

# **INSIDE THE BLACK BOX**

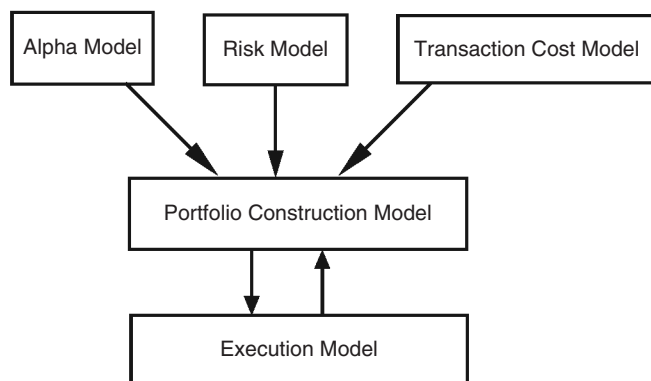
**A SIMPLE GUIDE TO SYSTEMATIC  
INVESTING, THIRD EDITION**

**BY RISHI K. NARANG**

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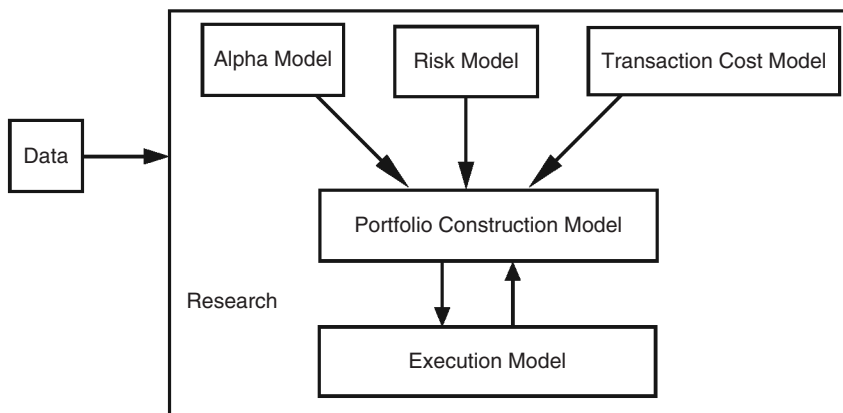
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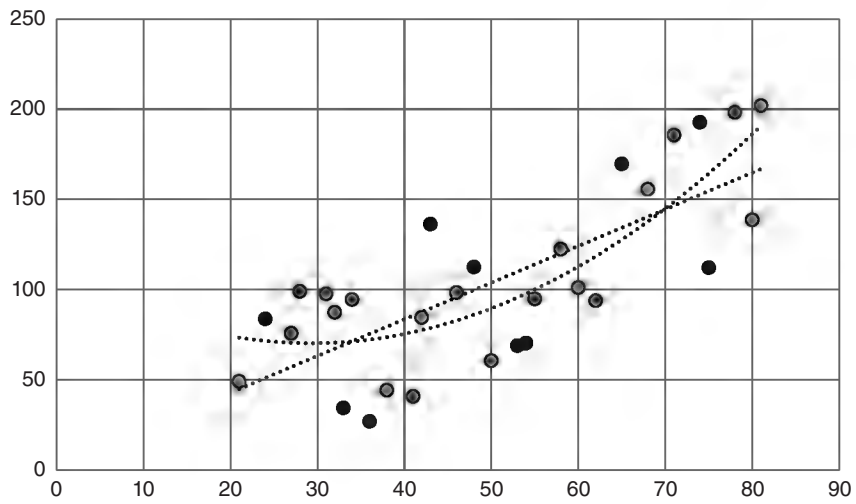
**EXHIBIT 2.1** Basic Structure of a Quant Trading Strategy

**EXHIBIT 2.2** Moving from an Existing Portfolio to a New Target Portfolio

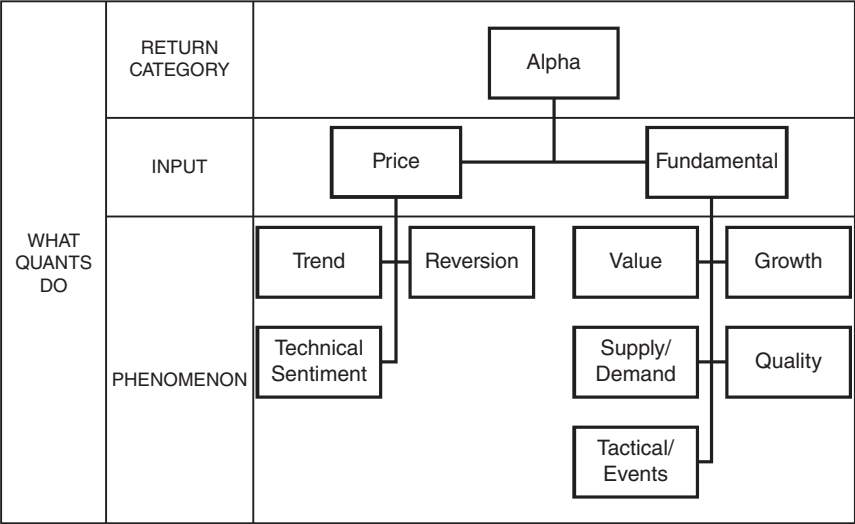
	Current Portfolio	New Target Portfolio	Trades to Execute
S&P500 Index	Short 30%	Short 25%	Buy to Cover 5%
EUROSTOXX Index	Long 20%	Long 25%	Buy 5%
U.S. 10-Year Treasury Notes	Long 40%	Long 25%	Sell 15%
German 10-Year Bunds	Short 10%	Short 25%	Sell Short 15%



**EXHIBIT 2.3** The Black Box Revealed

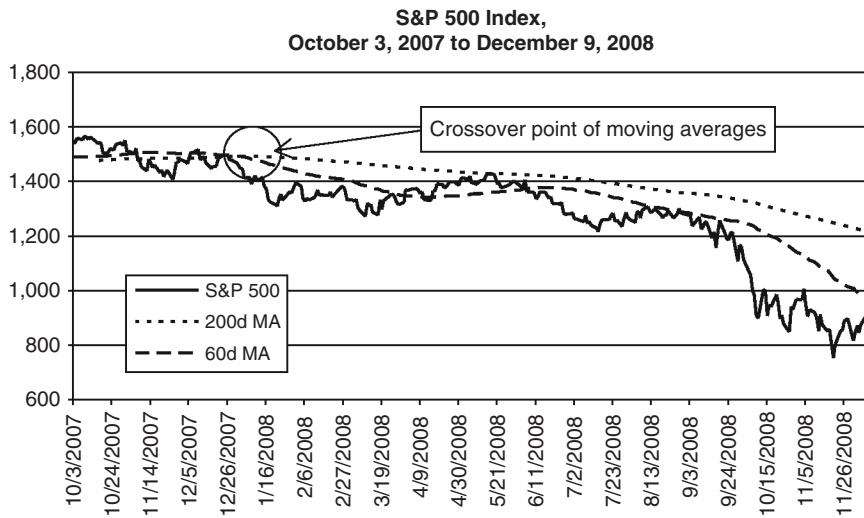


**EXHIBIT 3.1** Linearity of a Relationship

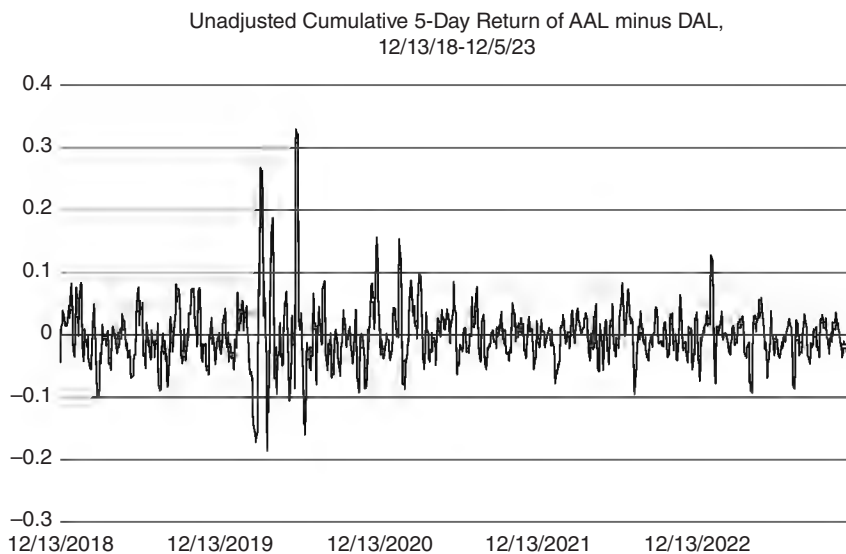


**EXHIBIT 3.2** A Taxonomy of Theory-Driven Alpha Models

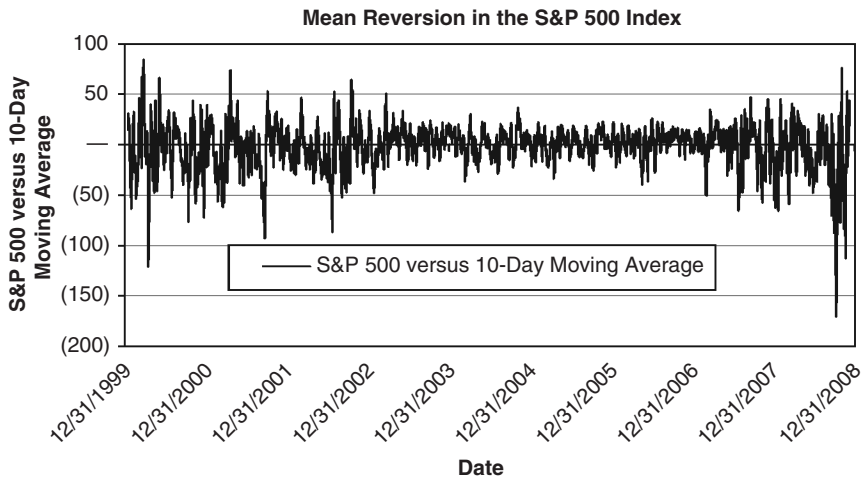
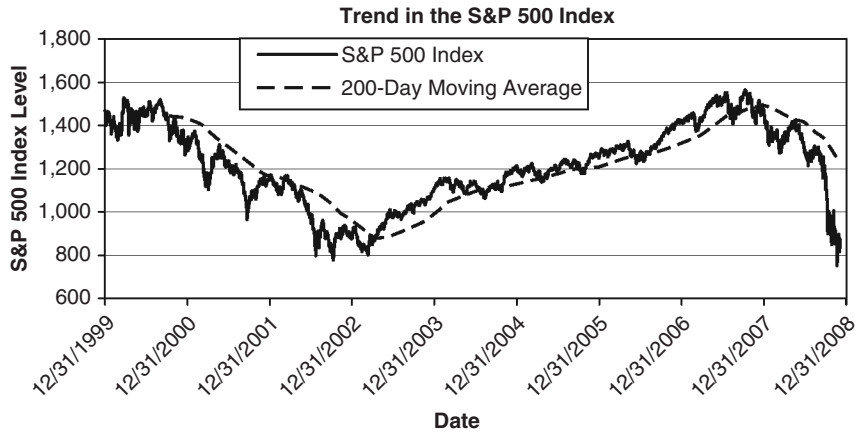




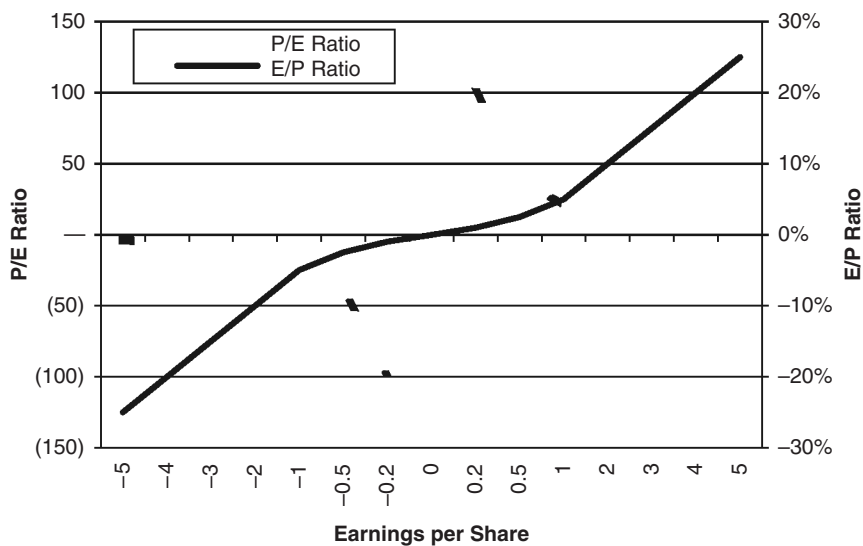
**EXHIBIT 3.3** S&P 500 Trend



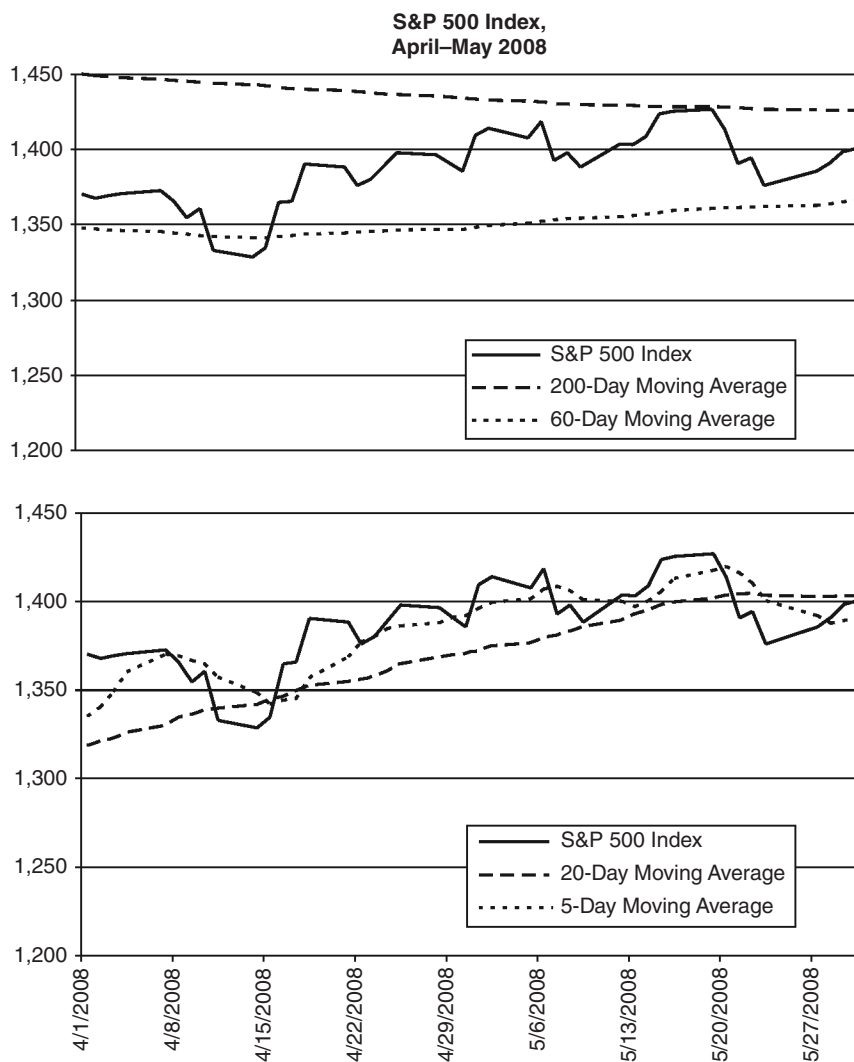
**EXHIBIT 3.4** Mean Reversion Between AAL and DAL



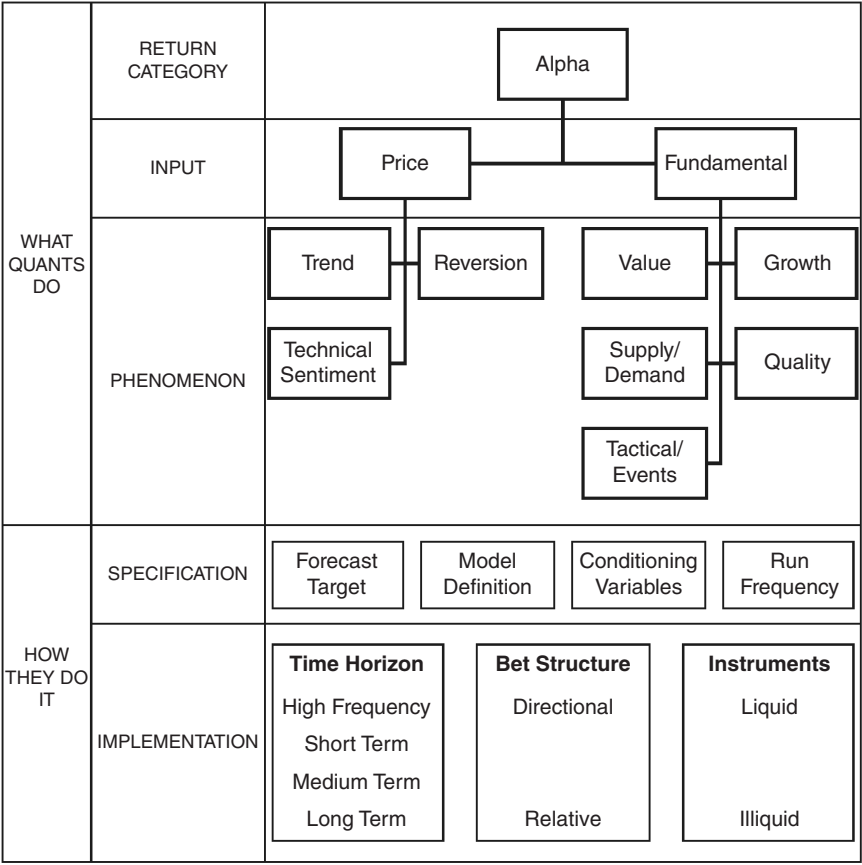
**EXHIBIT 3.5** Trend and Reversion Coexisting



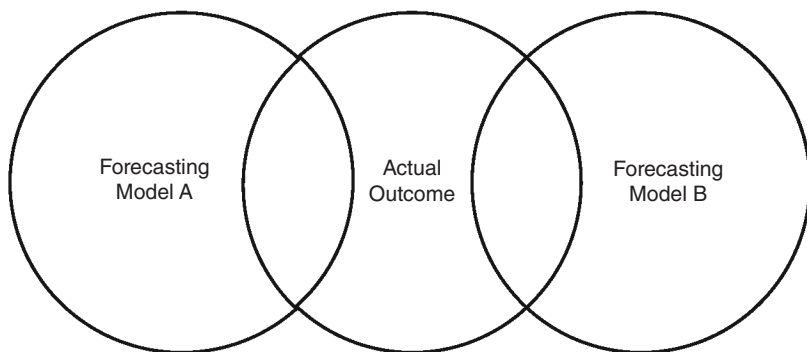
**EXHIBIT 3.6** P/E versus E/P (“Earnings Yield”)



**EXHIBIT 3.7** Same Strategy on Different Time Horizons



**EXHIBIT 3.8** Taxonomy of Theory-Driven Alpha Models and Their Implementations

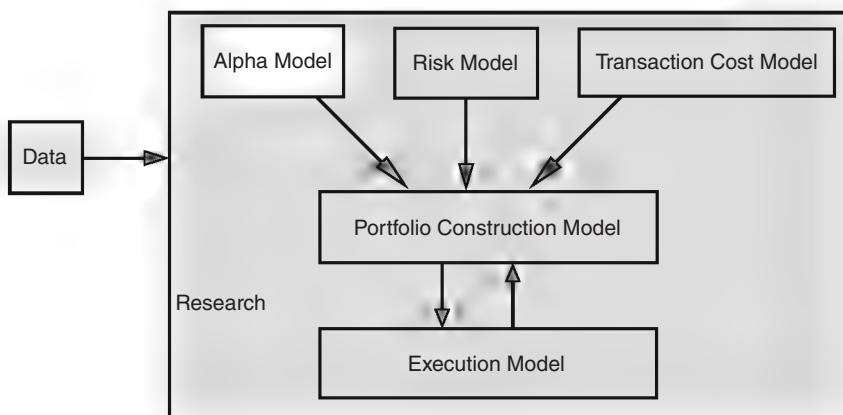


**EXHIBIT 3.9** A Visualization of Multiple Forecasts

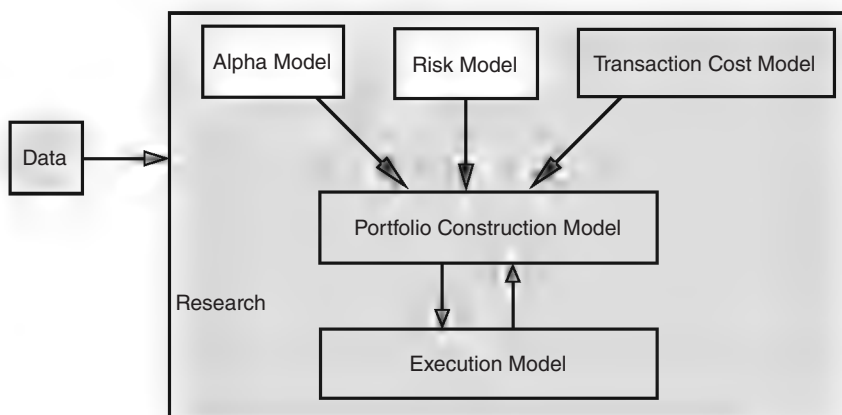
**EXHIBIT 3.10** A Simple Conditional (Nonlinear) Model for Blending Alphas

Value and Momentum Disagree	Value	Momentum	Signal
	Long	Short	None
Value and Momentum Agree	Value	Momentum	Signal
	Long	Long	Long

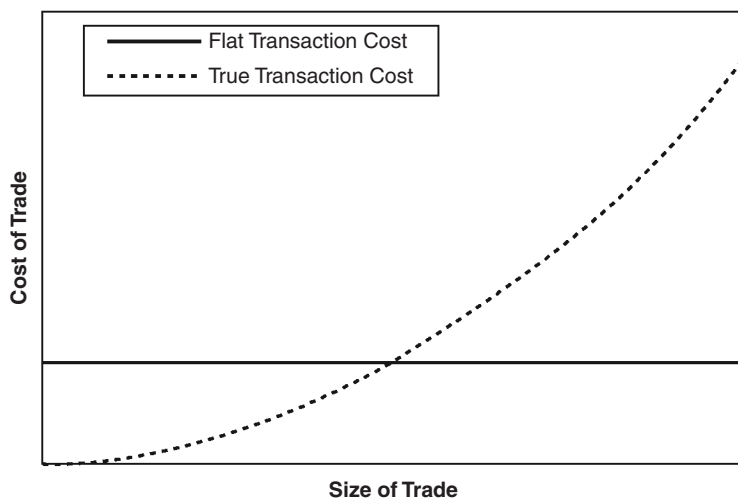




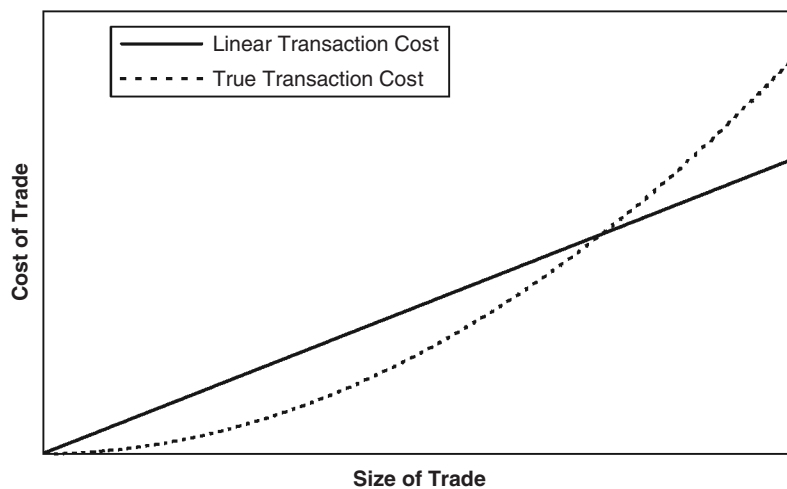
**EXHIBIT 3.11** Schematic of the Black Box



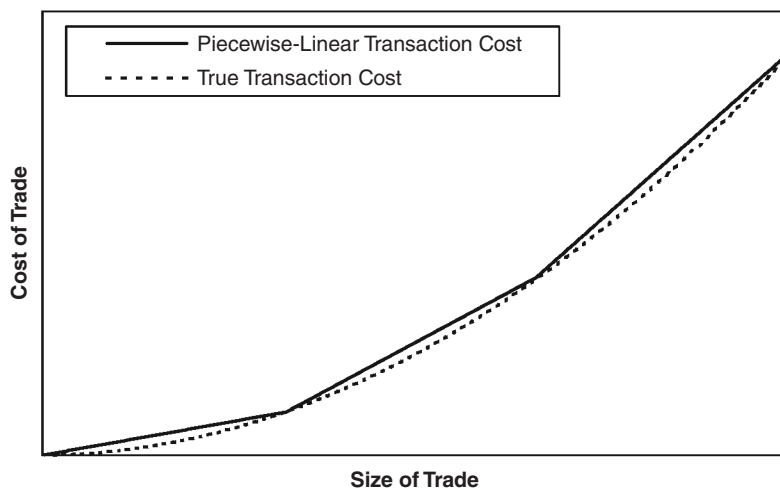
**EXHIBIT 4.1** Schematic of the Black Box



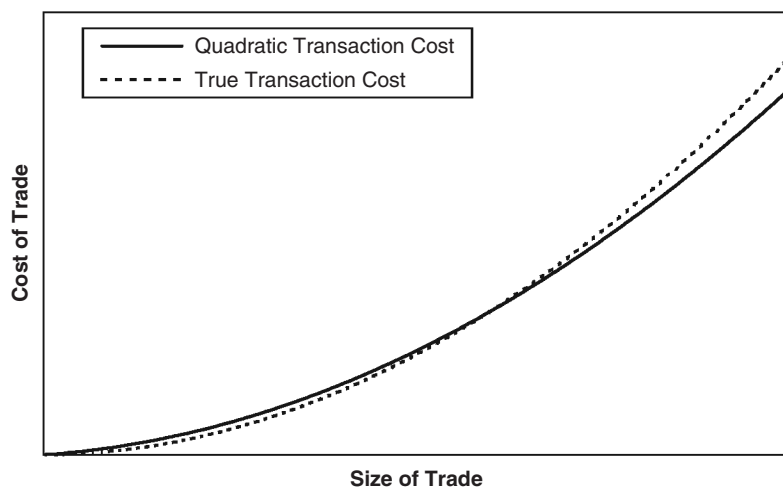
**EXHIBIT 5.1** Flat Transaction Cost Function



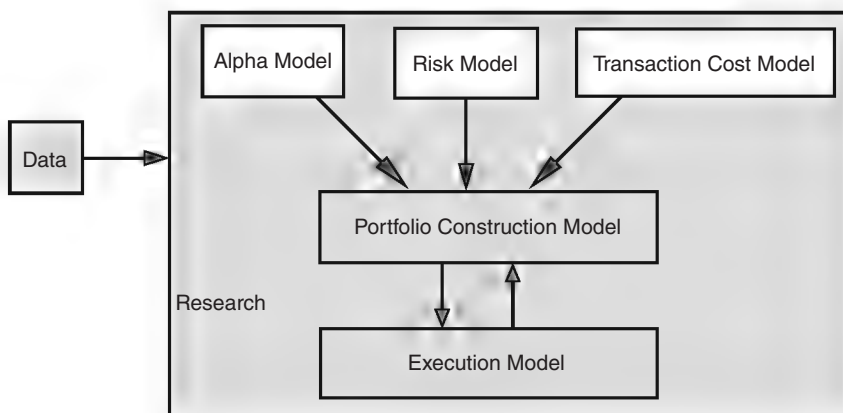
**EXHIBIT 5.2** Linear Transaction Cost Function



**EXHIBIT 5.3** Piecewise-Linear Transaction Cost Function



**EXHIBIT 5.4** Quadratic Transaction Cost Function

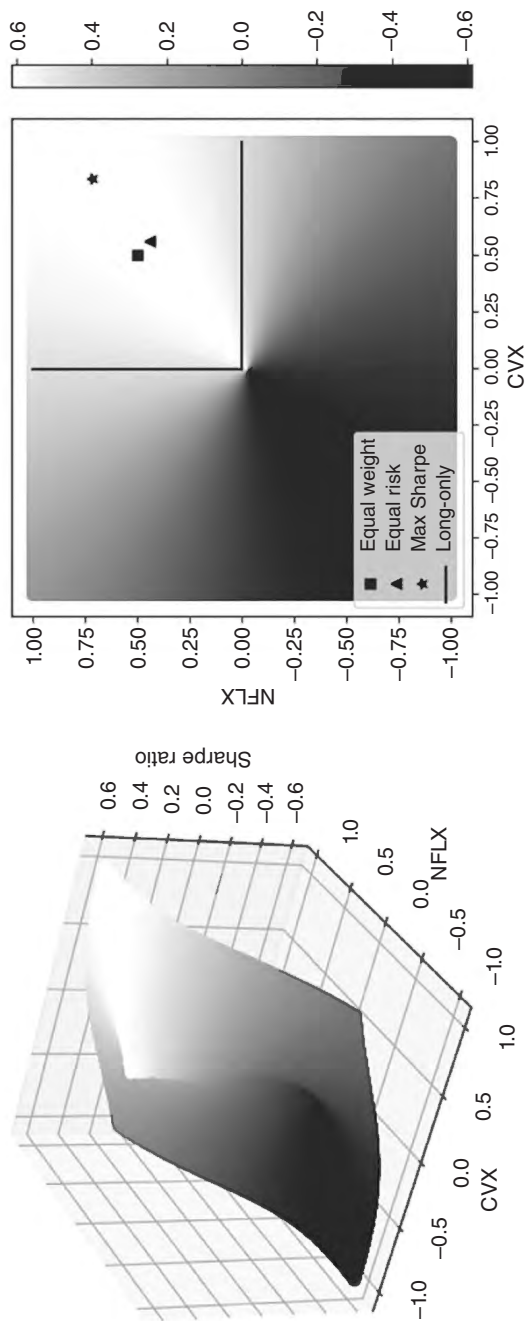


**EXHIBIT 5.5** Schematic of the Black Box

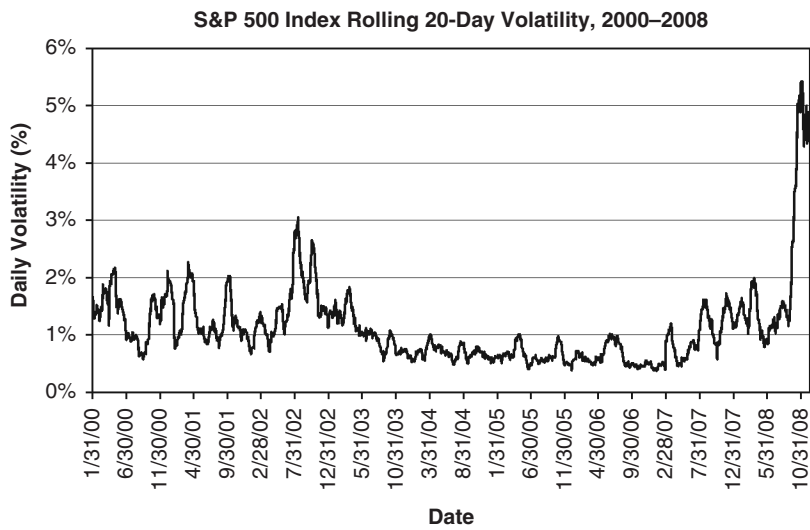
**EXHIBIT 6.1** A Simple Equal Risk Weighted Portfolio

	Equal Weight (%)	Volatility (%)	Volatility-Adjusted Weight (%)
GOOG	50	2.5	39
XOM	50	2.0	61

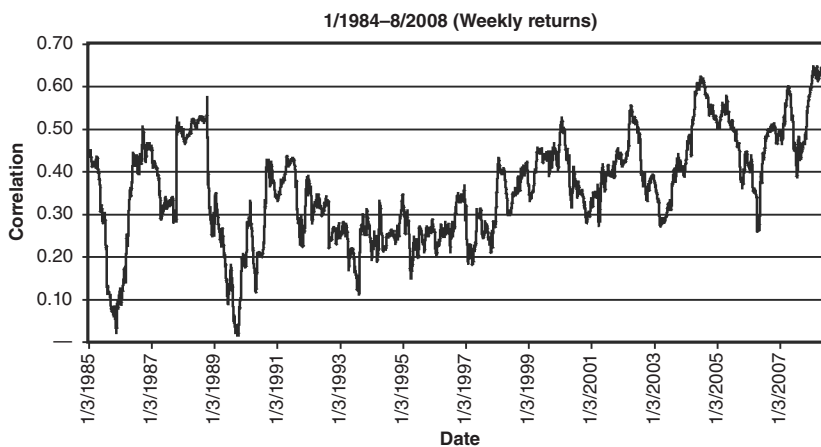




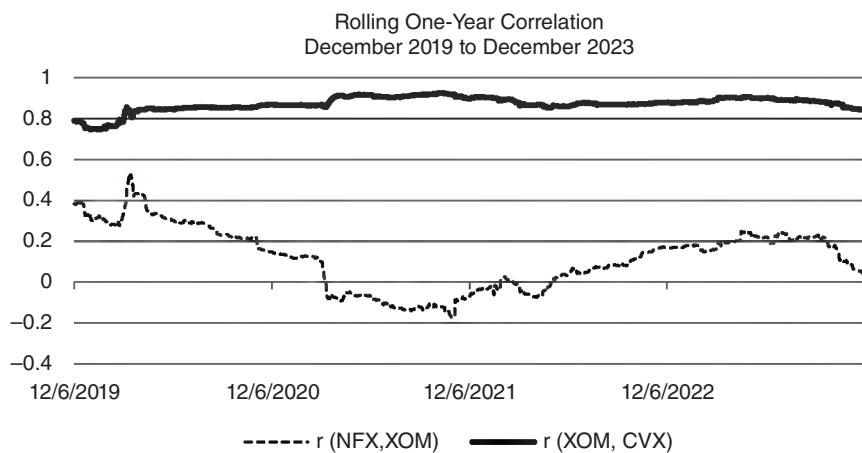
**EXHIBIT 6.2** Visual Representations of the Search Space for an Optimization



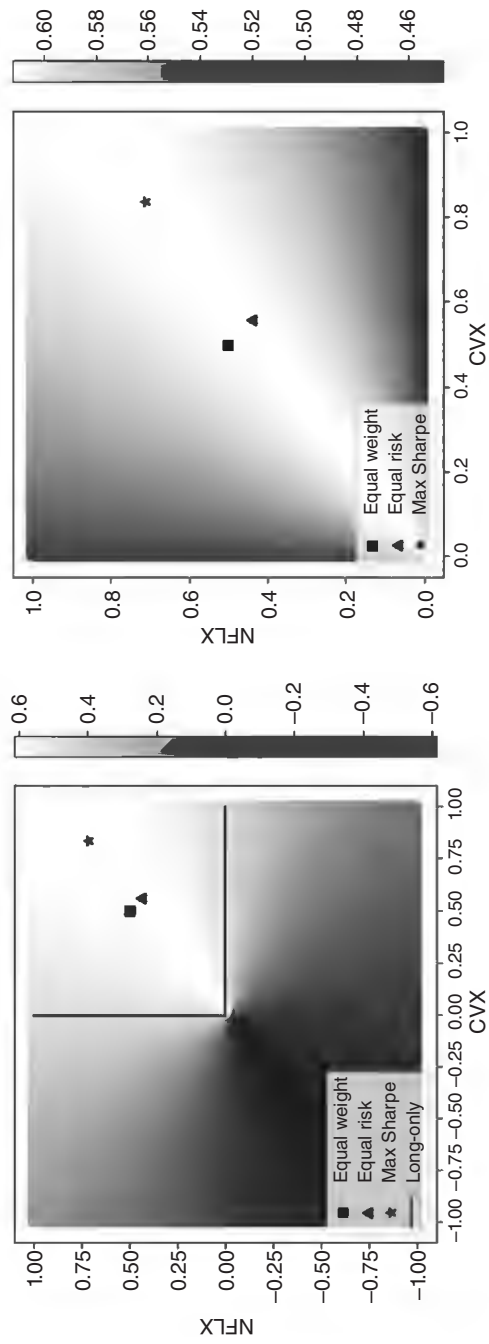
**EXHIBIT 6.3** Historical S&P 500 Volatility



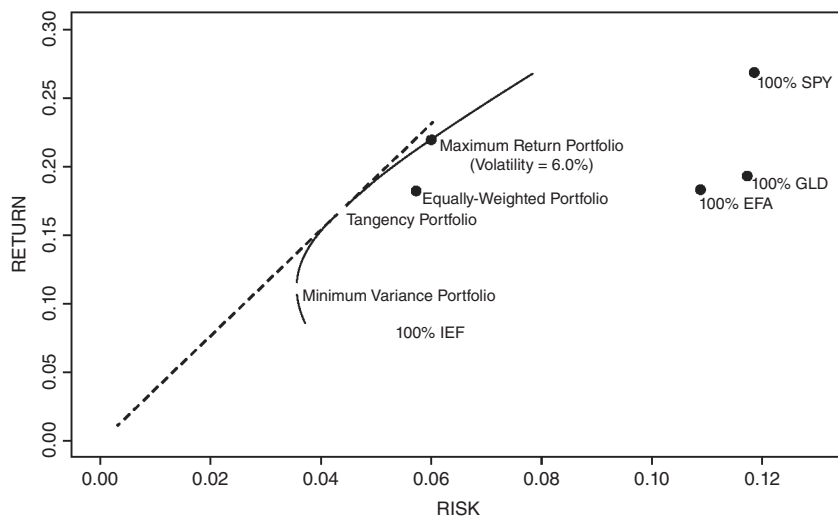
**EXHIBIT 6.4** Rolling Yearly Correlation Between S&P 500 and Nikkei 225



**EXHIBIT 6.5** Correlation Over Time Between Similar and Dissimilar Instruments

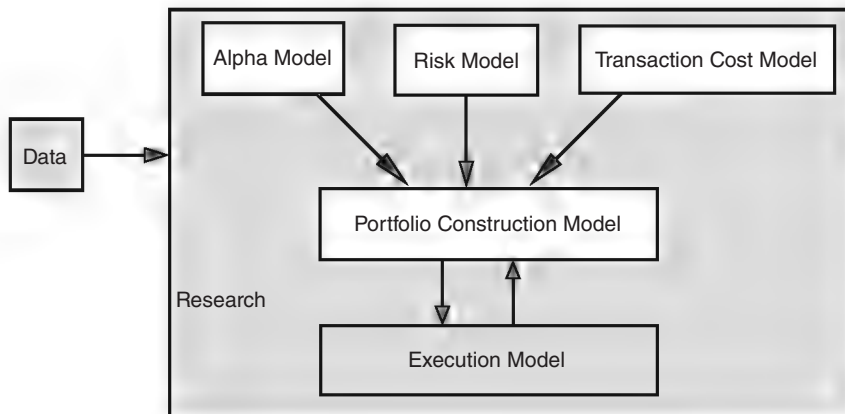


**EXHIBIT 6.6** Visual Representation of Constraining the Search Space for an Optimization

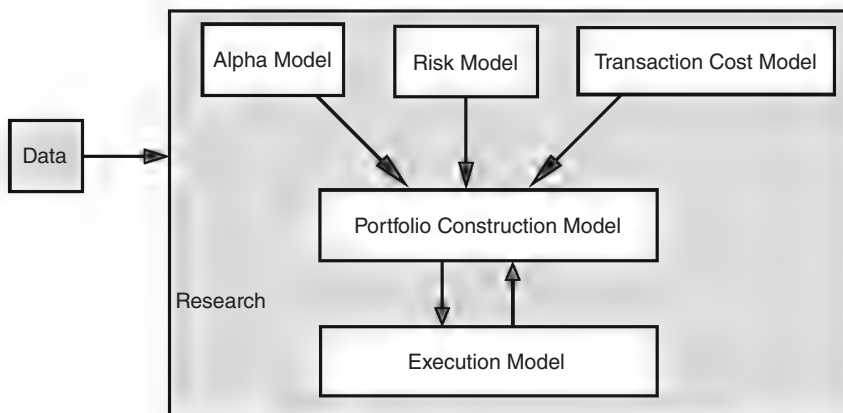


**EXHIBIT 6.7** The Efficient Frontier.

Source: Adapted from Daniela Hanicova, “Markowitz Model,” [www.quantpedia.com/markowitz-model](http://www.quantpedia.com/markowitz-model)

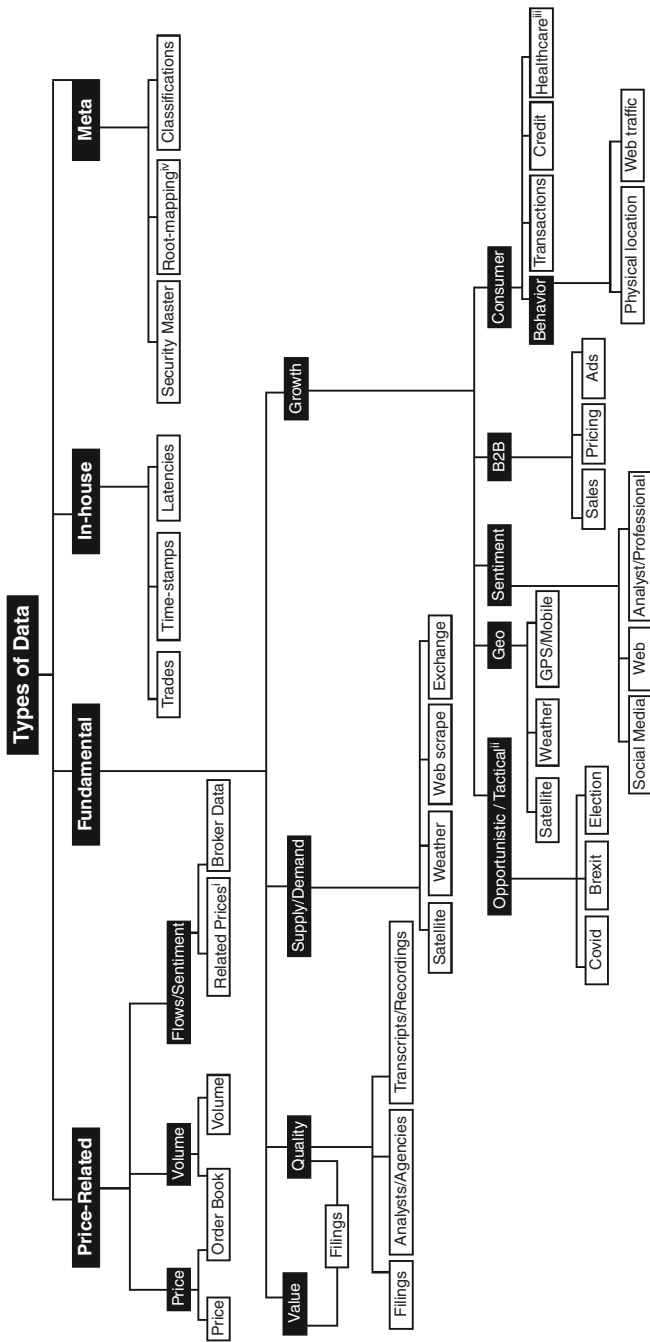


**EXHIBIT 6.8** Schematic of the Black Box



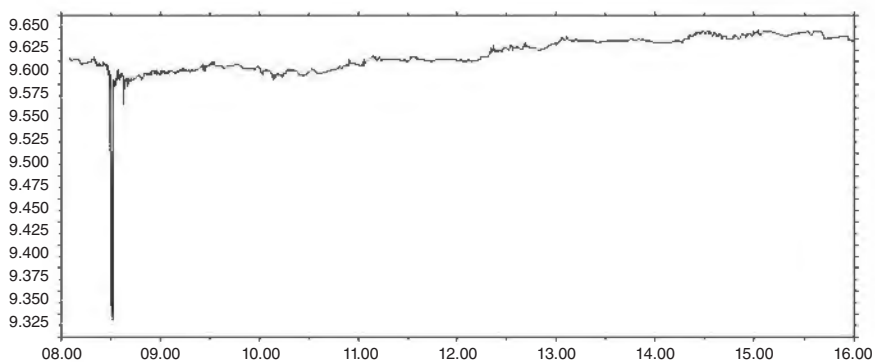
**EXHIBIT 7.1** Schematic of the Black Box



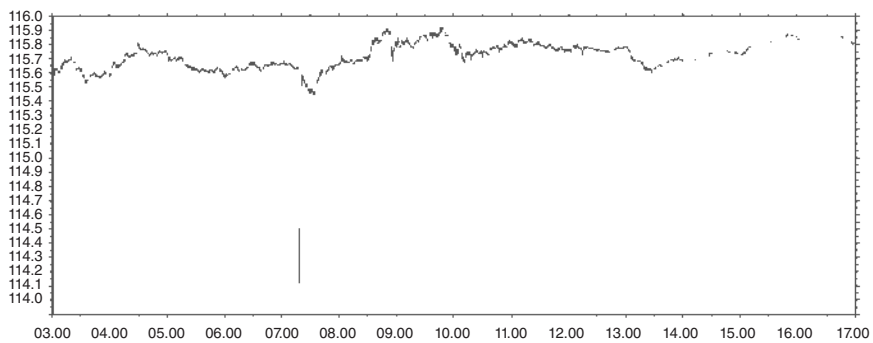


- Legend
- | category       |
|----------------|
| item or source |
- Notes
- the prices of related instruments, for example, options on the same underlying instrument, or price action of correlated instruments.
  - these are historical examples.
  - healthcare data are a newer area, not really available yet, and questionably included in this category.
  - we mean the mapping of a given instrument to the underlying asset. For example, there may be many bonds issued by a single issuer, but they all need to be mapped back to that issuer.

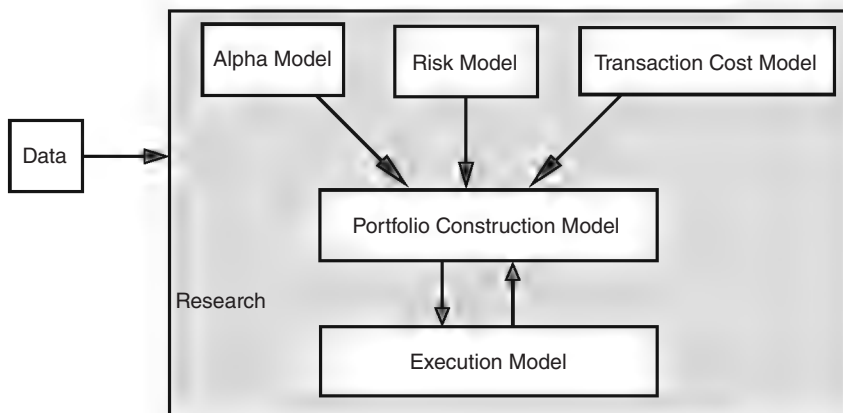
**EXHIBIT 8.1** A Taxonomy of Data



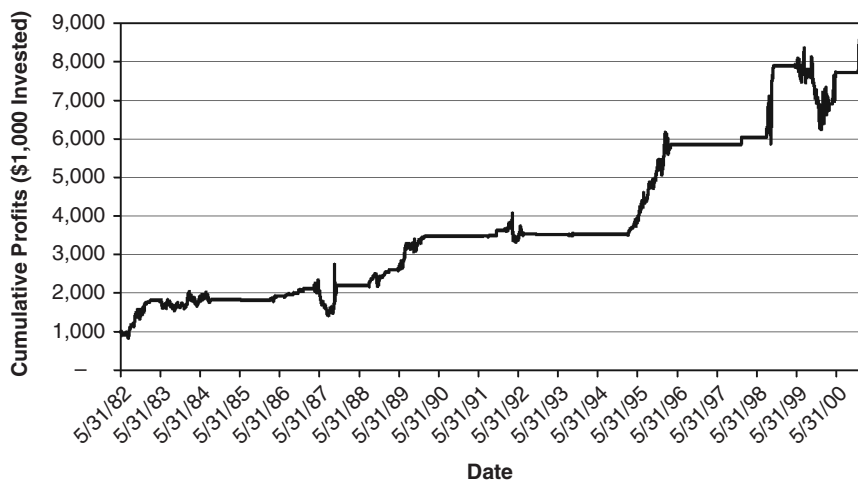
**EXHIBIT 8.2** September 2008 Mexican Peso Futures Contract on July 15, 2008



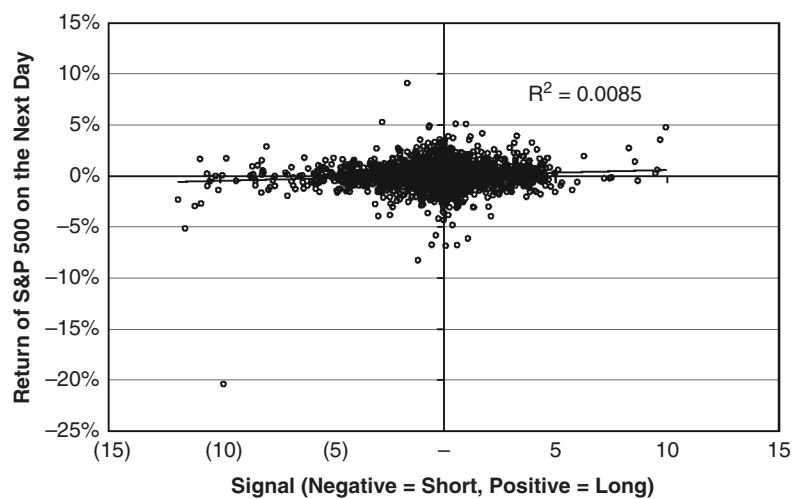
**EXHIBIT 8.3** June 2008 German Bund Futures Contract on March 28, 2008



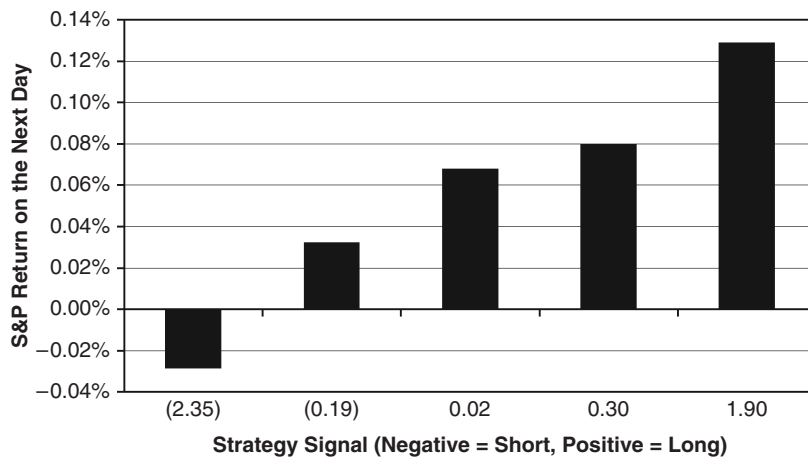
**EXHIBIT 8.4** Schematic of the Black Box



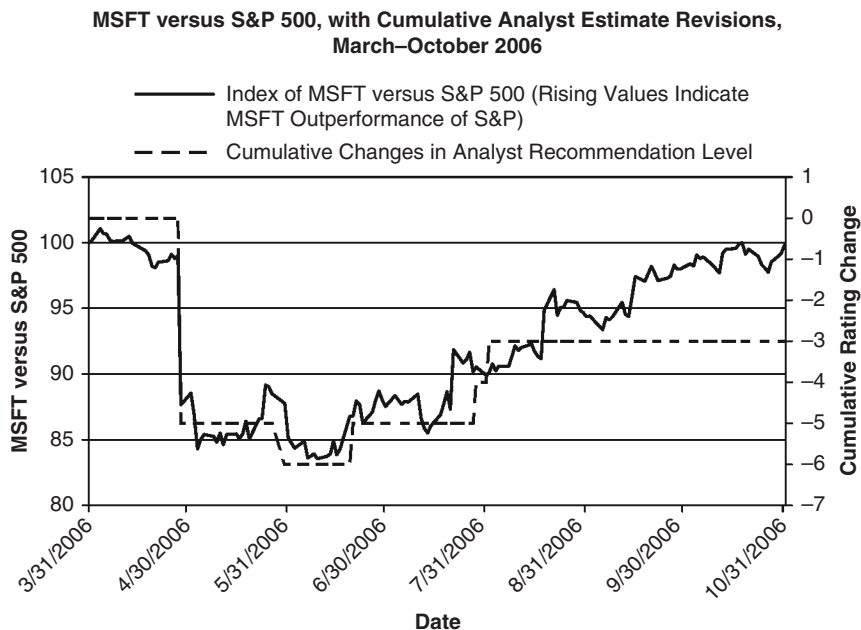
**EXHIBIT 9.1** Back-Tested Cumulative Profits of the S&P 500 Strategy



**EXHIBIT 9.2**  $R^2$  of the S&P 500 Strategy

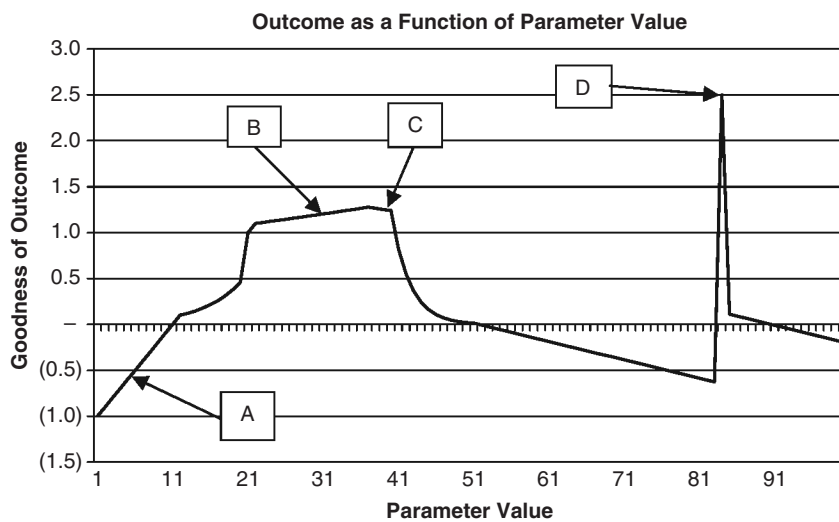


**EXHIBIT 9.3** Quintile Study of S&P 500 Strategy's Signals vs. S&P 500 Returns

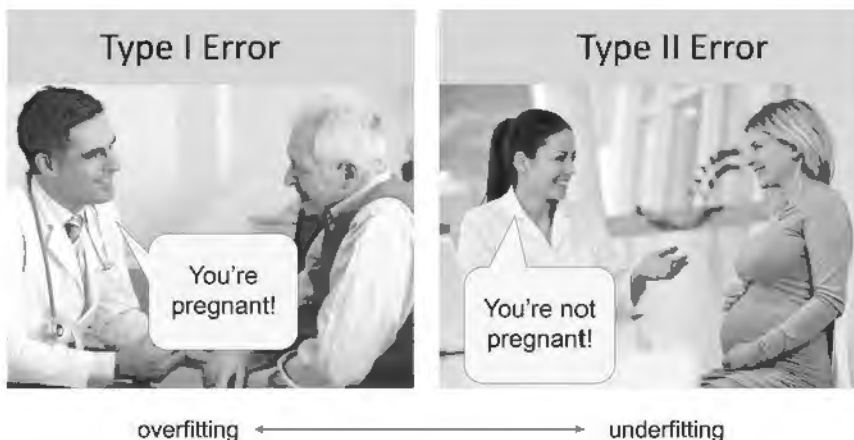


**EXHIBIT 9.4** Illustration of Time Decay of Alpha

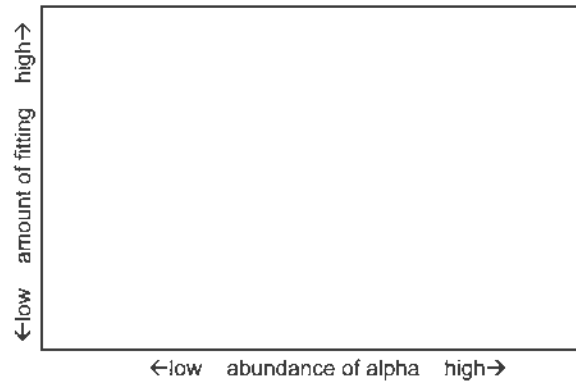




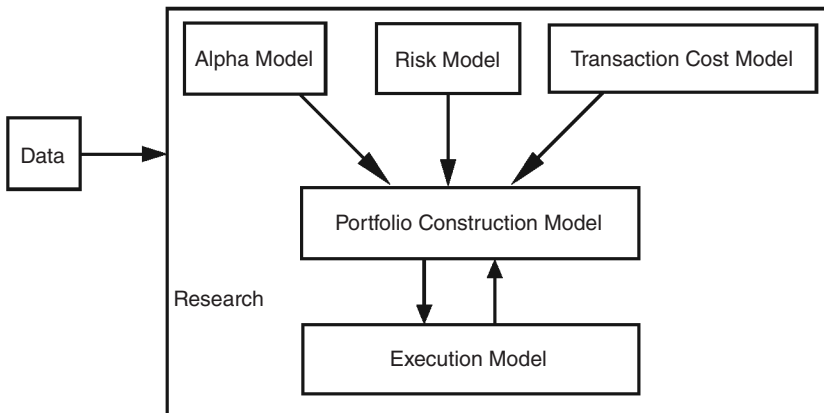
**EXHIBIT 9.5** Choosing the Right Parameter Values



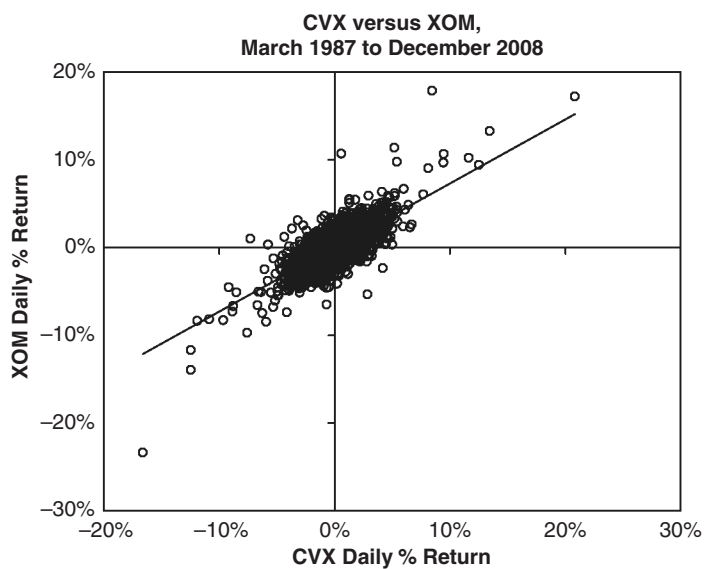
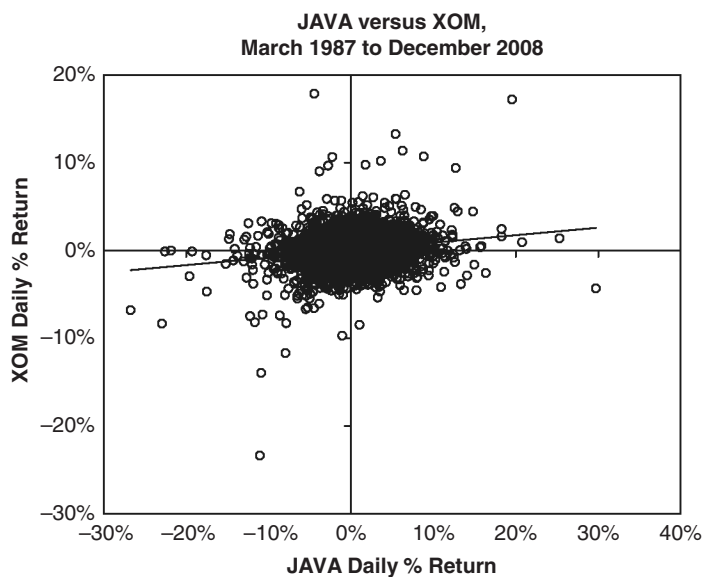
**EXHIBIT 9.6** Overfitting (Type I Error) vs Underfitting (Type II Error) Images/  
Shutterstock; skynesher/Getty Images



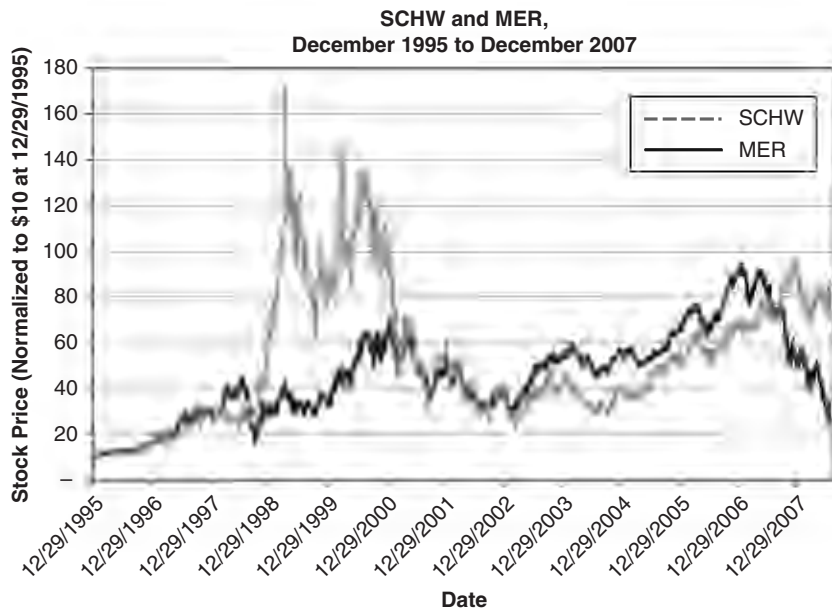
**EXHIBIT 9.7** Determining the Correct Balance Between Overfitting (Type I Error) vs Underfitting (Type II Error)



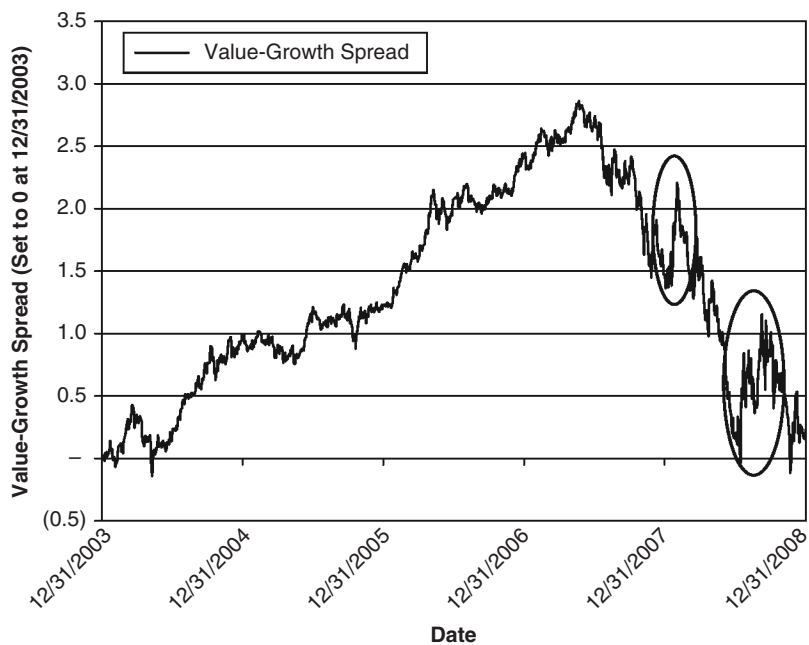
**EXHIBIT 9.8** Schematic of the Black Box



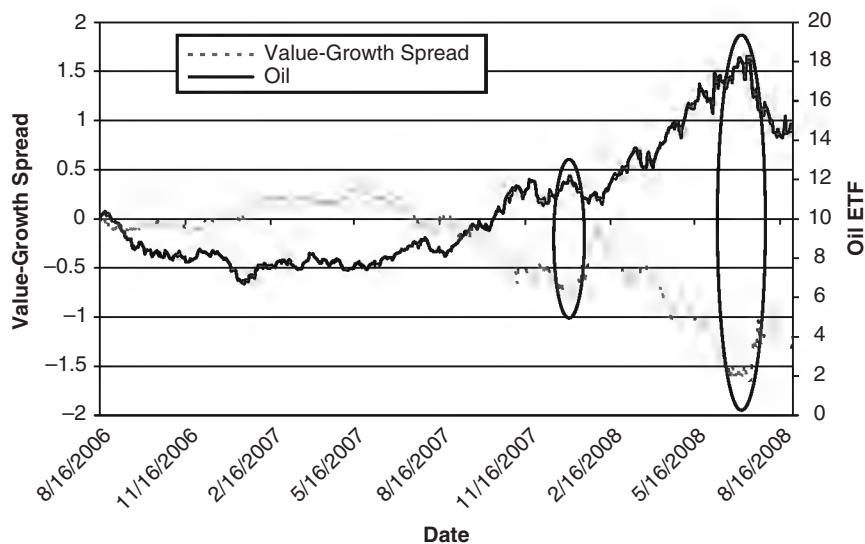
**EXHIBIT 10.1** A Demonstration of Nonlinear and Linear Relationships



**EXHIBIT 10.2** Regime Changes in a Relationship between Two Stocks

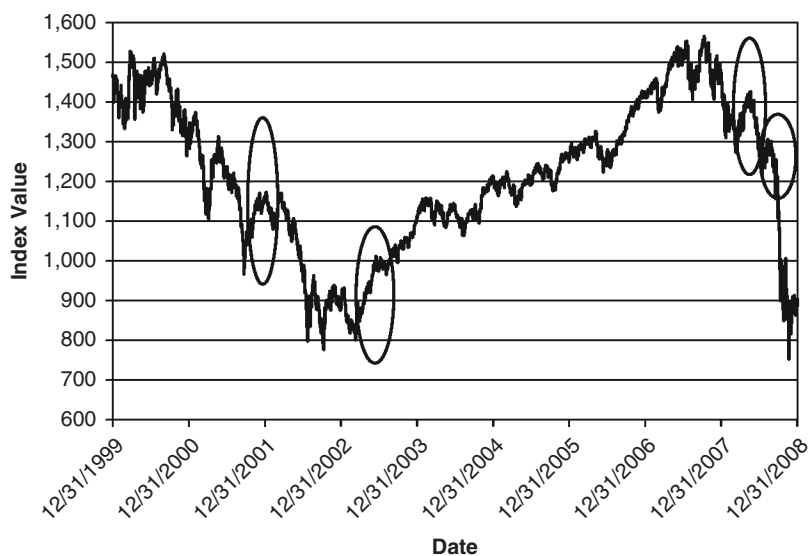


**EXHIBIT 10.3** Value/Growth Spread, 2003–2008



**EXHIBIT 10.4** Value/Growth Spreads versus Oil Prices, Normalized to August 16, 2006

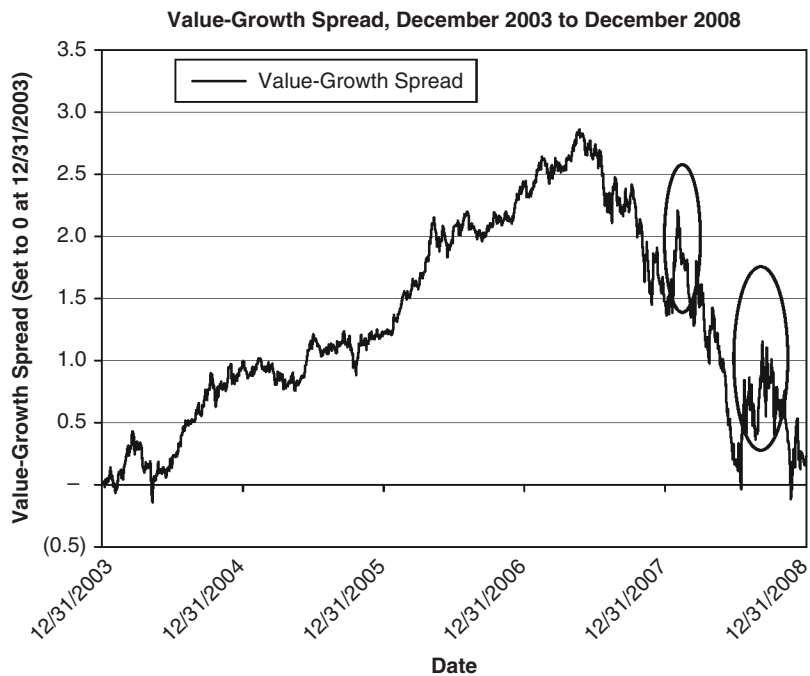




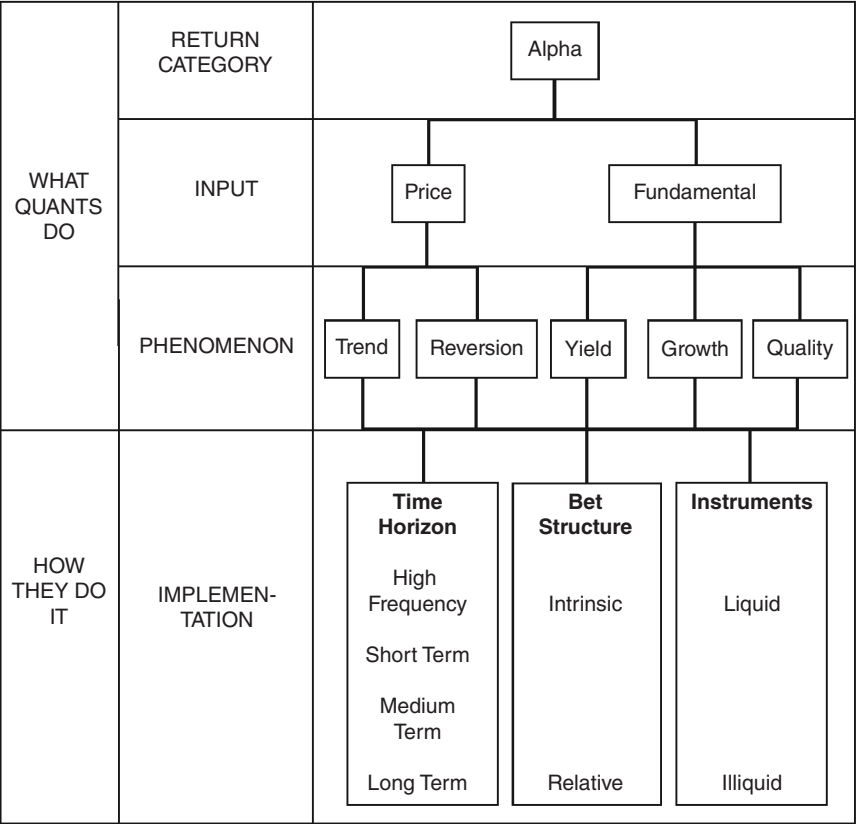
**EXHIBIT 10.5** S&P 500 Price Index, December 1999–December 2008

**EXHIBIT 10.6** Pulte Homes, Inc. (NYSE: PHM), May 31–August 31, 2007

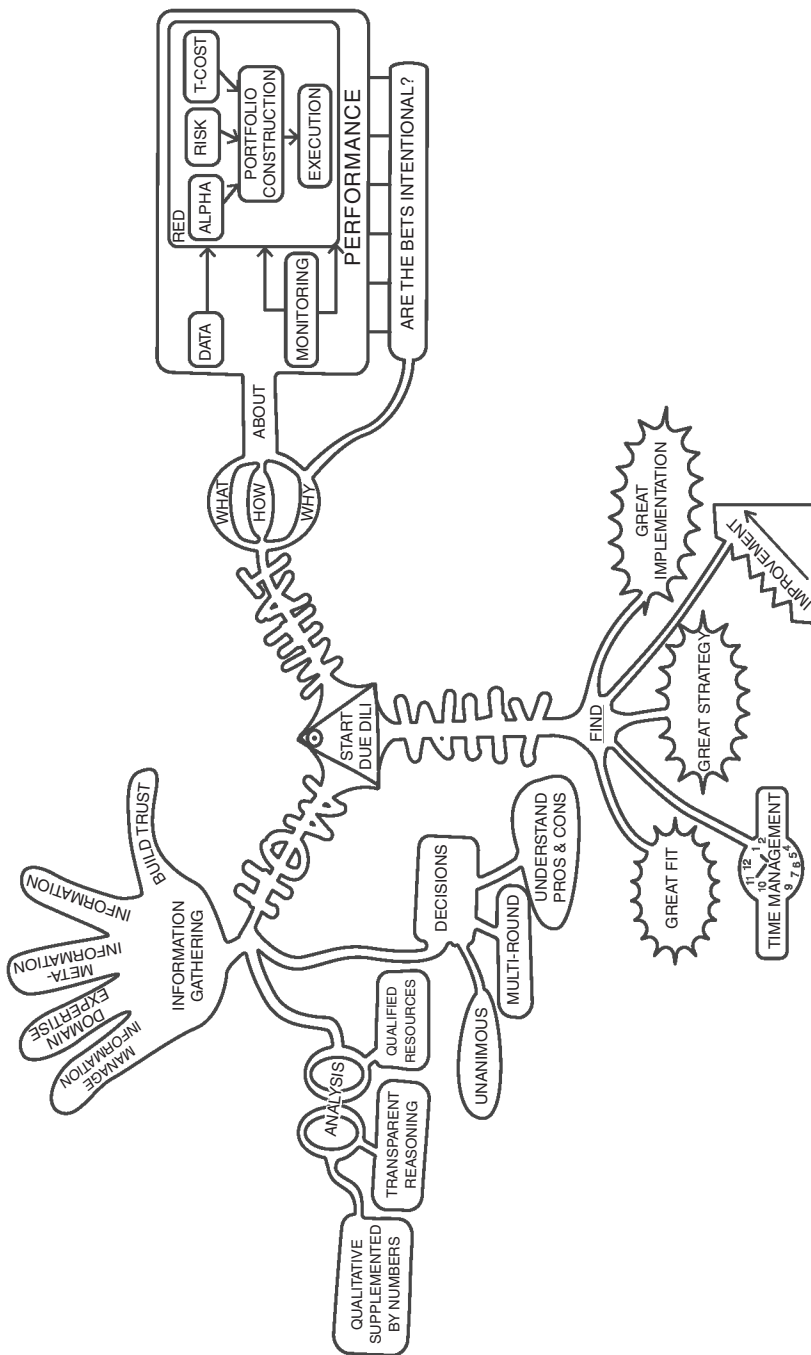
PHM, Summer 2007	Price Change (%)	Average Daily Volume (millions)
May 31–July 23	–22.0	3.5
July 24–August 3	–12.5	7.2
August 6–August 9	+15.6	10.4
August 10–August 31	–22.6	5.7



**EXHIBIT 11.1** Regime Changes, as Indicated by the Value/Growth Spread



**EXHIBIT 12.1** Taxonomy of Theory-Driven Alpha Strategies and Implementation Approaches



**EXHIBIT 12.2** A Mind Map of the Investment Due Diligence Process

**EXHIBIT 14.1** Mockup of an Order Book for a Fictitious Ticker

ID	Size	Bid	Offer	Size	ID
Bid1	55	100.00	100.01	2,000	Offer1
Bid2	1,000	100.00	100.02	2,950	Offer2
Bid3	3,100	99.99	100.02	600	Offer3
Bid4	200	99.99	100.03	300	Offer4
Bid5	5,000	99.98	100.04	1,000	Offer5

**EXHIBIT 14.2** Mockup of an Order Book for a Fictitious Ticker After a Large Market Order to Buy

ID	Size	Bid	Offer	Size	ID
Bid1	55	100.00	100.02	1,950	Offer2
Bid2	1,000	100.00	100.02	600	Offer3
Bid3	3,100	99.99	100.03	300	Offer4
Bid4	200	99.99	100.04	1,000	Offer5
Bid5	5,000	99.98			

**EXHIBIT 14.3** Mockup of an Order Book for a Fictitious Ticker after a Limit Order to Sell at the Bid

ID	Size	Bid	Offer	Size	ID
Bid2	55	100.00	100.02	1,950	Offer2
Bid3	3,100	99.99	100.02	600	Offer3
Bid4	200	99.99	100.03	300	Offer4
Bid5	5,000	99.98	100.04	1,000	Offer5



**EXHIBIT 14.4** Mockup of an Order Book for a Fictitious Ticker after a Limit Order to Sell, which Joins the Best Offer

ID	Size	Bid	Offer	Size	ID
Bid2	55	100.00	100.02	1,950	Offer2
Bid3	3,100	99.99	100.02	600	Offer3
Bid4	200	99.99	100.02	1,000	Offer6
Bid5	5,000	99.98	100.03	300	Offer4
			100.04	1,000	Offer5

**EXHIBIT 14.5** Mockup of an Order Book for a Fictitious Ticker after a Limit Order to Sell, which Improves the Best Offer

ID	Size	Bid	Offer	Size	ID
Bid2	55	100.00	100.01	2,000	Offer7
Bid3	3,100	99.99	100.02	1,950	Offer2
Bid4	200	99.99	100.02	600	Offer3
Bid5	5,000	99.98	100.02	1,000	Offer6
			100.03	300	Offer4
			100.04	1,000	Offer5

**EXHIBIT 14.6** Mockup of an Order Book for a Fictitious Ticker

ID	Size	Bid	Offer	Size	ID
Bid1	3,100	99.99	100.01	2,000	Offer1
Bid2	200	99.99	100.02	2,950	Offer2
Bid3	5,000	99.98	100.02	600	Offer3
			100.03	300	Offer4
			100.04	1,000	Offer5

**EXHIBIT 14.7** Mockup of an Order Book for a Fictitious Ticker with Additional Bids

ID	Size	Bid	Offer	Size	ID
Bid4	1,000	100.00	100.01	2,000	Offer1
Bid5	6,000	100.00	100.02	2,950	Offer2
Bid1	3,100	99.99	100.02	600	Offer3
Bid2	200	99.99	100.03	300	Offer4
Bid3	5,000	99.98	100.04	1,000	Offer5

**EXHIBIT 14.8** Mockup of an Order Book for a Fictitious Ticker After 1,000 Shares Have Been Removed from the Bid

ID	Size	Bid	Offer	Size	ID
Bid5	6,000	100.00	100.01	2,000	Offer1
Bid1	3,100	99.99	100.02	2,950	Offer2
Bid2	200	99.99	100.02	600	Offer3
Bid3	5,000	99.98	100.03	300	Offer4
			100.04	1,000	Offer5

**EXHIBIT 14.9** Mockup of an Order Book for a Fictitious Ticker after All \$100.00 Shares Have Been Removed from the Bid

ID	Size	Bid	Offer	Size	ID
Bid1	3,100	99.99	100.00	2,000	Offer6
Bid2	200	99.99	100.01	2,000	Offer1
Bid3	5,000	99.98	100.02	2,950	Offer2
			100.02	600	Offer3
			100.03	300	Offer4
			100.04	1,000	Offer5

**EXHIBIT 14.10** Mockup of an Order Book for a Fictitious Ticker After Two 2,000 Share Bids at \$100.01

ID	Size	Bid	Offer	Size	ID
Bid4	2,000	100.01	100.02	2,950	Offer2
Bid1	3,100	99.99	100.02	600	Offer3
Bid2	200	99.99	100.03	300	Offer4
Bid3	5,000	99.98	100.04	1,000	Offer5

**EXHIBIT 14.11** Breakdown of Messages at Various Intervals and Percentiles  
for EBAY on July 20, 2012

	50th Percentile	99th Percentile	99.9th Percentile	99.99th Percentile	99.999th Percentile
1 second	13	259	546	1755	4179
100 milliseconds	0	13	84	863	1306
10 milliseconds	0	1	7	269	557
1 millisecond	0	0	1	56	106



**EXHIBIT 15.1** Mockup of an Order Book for a Fictitious Ticker

ID	Size	Bid	Offer	Size	ID
Bid1	1,000	100.00	100.01	2,000	Offer1
Bid2	3,100	99.99	100.02	3,000	Offer2
Bid3	2,000	99.99	100.02	1,000	Offer3
Bid4	5,000	99.98	100.03	4,000	Offer4
Bid5	6,000	99.97	100.04	1,000	Offer5

**EXHIBIT 15.2** Mockup of an Order Book for a Fictitious Ticker after a Market Order to Buy 10,000 Shares Is Mostly Filled by a CMM Acting as an Agent of the Customer

ID	Size	Bid	Offer	Size	ID
Bid1	1,000	100.00	100.03	500	Offer4
Bid2	3,100	99.99	100.04	1,000	Offer5
Bid3	2,000	99.99			
Bid4	5,000	99.98			
Bid5	6,000	99.97			

**EXHIBIT A.1** Average Price Movement in SPY (%)

	2000–2006	2007–2012	% Difference
close:close	0.84	1.03	+23
open:close (intraday)	0.76	0.82	+8
close:open (overnight)	0.37	0.59	+59
high:low	1.47	1.72	+17

**EXHIBIT A.2** Median Price Movement in SPY (%)

	2000–2006	2007–2012	% Difference
close:close	0.62	0.67	+8
open:close (intraday)	0.55	0.53	–3
close:open (overnight)	0.26	0.39	+51
high:low	1.26	1.33	+5

**EXHIBIT A.3** Frequency of 3% or Greater Moves in SPY (%)

	2000–2006	2007–2012	% Difference
close:close	2.56	5.87	+129
open:close (intraday)	1.53	2.69	+75
close:open (overnight)	0.11	0.83	+629
high:low	6.20	10.91	+76

**EXHIBIT A.4** Frequency of 4% or Greater Moves in the SPY (%)

	2000–2006	2007–2012	% Difference
close:close	0.68	2.97	+335
open:close (intraday)	0.28	1.38	+386
close:open (overnight)	0.11	0.48	+325
high:low	1.65	5.73	+248