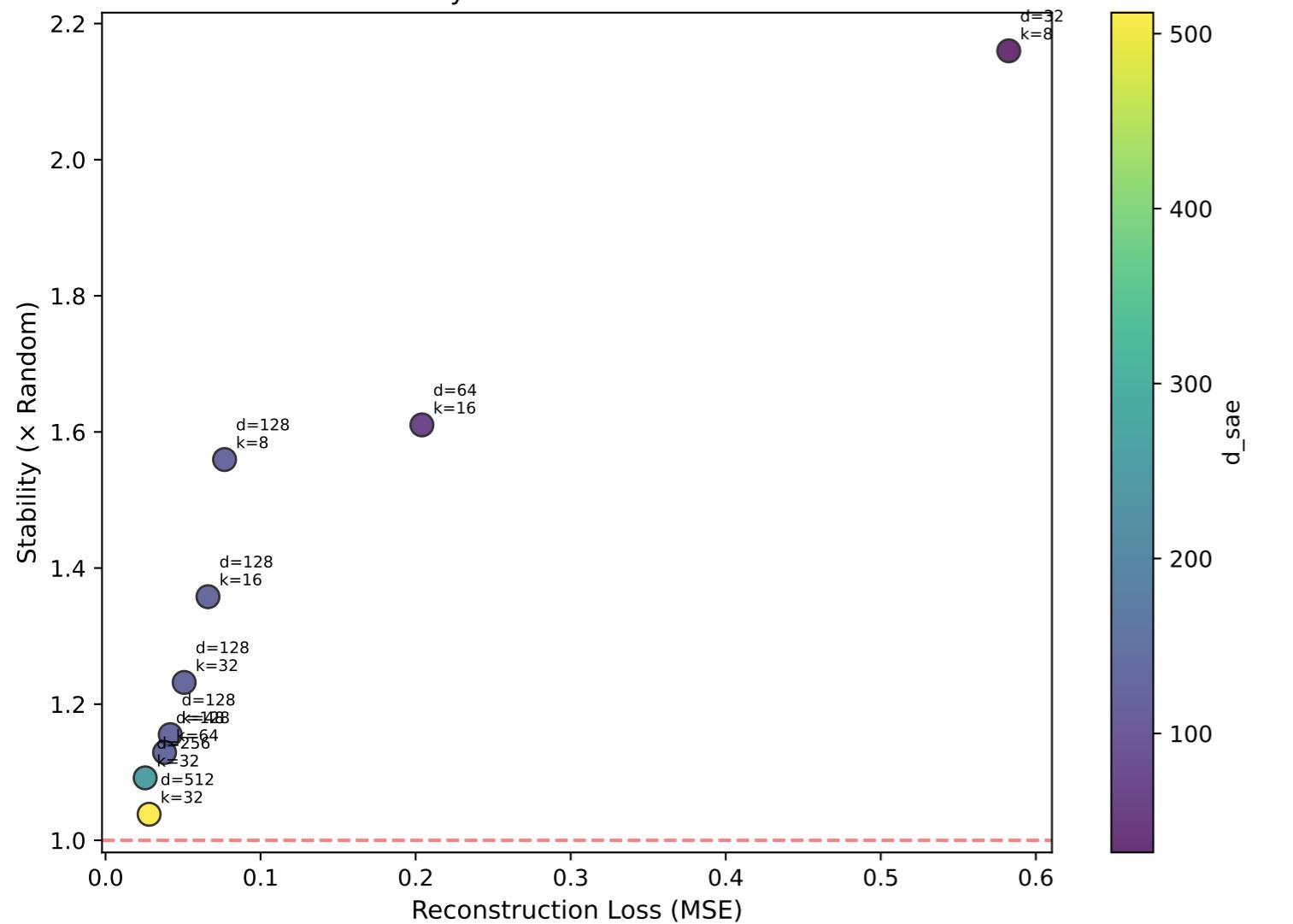


Stability vs Dictionary Size

Stability vs Sparsity ($d_{sae}=128$)

Stability-Reconstruction Tradeoff

**KEY FINDINGS**

1. STABILITY-RECONSTRUCTION TRADEOFF
 - Smaller SAEs → Higher stability, worse reconstruction
 - Larger SAEs → Lower stability (\approx random), better reconstruction
 - Matched regime ($d_{sae} \approx \text{eff_rank}$) offers best balance
2. STABILITY DECREASES WITH SPARSITY (k)
 - Lower $k \rightarrow$ Higher stability (more constrained)
 - Higher $k \rightarrow$ Lower stability (more freedom)
 - This is **OPPOSITE** to LLM findings!
3. FEATURE-LEVEL STABILITY IS UNIFORM
 - No predictor (frequency, magnitude, task correlation) significantly predicts feature stability
 - Stability is a **GLOBAL** property, not feature-specific
4. TASK-DEPENDENT STABILITY
 - On algorithmic tasks: constraint = stability
 - On LLMs: may have optimal sparsity for "correct" features
 - Semantic structure may be required for non-monotonic stability

IMPLICATIONS

- SAE stability findings from LLMs may **NOT** transfer to algorithmic tasks
- For interpretability: use matched regime ($d_{sae} \approx \text{eff_rank}$)
- Stability is fundamentally about **CONSTRAINT**, not correctness