SI 2: Lists and More Advanced Induction

1 List Vocabulary Review

For:

$$L = [a, b, c]$$

$$K = [1, 2, 3]$$

$$M = [red, green, blue]$$

Give the results of the following operations:

- 1. L++M
- 2. L++M++K
- 3. c::K
- 4. M::K
- 5. *c*::*b*
- 6. c ++ L

2 Proofs With Lists

- 7. Prove: rev(A++B) = rev(B) + +rev(A)
- 8. For a list L in which no elements repeat, and $i, j \in \mathbb{N}$ such that i, j < len(L) and $i \neq j$, prove that $L_i \neq L_j$
- 9. Prove: For two lists K and L, if len(K) = len(L), then len(K+L) = 2len(L)

3 A More Difficult Inductive Proof

Prove: For a tower of n disks, it takes $2^n - 1$ moves to solve the problem of the Towers of Hanoi.

The problem of the Towers of Hanoi: There are n disks stacked on one of 3 pegs, ordered from smallest disk to largest (smallest disk on the top). The task is to move all the disks to another peg following this set of rules:

- Only one disk may be moved at a time
- No disk may be placed on a peg with a smaller disk underneath it