## Exponential wave and sinusoidal wave comparison

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This extract evaluates wave equations using exponential methods in comparison to traditional sinusoidal methods. This method also evaluates the possible wave particle duality equation. Requirements are knowledge on complex numbers and the properties of wave equations with a brief view into electromagnetic applications.

#### INTRODUCTION

### EXPONENTIAL WAVES

When considering a circle we utilise radius and circumference. The ratio between these two lengths is  $2\pi$ . However, note that circumference is a Polar measurement as it is a curve while radius is Cartesian as it is a straight line.

$$iC/2r = \pi, \tag{1}$$

$$C/r = -2\pi i. (2)$$

Thus to be mathematically correct we get equations 1 and 2. If equation 1, has no i, circumference would also be a straight line similar to the radius and so  $2\pi$  is the ratio between two straight lines.

In order to repeat this ratio for lengths of greater magnitude we multiply by frequency f as follows,

$$f(C/r) = -2\pi f i, (3)$$

$$exp(fC/r) = exp(-2\pi fi). \tag{4}$$

$$y = W \exp(fCx/r) = W \exp(-2\pi f ix). \tag{5}$$

By observing equation 3 as a relativistic exponential in equation 4 we obtain a wave formula with amplitude W, in equation 5. One wavelength can be obtained by setting f = 1 and x = [0, 1] as seen in figure 4.

## REDEFINING EXPONENTIAL FUNCTION

$$E_c(x) = We^{2\pi f x},\tag{6}$$

$$E_s(x) = We^{2\pi fx - 0.5\pi i},\tag{7}$$

$$E_c(x - \frac{i}{4\pi f}) = E_s(x), \tag{8}$$

$$C(x) = We^{2\pi fxi} = E_c(ix), \tag{9}$$

$$S(x) = We^{2\pi f i(x - \frac{1}{4\pi f})} = E_s(ix). \tag{10}$$

### BEATS AND WAVE SPECTRUM FORMULA

Electromagnetism: 
$$S(E_c(x)) = We^{2\pi f i W e^{2\pi f x} - 0.5\pi i}$$
. (11)

Electronic beats: 
$$C(C(x)) = We^{2\pi f i W e^{2\pi f x}}$$
 (12)

Organic beats: 
$$S(C(x)) = We^{2\pi fiWe^{2\pi fxi}} - 0.5i$$
 (13)

# EXPONENTIALLY MODELLING SINUSOIDAL FUNCTIONS

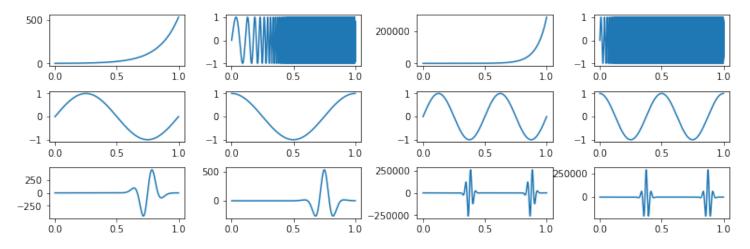
$$\frac{C(x) + C(-x)}{2} = \frac{We^{2\pi fxi} + We^{-2\pi fxi}}{2},$$
 (14)

$$\frac{C(x) + C(-x)}{2} = W \frac{e^{2\pi fxi} + e^{-2\pi fxi}}{2}, \qquad (15)$$

$$\frac{C(x) + C(-x)}{2} = WCos(2\pi f x), \tag{16}$$

$$S(x)^{2} + C(x)^{2} = W^{2}e^{2(2\pi fxi - 0.5i)} + W^{2}e^{2(2\pi fxi)}, (17)$$

$$S(x)^{2} + C(x)^{2} = W^{2}(e^{4\pi fxi - 0.5i} + e^{4\pi fxi}),$$
(18)



 ${
m FIG.}$  1. Top left we have exponential function seen in equation.

FIG. 2. MPS constructed for 100 elements with 1 bond dimension and 2 feature map dimensions.

$$S(x)^2 + C(x)^2 = W^2(\frac{e^{4\pi fxi}}{e^{0.5i}} + e^{4\pi fxi}),$$
 (19)

$$S(x)^2 + C(x)^2 = W^2 e^{4\pi fxi} (e^{-0.5i} + 1),$$
 (20)

$$S(x)^{2} + C(x)^{2} = W^{2}e^{(\pi i)(4fx)}(e^{-0.5i} + 1),$$
 (21)

$$S(x)^2 + C(x)^2 = W^2(-1)^{(4fx)}(e^{-0.5i} + 1),$$
 (22)

$$S(x)^{2} + C(x)^{2} = W^{2}(-1)^{(4fx)}(e^{-0.5i} + 1),$$
 (23)

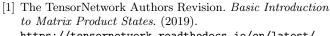
$$S(x)^{2} + C(x)^{2} = W^{2}(-1)^{(4fx)}(e^{-0.5i} + 1),$$
 (24)

Discrete exponential growth using (19)

## RESULTS

When attempting

In figure 1, an amplitude and frequency of 1 was used. In figure 1, an amplitude and frequency of 1 was used. In figure 2, an amplitude of 1 and frequency of 2 was applied.



https://tensornetwork.readthedocs.io/en/latest/basic\_mps.html.

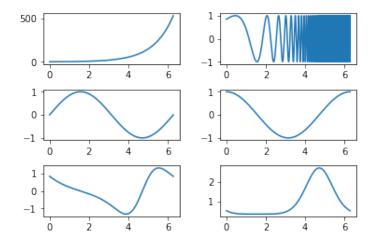


FIG. 3. Top left we have exponential function seen in equation

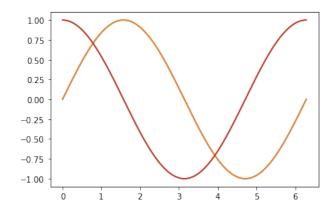


FIG. 4. MPS constructed for 100 elements with 1 bond dimension and 2 feature map dimensions.

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