

# **INSIDE THE BLACK BOX**

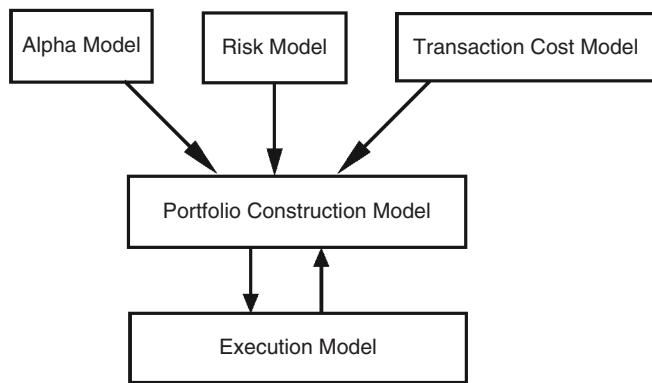
**A SIMPLE GUIDE TO SYSTEMATIC  
INVESTING, THIRD EDITION**

**BY RISHI K. NARANG**

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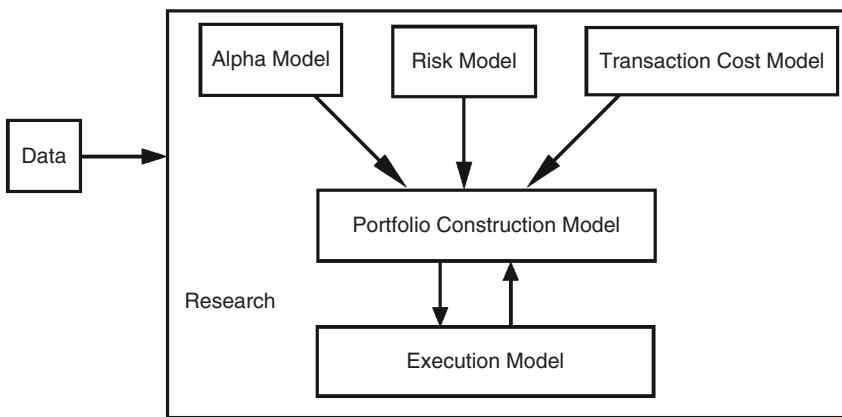
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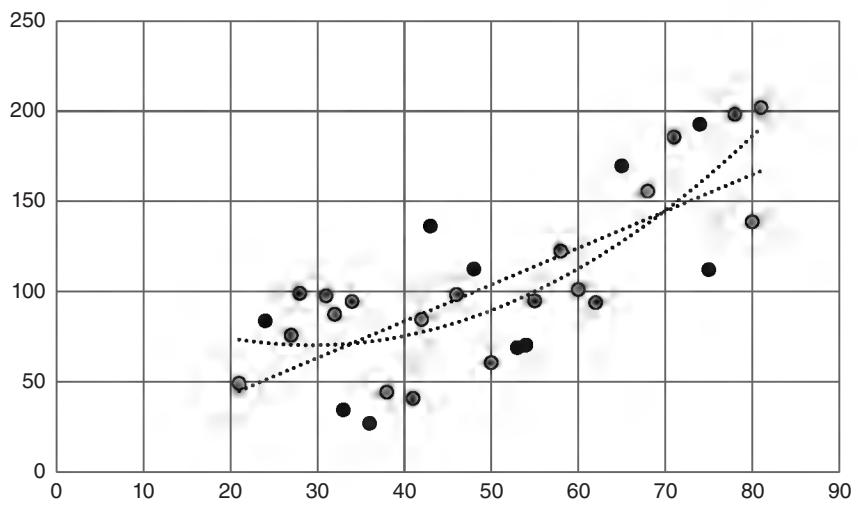
**EXHIBIT 2.1** Basic Structure of a Quant Trading Strategy

**EXHIBIT 2.2** Moving from an Existing Portfolio to a New Target Portfolio

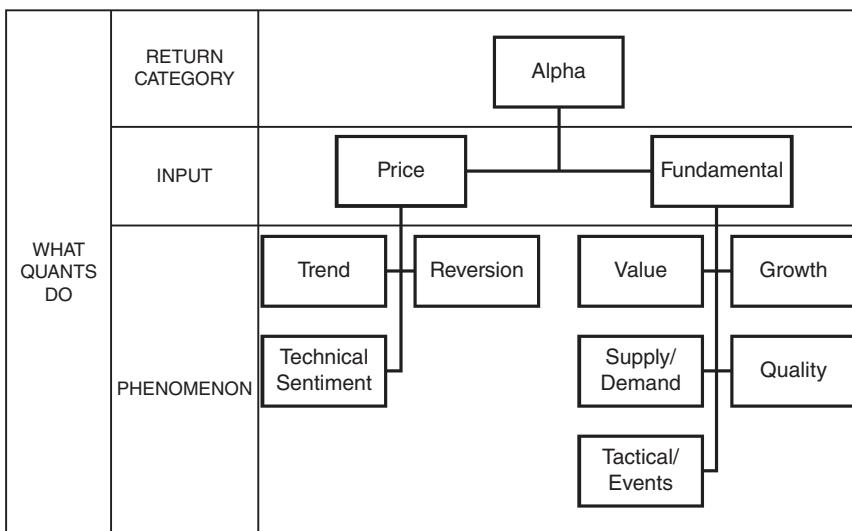
|                             | Current Portfolio | New Target Portfolio | Trades to Execute |
|-----------------------------|-------------------|----------------------|-------------------|
| S&P500 Index                | Short 30%         | Short 25%            | Buy to Cover 5%   |
| EUROSTOXX Index             | Long 20%          | Long 25%             | Buy 5%            |
| U.S. 10-Year Treasury Notes | Long 40%          | Long 25%             | Sell 15%          |
| German 10-Year Bunds        | Short 10%         | Short 25%            | Sell Short 15%    |



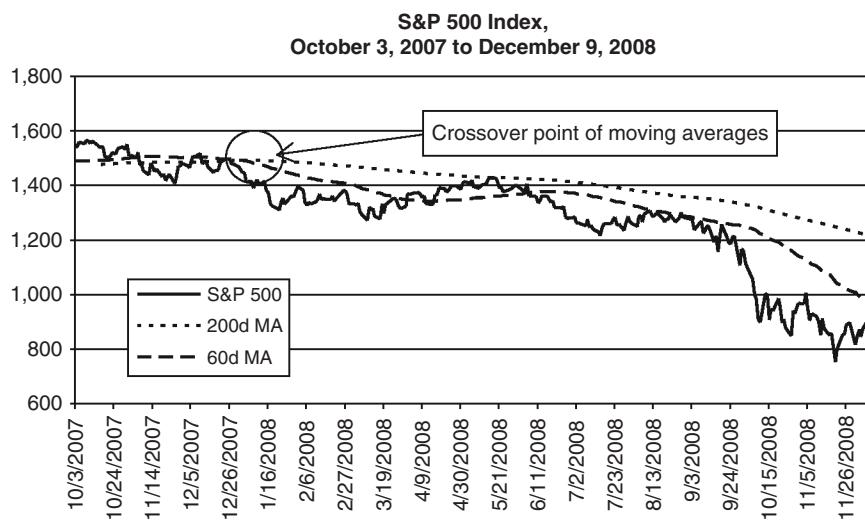
**EXHIBIT 2.3** The Black Box Revealed



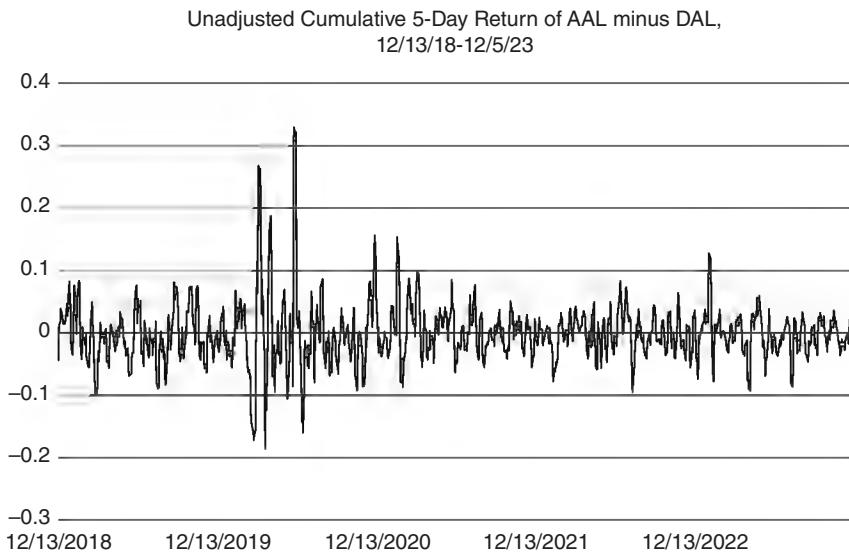
**EXHIBIT 3.1** Linearity of a Relationship



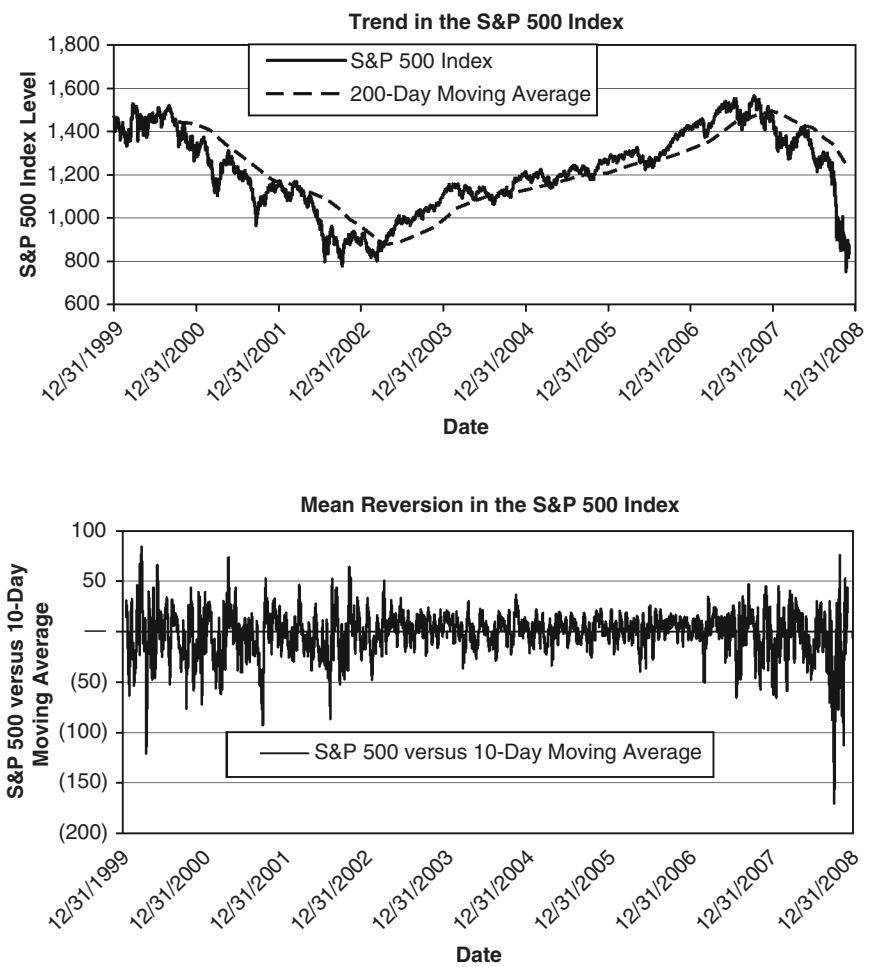
**EXHIBIT 3.2** A Taxonomy of Theory-Driven Alpha Models



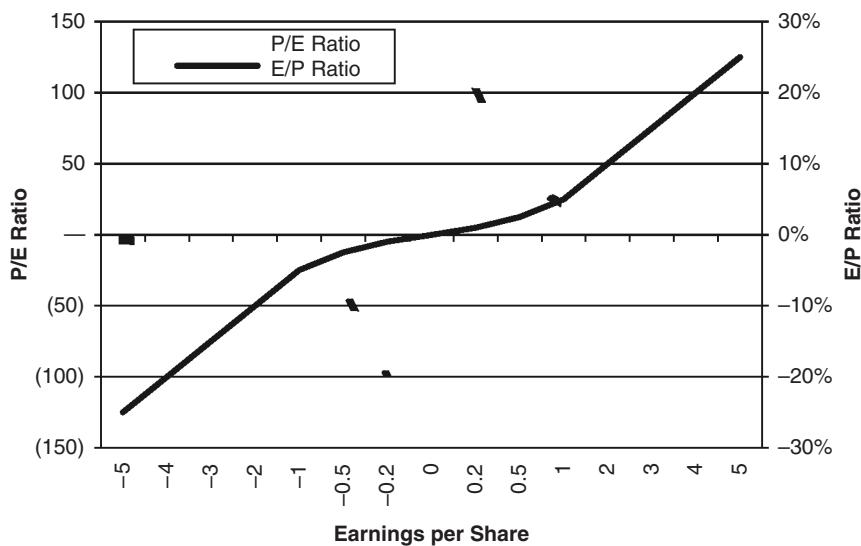
**EXHIBIT 3.3** S&P 500 Trend



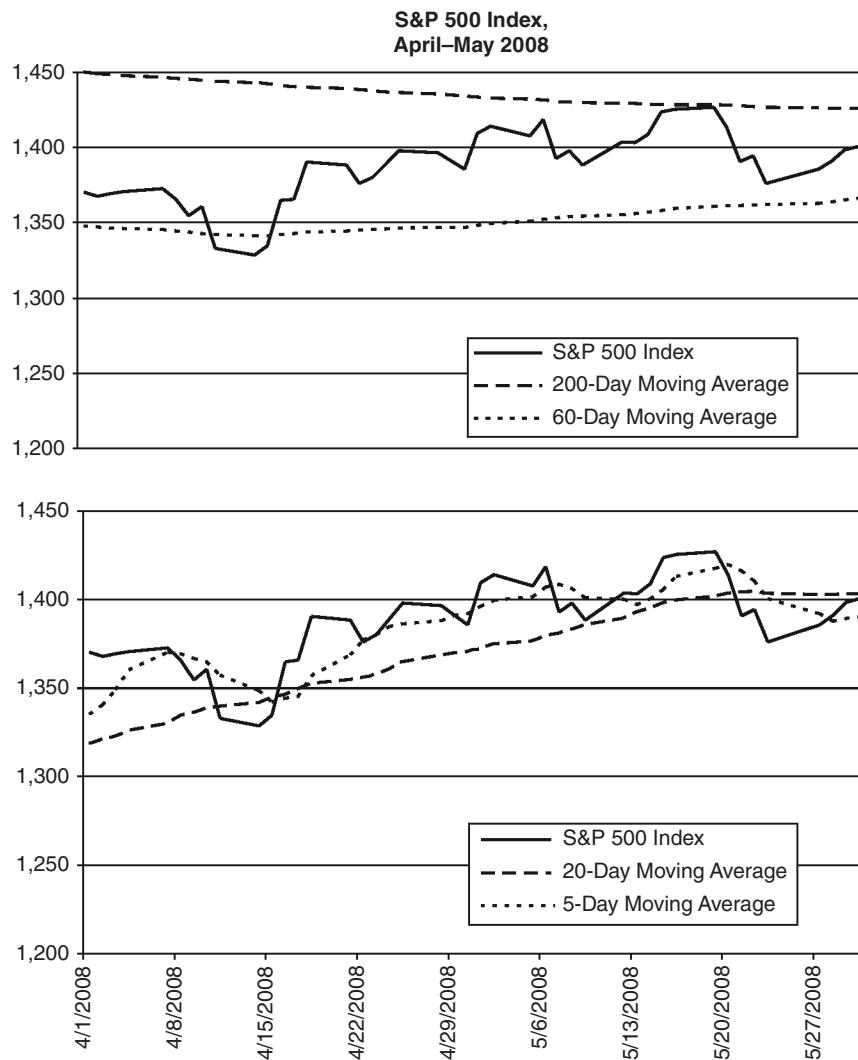
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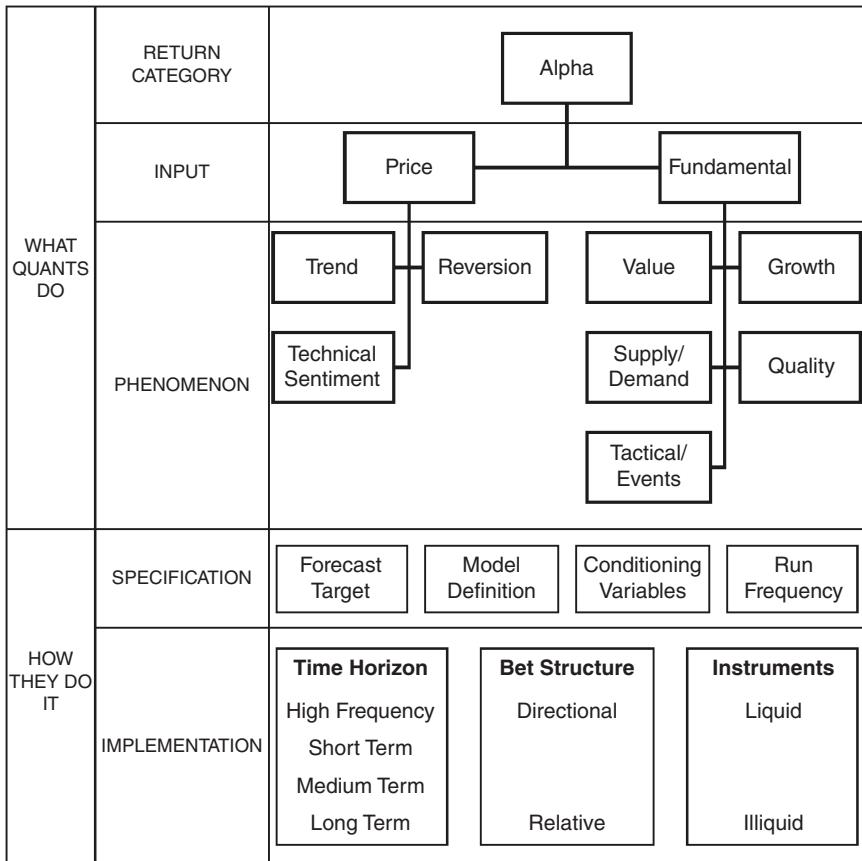
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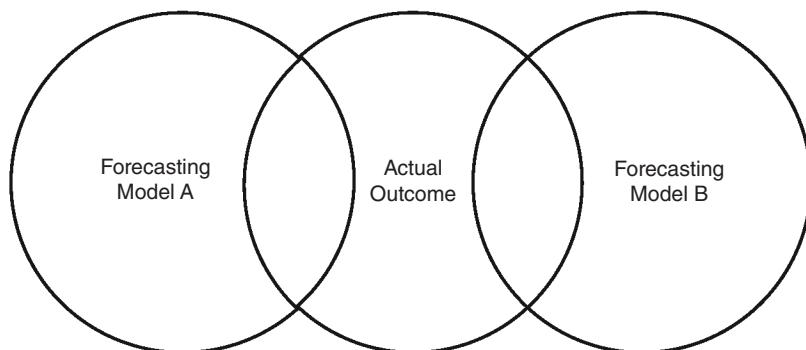
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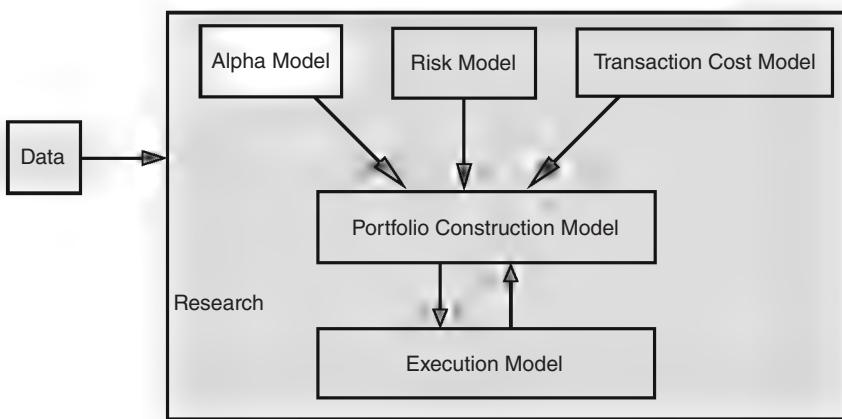
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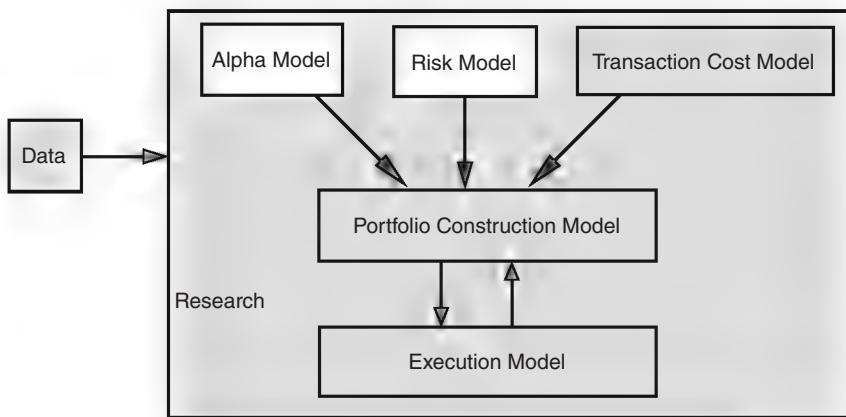
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**EXHIBIT 3.10** A Simple Conditional (Nonlinear) Model for Blending Alphas

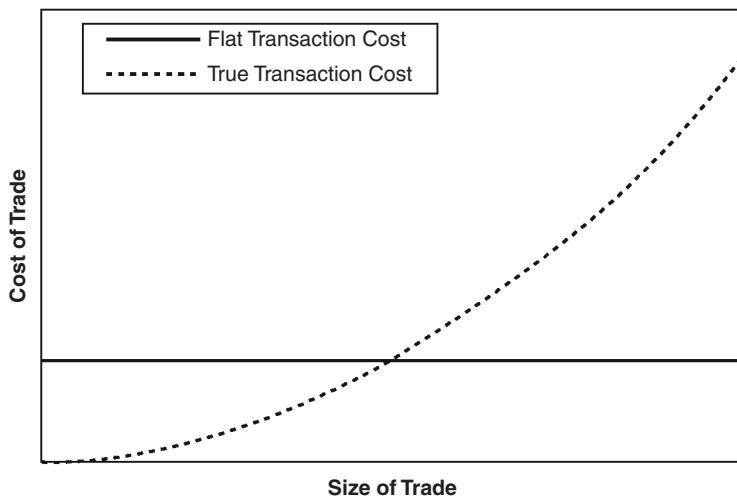
|                             | <b>Value</b> | <b>Momentum</b> | <b>Signal</b> |
|-----------------------------|--------------|-----------------|---------------|
| Value and Momentum Disagree | Long         | Short           | None          |
|                             | <b>Value</b> | <b>Momentum</b> | <b>Signal</b> |
| Value and Momentum Agree    | Long         | Long            | Long          |



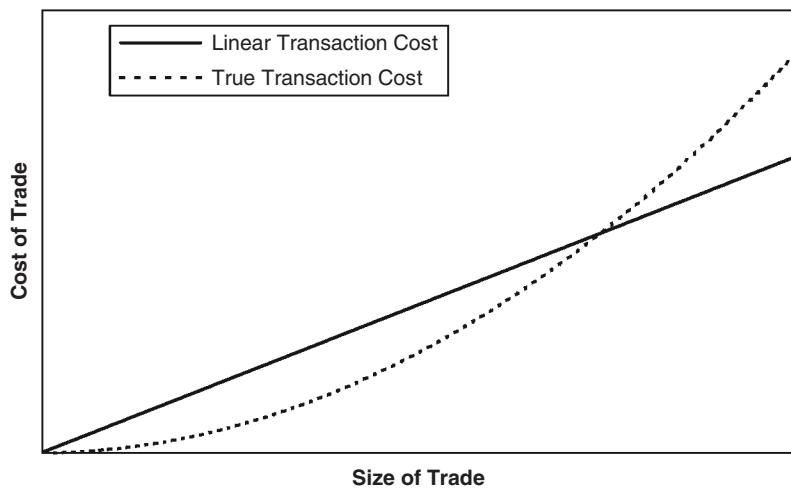
**EXHIBIT 3.11** Schematic of the Black Box



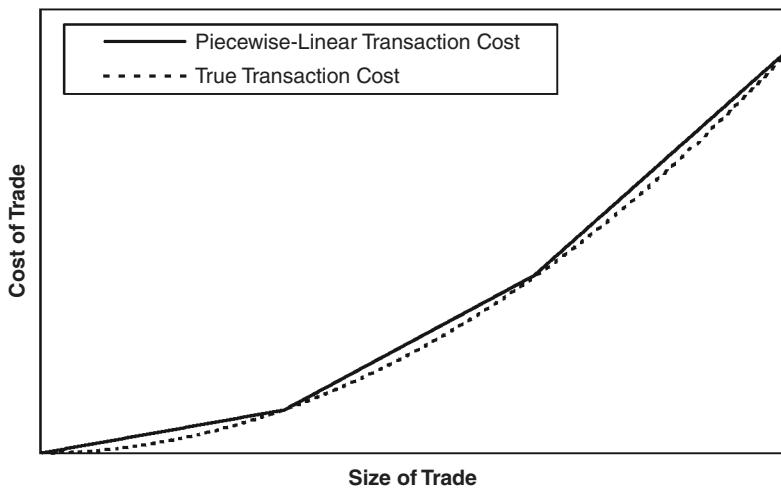
**EXHIBIT 4.1** Schematic of the Black Box



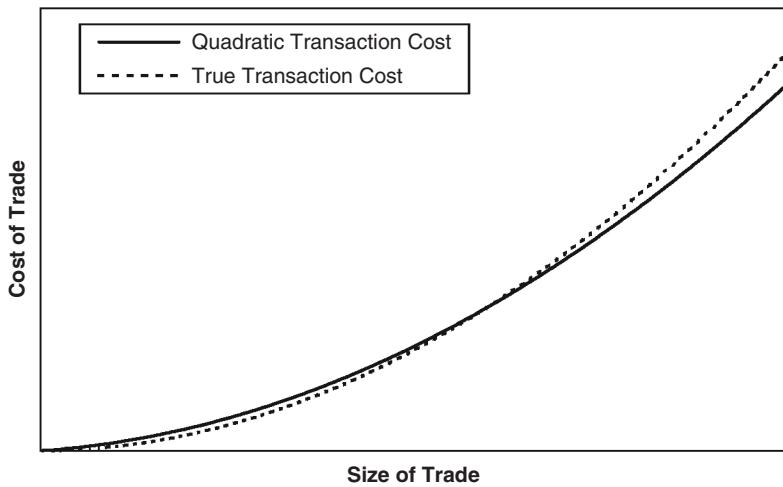
**EXHIBIT 5.1** Flat Transaction Cost Function



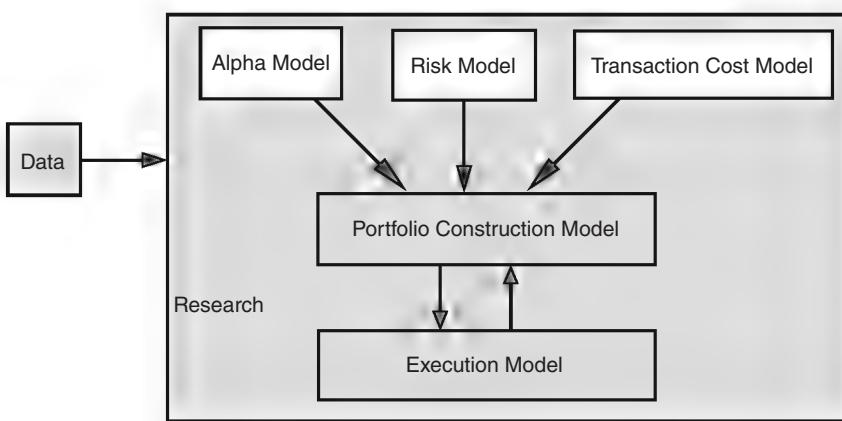
**EXHIBIT 5.2** Linear Transaction Cost Function



**EXHIBIT 5.3** Piecewise-Linear Transaction Cost Function



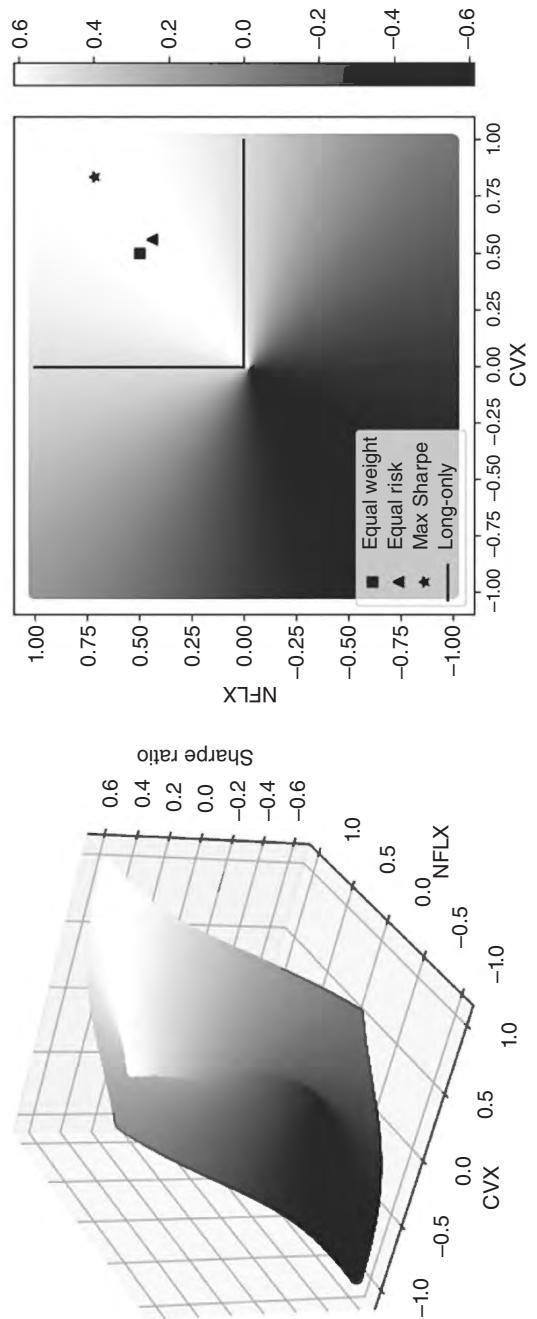
**EXHIBIT 5.4** Quadratic Transaction Cost Function



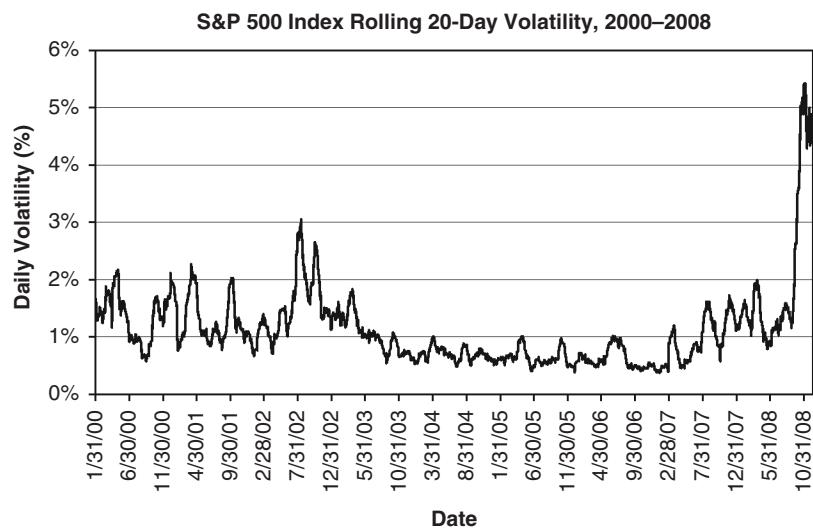
**EXHIBIT 5.5** Schematic of the Black Box

**EXHIBIT 6.1** A Simple Equal Risk Weighted Portfolio

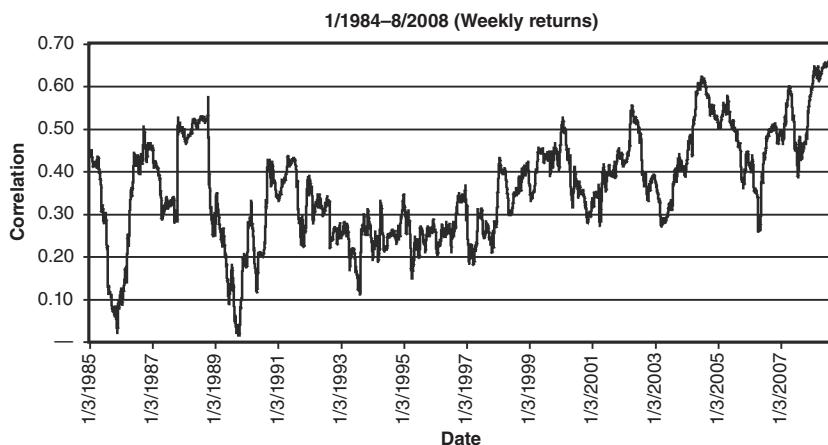
|      | Equal Weight (%) | Volatility (%) | Volatility-Adjusted Weight (%) |
|------|------------------|----------------|--------------------------------|
| GOOG | 50               | 2.5            | 39                             |
| XOM  | 50               | 2.0            | 61                             |



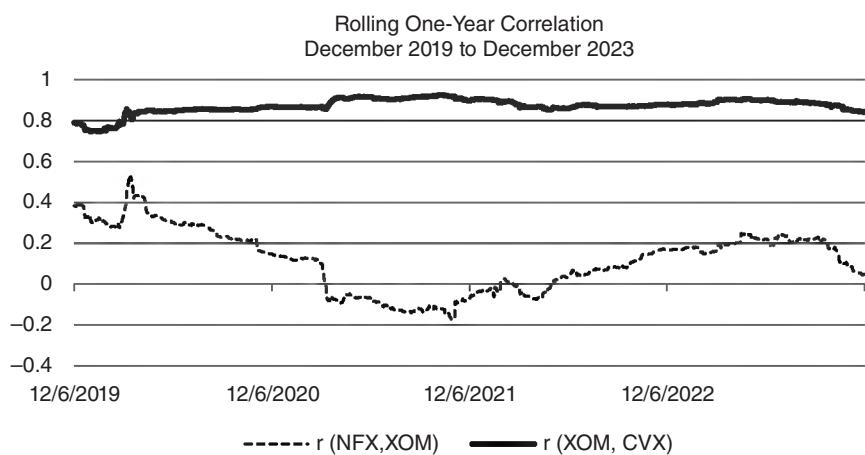
**EXHIBIT 6.2** Visual Representations of the Search Space for an Optimization



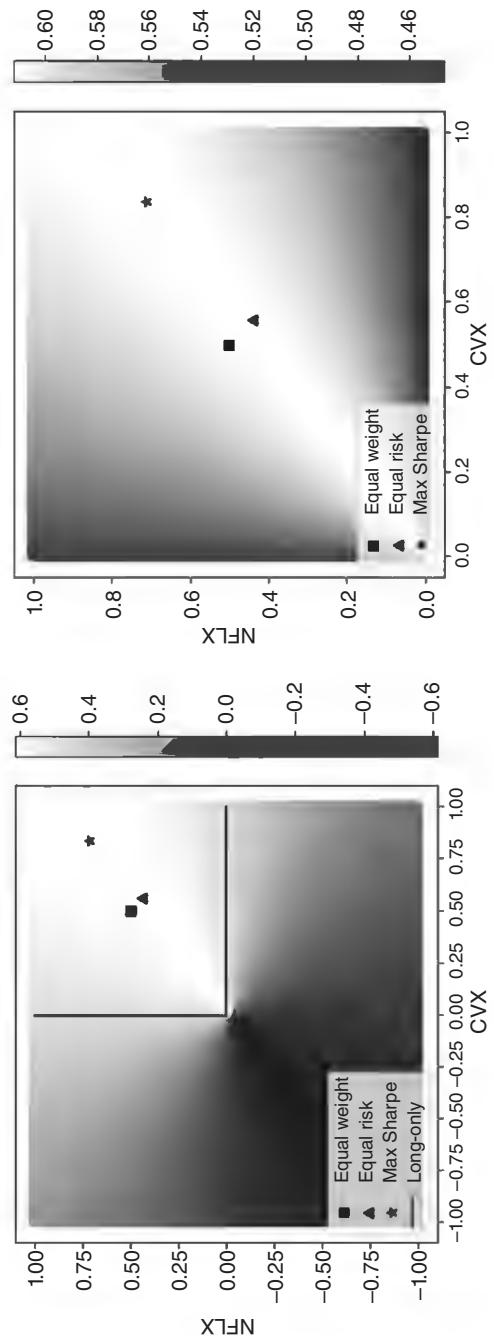
**EXHIBIT 6.3** Historical S&P 500 Volatility



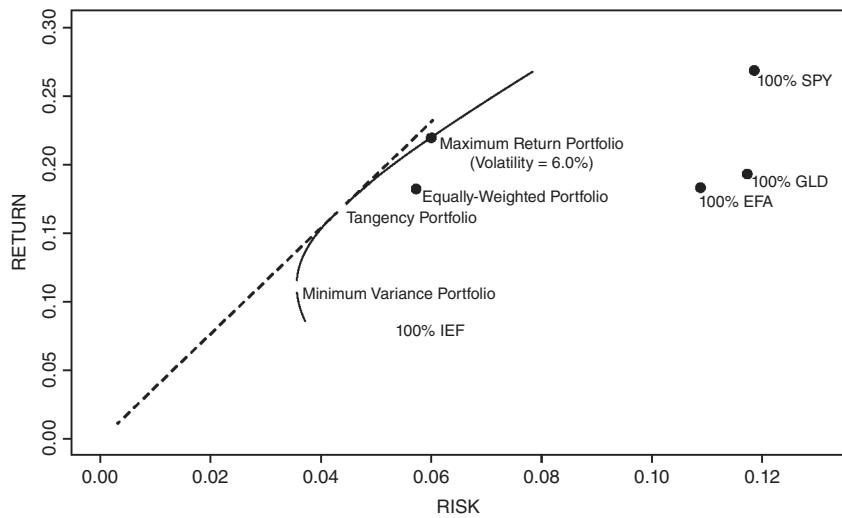
**EXHIBIT 6.4** Rolling Yearly Correlation Between S&P 500 and Nikkei 225



**EXHIBIT 6.5** Correlation Over Time Between Similar and Dissimilar Instruments

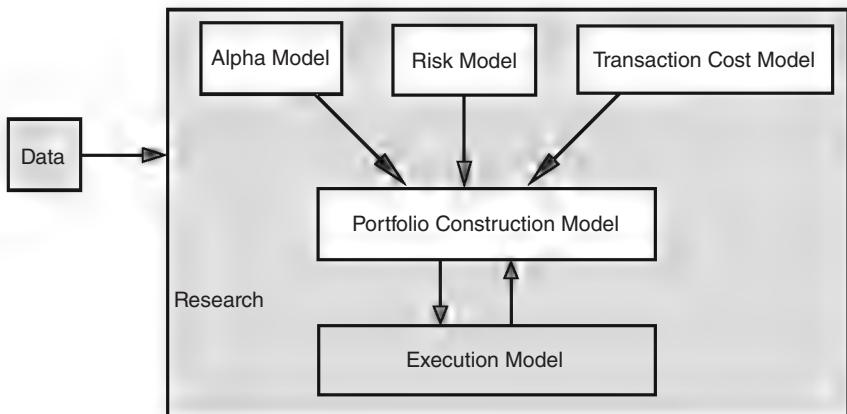


**EXHIBIT 6.6** Visual Representation of Constraining the Search Space for an Optimization

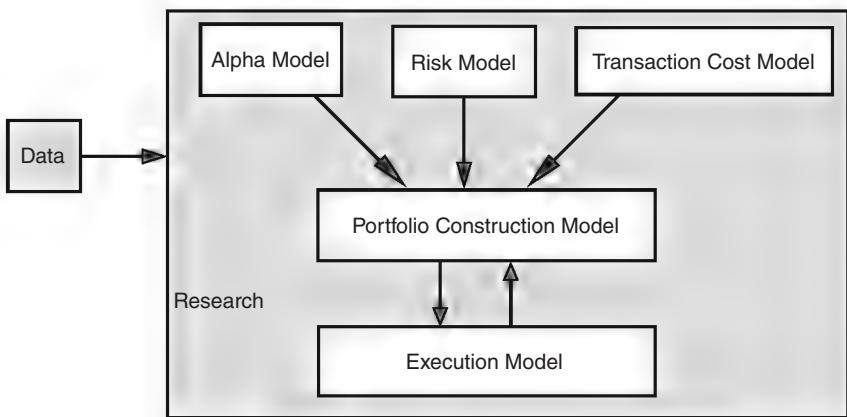


**EXHIBIT 6.7** The Efficient Frontier.

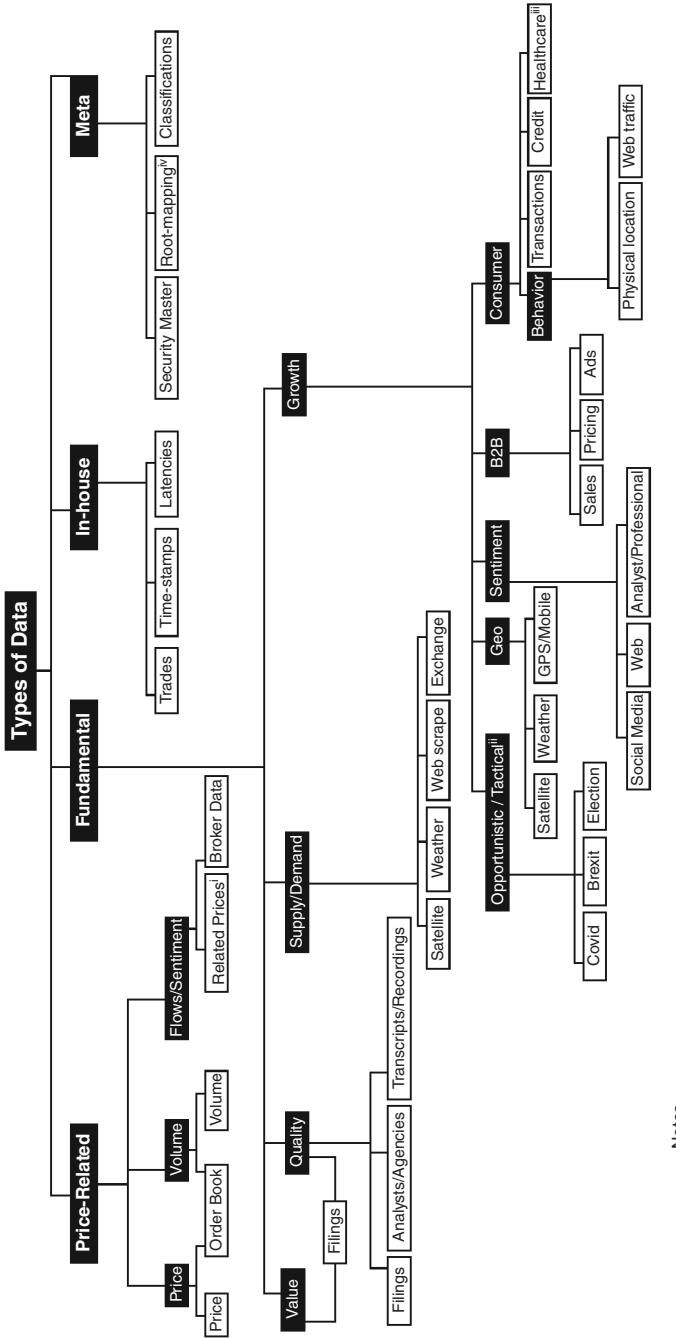
*Source:* Adapted from Daniela Hanicova, “Markowitz Model,” [www.quantpedia.com/markowitz-model](http://www.quantpedia.com/markowitz-model)



**EXHIBIT 6.8** Schematic of the Black Box



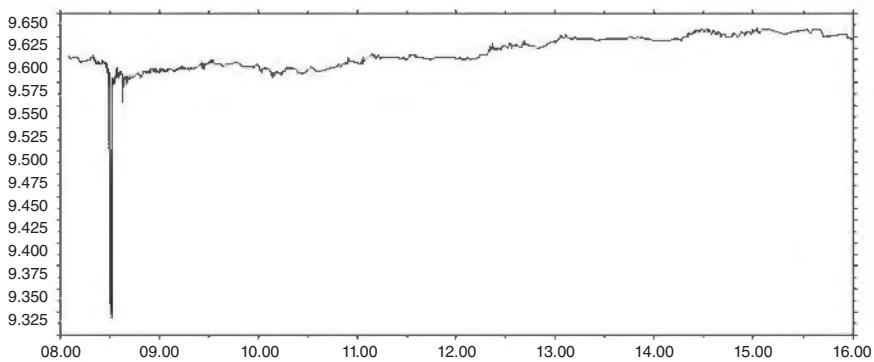
**EXHIBIT 7.1** Schematic of the Black Box



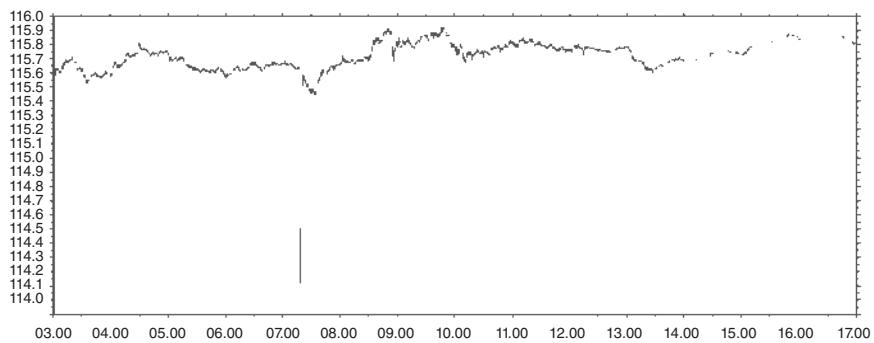
legend

|                 |  |
|-----------------|--|
| <b>category</b> |  |
| item or source  |  |

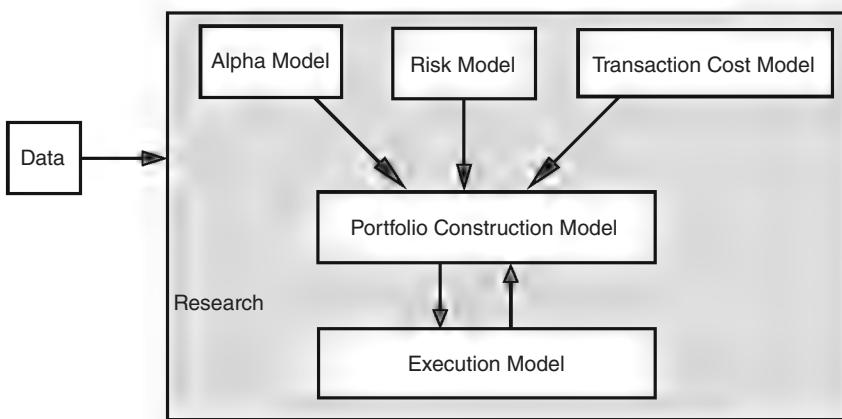
## EXHIBIT 8.1 A Taxonomy of Data



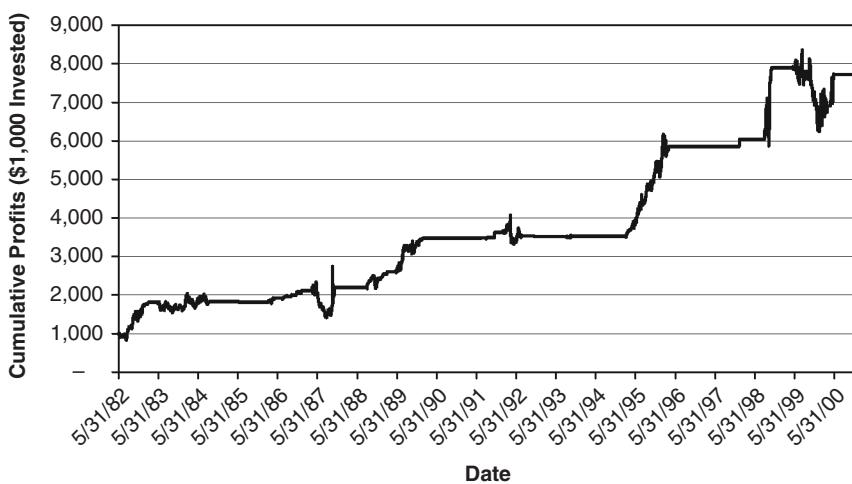
**EXHIBIT 8.2** September 2008 Mexican Peso Futures Contract on July 15, 2008



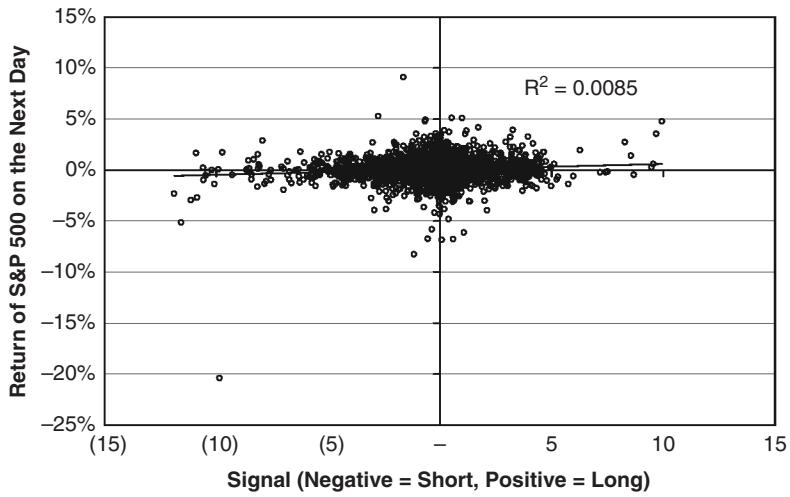
**EXHIBIT 8.3** June 2008 German Bund Futures Contract on March 28, 2008



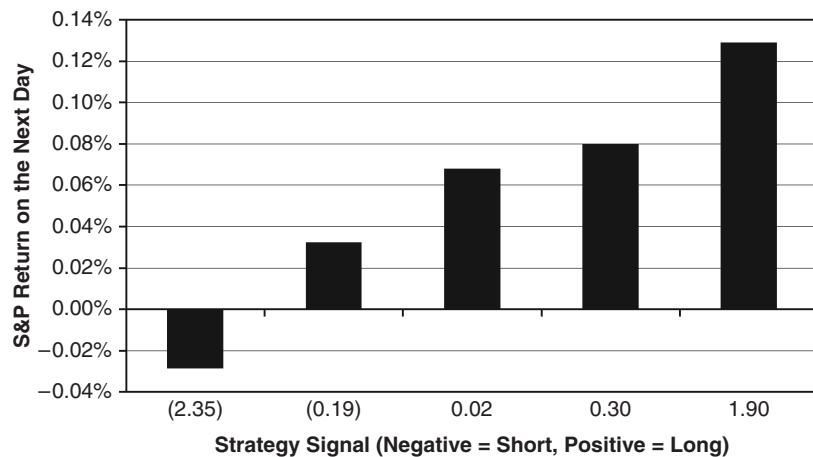
**EXHIBIT 8.4** Schematic of the Black Box



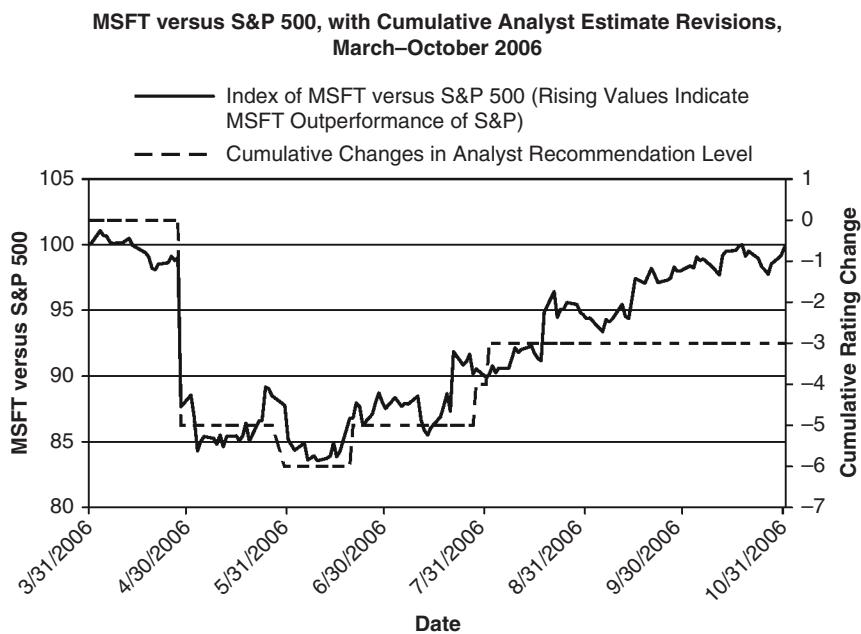
**EXHIBIT 9.1** Back-Tested Cumulative Profits of the S&P 500 Strategy



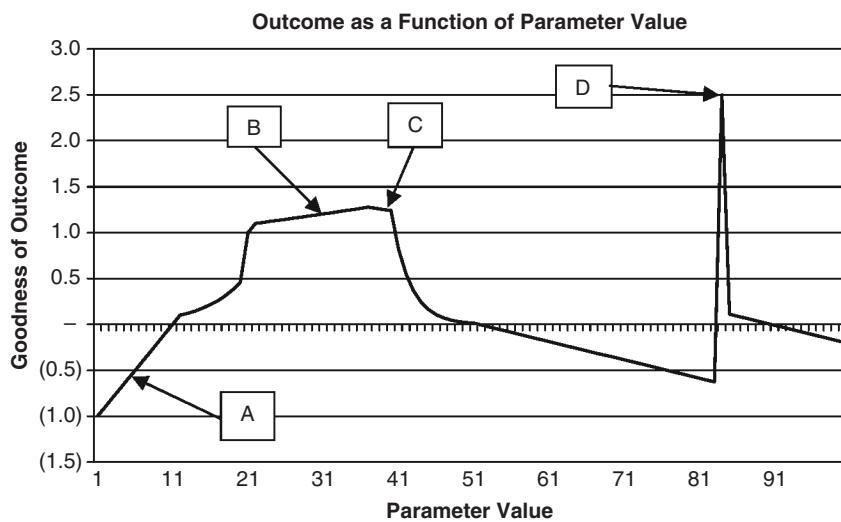
**EXHIBIT 9.2**  $R^2$  of the S&P 500 Strategy



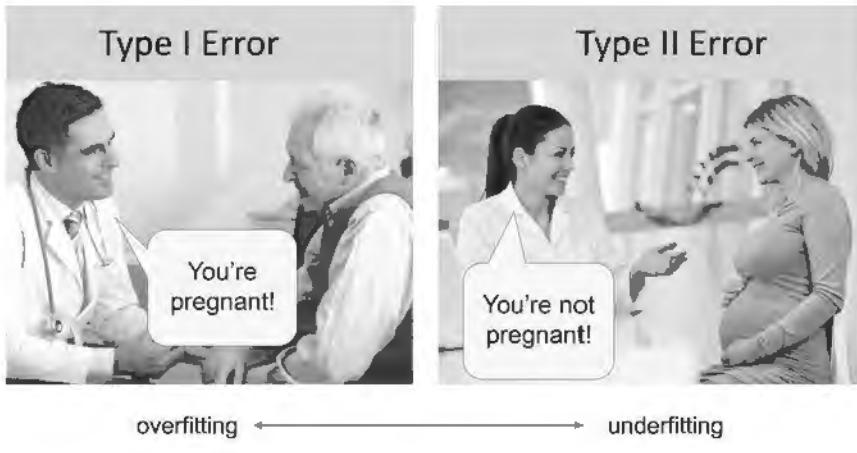
**EXHIBIT 9.3** Quintile Study of S&P 500 Strategy's Signals vs. S&P 500 Returns



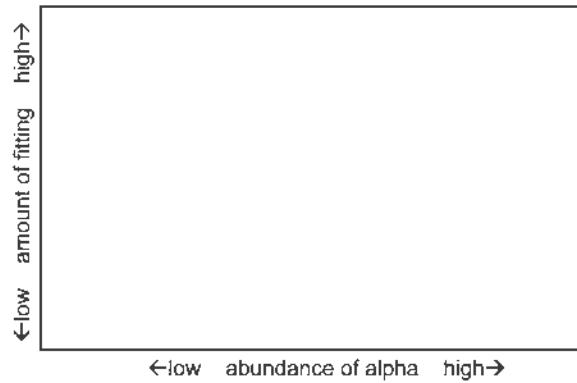
**EXHIBIT 9.4** Illustration of Time Decay of Alpha



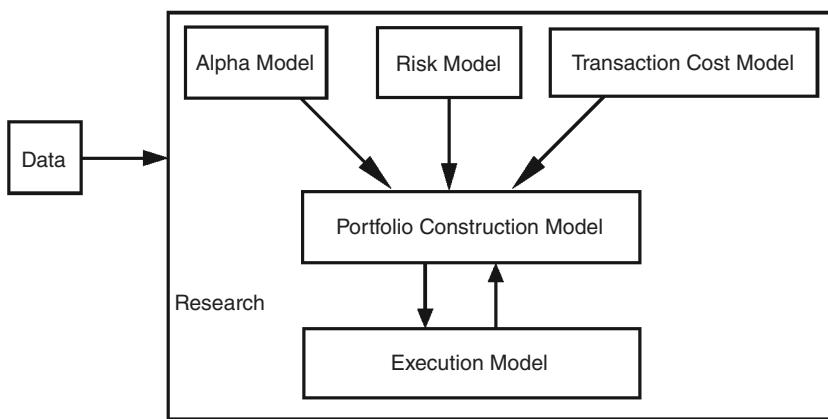
**EXHIBIT 9.5** Choosing the Right Parameter Values



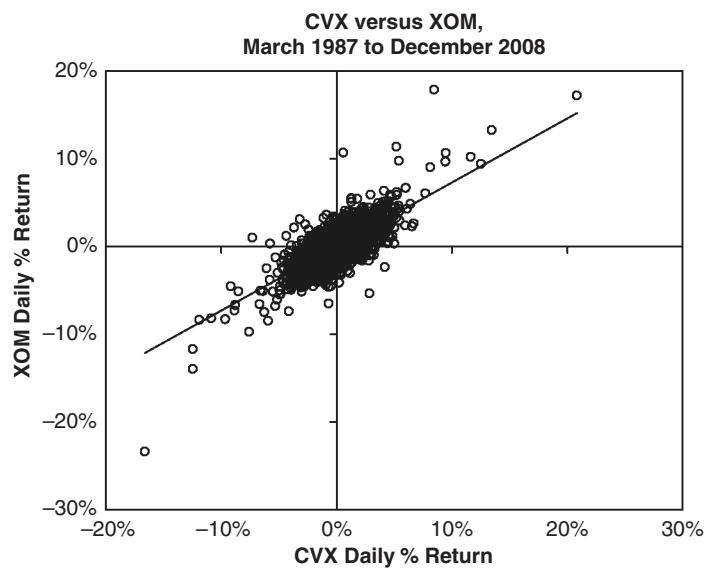
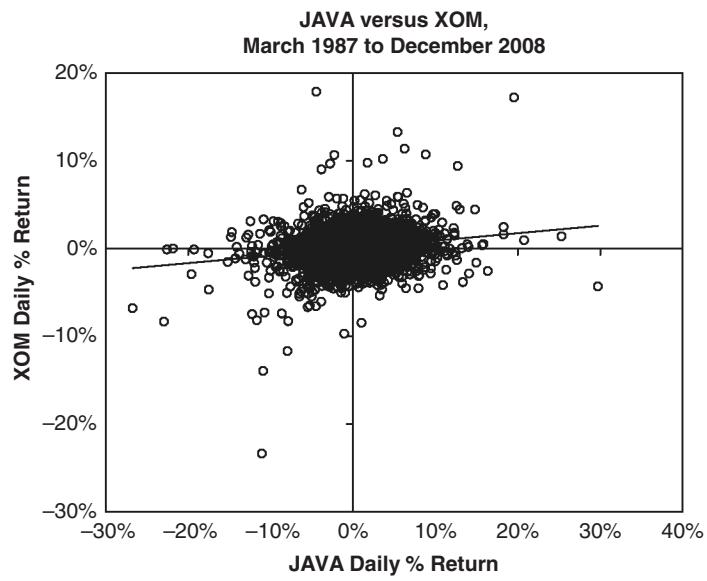
**EXHIBIT 9.6** Overfitting (Type I Error) vs Underfitting (Type II Error) Images/Shutterstock; skyneshher/Getty Images



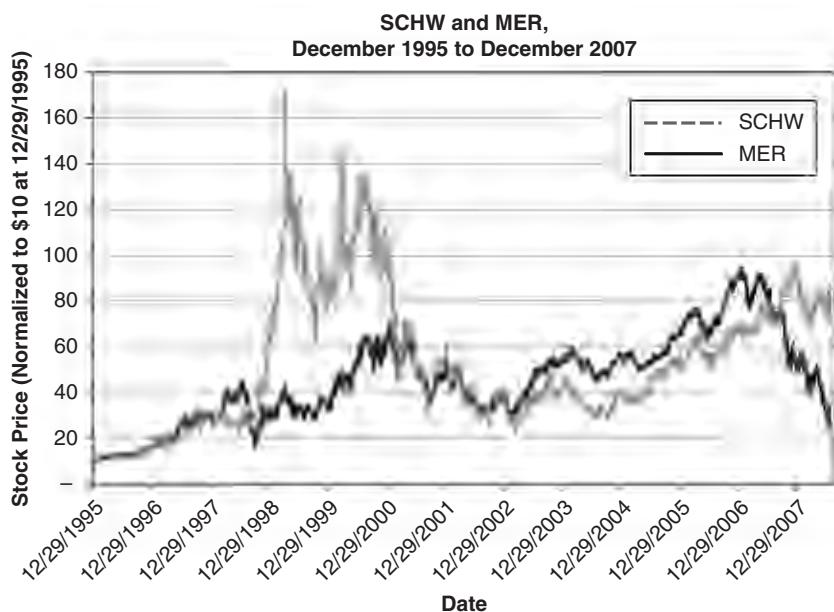
**EXHIBIT 9.7** Determining the Correct Balance Between Overfitting (Type I Error) vs Underfitting (Type II Error)



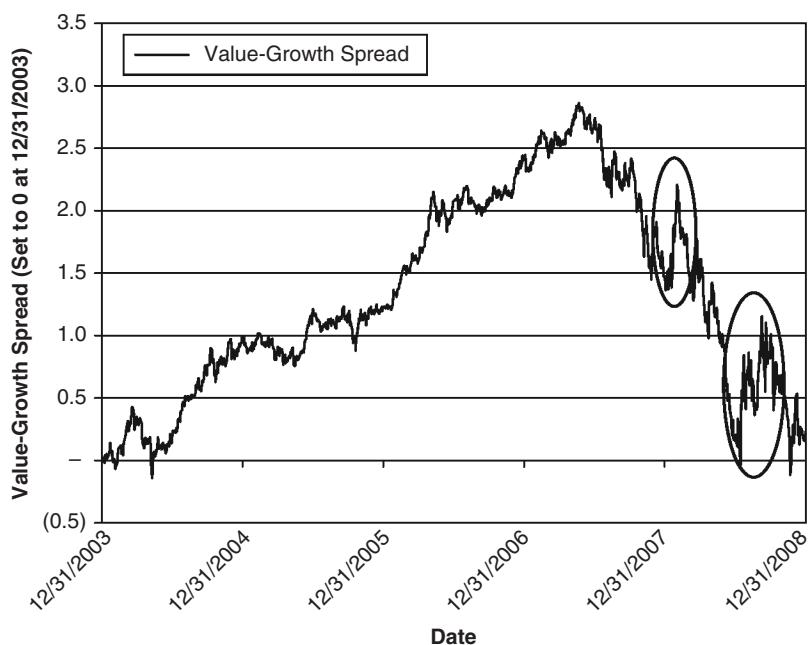
**EXHIBIT 9.8** Schematic of the Black Box



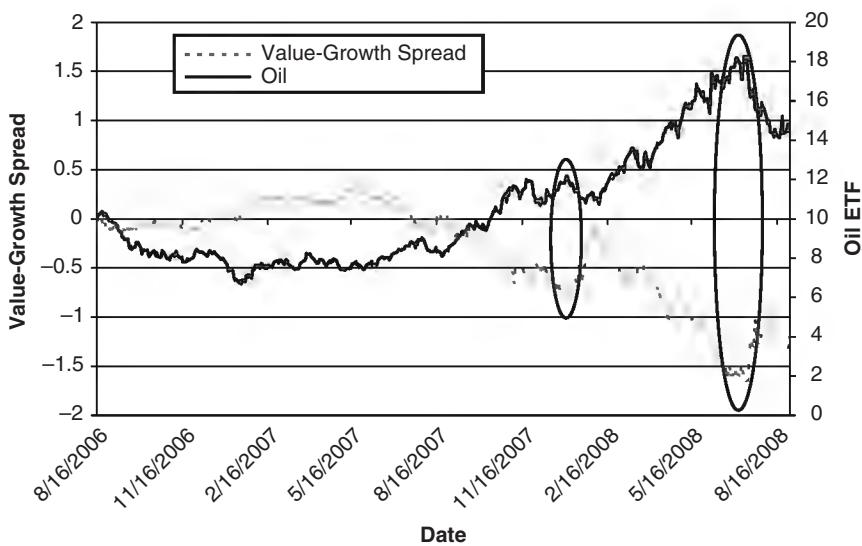
**EXHIBIT 10.1** A Demonstration of Nonlinear and Linear Relationships



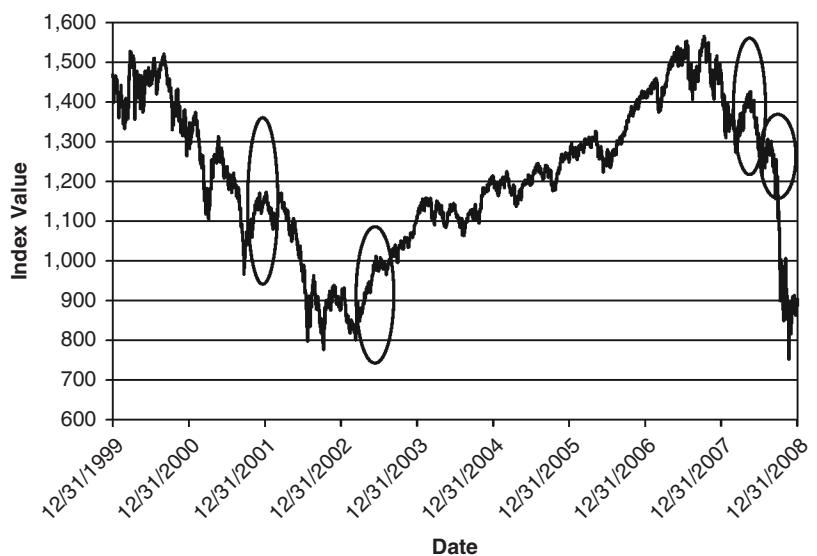
**EXHIBIT 10.2** Regime Changes in a Relationship between Two Stocks



**EXHIBIT 10.3** Value/Growth Spread, 2003–2008



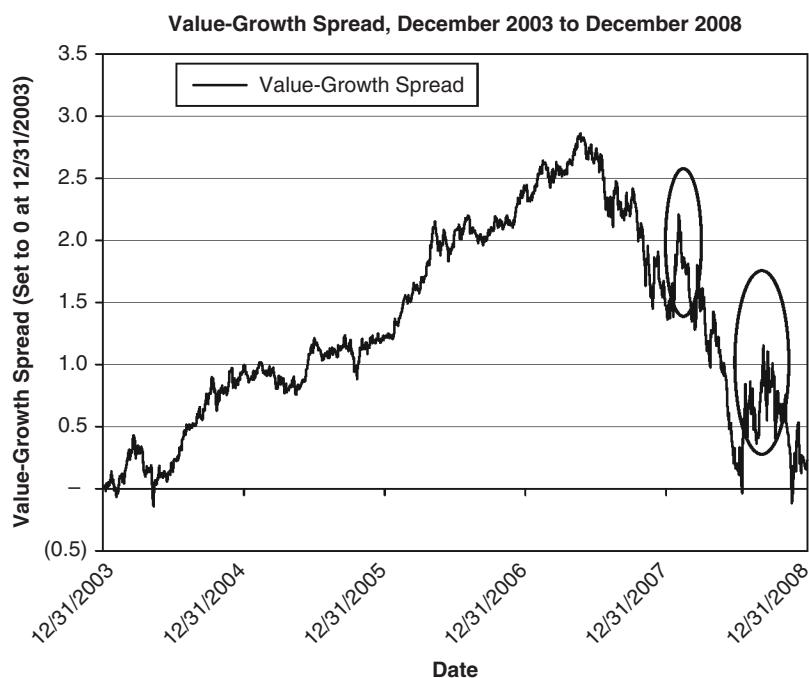
**EXHIBIT 10.4** Value/Growth Spreads versus Oil Prices, Normalized to August 16, 2006



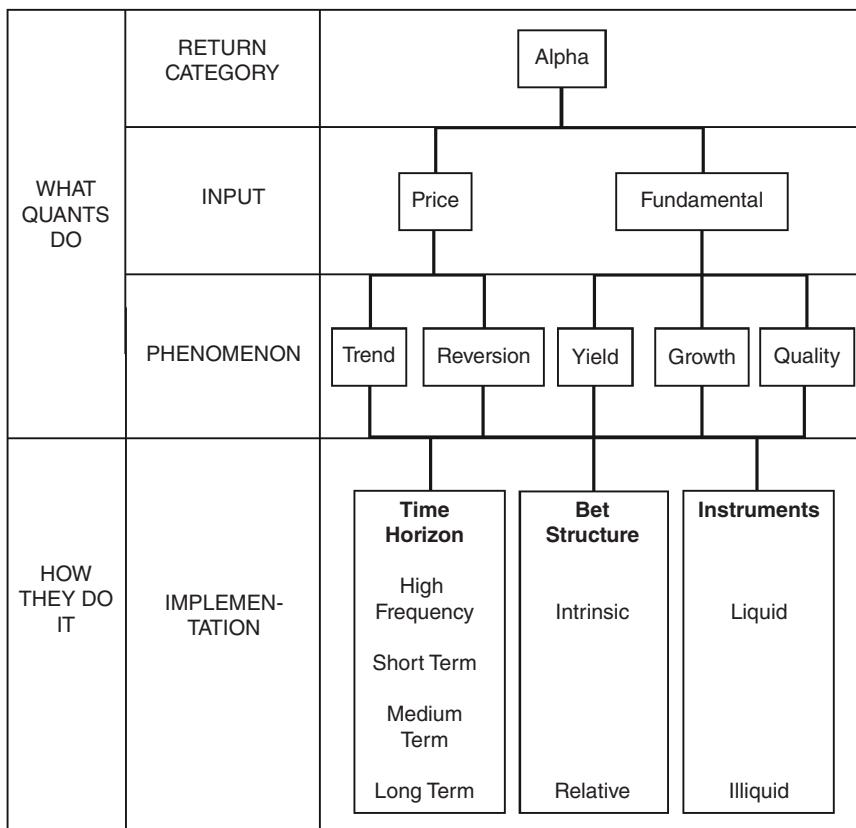
**EXHIBIT 10.5** S&P 500 Price Index, December 1999–December 2008

**EXHIBIT 10.6** Pulte Homes, Inc. (NYSE: PHM), May 31–August 31, 2007

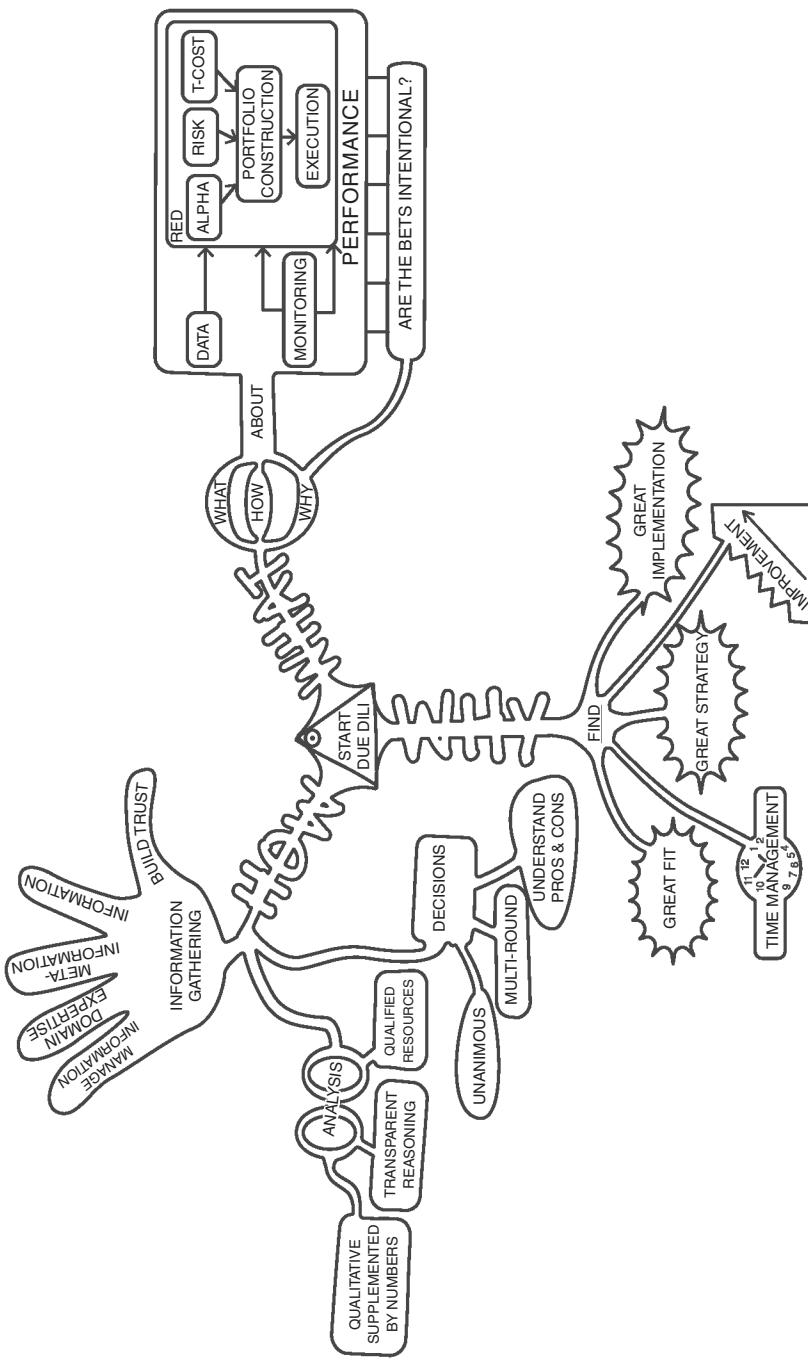
| PHM, Summer 2007    | Price Change (%) | Average Daily Volume (millions) |
|---------------------|------------------|---------------------------------|
| May 31–July 23      | −22.0            | 3.5                             |
| July 24–August 3    | −12.5            | 7.2                             |
| August 6–August 9   | +15.6            | 10.4                            |
| August 10–August 31 | −22.6            | 5.7                             |



**EXHIBIT 11.1** Regime Changes, as Indicated by the Value/Growth Spread



**EXHIBIT 12.1** Taxonomy of Theory-Driven Alpha Strategies and Implementation Approaches



**EXHIBIT 12.2** A Mind Map of the Investment Due Diligence Process

**EXHIBIT 14.1** Mockup of an Order Book for a Fictitious Ticker

| ID   | Size  | Bid    | Offer  | Size  | ID     |
|------|-------|--------|--------|-------|--------|
| Bid1 | 55    | 100.00 | 100.01 | 2,000 | Offer1 |
| Bid2 | 1,000 | 100.00 | 100.02 | 2,950 | Offer2 |
| Bid3 | 3,100 | 99.99  | 100.02 | 600   | Offer3 |
| Bid4 | 200   | 99.99  | 100.03 | 300   | Offer4 |
| Bid5 | 5,000 | 99.98  | 100.04 | 1,000 | Offer5 |

**EXHIBIT 14.2** Mockup of an Order Book for a Fictitious Ticker After a Large Market Order to Buy

| ID   | Size  | Bid    | Offer  | Size  | ID     |
|------|-------|--------|--------|-------|--------|
| Bid1 | 55    | 100.00 | 100.02 | 1,950 | Offer2 |
| Bid2 | 1,000 | 100.00 | 100.02 | 600   | Offer3 |
| Bid3 | 3,100 | 99.99  | 100.03 | 300   | Offer4 |
| Bid4 | 200   | 99.99  | 100.04 | 1,000 | Offer5 |
| Bid5 | 5,000 | 99.98  |        |       |        |

**EXHIBIT 14.3** Mockup of an Order Book for a Fictitious Ticker after a Limit Order to Sell at the Bid

| ID   | Size  | Bid    | Offer  | Size  | ID     |
|------|-------|--------|--------|-------|--------|
| Bid2 | 55    | 100.00 | 100.02 | 1,950 | Offer2 |
| Bid3 | 3,100 | 99.99  | 100.02 | 600   | Offer3 |
| Bid4 | 200   | 99.99  | 100.03 | 300   | Offer4 |
| Bid5 | 5,000 | 99.98  | 100.04 | 1,000 | Offer5 |

**EXHIBIT 14.4** Mockup of an Order Book for a Fictitious Ticker after a Limit Order to Sell, which Joins the Best Offer

| ID   | Size  | Bid    | Offer  | Size  | ID     |
|------|-------|--------|--------|-------|--------|
| Bid2 | 55    | 100.00 | 100.02 | 1,950 | Offer2 |
| Bid3 | 3,100 | 99.99  | 100.02 | 600   | Offer3 |
| Bid4 | 200   | 99.99  | 100.02 | 1,000 | Offer6 |
| Bid5 | 5,000 | 99.98  | 100.03 | 300   | Offer4 |
|      |       |        | 100.04 | 1,000 | Offer5 |

**EXHIBIT 14.5** Mockup of an Order Book for a Fictitious Ticker after a Limit Order to Sell, which Improves the Best Offer

| ID   | Size  | Bid    | Offer  | Size  | ID     |
|------|-------|--------|--------|-------|--------|
| Bid2 | 55    | 100.00 | 100.01 | 2,000 | Offer7 |
| Bid3 | 3,100 | 99.99  | 100.02 | 1,950 | Offer2 |
| Bid4 | 200   | 99.99  | 100.02 | 600   | Offer3 |
| Bid5 | 5,000 | 99.98  | 100.02 | 1,000 | Offer6 |
|      |       |        | 100.03 | 300   | Offer4 |
|      |       |        | 100.04 | 1,000 | Offer5 |

**EXHIBIT 14.6** Mockup of an Order Book for a Fictitious Ticker

| ID   | Size  | Bid   | Offer  | Size  | ID     |
|------|-------|-------|--------|-------|--------|
| Bid1 | 3,100 | 99.99 | 100.01 | 2,000 | Offer1 |
| Bid2 | 200   | 99.99 | 100.02 | 2,950 | Offer2 |
| Bid3 | 5,000 | 99.98 | 100.02 | 600   | Offer3 |
|      |       |       | 100.03 | 300   | Offer4 |
|      |       |       | 100.04 | 1,000 | Offer5 |

**EXHIBIT 14.7** Mockup of an Order Book for a Fictitious Ticker with Additional Bids

| ID   | Size  | Bid    | Offer  | Size  | ID     |
|------|-------|--------|--------|-------|--------|
| Bid4 | 1,000 | 100.00 | 100.01 | 2,000 | Offer1 |
| Bid5 | 6,000 | 100.00 | 100.02 | 2,950 | Offer2 |
| Bid1 | 3,100 | 99.99  | 100.02 | 600   | Offer3 |
| Bid2 | 200   | 99.99  | 100.03 | 300   | Offer4 |
| Bid3 | 5,000 | 99.98  | 100.04 | 1,000 | Offer5 |

**EXHIBIT 14.8** Mockup of an Order Book for a Fictitious Ticker After 1,000 Shares Have Been Removed from the Bid

| ID   | Size  | Bid    | Offer  | Size  | ID     |
|------|-------|--------|--------|-------|--------|
| Bid5 | 6,000 | 100.00 | 100.01 | 2,000 | Offer1 |
| Bid1 | 3,100 | 99.99  | 100.02 | 2,950 | Offer2 |
| Bid2 | 200   | 99.99  | 100.02 | 600   | Offer3 |
| Bid3 | 5,000 | 99.98  | 100.03 | 300   | Offer4 |
|      |       |        | 100.04 | 1,000 | Offer5 |

**EXHIBIT 14.9** Mockup of an Order Book for a Fictitious Ticker after All \$100.00 Shares Have Been Removed from the Bid

| ID   | Size  | Bid   | Offer  | Size  | ID     |
|------|-------|-------|--------|-------|--------|
| Bid1 | 3,100 | 99.99 | 100.00 | 2,000 | Offer6 |
| Bid2 | 200   | 99.99 | 100.01 | 2,000 | Offer1 |
| Bid3 | 5,000 | 99.98 | 100.02 | 2,950 | Offer2 |
|      |       |       | 100.02 | 600   | Offer3 |
|      |       |       | 100.03 | 300   | Offer4 |
|      |       |       | 100.04 | 1,000 | Offer5 |

**EXHIBIT 14.10** Mockup of an Order Book for a Fictitious Ticker After Two 2,000 Share Bids at \$100.01

| ID   | Size  | Bid    | Offer  | Size  | ID     |
|------|-------|--------|--------|-------|--------|
| Bid4 | 2,000 | 100.01 | 100.02 | 2,950 | Offer2 |
| Bid1 | 3,100 | 99.99  | 100.02 | 600   | Offer3 |
| Bid2 | 200   | 99.99  | 100.03 | 300   | Offer4 |
| Bid3 | 5,000 | 99.98  | 100.04 | 1,000 | Offer5 |

**EXHIBIT 14.11** Breakdown of Messages at Various Intervals and Percentiles  
for EBAY on July 20, 2012

|                  | 50th<br>Percentile | 99th<br>Percentile | 99.9th<br>Percentile | 99.99th<br>Percentile | 99.999th<br>Percentile |
|------------------|--------------------|--------------------|----------------------|-----------------------|------------------------|
| 1 second         | 13                 | 259                | 546                  | 1755                  | 4179                   |
| 100 milliseconds | 0                  | 13                 | 84                   | 863                   | 1306                   |
| 10 milliseconds  | 0                  | 1                  | 7                    | 269                   | 557                    |
| 1 millisecond    | 0                  | 0                  | 1                    | 56                    | 106                    |

**EXHIBIT 15.1** Mockup of an Order Book for a Fictitious Ticker

| ID   | Size  | Bid    | Offer  | Size  | ID     |
|------|-------|--------|--------|-------|--------|
| Bid1 | 1,000 | 100.00 | 100.01 | 2,000 | Offer1 |
| Bid2 | 3,100 | 99.99  | 100.02 | 3,000 | Offer2 |
| Bid3 | 2,000 | 99.99  | 100.02 | 1,000 | Offer3 |
| Bid4 | 5,000 | 99.98  | 100.03 | 4,000 | Offer4 |
| Bid5 | 6,000 | 99.97  | 100.04 | 1,000 | Offer5 |

**EXHIBIT 15.2** Mockup of an Order Book for a Fictitious Ticker after a Market Order to Buy 10,000 Shares Is Mostly Filled by a CMM Acting as an Agent of the Customer

| ID   | Size  | Bid    | Offer  | Size  | ID     |
|------|-------|--------|--------|-------|--------|
| Bid1 | 1,000 | 100.00 | 100.03 | 500   | Offer4 |
| Bid2 | 3,100 | 99.99  | 100.04 | 1,000 | Offer5 |
| Bid3 | 2,000 | 99.99  |        |       |        |
| Bid4 | 5,000 | 99.98  |        |       |        |
| Bid5 | 6,000 | 99.97  |        |       |        |

**EXHIBIT A.1** Average Price Movement in SPY (%)

|                        | 2000–2006 | 2007–2012 | % Difference |
|------------------------|-----------|-----------|--------------|
| close:close            | 0.84      | 1.03      | +23          |
| open:close (intraday)  | 0.76      | 0.82      | +8           |
| close:open (overnight) | 0.37      | 0.59      | +59          |
| high:low               | 1.47      | 1.72      | +17          |

**EXHIBIT A.2** Median Price Movement in SPY (%)

|                        | 2000–2006 | 2007–2012 | % Difference |
|------------------------|-----------|-----------|--------------|
| close:close            | 0.62      | 0.67      | +8           |
| open:close (intraday)  | 0.55      | 0.53      | -3           |
| close:open (overnight) | 0.26      | 0.39      | +51          |
| high:low               | 1.26      | 1.33      | +5           |

**EXHIBIT A.3** Frequency of 3% or Greater Moves in SPY (%)

|                        | 2000–2006 | 2007–2012 | % Difference |
|------------------------|-----------|-----------|--------------|
| close:close            | 2.56      | 5.87      | +129         |
| open:close (intraday)  | 1.53      | 2.69      | +75          |
| close:open (overnight) | 0.11      | 0.83      | +629         |
| high:low               | 6.20      | 10.91     | +76          |

**EXHIBIT A.4** Frequency of 4% or Greater Moves in the SPY (%)

|                        | 2000–2006 | 2007–2012 | % Difference |
|------------------------|-----------|-----------|--------------|
| close:close            | 0.68      | 2.97      | +335         |
| open:close (intraday)  | 0.28      | 1.38      | +386         |
| close:open (overnight) | 0.11      | 0.48      | +325         |
| high:low               | 1.65      | 5.73      | +248         |