

# Bounds, Semantics/Pragmatics-Divide, and Evolution

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## 1 The semantics-pragmatics divide

In linguistic theorizing, it is common to draw a distinction between semantics and pragmatics. Broadly speaking, the former concerns the truth-conditional content of expressions, whereas the latter concerns information beyond such literal meanings. For instance, the integration of context and the derivation of defeasible inferences. Thus, the information conveyed by an utterance is seldom, if ever, solely determined by semantics, but rather by its pragmatic enrichment. For instance, truth-conditionally, *Bill read five books* does not set an upper-bound to the amount of books that Bill read; he may have read six, seven, or more books. However, the (defeasible) inference that *Bill read no more than five books* may be drawn on pragmatic grounds. After all, if Bill had read, for example, six books, and had the speaker known this, she would have said so. In this manner, what is conveyed (pragmatically) can go beyond what is (literally) said.

Much research in semantics and pragmatics is aimed at characterizing the information conveyed by classes of expressions such as numerals in terms of either domain, or their interplay. Thus, while there is disagreement on where their boundary lies, the distinction between semantics and pragmatics plays an important (if tacit) role in linguistics. However, an issue that has received little attention is the justification of semantic structure in light of pragmatics. Put differently, this issue concerns the selection and pervasiveness of certain semantic structures over others under consideration of the informational enrichment provided by pragmatics.

Prima facie, it is puzzling that *Bill read five books* does not semantically rule out its more informative or “stronger” alternatives. More poignantly, would it not serve language users better if weak(er) expressions such as *warm*, *or*, *some* or *big* were truth-conditionally incompatible with stronger alternatives such as, respectively, *hot*, *and*, *all* and *huge*? After all, analogously to the example sketched above, this is what a pragmatically enriched interpretation yields; an upper-bound that rules out these alternatives through a so-called scalar inference (Horn 1972, Gazdar 1979). The present investigation focuses on the lack of lexicalization of such upper-bounds in natural languages. That is, we seek to provide an explanation for the selection of the particular semantics of scalar expressions, which in turn hinges on the semantics-pragmatics distinction for what is ultimately conveyed to interlocutors. However, once a distinction between semantics and pragmatics is drawn, similar questions can be posed for other types of pragmatic inferences, such as ignorance and manner inferences.

A number of recent investigations have begun to address issues pertaining to the development and selection of linguistic properties (see Steels 2015 and Tamariz and Kirby 2016 for recent overviews). Our starting point is given by the overarching account of competing pressures that has crystallized across these approaches: Natural languages need to allow for successful communication, on the one hand, and be well suited for acquisition, on the other. That is, they need to be well-adapted to the communicative needs within a linguistic community, as well as be learnable to survive their faithful transmission across generations. We proceed by instantiating these pressures in the replicator-mutator dynamics, commonly used in evolutionary game theory.

Overall, this model allows for general and precise means to model the dynamics of linguistic pressures by combining functional pressure on successful communication, effects of learning biases on (iterated) Bayesian learning (Griffiths and Kalish 2007), and probabilistic models of language use in populations with distinct lexica (Frank and Goodman 2012, Franke and Jäger 2014, Bergen et al. 2016). Drawing from the latter research strand allows for the representation of a distinction between semantics and pragmatics in communicative behavior. More broadly, it connects the recent surge in models of synchronic probabilistic rational language use with diachronic models of cultural evolution.

## 2 Conveying upper-bounds

Scalar inferences involve the pragmatic derivation of an upper-bound for weak scalar expressions provided the hearer assumes the speaker to be knowledgeable and cooperative. A scale is an informativity induced ordering of relevant alternatives. Here, informativity is understood as entailment. For instance, *all students came* entails *most students came*, which in turn entails *some students came*. In this sense, *some* is weaker than *all*. The inference derived from utterances involving weaker alternatives is that stronger ones do not hold, e.g. *some students came* may be taken to convey that *not all students came*.

say something about this pattern being widespread across languages. Give examples of classes of expressions in English, as alluded above (numerals, scalar adjectives, quantifiers)

Framed in Gricean terms (Grice 1975), the hearer reasons about the speaker’s choice of a weak alternative over a stronger one; had the speaker known that a stronger alternatives holds, she would have said so as this would have been more informative, since she did not, the hearer can infer that the stronger alternatives do not hold. Analogously, a speaker who reasons about her addressee may be rely on her to derive this inference. In this way, the strengthened, upper-bounded, state of affairs can be conveyed without codifying the bound explicitly in the semantics.

**Function-based explanations.** Two ingredients are key to this derivation; (the assumptions of) cooperation and knowledge about the issue at hand. It is not difficult to imagine cases were one or both are not given. The speaker may (be assumed to) want to withhold information about the students’ attendance, or may have left early without being able to verify the attendance to a satisfactory degree.

**Learning-based explanations.** start bottom up – from the behavior of agents to the overall dynamics. Here, begin with language use and introduce scalar inferences on the way as the object of study we will focus on here

**Language (fragments).**

**Signaling behavior.** With  $\lambda \geq 1$  (rationality parameter),  $\alpha \in [0, 1]$  (pragmatic violations) and  $pr \in \Delta(S)$  a common prior over  $S$  (uniform so far):

$$R_0(s|m; L) \propto pr(s) L_{sm} \tag{1}$$

$$S_0(m|s; L) \propto \exp(\lambda L_{sm}) \tag{2}$$

$$R_1(s|m; L) \propto pr(s) S_0(m|s; L) \tag{3}$$

$$S_1(m|s; L) \propto \exp(\lambda R_0(s|m; L)^\alpha) \tag{4}$$

### 3 Linguistic structure & selectional dynamics

The emergence and change of linguistic structure is driven by many factors, from biological and socio-ecological to cultural (Steels 2011, Tamariz and Kirby 2016). Broadly put, social and ecological pressures determine communicative needs, while biology determines the architecture available for its use. Our focus is on the latter, cultural, factor, wherein linguistic structure is analyzed in terms of its use, as well as its transmission across generations.

As already mentioned in §1, research on selectional forces that apply in the cultural evolution of language has focused on two main pressures: expressivity and learnability. However, while it is generally acknowledged that both play a pivotal role, past approaches have focused exclusively, or at least emphasized, the role of one over the other (a recent exception is Kirby et al. 2015).

Expressiveness, or communicative efficiency, has been at the center of applications of evolutionary game theory to linguistics (Nowak and Krakauer 1999, Huttegger and Zollman 2013), [explain RMD](#)

as well as [Luc Steels stuff](#).

In contrast, the iterated learning paradigm has focused on the effects of language transmission from generations of speakers to the next. [explain IL](#)

#### 3.1 Expressiveness

**Symmetrized expected utility.** With  $P \in \Delta(S)$  (uniform so far; therefore  $P = pr$ ):

- $U(t_i, t_j) = [U_S(t_i, t_j) + U_R(t_i, t_j)]/2$
- $U_S(t_i, t_j) = \sum_s P(s) \sum_m P_S(m|s; t_i) \sum_{s'} P_R(s'|m, t_j) \delta(s, s')$ , where  $\delta(s, s')$  returns 1 iff  $s = s'$  and otherwise 0
- $U_R(t_i, t_j) = U_S(t_j, t_i)$

#### 3.2 Learnability

**(II) Sequences and atomic observations.** Before, the set of all observations was  $O = \{\langle\langle s_1, m_i \rangle, \langle s_2, m_j \rangle \rangle | m_i, m_j \in M\}$ . A member of  $O$  encodes that a teacher produced  $m_i$  in state  $s_1$  and  $m_j$  in  $s_2$ , i.e., it encodes one witnessed message for each state. A datum  $d$  was a sequence of length  $k$  of members of  $O$ . Learners witnessed such data sequences. Now, more in line with Griffiths and Kalish (2007),  $O = \{\langle s_i, m_j \rangle | s_i \in S, m_j \in M\}$  and  $d$  is a sequence of length  $k$  of members of  $O$ . The main difference is that now some  $d$  do not provide any production information for some states.

**(III) Observations as production.** Instead of taking the space of all possible sequences of length  $k$  into consideration, we take sample from  $O$   $k$ -times according to the production probabilities of each type;  $P(o = \langle s, m \rangle | t_i) = P(s)P(m|s, t_i)$ .  $n$  such  $k$ -length sequences are sampled for each type. As a consequence, the data used for computing  $Q_i$  is not the same as that used for  $j$  ( $i \neq j$ ).

**(IV) Parametrized learning**  $Q_{ij} \propto \sum_d P(d|t_i) F(t_j, d)$ , where  $F(t_j, d) \propto P(t_j|d)^l$  and  $l = 1$  corresponds to probability matching and, as  $l$  increases towards infinity, to MAP.

The proportion of players of type  $i$ ,  $x_i$ , is initialized as an arbitrary distribution over  $T$ .  $p^* \in \Delta(T)$  is learning a prior over (player) types dependent only on the lexicon of the type.

- $f_i = \sum_j x_j U(x_i, x_j)$

- $\Phi = \sum_i x_i f_i$
- $Q_{ij} \propto [\sum_d P(d|t_i) P(t_j|d)]^l$ , where  $P(t_j|d) \propto p^*(t_j)P(d|t_j)$ ,  $d$  is a sequence of observations of length  $k$  of the form  $\langle s_i, m_j \rangle, \dots \langle s_k, m_l \rangle$ , and  $l \geq 1$  is a learning parameter.
- For parental learning (standard RMD):  $\dot{x}_i = \sum_j Q_{ji} \frac{x_j f_j}{\Phi}$

### 3.3 Summary

**Procedural description.** The game is initialized with some arbitrary distribution over player types. At the game’s onset we compute  $Q$  once based on the sets of sequences  $D$  (one for each parent type). Replicator dynamics are computed based on the fitness of each type in the current population as usual.  $Q$  is computed anew for each independent run (of  $g$  generations) given that it depends on  $D$ , which is sampled from production probabilities.

## 4 Analysis

**Languages.** We consider a population of players with two signaling behaviors, literal and Gricean (level 0 and 1 below), each equipped with one of 6 lexicons. This yields a total of 12 distinct player types  $t \in T$ .  $|M| = |S| = 2$ , i.e., a lexicon is a  $(2, 2)$ -matrix. These are listed in Table 1.

$$\begin{aligned} L_1 &= \begin{pmatrix} 0 & 0 \\ 1 & 1 \end{pmatrix} & L_2 &= \begin{pmatrix} 1 & 1 \\ 0 & 0 \end{pmatrix} & L_3 &= \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} \\ L_4 &= \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} & L_5 &= \begin{pmatrix} 0 & 1 \\ 1 & 1 \end{pmatrix} & L_6 &= \begin{pmatrix} 1 & 1 \\ 1 & 0 \end{pmatrix} \end{aligned}$$

Table 1: Set of possible  $(2, 2)$ -matrices, i.e., a lexicon.

As in the CogSci paper,  $L_4$  (semantic upper-bound for  $m_2$ ) and  $L_5$  (no semantic upper-bound for  $m_2$ ) are the target lexica. Gricean  $L_5$  users can convey/infer the bound pragmatically, while literal/Gricean  $L_4$  users do so semantically.

### 4.1 Model parameters & procedure

1. Sequence length  $k$
2. Pragmatic production parameter  $\alpha$
3. Rationality parameter  $\lambda$
4. Learning prior over types (lexica); cost parameter  $c$ .  $p^*(t_i) \propto n - c \cdot r$  where  $n$  is the total number of states and  $r$  that of upper-bounded messages only true of  $s_1$  in  $t_i$ ’s lexicon (if only  $s_1$  is true of a message, then this message encodes an upper-bound). Then the score for  $L_1, L_3, L_5$  is 2, that of  $L_4$  and  $L_6$  is  $2 - c$ , and that of  $L_2$  is  $2 - 2c$ ; Normalization over lexica scores yields the prior over lexica (which is equal to the prior over types).
5. Prior over meanings ( $pr$ ). We assume that  $pr(s) = \frac{1}{|S|}$  for all  $s$ .
6. True state distribution ( $P$ ). We currently assume that  $P = \frac{1}{|S|}$  but it may be interesting to vary this

7. Learning parameter  $l \geq 1$  with 1 corresponding to probability matching, and MAP as  $l$  approaches infinity
8.  $n$  is the sample of sequences of observations of length  $k$  sampled from the production probabilities of each type
9. Number of generations  $g$

## 5 Discussion

**(I) Cost for pragmatic reasoning.** At least in the CogSci setup the effect of adding cost to pragmatic reasoning is unsurprising: High cost for pragmatic signaling lowers the prevalence of pragmatic types. Lexica that semantically encode an upper-bound benefit the most from this. However, the cost needed to be substantial to make the pragmatic English-like lexicon stop being the incumbent type (particularly when learning is communal).

**(II) Negative learning bias.** Instead of penalizing complex semantics (semantic upper-bounds) one may consider penalizing simple semantics (no upper-bounds). This is useful as a sanity check but also yields unsurprising results in the CogSci setup: The more learners are biased against simple semantics, the more prevalent are lexica that semantically encode upper-bounds.

**(III) Inductive bias.** A second learning bias that codifies the idea that lexica should be uniform, i.e. be biased towards either lexicalizing an upper-bound for all weaker alternatives in a scalar pair or for none.

**(IV) Uncertainty.** The other advantage of non-upper bounded semantics lies in being non-committal to the negation of stronger alternatives when the speaker is uncertain. Adding this to the model requires the most changes to our present setup and some additional assumptions about the cues available to players to discern the speaker’s knowledge about the state she is in.

**(V) More scalar pairs.** Taking into consideration more than one scalar pair. Preliminary results suggest that this does not influence the results in any meaningful way without further additions, e.g. by (III).

**(VI) More lexica.** Not necessary. Preliminary results suggest that considering more lexica has no noteworthy effect on the dynamics (tested with all possible 2x2 lexica).

**(VII) State frequencies.** Variations on state frequencies. This may have an interesting interaction with (III).

**(VIII) Reintroduction of communal learning.** One possibility: The probably  $N_{ij}$  with which a child of  $t_i$  adopts  $t_j$  could be the weighted sum of  $Q_{ij}$  (as before) and a vector we get from learning from all of the population:  $L_j = \sum_d P(d|\vec{p})P(t_j|d)$ , where  $P(d|\vec{p}) = \sum_i P(d|t_i)\vec{p}_i$  is the probability of observing  $d$  when learning from a random member of the present population distribution.

## 6 Conclusion

### References

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