# **Experiment No. 7**

**Aim**: To implement clustering algorithms.

## **Problem Statement:**

- 1. Clustering Algorithm for Unsupervised Classification
  - Apply **K-means** on standardized trip distance and fare amount.
- 2. Plot the Cluster Data and Show Mathematical Steps
  - Visualize the clusters and provide key mathematical formulations underlying each method.

# **Theory**

## 1. K-means Clustering

- Mathematical Steps:
  - 1. Selecting K initial cluster centroids randomly.
  - 2. Assigning each data point to the nearest centroid.
  - 3. Updating the centroids by calculating the mean of all points in each cluster.
  - 4. Repeating steps 2 and 3 until convergence (i.e., centroids stop changing significantly).
- Objective Function:

$$J = \sum_{i=1}^k \sum_{x \in C_i} \|x - \mu_i\|^2$$

Minimizes the sum of squared distances within clusters.

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## Steps:

## **Step 1: Data Preparation**

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
from sklearn.preprocessing import StandardScaler
from sklearn.cluster import KMeans, DBSCAN, AgglomerativeClustering
from scipy.cluster.hierarchy import dendrogram, linkage
file path = "/content/yellow tripdata 2016-03.csv"
df = pd.read csv(file path, parse dates=['tpep pickup datetime',
'tpep dropoff_datetime'])
df.head()
features = ['trip distance', 'fare amount']
df clean = df[features].dropna()
df clean = df clean[(df clean['trip distance'] > 0) & (df clean['fare amount'] >
0)]
df sample = df clean.sample(n=5000, random state=42)
scaler = StandardScaler()
X = scaler.fit transform(df sample)
```

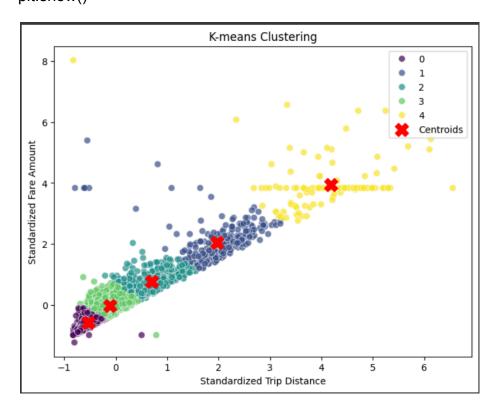
#### Inference

- Data Loaded & Parsed: The CSV is read, and date columns are converted to datetime objects.
- Feature Selection: Only trip\_distance and fare\_amount are retained for clustering.
- Data Cleaning: Removes missing entries and filters out any non-positive values.
- **Sampling**: Speeds up computation on large data (5,000 rows).
- **Standardization**: Ensures both features contribute equally to distance measures.

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#### Step 2.1: K-means Clustering

```
k = 5 # Number of clusters (tune as needed)
kmeans = KMeans(n_clusters=k, random_state=42)
labels_km = kmeans.fit_predict(X)
centroids = kmeans.cluster_centers_
# Plot K-means clusters
plt.figure(figsize=(8, 6))
sns.scatterplot(x=X[:, 0], y=X[:, 1], hue=labels_km, palette='viridis', s=50, alpha=0.7)
plt.scatter(centroids[:, 0], centroids[:, 1], s=200, c='red', marker='X', label='Centroids')
plt.title("K-means Clustering")
plt.xlabel("Standardized Trip Distance")
plt.ylabel("Standardized Fare Amount")
plt.legend()
plt.show()
```

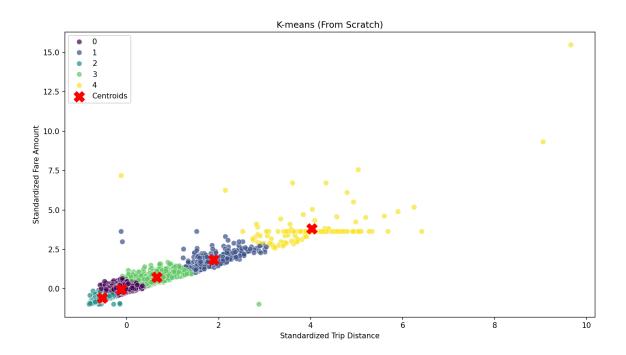


Step 2.2: K-means Clustering (Formula)

```
def kmeans_from_scratch(X, k, max_iter=100, tol=1e-4):
    """
    K-means clustering from scratch.
    """
    n_samples, n_features = X.shape

# Randomly choose k distinct points from X as initial centroids
    rng = np.random.default_rng(42)
    random indices = rng.choice(n_samples, size=k, replace=False)
```

```
centroids = X[random indices].copy()
  for iteration in range(max iter):
     # Compute distances to each centroid
     distances = np.empty((n samples, k))
     for i in range(k):
       diff = X - centroids[i]
       distances[:, i] = np.sum(diff * diff, axis=1) # squared distance
     labels = np.argmin(distances, axis=1)
     # Update centroids
     old centroids = centroids.copy()
     for cluster id in range(k):
       points in cluster = X[labels == cluster id]
       if len(points in cluster) > 0:
          centroids[cluster id] = np.mean(points in cluster, axis=0)
     # Check convergence
     shift = np.linalg.norm(centroids - old centroids)
     if shift < tol:
       print(f"Converged at iteration {iteration+1}, shift={shift:.5f}")
       break
  return labels, centroids
def kmeans scratch demo(X, k=5):
  print("=== K-means (From Scratch) ===")
  labels, centroids = kmeans from scratch(X, k=k, max iter=100)
  # Plot
  plt.figure(figsize=(8, 6))
  sns.scatterplot(x=X[:, 0], y=X[:, 1], hue=labels, palette='viridis', s=50, alpha=0.7)
  plt.scatter(centroids[:, 0], centroids[:, 1], s=200, c='red', marker='X',
label='Centroids')
  plt.title("K-means (From Scratch)")
  plt.xlabel("Standardized Trip Distance")
  plt.ylabel("Standardized Fare Amount")
  plt.legend()
  plt.show()
```

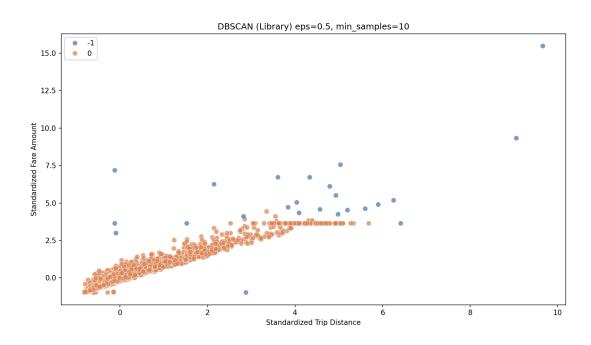


## Inference

- **Positive Relationship**: The data shows a roughly linear trend: as distance increases, fare typically increases.
- **Five Clusters**: K-means partitioned the data into 5 groups, each cluster capturing a different range of distance/fare.
- **Centroids**: Red X's mark the center in standardized space for each cluster.
- **Cluster Shapes**: K-means tends to form roughly spherical clusters. The points with very high or low fare/distance appear at the extremes.

#### Step 3.1 : DBSCAN Clustering

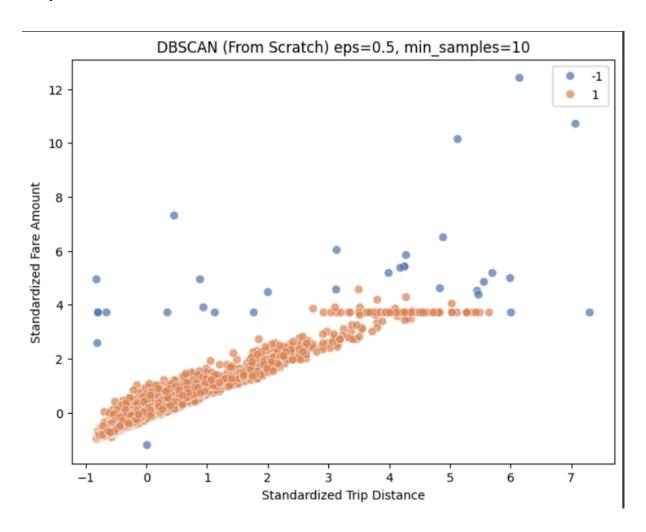
```
dbscan = DBSCAN(eps=0.5, min_samples=10)
labels_db = dbscan.fit_predict(X)
# Plot DBSCAN clusters (noise points are labeled as -1)
plt.figure(figsize=(8, 6))
sns.scatterplot(x=X[:, 0], y=X[:, 1], hue=labels_db, palette='deep', s=50, alpha=0.7)
plt.title("DBSCAN Clustering")
plt.xlabel("Standardized Trip Distance")
plt.ylabel("Standardized Fare Amount")
plt.show()
```



## Step 3.2 : DBSCAN Clustering (Formula)

```
def dbscan_from_scratch(X, eps=0.5, min_samples=10):
  Basic DBSCAN from scratch:
  - RegionQuery, ExpandCluster, etc.
  n samples = X.shape[0]
  labels = np.full(n samples, -1, dtype=int) # -1 = noise by default
  visited = np.zeros(n samples, dtype=bool)
  cluster id = 0
  def euclidean distance(a, b):
    return np.sqrt(np.sum((a - b)**2))
  def region_query(point_idx):
    neighbors = []
    for i in range(n samples):
       if euclidean distance(X[point idx], X[i]) <= eps:
          neighbors.append(i)
    return neighbors
  for i in range(n_samples):
    if visited[i]:
       continue
    visited[i] = True
    neighbors = region_query(i)
    if len(neighbors) < min samples:
```

```
labels[i] = -1 # noise
     else:
       # create new cluster
       cluster id += 1
       labels[i] = cluster id
       seeds = neighbors.copy()
       seeds.remove(i) # remove itself if present
       # Expand cluster
       while seeds:
          current point = seeds.pop()
          if not visited[current point]:
            visited[current point] = True
            neighbors2 = region query(current point)
            if len(neighbors2) >= min samples:
              # add new neighbors
              for nb in neighbors2:
                 if nb not in seeds:
                    seeds.append(nb)
          if labels[current_point] == -1:
            labels[current point] = cluster id
  return labels
def dbscan scratch demo(X, eps=0.5, min samples=10):
  print("=== DBSCAN (From Scratch) ===")
  labels = dbscan from scratch(X, eps=eps, min samples=min samples)
  # Plot
  plt.figure(figsize=(8, 6))
  sns.scatterplot(x=X[:, 0], y=X[:, 1], hue=labels, palette='deep', s=50,
alpha=0.7)
  plt.title(f"DBSCAN (From Scratch) eps={eps},
min samples={min samples}")
  plt.xlabel("Standardized Trip Distance")
  plt.ylabel("Standardized Fare Amount")
  plt.show()
```



## Inference

- **Single Major Cluster**: DBSCAN lumps the majority of points into one cluster (label 0).
- **Noise/Outliers**: Points labeled "-1" deviate from the main density; these may be unusually short or long rides relative to their fares.
- **Parameter Sensitivity**: With eps=0.5 and min\_samples=10, you get just one cluster + noise. Different parameters might reveal more subclusters.
- **Linear Trend**: The main cluster still follows the same linear pattern (distance vs. fare).

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## **Conclusion:**

In this experiment, clustering algorithms were applied to NYC Yellow Taxi data using standardized trip distance and fare amount. K-means effectively grouped the rides into five clusters, highlighting a clear linear relationship between distance and fare, with each cluster representing different ride patterns. The centroids indicated the average values within each group. In comparison, DBSCAN identified one dense cluster and several outliers, showcasing its ability to detect anomalies. Overall, the experiment demonstrated how unsupervised clustering can reveal patterns and outliers in real-world transportation data for deeper insights.