Time Complexity Analysis

Question #7

```
Public BinarySearchTree transformation(E[] arr, BinaryTree<E> bt){
  int index;                                              O(1)
  E value;                                                O(1)
  int i=0;                                                O(1)
  Arrays.sort(arr);                                       O(n^2).
  while(i<arr.length){                                    O(n)
     add(bt.root, arr[i]);                                O(n.2^n)
  }
  BinarySearchTree bst = new BinarySearchTree();          O(1)
  bst.root = bt.root;                                     O(1)
  return bst;                                             O(1)
}
```

worst case: $O(n2^n)$ — best case: $O(1)$

```
private boolean add(BinaryTree.Node<E> localRoot, E item){
   boolean flag = false;                                  O(1)
   if(localRoot != null){                                 O(1)
      if(localRoot.left != null){                         T(n-1)
         flag = add(localRoot.left, item);
      }
      if(flag == false && localRoot.status == false){     O(1)
         localRoot.data = item;
         localRoot.status = true;
         return true;
      }
      if(flag == flag && localRoot.right != null){        O(1)
         return add(localRoot.right, item);               T(n-1)
       }
       return flag;
   }
   return flag                                            O(1)
}                                                         O(1)
```

$T(n) = 2T(n-1) + 1$ — ①

$T(n) = 2[2T(n-2)+1] + 1$

$T(n) = 2^2 T(n-2) + 2 + 1$ — ②

$T(n) = 2^2[2T(n-3)+1] + 2 + 1$ — ③

$T(n) = 2^3 T(n-3) + 2^2 + 2 + 1$ — ④

$T(n) = 2^k T(n-k) + 2^{k-1} + \cdots + 2^2 + 2 + 1$ — ⑤

Assume $n - k = 0$

$n = k$

$= 2^n T(0) + 2^{n-1} + \cdots + 2^2 + 2 + 1$

$= 2^n \times 1 + 2^{n-1} + \cdots + 2^2 + 2 + 1$

$= 2^n + 2^{n-1} - 1$

$T(n) = 2^{n+1} - 1$

$O(2^n)$

$\Omega(2^n)$

$\Theta(2^n)$

$O(2^n)$

Best case

$\Theta(1)$

Worst case

$O(2^n)$

Question #2

```
Public BinarySearchTree transformation(BinarySearchTree bst){
  BinarySearchTree tree = new BinarySearchTree();          O(1)
  if(bst.root != null){                                    O(1)
     bst.root = inOrder(bst.root);                         O(n^2)
  }
  return bst;                                              O(1)
}
```

worst case: O(n^2) next case: O(1)

```
Private BinaryTree.Node<E> inOrder(BinaryTree.Node<E> root){
  if(root == null){                                        O(1)
     return null;
  root = rotation(root);                                   O(n^2)
  root.left = inOrder(root.left);                          T(n-1)
  root = rotation(root);                                   O(n^2)
  root.right = inOrder(root.right);                        T(n-1)
  root = rotation(root);                                   O(n^2)
  return root;                                             O(1)
}
```

worst case: O(n^2) next case: O(1)

```
Private BinaryTree.Node<E> rotation(BinaryTree.Node<E> root){
    if(root != null)
      int balance = getBalance(root);
        while(balance > 1 || balance < -1){                n
           root = bstRotation(root);                       O(n)
           balance = getBalance(root);                     O(n)
        }
      return root;
    }
    else{
       return null;
    }
}
```

worst case: O(n^2) best case: O(1)

```
Private BinaryTree.Node<E> bstRotation(BinaryTree.Node<E> root){
  int balance = getBalance(root);
  if(root.left != null && root.left.left != null){
     if(balance > 1 && maxDepth(root.left) - maxDepth(root.left.left) >0){
        root = rightRotate(root);
     }
}
```

```
if (root.right != null && root.right.right != null)
    if (balance < -1 && maxDepth(root.right) - maxDepth(root.right.right) > 0)
        root = leftRotate(root);

}

if (root.left != null && root.left.right != null) {
    if (balance > 1 && maxDepth(root.left.right) - maxDepth(root.left.left
        > 0) {
        root.left = leftRotate(root.left);
        root = rightRotate(root);
    }
if (root.right != null && root.right.left != null) {
    if (balance < -1 && maxDepth(root.right.left) - maxDepth(root.right.right
        > 0) {
        root.right = rightRotate(root.right);
        root = leftRotate(root);
        }
}
return root;
}
```

Best case	Worst case
$O(1)$	$O(n)$

Question #3

```
Public void insert(E item){
  if(head == null){
    head = new SLNode(2,item);
    head.links[0] = null;
  }
  else{
    add(item);
  }
  size++;
  if(size > (maxLevel-1)*100){
     maxLevel++;
     increaseLevel();
     connect();
  }
}
private void increaseLevel(){
  SLNode<E> iter = head;
  SLNode<E> tmpIter;
  int tmpLevel = 0;
  while(iter != null){
    if(iter.links.length > tmpLevel){
        tmpLevel = iter.links.length;
    }
    iter = iter.links[0];
  }
  iter = head;
  while(iter.links[0] != null){
    if(iter.links[0].links.length == tmpLevel){
       tmpIter = iter.links[0];
       iter.links[0] = new SLNode(tmpLevel+1, iter.links[0].data);
       iter.links[0].links[0] = tmpIter.links[0];
    }
    iter = iter.links[0];
  }
}
```

Best case: O(1)

Worst case: O(n)

Worst case: O(n)

Best case: O(1)

```
Private void add(E item) {
int length;
int level;
SLNode<E> iter=head;
SLNode<E> lastItem=null;
boolean flag = false;
if(head.data.compareTo(item) >0) {
    level=getLevel();
    SLNode<E> tmp = new SLNode(level,item);
    tmp.links[0]=head;
    this.head=tmp;
    flag=true;
    connect();
}
while(iter != null) {
    lastItem =iter;
    if(iter.links[0].data.compareTo(item) <0 && iter.links[0] !=null)
    {
      if(iter.links[0].data.compareTo(item) >0 ){
        length = Math.abs(length-iter);
        level = getLevel(length);
        SLNode<E> tmp= new SLNode(level,item);
        tmp.links[0]=iter.links[0];
        iter.links[0]=tmp;
        connect();
        flag=true;
        break;
      }
}
iter=iter.links[0];
}
if(lastItem.!=null && flag==false){
  length = Math.abs(length-item);
  level=getLevel(length);
  SLNode<E> tmp = new SLNode(level,item);
  tmp.links[0]=null;
  lastItem.links[0]=tmp;
}
```

Worst case	Best case
O(n)	Ω(1)