# Simulating Exponential Distributions

Ryan Tillis August 9, 2016

### **Synopsis**

R is loaded with powerful methods for simulating, modeling and analyzing data. In this document I give a basic simulation of exponential data and compare that data with a theoretical model.

#### Simulation

We start by simulating 1000 trials with 40 observations each. This is accomplished using a for loop and the rexp() function. The means and standard deviations for each trial are saved in respective data frames.

```
lambda <- .2
n <- 40
s <- 1000

mns = NULL
sd = NULL
dat = NULL
for (i in 1:s) {
        set.seed(i)
            dat = c(dat, rexp(n, lambda))
            mns = c(mns, mean(rexp(n, lambda)))
            sd = c(sd, sd(rexp(n, lambda)))
}</pre>
```

#### Sample Mean vs Theoretical Mean

Using the data we can calculate the simulated and theoretical means.

```
sample_mean = mean(mns)
sample_mean

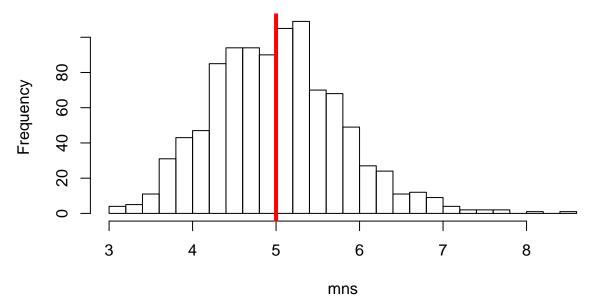
## [1] 5.011243

theor_mean = 1/lambda
theor_mean

## [1] 5

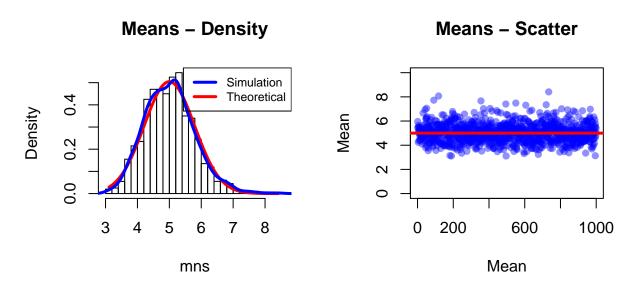
hist(mns, 22, main = "Figure 2 - Distribution of Sample Means")
abline(v=5,lw=4,col="red")
```

Figure 2 - Distribution of Sample Means



The results show that the sample mean is off by only .011. In the figure below we can further see that the distirbution of the means is approximately normal.

Figure 3 – Distribution of Sample Means



#### Sample Variance vs Theoretical Variance

Next we calculate the standard deviations and variances.

```
sample_var <- var(mns)
sample_var</pre>
```

## [1] 0.60981

```
theor_var <- (1/lambda^2)/n
theor_var</pre>
```

## [1] 0.625

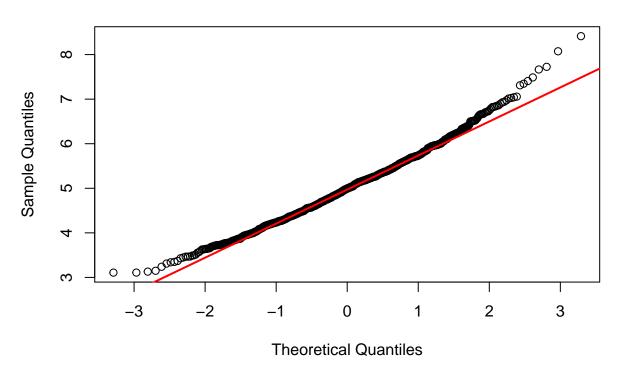
The variances match up closely. Below is a chart comparing theoretical standard deviation distribution versus the standard deviation of the sample data.

Figure 4 – Distribution of Standard Deviations

#### **Standard Deviation – Density Standard Deviation - Scatter** Simulation Theoretical Density 0.2 0.0 0 6 8 10 0 200 600 1000 4 Index sd

Finally, we can test the normality using a q-q plot.

Figure 5 – Normality Test



## Appendix - Plot Codes

```
plot(dat, pch = 16, col = adjustcolor("purple", alpha=0.05), ylim = c(0,25), ylab = "Variable", main =
sample_mean = mean(mns)
sample_mean
theor_mean = 1/lambda
theor_mean
hist(mns, 22, main = "Figure 2 - Distribution of Sample Means")
abline(v=5,lw=4,col="red")
#FIGURE 3
par(mfrow=c(1,2))
#Generating histogram as a density function
hist(mns, 22, freq = FALSE)
#Fitting the theoretical line
xfit <- seq(min(mns), max(mns), length = 100)</pre>
yfit <- dnorm(xfit, mean = 1/lambda, sd = 1/lambda/sqrt(n))</pre>
lines(xfit, yfit, pch=22, lty = 1, lw = 3, col = "red")
#Fitting the line to the data
lines(density(mns), lw = 3, col = "blue")
#Adding a legend
legend('topright', c("Simulation", "Theoretical"), col=c("blue", "red"), lw=c(3,3), cex = .75)
#plotting the data on the mean for the 1000 simulations
plot(mns, main = "Mean", ylab = "Mean", xlim = c(0,s), ylim = c(0,10), xlab = "Mean", pch = 16, col = a
abline(h=5, col = "red", lw =3)
par(mfrow=c(1,2), oma=c(2,0,2,0))
hist(sd, 22, freq = FALSE, ylim = c(0,.5), main = "Standard Deviation - Density")
#Fitting the theoretical line
xfit <- seq(min(sd), max(sd), length = 100)</pre>
yfit <- dnorm(xfit, mean = 1/lambda, sd = 1/lambda/sqrt(n))</pre>
lines(xfit, yfit, pch=22, lty = 1, lw = 3, col = "red")
#Fitting the line to the data
lines(density(sd), lw = 3, col = "blue")
#Adding a legend and title
legend('topright', c("Simulation", "Theoretical"), col=c("blue", "red"), lw=c(3,3), cex = .75)
mtext("Figure 4 - Distribution of Standard Deviations", outer = TRUE, cex = 1.5)
plot(sd, main = "Standard Deviation - Scatter", ylab = "Stdev", xlim = c(0,s), ylim = c(0,10),pch = 16,
abline(h=5, col = "red", lw =3)
```

```
qqnorm(mns, main= "Figure 5 - Normality Test")
qqline(mns, col="red", lw = "2")
```

Check out my website at: http://www.ryantillis.com/