Machine Translation Word-based models and the EM algorithm

Miles Osborne (Original slides by Philipp Koehn and Barry Haddow)

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Lexical translation

ullet How to translate a word o look up in dictionary

Haus — house, building, home, household, shell.

- Multiple translations
 - some more frequent than others
 - for instance: *house*, and *building* most common
 - special cases: Haus of a snail is its shell
- Note: During all the lectures, we will translate from a foreign language into English



Collect statistics

• Look at a *parallel corpus* (German text along with English translation)

Translation of Haus	Count
house	8,000
building	1,600
home	200
household	150
shell	50



Estimate translation probabilities

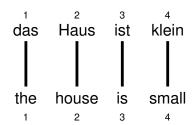
• Maximum likelihood estimation

$$p_f(e) = \begin{cases} 0.8 & \text{if } e = \textit{house}, \\ 0.16 & \text{if } e = \textit{building}, \\ 0.02 & \text{if } e = \textit{home}, \\ 0.015 & \text{if } e = \textit{household}, \\ 0.005 & \text{if } e = \textit{shell}. \end{cases}$$



Alignment

• In a parallel text (or when we translate), we **align** words in one language with the words in the other



• Word *positions* are numbered 1–4

informatics

Alignment

Alignments:

- Specify word translations
- Allow us to recover word order

They are not given, so we need *EM*



Alignment function

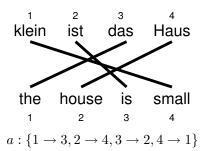
- Formalizing alignment with an alignment function
- \bullet Mapping an English target word at position i to a German source word at position j with a function $a:i\to j$
- Example

$$a:\{1\rightarrow 1,2\rightarrow 2,3\rightarrow 3,4\rightarrow 4\}$$



Reordering

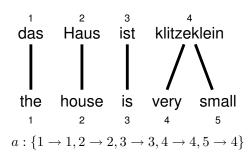
• Words may be **reordered** during translation





One-to-many translation

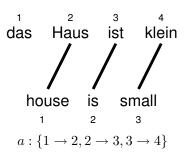
• A source word may translate into **multiple** target words





Dropping words

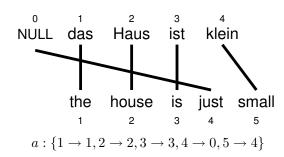
- Words may be **dropped** when translated
 - The German article *das* is dropped





Inserting words

- Words may be added during translation
 - The English *just* does not have an equivalent in German
 - We still need to map it to something: special ${\scriptstyle \mathrm{NULL}}$ token



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IBM Models

- SMT systems are based upon aligned parallel corpora.
- We use machine learning to tell us this alignment.

IBM Models are a series of translation models for word alignment



IBM Model 1

IBM Model 1 only uses lexical translation

- Translation probability

 - for a foreign sentence $\mathbf{f}=(f_1,...,f_{l_f})$ of length l_f to an English sentence $\mathbf{e}=(e_1,...,e_{l_e})$ of length l_e with an alignment of each English word e_j to a foreign word $f_{a(j)}$ according to the alignment function $a: j \rightarrow i$

$$p(\mathbf{e}, a|\mathbf{f}) = \frac{\epsilon}{(l_f + 1)^{l_e}} \prod_{j=1}^{l_e} t(e_j|f_{a(j)})$$

- parameter ϵ is a normalisation constant



Example

aas		
e	t(e f)	
the	0.7	
that	0.15	
which	0.075	
who	0.05	
this	0.025	

Haus		
e	t(e f)	
house	0.8	
building	0.16	
home	0.02	
household	0.015	
shell	0.005	

$oldsymbol{ist}$		
t(e f)		
8.0		
0.16		
0.02		
0.015		
0.005		

klein		
e	t(e f)	
small	0.4	
little	0.4	
short	0.1	
minor	0.06	
petty	0.04	
`		

$$\begin{split} p(e,a|f) &= \frac{\epsilon}{5^4} \times t(\text{the}|\text{das}) \times t(\text{house}|\text{Haus}) \times t(\text{is}|\text{ist}) \times t(\text{small}|\text{klein}) \\ &= \frac{\epsilon}{5^4} \times 0.7 \times 0.8 \times 0.8 \times 0.4 \end{split}$$



Learning lexical translation models

- ullet We would like to $\it estimate$ the lexical translation probabilities $\it t(e|f)$ from a parallel corpus
- ... but we do not have the alignments
- Chicken and egg problem
 - if we had the *alignments*,
 - \rightarrow we could estimate the *parameters* of our generative model
 - if we had the *parameters*,
 - \rightarrow we could estimate the *alignments*



EM algorithm

- Expectation Maximization (EM) in a nutshell
 - initialise model parameters (e.g. uniform)
 - assign probabilities to the missing data (ie guess probability of data given model)
 - (re) estimate model parameters from completed data
 - iterate



EM algorithm

... la maison ... la maison blue ... la fleur ...







- Initial step: all alignments equally likely
- Model learns that, e.g., *la* is often aligned with *the*



EM algorithm

... la maison ... la maison blue ... la fleur ...







- After one iteration
- Alignments, e.g., between *la* and *the* are more likely



EM algorithm

... la maison ... la maison bleu ... la fleur ...







- After another iteration
- It becomes apparent that alignments, e.g., between *fleur* and *flower* are more likely



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EM algorithm

... la maison ... la maison bleu ... la fleur the house ... the blue house ... the flower ...

Convergence

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• Inherent hidden structure revealed by EM

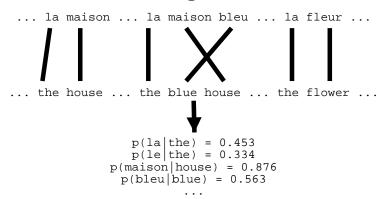
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EM algorithm



• Parameter estimation from the aligned corpus

IBM Model 1 and EM

- EM Algorithm consists of two steps
- Expectation-Step: Apply model to the data
 - parts of the model are hidden (here: alignments)
 - using the model, assign probabilities to possible values
- Maximization-Step: Estimate model from data
 - take assigned values as fact
 - collect counts (weighted by probabilities)
 - estimate model from counts
- Iterate these steps until **convergence**



IBM Model 1 and EM

- We need to be able to:
 - Compute probability of alignments (for weighing counts)
 - Collect counts and update parameters

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IBM Model 1 and EM

- $\begin{array}{ll} \bullet \ \ \, \textbf{Probabilities} & p(\mathsf{the}|\mathsf{la}) = 0.7 & p(\mathsf{house}|\mathsf{la}) = 0.05 \\ p(\mathsf{the}|\mathsf{maison}) = 0.1 & p(\mathsf{house}|\mathsf{maison}) = 0.8 \end{array}$
- Alignments

la • the maison • house maison • the maison • house
$$p(\mathbf{e}, a|\mathbf{f}) = 0.56$$
 $p(\mathbf{e}, a|\mathbf{f}) = 0.035$ $p(\mathbf{e}, a|\mathbf{f}) = 0.08$ $p(\mathbf{e}, a|\mathbf{f}) = 0.005$ $p(a|\mathbf{e}, \mathbf{f}) = 0.824$ $p(a|\mathbf{e}, \mathbf{f}) = 0.052$ $p(a|\mathbf{e}, \mathbf{f}) = 0.118$ $p(a|\mathbf{e}, \mathbf{f}) = 0.007$

• Counts c(the|Ia) = 0.824 + 0.052 c(house|Ia) = 0.052 + 0.007 c(the|maison) = 0.118 + 0.007 c(house|maison) = 0.824 + 0.118



IBM Model 1 and EM: Expectation Step

- We need to compute $p(a|\mathbf{e},\mathbf{f})$
- Applying the *chain rule*:

$$p(a|\mathbf{e}, \mathbf{f}) = \frac{p(\mathbf{e}, a|\mathbf{f})}{p(\mathbf{e}|\mathbf{f})}$$

• We already have the formula for $p(\mathbf{e}, a|\mathbf{f})$ (definition of Model 1)



IBM Model 1 and EM: Expectation Step

ullet We need to compute $p(\mathbf{e}|\mathbf{f})$

$$p(\mathbf{e}|\mathbf{f}) = \sum_{a} p(\mathbf{e}, a|\mathbf{f})$$

$$= \frac{\epsilon}{(l_f + 1)^{l_e}} \prod_{j=1}^{l_e} \sum_{i=0}^{l_f} t(e_j|f_i)$$

- This sums over a possibly exponential number of alignments
- Algebraic manipulation reduces the computation and makes it tractable

IBM Model 1 and EM: Maximization Step

- Now we have to *collect counts*
- ullet Evidence from a sentence pair **e,f** that word e is a translation of word f:

$$c(e|f; \mathbf{e}, \mathbf{f}) = \sum_{a} p(a|\mathbf{e}, \mathbf{f}) \sum_{j=1}^{l_e} \delta(e, e_j) \delta(f, f_{a(j)})$$

Note:

- ullet $\delta(e,e_j)=1$ if word e appears in position e_j , 0 otherwise
- These are expected (not true or observed) counts

IBM Model 1 and EM: Expectation Step

• Combine what we have:

$$\begin{split} p(a|\mathbf{e},\mathbf{f}) &= p(\mathbf{e},a|\mathbf{f})/p(\mathbf{e}|\mathbf{f}) \\ &= \frac{\frac{\epsilon}{(l_f+1)^{l_e}} \prod_{j=1}^{l_e} t(e_j|f_{a(j)})}{\frac{\epsilon}{(l_f+1)^{l_e}} \prod_{j=1}^{l_e} \sum_{i=0}^{l_f} t(e_j|f_i)} \\ &= \prod_{j=1}^{l_e} \frac{t(e_j|f_{a(j)})}{\sum_{i=0}^{l_f} t(e_j|f_i)} \end{split}$$



IBM Model 1 and EM: Maximization Step

• After collecting these counts over a corpus, we can estimate the model:

$$t(e|f;\mathbf{e},\mathbf{f}) = \frac{\sum_{(\mathbf{e},\mathbf{f})} c(e|f;\mathbf{e},\mathbf{f}))}{\sum_{f} \sum_{(\mathbf{e},\mathbf{f})} c(e|f;\mathbf{e},\mathbf{f}))}$$

(ie for a given word f, count how many times it was translated to a given e and normalise by the number of times f was translated to any word)



IBM Model 1 and EM: Pseudocode

```
initialize t(e|f) uniformly
do until convergence
 set count(e|f) to 0 for all e,f
  set total(f) to 0 for all f
 for all sentence pairs (e_s,f_s)
   for all words e in e_s
     total_s(e) = 0
     for all words f in f_s
        total_s(e) += t(e|f)
    for all words e in e_s
     for all words f in f_s
        count(e|f) += t(e|f) / total_s(e)
        total(f) += t(e|f) / total_s(e)
 for all f
   for all e
     t(e|f) = count(e|f) / total(f)
```

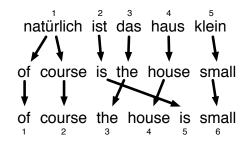
Higher IBM Models

IBM Model 1	lexical translation
IBM Model 2	adds absolute reordering model
IBM Model 3	adds fertility model
IBM Model 4	relative reordering model
IBM Model 5	fixes deficiency

- Only IBM Model 1 has global maximum
 - training of a higher IBM model builds on previous model
- Computationally biggest change in Model 3
 - trick to simplify estimation does not work anymore
- → *exhaustive* count collection becomes computationally too expensive
- sampling over high probability alignments is used instead

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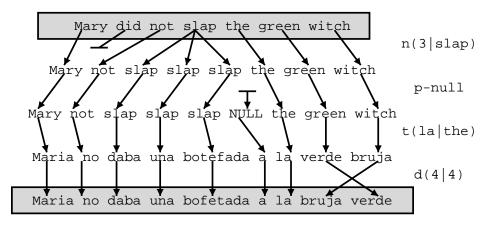
IBM Model 2



lexical translation step

alignment step

IBM Model 3



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Summary

- Word-based Models
 - Lexical translation
 - Alignment
- IBM Model 1
- Training with EM
- Higher IBM Models