

Homework 1

Machine Learning in Economics

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Due: next week April 8th, 2021

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Arrange your answers in an `.Rmd` file (you can take `HW01_MLinEcon.Rmd` as a template) and produce a html file containing your answers. You need to upload your files to the Google Classroom by the deadline.

Part 1

Question

In this exercise you will simulate a data set and run a simple regression. To ensure reproducible results, make sure you use `set.seed(1)`. This exercise is similar to the one we saw in class (see [regression lab](#)).

- Using the `rnorm()` function create vector X that contains 200 observations from $N(0, 1)$ distribution.
- Similarly, create a 200 element vector, `epsilon` (ϵ), drawn from $N(0, 0.25)$ distribution. This is the irreducible error.
- Create the response data using the following relationship:

$$Y = -1 + 0.5X + \epsilon$$

- Now using your simulated data set, fit a linear regression of Y on X using `lm()` function. Display the summary statistics and interpret the diagnostic plots. In a single graph, draw a scatter diagram of Y and X values, and the fitted line.
- Now, fit a quadratic model by adding the X^2 into the model. Discuss whether there is improvement in the fit or not. Draw scatter diagram and fitted line similar to the previous part. Interpret the diagnostic plots.
- Using the `sample()` function create train and test sets just like we did in class. Obtain predicted values (from the test set) for the linear and quadratic fits. Compare their MSEs. Which model is better in terms of predictions?

Answer

Put your answers, explanations, interpretations here.

You can fill in the following code chunk.

```
library(ggplot2)
library(broom)
```

```
## Warning: package 'broom' was built under R version 4.0.5
```

```
library(tidyr)
library(tidyverse)
```

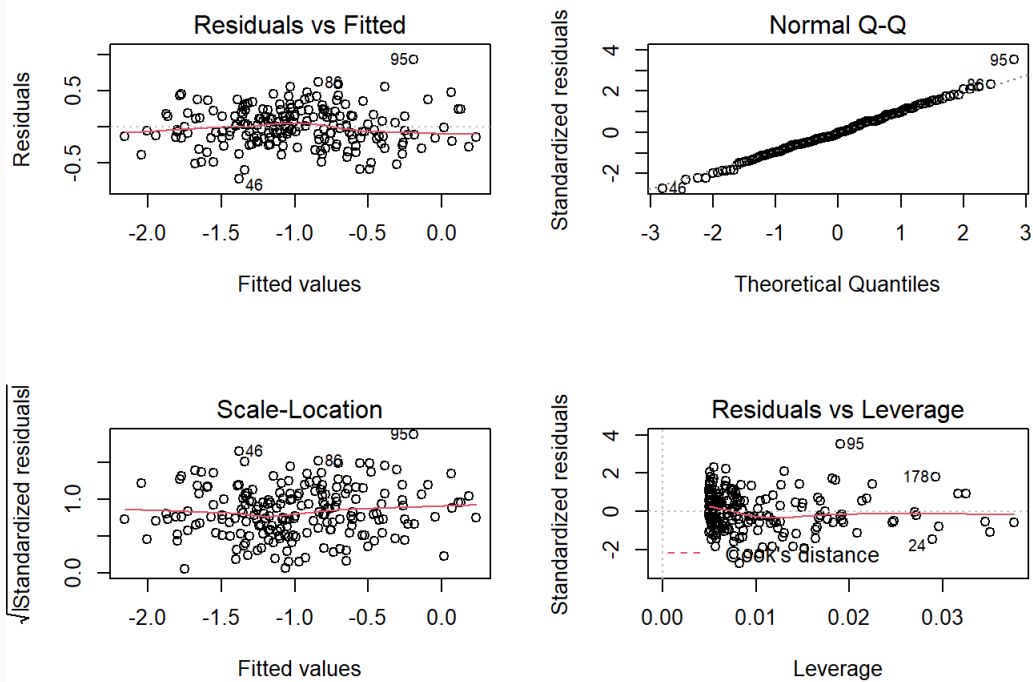
```
## Warning: package 'tidyverse' was built under R version 4.0.5
```

```
## -- Attaching packages ----- tidyverse 1.3.1 --
```

```
## v tibble 3.1.0      v dplyr 1.0.5
## v readr 1.4.0      v stringr 1.4.0
## v purrr 0.3.4      v forcats 0.5.1
```

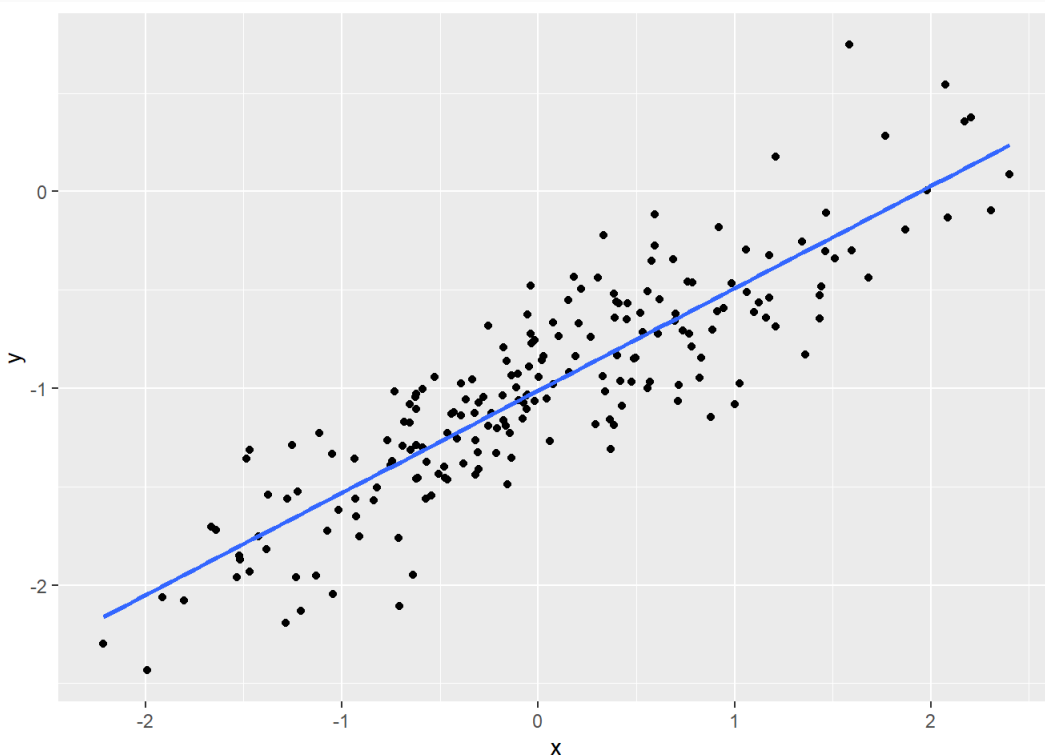
```
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()     masks stats::lag()
```

```
library(dplyr)
set.seed(1)
n <- 200
set.seed(1)
x <- rnorm(n, mean = 0, sd = 1)
epsilon <- rnorm(n, mean = 0, sd = 0.25)
y = -1 + 0.5*x + rnorm(n, mean = 0, sd = 0.25)
reg1 <- lm(formula = y ~ x)
tidy(reg1)
par(mfrow=c(2,2))
plot(reg1)
```



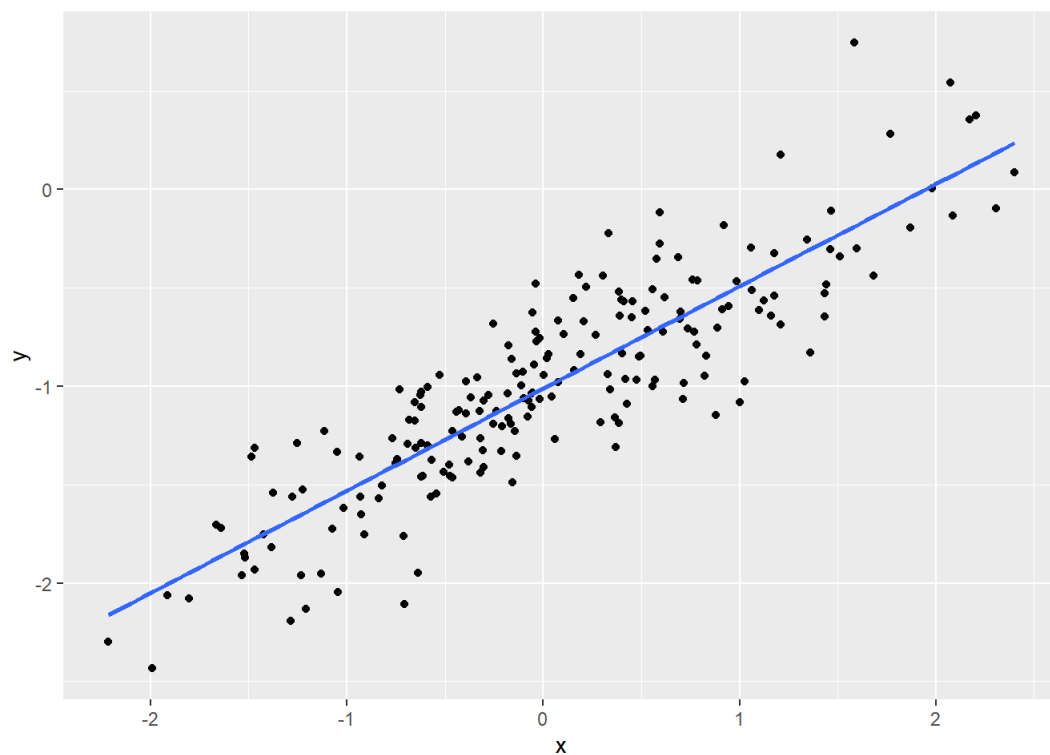
```
ggplot(reg1, aes(x = x, y = y)) + geom_point() + geom_smooth(method = "lm", se = FALSE)
```

```
## `geom_smooth()` using formula 'y ~ x'
```

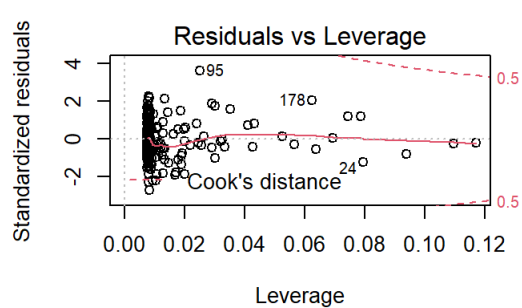
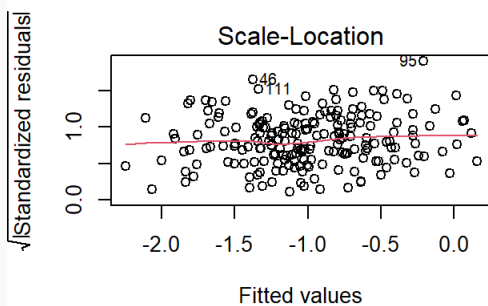
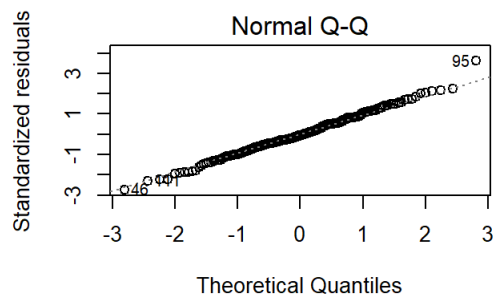
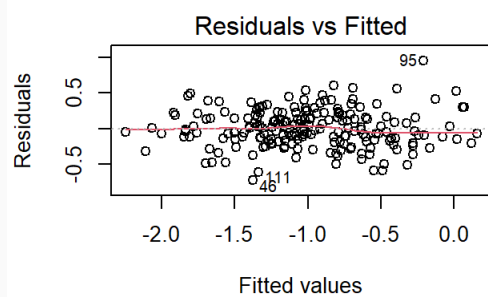


```
reg2 <- lm(formula = y~x + I(x^2))
anova(reg1, reg2)
ggplot(reg2, aes(x = x, y = y)) +geom_point() + geom_smooth(method = "lm", se = FALSE)
```

```
## `geom_smooth()` using formula 'y ~ x'
```



```
par(mfrow=c(2,2))
plot(reg2)
```



```

set.seed(1)
df1 <- tibble(id=1:n, y, x)
train <- sample(n, 100)
train_data <- df1[train, ]
test_data <- df1[-train, ]
lfit <- lm(y ~ x, data = train_data)
qfit <- lm(y ~ x, I(x^2), data = train_data)
lin_predict <- predict(lfit, test_data)
lin_error <- test_data$y - lin_predict
MSE_lfit <- mean(lin_error^2)
MSE_lfit
qpredict <- predict(qfit, test_data)
querror <- test_data$y - qpredict
MSE_qfit <- mean(querror^2)
MSE_qfit

```

```

## # A tibble: 2 x 5
##   term      estimate std.error statistic  p.value
##   <chr>      <dbl>    <dbl>    <dbl>    <dbl>
## 1 (Intercept) -1.01      0.0189   -53.4 1.54e-119
## 2 x           0.520    0.0204    25.5 2.37e- 64
## Analysis of Variance Table
##
## Model 1: y ~ x
## Model 2: y ~ x + I(x^2)
##   Res.Df    RSS Df Sum of Sq    F Pr(>F)
## 1     198 14.174
## 2     197 14.087  1  0.087729 1.2269 0.2694
## [1] 0.08039026
## [1] 0.08635954

```

e. Quadratic model is not better according to F test from anova function.

f. It looks like test MSE = 0.0598797 from the linear model and MSE = 0.059424 for the quadratic model. The difference is very small, 0.0004560702. It looks like we can use both models in our predictions.

Part 2

Question

Boston house data set (part of `MASS` package) that we saw in class has a variable that measures per capita crime rate by town (`crim`). Now suppose that the `crim` is the response variable and all the remaining variables are features. Fit a multiple linear regression model and interpret the results.

Answer

```

# put your code here
library(MASS)

```

```

##
## Attaching package: 'MASS'

```

```
## The following object is masked from 'package:dplyr':
##
##      select
```

```
regboston <- lm(formula = crim ~ . , data = Boston)
summary(regboston)
```

```
##
## Call:
## lm(formula = crim ~ ., data = Boston)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.924 -2.120 -0.353  1.019 75.051
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  17.033228   7.234903   2.354 0.018949 *
## zn           0.044855   0.018734   2.394 0.017025 *
## indus        -0.063855   0.083407  -0.766 0.444294
## chas         -0.749134   1.180147  -0.635 0.525867
## nox          -10.313535   5.275536  -1.955 0.051152 .
## rm           0.430131   0.612830   0.702 0.483089
## age          0.001452   0.017925   0.081 0.935488
## dis          -0.987176   0.281817  -3.503 0.000502 ***
## rad           0.588209   0.088049   6.680 6.46e-11 ***
## tax          -0.003780   0.005156  -0.733 0.463793
## ptratio      -0.271081   0.186450  -1.454 0.146611
## black        -0.007538   0.003673  -2.052 0.040702 *
## lstat        0.126211   0.075725   1.667 0.096208 .
## medv        -0.198887   0.060516  -3.287 0.001087 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.439 on 492 degrees of freedom
## Multiple R-squared:  0.454, Adjusted R-squared:  0.4396
## F-statistic: 31.47 on 13 and 492 DF, p-value: < 2.2e-16
```

```
names(regboston)
```

```
## [1] "coefficients" "residuals"      "effects"        "rank"
## [5] "fitted.values" "assign"          "qr"             "df.residual"
## [9] "xlevels"      "call"           "terms"          "model"
```

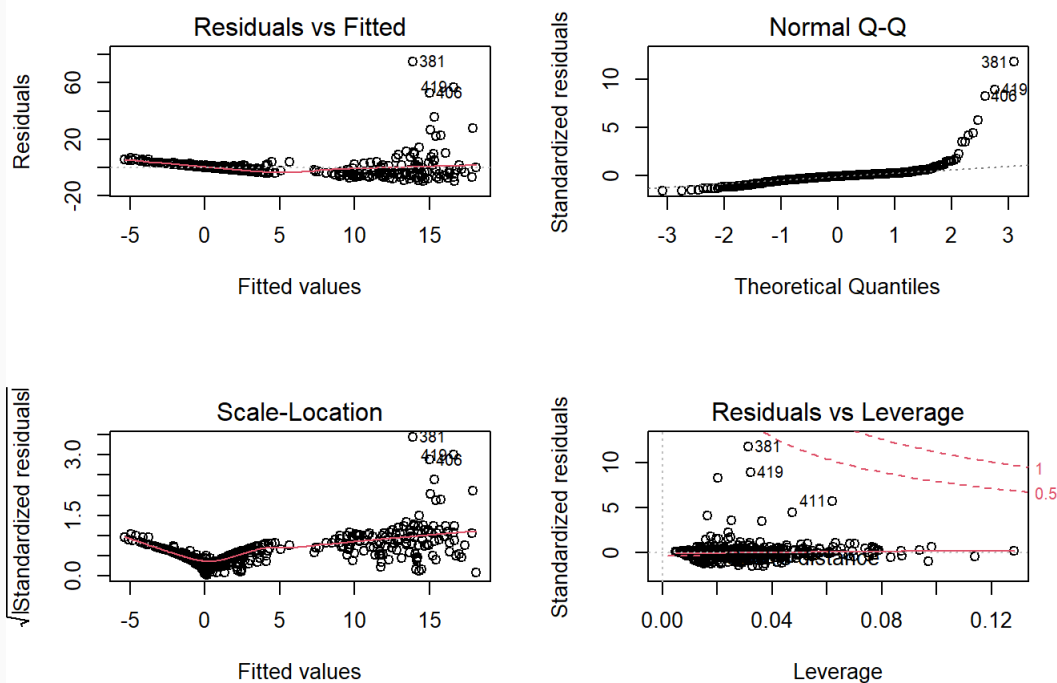
```
coef(regboston)
```

```
##      (Intercept)          zn          indus          chas          nox
## 17.033227523    0.044855215  -0.063854824  -0.749133611 -10.313534912
##           rm          age          dis          rad          tax
## 0.430130506    0.001451643  -0.987175726   0.588208591  -0.003780016
##      ptratio        black        lstat          medv
## -0.271080558  -0.007537505   0.126211376  -0.198886821
```

```
confint(regboston)
```

```
##              2.5 %      97.5 %
## (Intercept)  2.818109179 31.2483458660
## zn           0.008046562  0.0816638671
## indus       -0.227733150  0.1000235023
## chas        -3.067882868  1.5696156471
## nox        -20.678894713  0.0518248891
## rm          -0.773956866  1.6342178774
## age         -0.033767600  0.0366708869
## dis         -1.540889544 -0.4334619069
## rad          0.415209611  0.7612075719
## tax         -0.013909700  0.0063496670
## ptratio     -0.637417996  0.0952568794
## black       -0.014754837 -0.0003201725
## lstat       -0.022572584  0.2749953365
## medv        -0.317788478 -0.0799851646
```

```
par(mfrow=c(2,2))
plot(regboston)
```



Part 3

Question

Prepare a simple table that shows the most popular women's names in Turkey in 2018 (see the example we discussed in class). Prepare a similar table for the year 2017 and compare the two tables. Are there any differences?

Answer

```
# put your code here
# the data set is already available in the HW project folder
# you can read it into R using:
library(tidyverse)
library(readxl)
womennames2018 <- read_excel("womennames2018.xls", range = "A4:AQ338")
```

```
## New names:
## * `` -> ...1
```

```
head(womennames2018)
```

```
## # A tibble: 6 x 43
##   ...1 `1950` `1960` `1970` `1980` `1981` `1982` `1983` `1984` `1985` `1986`
##   <chr>   <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1 Ada      NA      NA      NA      NA      NA      NA      NA      NA      NA      NA
## 2 Ahsen     NA      NA      NA      NA      NA      NA      NA      NA      NA      NA
## 3 Aleyna    NA      NA      NA      NA      NA      NA      NA      NA      NA      NA
## 4 Aliye     98      NA      NA      NA      NA      NA      NA      NA      NA      NA
## 5 Alya      NA      NA      NA      NA      NA      NA      NA      NA      NA      NA
## 6 Amine     NA      NA      NA      NA      NA      NA      NA      NA      NA      NA
## # ... with 32 more variables: 1987 <dbl>, 1988 <dbl>, 1989 <dbl>, 1990 <dbl>,
## #   1991 <dbl>, 1992 <dbl>, 1993 <dbl>, 1994 <dbl>, 1995 <dbl>, 1996 <dbl>,
## #   1997 <dbl>, 1998 <dbl>, 1999 <dbl>, 2000 <dbl>, 2001 <dbl>, 2002 <dbl>,
## #   2003 <dbl>, 2004 <dbl>, 2005 <dbl>, 2006 <dbl>, 2007 <dbl>, 2008 <dbl>,
## #   2009 <dbl>, 2010 <dbl>, 2011 <dbl>, 2012 <dbl>, 2013 <dbl>, 2014 <dbl>,
## #   2015 <dbl>, 2016 <dbl>, 2017 <dbl>, 2018 <dbl>
```

```
womennames2018 <- rename(womennames2018, "name" = "...1")
head(womennames2018)
```

```
## # A tibble: 6 x 43
##   name `1950` `1960` `1970` `1980` `1981` `1982` `1983` `1984` `1985` `1986`
##   <chr>   <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1 Ada      NA      NA      NA      NA      NA      NA      NA      NA      NA      NA
## 2 Ahsen     NA      NA      NA      NA      NA      NA      NA      NA      NA      NA
## 3 Aleyna    NA      NA      NA      NA      NA      NA      NA      NA      NA      NA
## 4 Aliye     98      NA      NA      NA      NA      NA      NA      NA      NA      NA
## 5 Alya      NA      NA      NA      NA      NA      NA      NA      NA      NA      NA
## 6 Amine     NA      NA      NA      NA      NA      NA      NA      NA      NA      NA
## # ... with 32 more variables: 1987 <dbl>, 1988 <dbl>, 1989 <dbl>, 1990 <dbl>,
## #   1991 <dbl>, 1992 <dbl>, 1993 <dbl>, 1994 <dbl>, 1995 <dbl>, 1996 <dbl>,
## #   1997 <dbl>, 1998 <dbl>, 1999 <dbl>, 2000 <dbl>, 2001 <dbl>, 2002 <dbl>,
## #   2003 <dbl>, 2004 <dbl>, 2005 <dbl>, 2006 <dbl>, 2007 <dbl>, 2008 <dbl>,
## #   2009 <dbl>, 2010 <dbl>, 2011 <dbl>, 2012 <dbl>, 2013 <dbl>, 2014 <dbl>,
## #   2015 <dbl>, 2016 <dbl>, 2017 <dbl>, 2018 <dbl>
```

```
womennames <- womennames2018 %>%
  pivot_longer(-name, names_to="year", values_to = "rank")
womennames %>%
  arrange(year, name) %>%
  head(10)
```



```
## # A tibble: 10 x 3
##   name    year  rank
##   <chr>  <chr> <dbl>
## 1 Ada    1950    NA
## 2 Ahsen  1950    NA
## 3 Aleyna 1950    NA
## 4 Aliye  1950    98
## 5 Alya   1950    NA
## 6 Amine  1950    NA
## 7 Arife  1950    80
## 8 Arin   1950    NA
## 9 Arya   1950    NA
## 10 Arzu  1950    NA
```

```
top10_2018 <- womennames %>%
  filter(year==2018, rank<11) %>%
  arrange(rank)
top10_2018
```

```
## # A tibble: 10 x 3
##   name    year  rank
##   <chr>  <chr> <dbl>
## 1 Zeynep 2018     1
## 2 Elif   2018     2
## 3 Defne  2018     3
## 4 Ebrar  2018     4
## 5 Eylül  2018     5
## 6 Hiranur 2018     6
## 7 Asel   2018     7
## 8 Meryem 2018     8
## 9 Zehra  2018     9
## 10 Miray 2018    10
```

```
top10_2017 <- womennames %>%
  filter(year==2017, rank<11) %>%
  arrange(rank)
top10_2017
```

```
## # A tibble: 10 x 3
##   name    year  rank
##   <chr>  <chr> <dbl>
## 1 Zeynep 2017     1
## 2 Elif   2017     2
## 3 Defne  2017     3
## 4 Hiranur 2017     4
## 5 Ebrar  2017     5
## 6 Eylül  2017     6
## 7 Miray  2017     7
## 8 Zehra  2017     8
## 9 Ecrin  2017     9
## 10 Azra   2017    10
```

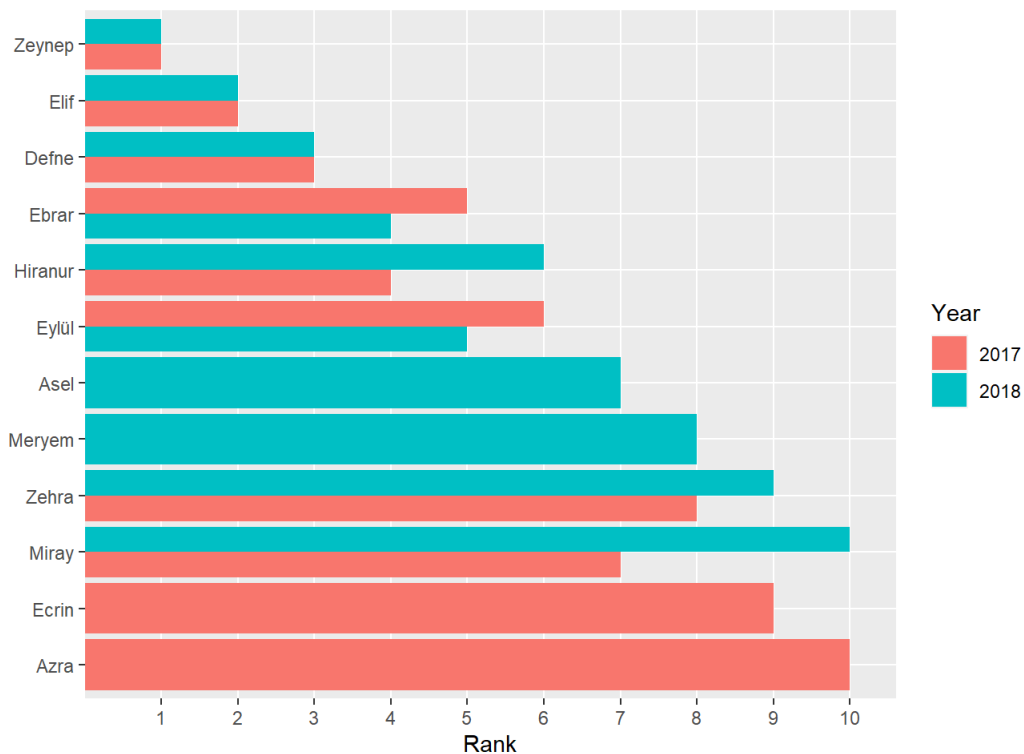
```
top10 <- full_join(top10_2017, top10_2018)
```

```
## Joining, by = c("name", "year", "rank")
```

```
top10
```

```
## # A tibble: 20 x 3
##   name      year  rank
##   <chr>   <chr> <dbl>
## 1 Zeynep  2017     1
## 2 Elif    2017     2
## 3 Defne   2017     3
## 4 Hiranur 2017     4
## 5 Ebrar   2017     5
## 6 Eylül   2017     6
## 7 Miray   2017     7
## 8 Zehra    2017     8
## 9 Ecrin    2017     9
## 10 Azra    2017    10
## 11 Zeynep  2018     1
## 12 Elif    2018     2
## 13 Defne   2018     3
## 14 Ebrar   2018     4
## 15 Eylül   2018     5
## 16 Hiranur 2018     6
## 17 Asel    2018     7
## 18 Meryem  2018     8
## 19 Zehra    2018     9
## 20 Miray   2018    10
```

```
top10 %>%
  mutate(Name = factor(name), Rank = factor(rank), Year=factor(year)) %>%
  ggplot(aes(x=reorder(name,-rank), Rank, fill=Year)) +
  geom_bar(position=position_dodge(), stat = "identity") +
  xlab("") +
  coord_flip()
```



See the example in [Introduction to the R Tidyverse](#)

There are a total of 12 names in top 10 in years 2017 and 2018. Zeynep, Elif, and Defne are in the top 3,

respectively, in both years. Ecrin and Azra were in the top 10 in 2017 but not in 2018. We see that Asel and Meryem entered the top 10 in 2018 at 7th and 8th places, respectively. Miray and Zehra became less popular as they went from the 8th to 9th and 7th to 10th places, respectively. Ebrar and Eylül, on the other hand, became more popular.

Processing math: 100%