

# Co-evolution of lexical meaning & pragmatic use

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## Abstract

According to standard linguistic theory, the meaning of an utterance is the product of conventional semantic meaning and general pragmatic rules on language use. To investigate how cultural evolution of language plays out under this picture of the semantics-pragmatics interface, we present a game theoretic model of the competition between types of language users, each endowed with a selection of lexical concepts and a particular pragmatic disposition to act on them. Our model traces two evolutionary forces and their interaction: (i) fitness-based pressure towards communicative efficiency and (ii) potential learning biases during the transfer of linguistic knowledge. We illustrate the model based on a case study on scalar implicatures. In this case study learning biases that favor simple semantic representations can foster the evolution of more sophisticated pragmatic reasoning types and so prevent the lexicalization of scalar implicatures.

## 1 Introduction

What is conveyed usually goes beyond what is said. A request for a blanket can be politely veiled by uttering “I’m cold;” temporal succession of events can be communicated by the order in which conjuncts appear as in “I traveled to Paris and got married;” an invitation can be declined by saying “I have to work.” An influential explanation of the relation between the literal meaning of expressions and what they may convey in context is due to Grice (1975), who characterizes pragmatic use and interpretation as a process of mutual reasoning about rational language use. For instance, under the assumption that the speaker is cooperative and relevant, “I have to work” may be interpreted as providing a reason why the speaker will not be able to accept an invitation, going beyond its literal meaning. Some of these enrichments are rather *ad hoc*. Others show striking regularities, such as the use of ability questions for polite requests (“Could you please ...?”), or certain enrichments of lexical meanings such as *and* to convey *and then*.

A particularly productive and well studied class of systematic pragmatic enrichments are scalar implicatures (Horn 1984, Hirschberg 1985, Levinson 1983, Geurts 2010). Usually, the utterance of a sentence like “I own some of Johnny Cash’s albums” will be taken to mean that the speaker does not own all of them. This is because, if the speaker instead owned them all, she

could have used the word *all* instead of *some* in his utterance, thereby making a more informative statement. Scalar implicatures, especially the inference from *some* to *some but not all*, have been studied extensively, both theoretically (e.g., Sauerland 2004, Chierchia et al. 2012, van Rooij and de Jager 2012) as well as experimentally (e.g., Bott and Noveck 2004, Huang and Snedeker 2009, Grodner et al. 2010, Goodman and Stuhlmüller 2013, Degen and Tanenhaus 2015). While there is much dispute in this domain about many details, a position endorsed by a clear majority is that a scalar item like *some* is underspecified to mean *some and maybe all* and that the enrichment to *some but not all* is part of some regular process with roots in pragmatics.

If this majority view is correct, the question arises how such a division of labor between semantics and pragmatics could have evolved and why it would be so pervasive across natural languages. Models of language evolution abound. There are simulation-based models studying the evolution of language in populations of communicating agents (Hurford 1989, Steels 1995, Lenaerts et al. 2005, Steels and Belpaeme 2005, Baronchelli et al. 2008, Steels 2011, Spike et al. 2016) and there are mathematical models of language evolution, mostly coming from game theory (Lewis 1969, Wärneryd 1993, Blume et al. 1993, Nowak and Krakauer 1999, Huttegger 2007, Skyrms 2010). Much of this work has focused on explaining basic properties such as compositionality and combinatoriality (e.g., Batali 1998, Nowak and Krakauer 1999, Nowak et al. 2000, Kirby and Hurford 2002, Kirby 2002, Smith et al. 2003, Gong 2007, Kirby et al. 2015, Verhoef et al. 2014, Franke 2016), but little attention has been paid to the interaction between conventional meaning and pragmatic use. What is more, many mathematical models explain evolved meaning as a regularity in the overt behavior of agents. In contrast, we will here look at language users with a richer cognitive make-up.

We spell out a model of the co-evolution of conventional meaning and pragmatic reasoning types. The objects of replication and selection are pairs of lexical meanings and general types of pragmatic behavior, which we represent using probabilistic models of pragmatic language use (Frank and Goodman 2012, Franke and Jäger 2016, Goodman and Frank 2016). Replication and selection are described by the *replicator mutator dynamic*, a general and established model of evolutionary change in large and homogeneous populations (Hofbauer 1985, Nowak et al. 2000; 2001, Hofbauer and Sigmund 2003, Nowak 2006). This approach allows us to study the interaction between (i) evolutionary pressure towards communicative efficiency and (ii) possible infidelity in the transmission of linguistic knowledge, caused by factors such as inductive learning biases and sparse learning data. Considering transmission of linguistic knowledge is important because neither semantic meanings nor pragmatic usage patterns are directly observable. Instead, language learners have to infer these unobservables from the observable behavior in which they result. We formalize this process as a form of Bayesian inference. Our approach thereby contains a well-understood model of iterated Bayesian learning (Griffiths and Kalish 2007) as a special

case, but combines it with functional selection, here formalized as the most versatile dynamic from evolutionary game theory; the replicator dynamic (Taylor and Jonker 1978). Section 2 introduces this model.

Section 3 applies this model to a case study on scalar implicatures. We discuss a setting in which the majority view of underspecified lexical meanings and pragmatic enrichments emerges if selection and transmission infidelity are combined. In particular, we show that inductive learning biases of Bayesian learners that favor simpler lexical meanings can prevent the lexicalization of scalar inferences and lead to the emergence of Gricean-like pragmatic reasoning types. Results of this case study are critically assessed in the light of the assumptions that feed our model in Section 4.

## **2 A model of co-evolving lexical concepts and pragmatic behavior**

### **2.1 Communicative success and learnability**

The emergence and change of linguistic structure is influenced by many intertwined factors. These range from biological and socio-ecological to cultural ones (Benz et al. 2005, Steels 2011, Tamariz and Kirby 2016). Social and ecological pressures determine communicative needs, while biology determines the architecture that enables and constrains the means by which they can be fulfilled. In the following, our focus lies on cultural aspects, wherein processes of linguistic change are viewed as shaped by language use and its transmission, i.e., as a result of a process of cultural evolution (Pagel 2009, Thompson et al. 2016).

The idea that language is an adaptation to serve a communicative function is fundamental to many synchronic and diachronic analyses at least since Zipf's (1949) explanation of word frequency rankings as a result of competing hearer and speaker preferences (e.g., in Martinet 1962, Horn 1984, Jäger and van Rooij 2007, Jäger 2007, Piantadosi 2014, Kirby et al. 2015). If processes of selection, such as conditional imitation or reinforcement, favor more communicatively efficient types of behavior, languages are driven towards semantic expressivity (e.g., Nowak and Krakauer 1999, Skyrms 2010). But pressure towards communicative efficiency is not the only force that shapes language. Learnability is another. Natural languages need to be learnable to survive their faithful transmission across generations. Furthermore, even small learning biases implicit in acquisition can build up and have quite striking effects on an evolving language in a process of iterated learning (Kirby and Hurford 2002, Smith et al. 2003, Kirby et al. 2014).

While natural languages are pressured for both communicative success and learnability, these forces may pull in opposite directions. Their opposition becomes particularly clear when considering the extreme (cf. Kemp and Regier 2012, Kirby et al. 2015). A language consisting of a single form-meaning association is easy to learn but lacking in expressivity. Conversely, a lan-

guage that lexicalizes a distinct form for a large number of different meanings is highly expressive but challenging to acquire.

## 2.2 The replicator mutator dynamic

An elegant formal approach to capture the interaction between communicative success and learnability is the *replicator mutator dynamic* (Hofbauer 1985, Nowak et al. 2000; 2001, Hofbauer and Sigmund 2003, Nowak 2006). In its simplest, discrete-time formulation, the RMD defines the frequency  $x'_i$  of each type  $i$  in a population at the next time step as a function of: (i) the frequency  $x_i$  of each type  $i$  before the update step, (ii) the fitness  $f_i$  of each type  $i$  before the update, and (iii) the probability  $Q_{ji}$  that an agent who wants to imitate, adopt, or learn the type of an agent with type  $j$  ends up acquiring type  $i$ :

$$x'_i = \sum_j Q_{ji} \frac{x_j f_j}{\sum_k x_k f_k}. \quad (1)$$

The RMD consists of two components: fitness-based selection and transmission biases. This becomes most transparent when we consider an equivalent formulation in terms of a step-wise application of the discrete-time replicator dynamic (Taylor and Jonker 1978) on the initial population vector  $\vec{x}$  and its subsequent multiplication with a mutation matrix  $Q$ :

$$x'_i = (\mathbf{M}(\mathbf{RD}(\vec{x})))_i, \quad (2)$$

where

$$(\mathbf{RD}(\vec{x}))_i = \frac{x_i f_i}{\sum_k x_k f_k} \quad \text{and} \quad (\mathbf{M}(\vec{x}))_i = (\vec{x} \cdot Q)_i = \left( \sum_j x_j Q_{ji} \right)_i.$$

If the transmission matrix  $Q$  is trivial in the sense that  $Q_{ji} = 1$  whenever  $j = i$ , the dynamic reduces to the replicator dynamic. The replicator dynamic is a model of fitness-based selection in which the relative frequency of type  $i$  will increase with a gradient proportional to its average fitness in the population. This dynamic is popular and versatile because it can be derived from many abstract processes of biological and cultural transmission and selection (for overview and several derivations see Sandholm 2010), including conditional imitation (e.g., Helbing 1996, Schlag 1998) or reinforcement learning (e.g., Börgers and Sarin 1997, Beggs 2005). If fitness  $f_i$  is the same for all types  $i$ , the replicator step is the identity map  $(\mathbf{RD}(\vec{x}))_i = x_i$  and the dynamic reduces to a process of iteration of the transmission bias encoded in  $Q$ . In this way, the process in (1), equivalently (2), contains a model of iterated learning (Griffiths and Kalish 2007).

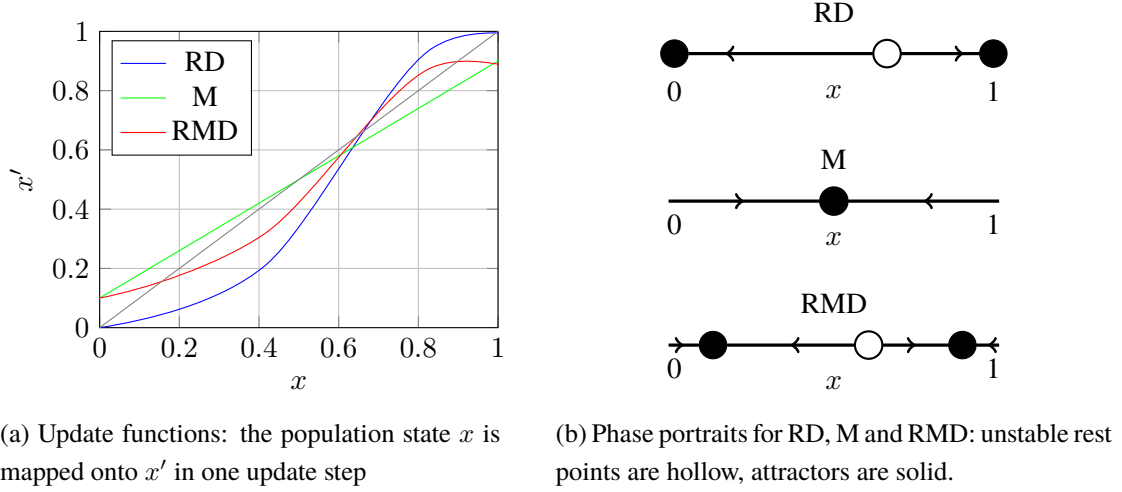


Figure 1: Example

**Example.** Consider a simple coordination game. Agents are of two types: positive or negative. If agents of different type play with each other, they obtain a payoff of 0. If negative meets negative, each receives a payoff of 1. If positive meets positive, they get a payoff of 2. A population state is completely characterized by the proportion  $x$  of negatives. The fitness of negatives in population state  $x$  is  $f_n(x) = x$ , that of positives is  $f_p(x) = 2 - 2x$ . The average fitness is  $\Phi(x) = xf_n(x) + (1 - x)f_p(x) = 3x^2 - 4x + 2$ . Without mutation, the replicator dynamic will then update  $x$  to  $RD(x) = x^2/\Phi(x)$ . The update function  $RD(x)$  of the replicator step is plotted in Figure 1a as the blue line. Rest points, for which  $RD(x) = x$ , are at  $x = 0$ ,  $x = 1$  and  $x = 2/3$ . The former are attractors as nearby points converge to them. Points near  $x = 2/3$  move towards 0 or 1. This is schematically pictured in the topmost phase portrait in Figure 1b.

Adding mutation changes the dynamic and its rest points. Let's assume that  $Q_{ji} = .9$  when  $j = i$ . The update effect of mutation alone is  $M(x) = .9x + .1(1 - x) = .8x + .1$  and is plotted as the linear green line in Figure 1a. It has only one stable rest point at  $x = 0.5$  (see Figure 1b). If we first take the replicator step and then the mutation step in sequence, we obtain the replicator mutator dynamic  $RMD(x) = M(RD(x)) = .9x^2 - .2x + .2/3x^2 - 4x + 2$ , which is plotted in red in Figure 1a. The rest points are at  $x = .121$ ,  $x = .903$  and  $x = .609$ . The former two are attractors (see Figure 1b).

### 2.3 Fitness & learnability of lexical meanings & pragmatic strategies

Moving beyond an abstract example, our goal is to apply the RMD to investigate the co-evolution of lexical concepts and pragmatic behavior. To do so, we need to fix three things: (i) what the

relevant types are, (ii) how fitness derives from communicative success and (iii) how the mutation matrix  $Q$  is computed. These issues are addressed, one by one, in the following.

### 2.3.1 Types: Lexica and pragmatic strategies

Types are what evolution operates on. They define an agent's fitness, usually through a payoff accrued in single interactions with other agents. Often types can be identified as the possible acts in a game, e.g., either cooperating or defecting in a prisoner's dilemma. In other cases, they may be thought of as general properties of an agent that influences her fitness, such as being positive or negative in our previous example (whatever that means). For our present purposes, types are identified more concretely by specific assumptions about their cognitive make-up. Since we are interested in the evolutionary competition between different lexical concepts and ways of using them in communication, a type is here defined as a pair consisting of a lexicon and a pragmatic strategy.

Agents play signaling games, in which the speaker wants to communicate a world state  $s$  with a message  $m$  to a hearer who receives  $m$  but does not know  $s$  (e.g. Lewis 1969, Skyrms 2010). A lexicon associates each message with a (possibly fuzzy) set of states. A pragmatic type maps a lexicon onto a probabilistic speaker rule (a probabilistic choice of message for each state) and a probabilistic hearer rule (a probabilistic choice of state for each message). There are many ways of making these general notions more concrete. Here is what we will assume in the remainder of this paper.

Lexica codify the truth-conditions of expressions. A convenient way to represent lexica is by  $(|S|, |M|)$ -Boolean matrices, where  $S$  is a set of states (meanings) and  $M$  a set of messages (forms available in the language). For example, suppose that there are two relevant world states  $S = \{s_{\exists-\forall}, s_{\forall}\}$ . In state  $s_{\exists-\forall}$  Chris owns some but not all of Johnny Cash's albums while in  $s_{\forall}$  Chris owns them all. Suppose that there are two messages  $M = \{m_{\text{some}}, m_{\text{all}}\}$  where  $m_{\text{some}}$  is short for a sentence like *Chris owns some of Johnny Cash's albums* and  $m_{\text{all}}$  for the same sentence with *some* replaced by *all*. Lexica for this case would assign a Boolean truth value, either 0 for false or 1 for true, to each state-message pair. The following two lexica are minimal examples for the distinction between a lexicalized upper-bound for *some* in  $L_{\text{bound}}$  and the widely assumed logical semantics with only a lower-bound in  $L_{\text{lack}}$ .

$$L_{\text{bound}} = \begin{array}{cc} & \begin{array}{cc} m_{\text{some}} & m_{\text{all}} \end{array} \\ \begin{array}{c} s_{\exists-\forall} \\ s_{\forall} \end{array} & \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \end{array} \qquad L_{\text{lack}} = \begin{array}{cc} & \begin{array}{cc} m_{\text{some}} & m_{\text{all}} \end{array} \\ \begin{array}{c} s_{\exists-\forall} \\ s_{\forall} \end{array} & \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix} \end{array}$$

Pragmatic types define dispositions to produce and interpret messages given a lexicon. We distinguish between two kinds of pragmatic types. *Literal interlocutors* produce and interpret messages literally, being guided only by their lexica. *Pragmatic interlocutors* instead engage in mutual reasoning to inform their choices. Recent probabilistic models of rational language use (Frank and Goodman 2012, Franke and Jäger 2016, Goodman and Frank 2016) capture different types of pragmatic behavior in a reasoning hierarchy. The hierarchy’s bottom, level 0, corresponds to literal language use, as in Equations (3) and (4). Pragmatic language users of level  $n + 1$  act (approximately) rational with respect to level- $n$  behavior of their interlocutors, as in Equations (5) and (6).

$$H_0(s \mid m; L) \propto pr(s) L_{sm} \quad (3)$$

$$S_0(m \mid s; L) \propto \exp(\lambda L_{sm}) \quad (4)$$

$$H_{n+1}(s \mid m; L) \propto pr(s) S_n(m \mid s; L) \quad (5)$$

$$S_{n+1}(m \mid s; L) \propto \exp(\lambda H_n(s \mid m; L)) \quad (6)$$

According to (3), a literal hearer’s interpretation of a message depends on her lexicon and her prior over states,  $pr \in \Delta(S)$ , which is here assumed flat, for simplicity. Literal interpreters thereby choose an arbitrary true interpretation for each message. Pragmatic hearers, defined in (5), use Bayes rule to weigh interpretations based on a conjecture about speaker behavior. Speaker behavior is regulated by a soft-max parameter  $\lambda$ ,  $\lambda \geq 0$  (Luce 1959, Sutton and Barto 1998). As  $\lambda$  increases, choices approximate strict maximization of expected utilities. Expected utility of a message  $m$  in state  $s$  for a level  $n + 1$  speaker is here defined as  $H_n(s \mid m; L)$ , the probability that the hearer will assign to or choose the correct meaning. For literal speakers, utility only tracks truthfulness. Literal speakers choose any true message with equal probability but may send false messages as well with a probability dependent on  $\lambda$ .

The following examples illustrate these behaviors. A literal interpreter with lexicon  $L_{\text{bound}}$  assigns  $s_{\exists \neg \forall}$  a probability of  $H_0(s_{\exists \neg \forall} \mid m_{\text{some}}; L_{\text{bound}}) = 1$  after hearing  $m_{\text{some}}$ , while a literal interpreter with  $L_{\text{lack}}$  has  $H_0(s_{\exists \neg \forall} \mid m_{\text{some}}; L_{\text{lack}}) = 0.5$ :

$$H_0(\cdot \mid \cdot, L_{\text{bound}}) = \begin{matrix} & s_{\exists \neg \forall} & s_{\forall} \\ \begin{matrix} m_{\text{some}} \\ m_{\text{all}} \end{matrix} & \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \end{matrix} \quad H_0(\cdot \mid \cdot, L_{\text{lack}}) = \begin{matrix} & s_{\exists \neg \forall} & s_{\forall} \\ \begin{matrix} m_{\text{some}} \\ m_{\text{all}} \end{matrix} & \begin{bmatrix} .5 & .5 \\ 0 & 1 \end{bmatrix} \end{matrix}$$

If  $\lambda = 1$  literal speaker behavior looks like this:

$$S_0(\cdot \mid \cdot, L_{\text{bound}}) \approx \begin{matrix} & m_{\text{some}} & m_{\text{all}} \\ \begin{matrix} s_{\exists \neg \forall} \\ s_{\forall} \end{matrix} & \begin{bmatrix} .73 & .27 \\ .27 & .73 \end{bmatrix} \end{matrix} \quad S_0(\cdot \mid \cdot, L_{\text{lack}}) \approx \begin{matrix} & m_{\text{some}} & m_{\text{all}} \\ \begin{matrix} s_{\exists \neg \forall} \\ s_{\forall} \end{matrix} & \begin{bmatrix} .73 & .27 \\ .5 & .5 \end{bmatrix} \end{matrix}$$

If  $\lambda = 20$ , literal speakers will choose true utterances with less slack:

$$S_0(\cdot \mid \cdot, L_{\text{bound}}) \approx \begin{matrix} & m_{\text{some}} & m_{\text{all}} \\ s_{\exists \neg \forall} & \begin{bmatrix} 1 & 0 \end{bmatrix} \\ s_{\forall} & \begin{bmatrix} 0 & 1 \end{bmatrix} \end{matrix} \quad S_0(\cdot \mid \cdot, L_{\text{lack}}) \approx \begin{matrix} & m_{\text{some}} & m_{\text{all}} \\ s_{\exists \neg \forall} & \begin{bmatrix} 1 & 0 \end{bmatrix} \\ s_{\forall} & \begin{bmatrix} .5 & .5 \end{bmatrix} \end{matrix}$$

Pragmatic hearers of level 1 have the following probabilistic interpretation behavior for  $\lambda = 1$ :

$$H_1(\cdot \mid \cdot, L_{\text{bound}}) \approx \begin{matrix} & s_{\exists \neg \forall} & s_{\forall} \\ m_{\text{some}} & \begin{bmatrix} .73 & .27 \end{bmatrix} \\ m_{\text{all}} & \begin{bmatrix} .27 & .73 \end{bmatrix} \end{matrix} \quad H_1(\cdot \mid \cdot, L_{\text{lack}}) \approx \begin{matrix} & s_{\exists \neg \forall} & s_{\forall} \\ m_{\text{some}} & \begin{bmatrix} .59 & .41 \end{bmatrix} \\ m_{\text{all}} & \begin{bmatrix} 0.35 & 0.65 \end{bmatrix} \end{matrix}$$

For  $\lambda = 20$ , there will be less slack again:

$$H_1(\cdot \mid \cdot, L_{\text{bound}}) \approx \begin{matrix} & s_{\exists \neg \forall} & s_{\forall} \\ m_{\text{some}} & \begin{bmatrix} 1 & 0 \end{bmatrix} \\ m_{\text{all}} & \begin{bmatrix} 0 & 1 \end{bmatrix} \end{matrix} \quad H_1(\cdot \mid \cdot, L_{\text{lack}}) \approx \begin{matrix} & s_{\exists \neg \forall} & s_{\forall} \\ m_{\text{some}} & \begin{bmatrix} 0.67 & 0.33 \end{bmatrix} \\ m_{\text{all}} & \begin{bmatrix} 0 & 1 \end{bmatrix} \end{matrix}$$

With  $\lambda = 1$ , pragmatic speakers of level 1 will have:

$$S_1(\cdot \mid \cdot, L_{\text{bound}}) \approx \begin{matrix} & m_{\text{some}} & m_{\text{all}} \\ s_{\exists \neg \forall} & \begin{bmatrix} .73 & .27 \end{bmatrix} \\ s_{\forall} & \begin{bmatrix} .27 & .73 \end{bmatrix} \end{matrix} \quad S_1(\cdot \mid \cdot, L_{\text{lack}}) \approx \begin{matrix} & m_{\text{some}} & m_{\text{all}} \\ s_{\exists \neg \forall} & \begin{bmatrix} .62 & .38 \end{bmatrix} \\ s_{\forall} & \begin{bmatrix} .38 & .62 \end{bmatrix} \end{matrix}$$

For high  $\lambda = 20$ , pragmatic speakers of level 1 give us:

$$S_1(\cdot \mid \cdot, L_{\text{bound}}) \approx \begin{matrix} & m_{\text{some}} & m_{\text{all}} \\ s_{\exists \neg \forall} & \begin{bmatrix} 1 & 0 \end{bmatrix} \\ s_{\forall} & \begin{bmatrix} 0 & 1 \end{bmatrix} \end{matrix} \quad S_1(\cdot \mid \cdot, L_{\text{lack}}) \approx \begin{matrix} & m_{\text{some}} & m_{\text{all}} \\ s_{\exists \neg \forall} & \begin{bmatrix} 1 & 0 \end{bmatrix} \\ s_{\forall} & \begin{bmatrix} 0 & 1 \end{bmatrix} \end{matrix}$$

It is important to note that pragmatic agents of level 1 using  $L_{\text{lack}}$  associate  $m_{\text{some}}$  preferentially with  $s_{\exists \neg \forall}$ , in contrast to their literal counterparts of level 0. This association is not perfect, and usually less strong than what agents with a lexicalized upper bound in  $L_{\text{bound}}$  can achieve, even without pragmatic reasoning. Higher order reasoning types leads to stronger associations of  $m_{\text{some}}$  and  $s_{\exists \neg \forall}$  also for the hearer. Still, the case study presented in Section 3 will consider speaker and hearer behavior at levels 0 and 1, as the latter are the simplest pragmatic reasoning types which show a tendency to communicatively attuned pragmatic enrichment. Using only level 1 reasoning types is therefore a conservative choice that works against the fitness-based selection of pragmatic language use for a notion of fitness based on communicative efficiency, which is introduced next.



### 2.3.2 Fitness & fitness-based selection based on communicative success

Under the replicator dynamic the proportion of type  $i$  in a population will increase or decrease as a function of its relative fitness  $f_i$ . In the context of language evolution, fitness is usually associated with the ability to successfully communicate with other language users from the same population (e.g., Nowak and Krakauer 1999, Nowak et al. 2000; 2002). Under a biological interpretation the assumption is that organisms have a higher chance of survival and reproduction if they are able to share and receive useful information via communication with peers. Under a cultural interpretation the picture is that agents themselves strive towards communicative success and therefore occasionally adapt or revise their behavior to achieve higher communicative success (see Benz et al. 2005:§3.3 for discussion).

The replicator equation gives us the means to make the ensuing dynamic precise, without necessarily committing to a biological or cultural interpretation. As above, the proportion of types in a given population is codified in a vector  $\vec{x}$ , where  $x_i$  is the proportion of type  $i$ . The fitness of type  $i$  is its average expected communicative success, or *expected utility* (EU), given the frequencies of types in the current population:

$$f_i = \sum_j x_j \text{EU}(t_i, t_j) .$$

In signaling games, the expected utility  $\text{EU}(t_i, t_j)$  for type  $i$  when communicating with type  $j$  is the average success of  $i$  when talking or listening to  $j$ . If agents are speakers half of the time, this yields:

$$\text{EU}(t_i, t_j) = 1/2 \text{EU}_S(t_i, t_j) + 1/2 \text{EU}_H(t_i, t_j) ,$$

where  $\text{EU}_S(t_i, t_j)$  and  $\text{EU}_H(t_i, t_j)$  are the expected utilities for  $i$  as a speaker and as a hearer when communicating with  $j$ , defined as follows, where  $n_i$  and  $n_j$  are type  $i$ 's and type  $j$ 's pragmatic reasoning types and  $L_i$  and  $L_j$  are their lexica:

$$\begin{aligned} \text{EU}_S(t_i, t_j) &= \sum_s P(s) \sum_m S_{n_i}(m \mid s; L_i) \sum_{s'} H_{n_j}(s' \mid m; L_j) \delta(s, s') , \\ \text{EU}_H(t_i, t_j) &= \text{EU}_S(t_j, t_i) . \end{aligned}$$

As usual,  $\delta(s, s') = 1$  iff  $s = s'$  and 0 otherwise.

### 2.3.3 Learnability

Languages are shaped not only by functionalist forces towards greater communicative success. Another important factor is the fidelity with which linguistic knowledge is transmitted. Among

others, linguistic production can be prone to errors, states or messages may be perceived incorrectly, and multiple languages may be compatible with the data learners are exposed to. These sources of uncertainty introduce variation in the transmission of linguistic knowledge from one generation to the next. In particular, learning biases in the iterated transmission process can influence language evolution substantially.

In biological evolution, where types are expressed genetically, transmission infidelity comes into the picture through infrequent and mostly random genetic mutations. However, an agent’s lexicon and pragmatic reasoning behavior is likely not inherited genetically. They need to be learned from observation. Concretely, when agents of type  $j$  want to adopt or imitate the linguistic behavior of type  $i$ , they observe the overt linguistic behavior of type  $i$  and need to infer the covert type that most likely produced the visible behavior. Iterated learning is a process in which languages are learned repeatedly from the observation of linguistic behavior of agents who have themselves acquired the language from observation and inference. In the simplest case there is a single teacher and a single learner. After sufficient training the learner becomes a teacher and produces behavior that serves as input for a new learner. Due to the pressure towards learnability it exerts, iterated learning alone generally leads to simpler and more regular languages (see Kirby et al. 2014 and Tamariz and Kirby 2016 for recent surveys).

Following Griffiths and Kalish (2007) we model language acquisition as a process of Bayesian inference in which learners combine the likelihood of a type producing the witnessed learning input with prior inductive biases. Experimental and mathematical results on iterated learning suggest that the outcome of this process reflects learners’ inductive biases (e.g., Kirby et al. 2014). In a Bayesian setting these biases can be codified in a prior  $P \in \Delta(T)$ , which reflects the amount of data a learner requires to faithfully acquire the language of the teacher (cf. Griffiths and Kalish 2007:450). The extent of the prior’s influence has been shown to heavily depend on the learning strategy assumed to underlie the inference process. On the one hand, early simulation results suggested that weak biases could be magnified by exposing learners to only small data samples (e.g. in Brighton 2002). On the other, Griffiths and Kalish’s (2007) mathematical characterization showed that iterated learning converges to the prior in the limit, i.e., that the resulting distribution over languages corresponds to the learners’ prior distribution and is not influenced by the amount of input given to them. This difference in predictions can be traced back to differences in the selection of hypotheses from the posterior. Griffith & Kalish’s convergence to the prior holds for learners that sample from the posterior. More deterministic strategies such as the adoption of the type with the highest posterior probability, so-called *maximum a posteriori estimation* (MAP), increase the influence of both the prior and the data (Griffiths and Kalish 2007, Kirby et al. 2007). In the following, we use a parameter  $l \geq 1$  to modulate between posterior sampling and the MAP strategy. When  $l = 1$  learners sample from the posterior. The learners’ propensity to maximize

the posterior grows as  $l$  increases.

Let  $D$  be the set of possible data that learners may be exposed to. This set  $D$  contains all sequences of state-message pairs of length  $k$ , e.g.,  $\langle \langle s_1, m_1 \rangle, \dots, \langle s_k, m_k \rangle \rangle$ . As  $k$  increases, learners have more data to base their inference on and so tend to recover the true types that generated a given sequence with higher probability. The mutation matrix  $Q$  of the replicator mutator dynamic in (1) can then be defined as follows:  $Q_{ji}$  is the probability that a learner acquires type  $i$  when learning from an agent of type  $j$ . The learner observes a length- $k$  sequence  $d$  of state-message pairs, but the probability  $P(d | t_j)$  with which sequence  $d = \langle \langle s_1, m_1 \rangle, \dots, \langle s_k, m_k \rangle \rangle$  is observed depends on type  $j$ 's behavior:

$$P(d = \langle \langle s_1, m_1 \rangle, \dots, \langle s_k, m_k \rangle \rangle | t_j) = \prod_{i=1}^k S_{n_j}(m_i | s_i; L_j),$$

where, as before,  $n_j$  is  $j$ 's pragmatic reasoning type and  $L_j$  is  $j$ 's lexicon. For a given observation  $d$ , the probability of acquiring type  $i$  is  $F(t_i | d)$ , so that:

$$Q_{ji} \propto \sum_{d \in D} P(d | t_j) F(t_i | d).$$

The acquisition probability  $F(t_i | d)$  given datum  $d$  is obtained by probability matching  $l = 1$  or a tendency towards choosing the most likely type  $l > 1$  from the posterior distribution  $P(\cdot | d)$  over types given the data, which is calculated by Bayes' rule:

$$F(t_i | d) \propto P(t_i | d)^l \text{ and} \\ P(t_i | d) \propto P(t_i) P(d | t_i).$$

## 2.4 Model summary

Communicative success and learnability are central to the cultural evolution of language. These components can be modelled, respectively, as replication based on a measure of fitness in terms of communicative efficiency and iterated Bayesian learning. Their interaction is described by the discrete time replicator mutator dynamic in (1), repeated here:

$$x'_i = \sum_j Q_{ji} \frac{x_j f_j}{\sum_k x_k f_k}.$$

This equation defines the frequency  $x'_i$  of type  $i$  at the next time step, based on its frequency  $x_i$  before the step, its fitness  $f_i$ , and the probability that a learner infers  $i$  when observing the behavior of a type- $j$  agent. Fitness-based selection is here thought of not as biological (fitness as expected relative number of offspring) but cultural (fitness as likelihood of being imitated

or repeated) evolution, since the types that the dynamic operates on are pairs consisting of a lexicon and a pragmatic use pattern. A type’s communicative success depends on how well it communicates within a population while its learnability depends on the fidelity by which it is inferred by new generations of learners. The learners’ task is consequently to perform a joint inference over types of linguistic behavior and lexical meaning.

The model has three parameters:  $\lambda$  regulates the degree to which pragmatic speakers choose messages that maximize the chance of communicative success;  $k$  is the number of observations for each language learner;  $l$  regulates where the learners’ inference behavior lies on a spectrum from probability matching to choice of the most likely parent type.

### 3 Case study: scalar implicatures

The model of the previous section formalizes the evolutionary competition between different pairs of lexical concepts and ways of using them. This section looks at a case study on scalar implicatures. It engages in a following formal thought experiment to address the question: if a population of language users could freely combine different lexica with different pragmatic strategies, what are conditions under which the majority view of scalar implicatures could have evolved?

Recall that the majority view is that scalar implicatures are non-lexicalized pragmatic enrichments. Scalar implicature triggers like *some*, *warm* or *may* are semantically weak expressions for which logically stronger expressions are salient, e.g., *all*, *hot* or *must*. For instance, *some* is entailed by *all*. If the sentence “Chris owns all of Johnny Cash’s albums” is true, then “Chris owns some of Johnny Cash’s albums” is also true. However, while weaker expressions such as *some* are truth-conditionally compatible with stronger alternatives such as *all*, this is not what their use is normally taken to convey. Instead, the use of a less informative expression when a more informative one could have been used can license a defeasible inference that stronger alternatives do not hold (cf. Horn 1972, Gazdar 1979). In this way, “Chris owns some of Johnny Cash’s albums” is strengthened to convey that she owns *some but not all* albums. According to the majority view, this is a pragmatic inference, not part of the conventional meaning.

In the following we consider a specific application of the model from Section 2 which allows to address the question if or when scalar inferences might (not) lexicalize. We consider what is perhaps one of the simplest non-trivial setups that speak to this matter and reflect on its limitations in Section 4. The setup is introduced in Section 3.1. Section 3.2 describes the simulations and their results.

### 3.1 Setup

To fill the model from Section 2 with life, we need to specify the sets of states, messages and lexica (Section 3.1.1). Additionally, we want to explore the effects of a learning bias in favor of simple lexical concepts. One way of motivating and formalizing such a bias is introduced below in Section 3.1.2.

#### 3.1.1 States, messages, concepts and lexica

Consider a state space with three states  $S = \{s_\emptyset, s_{\exists-\forall}, s_\forall\}$  and think of it as a partition of possible worlds into cells where none, some or all of the  $A$ s are  $B$ s, for some arbitrary fixed predicates  $A$  and  $B$ . Eight concepts can be distinguished based on their truth or falsity in three world states, six of which are not contradictory or tautological (see Table 2 below).

A lexicon  $L$  is a mapping  $M \rightarrow C$  from messages to concepts. With three messages there are  $6^3 = 216$  possible lexica. Some assign the same concept to more than one message and others lexicalize the same concepts but associate them with different messages. Out of these possible lexica, three kinds are of particular relevance. First, lexica that assign the same concept to more than one message. Such lexica lack in expressivity but may be favored by particular learning biases nonetheless (see below). Second, lexica that conventionalize upper-bounds to realize a one-to-one mapping of messages to states. Finally, lexically that do not lexicalize an upper bound but allow it to be conveyed pragmatically due to the presence of a stronger lexical item. There are six lexica of the second kind and six of the third. The following three lexica exemplify each kind:

|                       | <u><math>L_{\text{all}}</math></u> |                   |                  | <u><math>L_{\text{bound}}</math></u> |                   |                  | <u><math>L_{\text{lack}}</math></u> |                   |                  |
|-----------------------|------------------------------------|-------------------|------------------|--------------------------------------|-------------------|------------------|-------------------------------------|-------------------|------------------|
|                       | $m_{\text{none}}$                  | $m_{\text{some}}$ | $m_{\text{all}}$ | $m_{\text{none}}$                    | $m_{\text{some}}$ | $m_{\text{all}}$ | $m_{\text{none}}$                   | $m_{\text{some}}$ | $m_{\text{all}}$ |
| $s_\emptyset$         | 0                                  | 0                 | 0                | 1                                    | 0                 | 0                | 1                                   | 0                 | 0                |
| $s_{\exists-\forall}$ | 0                                  | 0                 | 0                | 0                                    | 1                 | 0                | 0                                   | 1                 | 0                |
| $s_\forall$           | 1                                  | 1                 | 1                | 0                                    | 0                 | 1                | 0                                   | 1                 | 1                |

Lexicon  $L_{\text{all}}$  is clearly bad for communication: all message and interpretation choices will be equally likely for all types; no information about the observed world state will be conveyed by its users. In contrast, users of  $L_{\text{bound}}$  can communicate world states perfectly, no matter whether they are literal or pragmatic users. Users of  $L_{\text{lack}}$  can also communicate information about the actual world state but need pragmatic language use to approximate a one-to-one mapping between message use and states (see Section 2.3.1).

Recall that types are a combination of a lexicon and a manner of language use. We analyze the model's predictions in populations of types with one of the two behaviors introduced earlier;

|                                 |                                    |                                 |
|---------------------------------|------------------------------------|---------------------------------|
| $C \rightarrow_2 C \wedge C$    | $C \rightarrow_2 \neg C$           |                                 |
| $C \rightarrow_1 X \subseteq X$ | $C \rightarrow_1 X \neq \emptyset$ | $C \rightarrow_1 X = \emptyset$ |
| $X \rightarrow_1 \{A, B\}$      | $X \rightarrow_1 X \cap X$         | $X \rightarrow_1 X \cup X$      |

Table 1: Toy grammar in a set-theoretic LOT with weighted rules.

literal or pragmatic. The former correspond to level 0 reasoners and the latter to level 1. Accordingly, we consider a total of 432 types. Six are variants of pragmatic language users with  $L_{\text{lack}}$ -like lexica. We refer to these as *target types*, because they represent lexica and language use that conform to the majority view of scalar implicatures. Twelve types are either literal or pragmatic speakers with lexical of the  $L_{\text{bound}}$  kind. We refer to these as *competitor types*, because they are expected to be the target types’ main competitors in evolutionary competition.

### 3.1.2 An inductive learning bias for semantic simplicity

There is a growing effort to develop empirically testable representational languages that allow for the measure of semantic complexity. For instance, so-called *languages of thought* (LOTs) have been put to test in various rational probabilistic models that show encouraging results (see, e.g., Katz et al. 2008, Piantadosi et al. view; 2012 and Piantadosi and Jacobs 2016 for recent discussion). At its core, a LOT defines a set of operations and composition rules from which concepts can be derived. As a first approximation and for the sake of concreteness, we follow this approach to motivate and formalize a preference of learners for simpler semantic representations (Feldman 2000, Chater and Vitányi 2003, Piantadosi et al. 2012, Kirby et al. 2015, Piantadosi et al. under review). A concept’s complexity is a function of its derivation cost in a weighed generative LOT.

Our toy grammar of concepts is given in Table 1. This grammar uses basic set-theoretic operations to form expressions which can be evaluated as true or false in states  $s_\emptyset$ ,  $s_{\exists-\forall}$  or  $s_\forall$  from above. Applications of generative rules have a cost attached to them. Here we simply assume that the formation of Boolean combinations of concepts incurs 2 cost units, while all other rule applications incur only 1 cost unit. Table 2 lists all six concepts relevant here, their truth conditions and the simplest formula that expresses this concept from the grammar in Table 1.

The complexity measure for lexical concepts from Table 2 is used to define a learning bias that favors simpler concepts over more complex ones. The prior probability of a type is just the prior probability of its lexicon. The prior of a lexicon is a function of the complexity of the lexical representations in its image set. Lexica with simpler concepts have a higher prior. One simple

| intuitive name     | $s_{\emptyset}$ | $s_{\exists-\forall}$ | $s_{\forall}$ | least complex formula                                   | complexity |
|--------------------|-----------------|-----------------------|---------------|---|------------|
| “all”              | 0               | 0                     | 1             | $A \subseteq B$   | 3          |
| “some but not all” | 0               | 1                     | 0             | $A \cap B \neq \emptyset \wedge A \neq \emptyset$       | 8          |
| “some”             | 0               | 1                     | 1             | $A \cap B \neq \emptyset$                               | 4          |
| “none”             | 1               | 0                     | 0             | $A \cap B = \emptyset$                                  | 4          |
| “none or all”      | 1               | 0                     | 1             | $\neg(A \cap B \neq \emptyset \wedge A \neq \emptyset)$ | 10         |
| “not all”          | 1               | 1                     | 0             | $\neg(A \subseteq B)$                                   | 5          |

Table 2: Available concepts and their minimal derivation cost

way of defining such priors over lexica (and thereby types) is:

$$P(L) \propto \prod_{c \in \text{Im}(L)} P(c), \text{ with } P(c) \propto \max_{c'} \text{Compl}(c') - \text{Compl}(c) + 1,$$

where  $\text{Compl}(c)$  is the complexity of the minimal derivation cost of  $c$  according to the LOT-grammar (see Table 2). Applied to our space of lexica, this construal assigns the highest probability to a lexicon of type  $L_{\text{all}}$ , which only uses the simplest concept “all” for all messages. Lexica of type  $L_{\text{lack}}$  are less likely, but more likely than  $L_{\text{bound}}$ .

There are many ways to define priors over lexica (see, e.g., Goodman et al. 2008, Piantadosi et al. 2012) but the key assumption here, common to all of them, is that simple representational expressions should be favored over more complex ones. We should stress that these details – from the generative grammar to its complexity measure – are to be regarded as one convenient operationalization of one general approach to explicating learning biases; this is not a commitment that this general approach is necessarily superior or that, within it, this particular instrumentalization is the single most plausible.

### 3.2 Simulation results

Recall that there are three parameters: soft-max parameter  $\lambda$  affects how strongly speakers favor messages that appear best from their subjective point of view; the bottleneck size  $k$  influences how faithfully learners can identify their teacher type;  $l$  defines the learners’ disposition towards choosing the most likely teacher type from the posterior distribution. We expect that competitor types (types with lexica of the kind  $L_{\text{bound}}$ ) have a fitness advantage over target types (pragmatic agents with lexica of the kind  $L_{\text{lack}}$ ), especially for very low levels of  $\lambda$ . Selection based on fitness alone may therefore not lead to prevalence of target types in the population. On the other hand, lexica of type  $L_{\text{lack}}$  are simpler than those of type  $L_{\text{bound}}$  by the postulated measure from

above. This may make them more likely to be adopted by learners, especially when  $k$  is low so that different teacher types are relatively indistinguishable based on their behavior and when  $l$  is high. Still, lexica of the kind  $L_{\text{all}}$  are in turn more likely *a priori* than lexica of the kind  $L_{\text{lack}}$ . Simulation results will shed light on the question whether target types can emerge and for which parameter constellations.

To better understand the workings of a pressure towards communicative efficiency and a pressure towards learnability, we look at the behavior of the replicator and mutator step first in isolation, and then in combination. All simulation runs are initialized with an arbitrary distribution over types, constituting a population’s first generation. All reported results are the outcome of 50 update steps. These outcomes correspond to developmental plateaus in which change is, if not absent, then at least very slow. In other words, even if the resulting states do not correspond to an eventual attracting state, they characterize long almost stationary states in which the system remains for a very long time. As specified in §2.3.3, the mutation matrix  $Q$  can be obtained by considering all possible state-message sequences of length  $k$ . Given that this is intractable for large  $k$ , the sets of data learners are exposed to are approximated by sampling 250  $k$ -length sequences from each type’s production probabilities.

### 3.2.1 Replication only: selection based on expressivity and communicative success

As expected, selection based on communicative success is sensitive to  $\lambda$  as it influences signaling behavior, which in turn determines communicative success. This is showcased in Figure 2, which depicts the proportion of target types in 5 independent populations after 50 replicator steps. The plot also shows the proportion of the *majority type*, i.e., the type with the highest proportion in the final population. With low  $\lambda$  many types have very similar behavior, so that evolutionary selection lacks grip and becomes very slow. The result is a very long transition with near stagnancy in a rather homogeneous population with many types. Conversely, higher  $\lambda$  promotes more rational linguistic behavior, widening the gap in expressivity between types and promoting more homogeneous populations. As suggested by Figure 2, the majority in most populations is not one of the six pragmatic  $L_{\text{lack}}$ -style types. That is, a pressure only for communicative success does not lead to a prevalence of target types under any  $\lambda$ -value. For instance, with  $\lambda = 20$  1000 independent populations only had 11 cases in which the target type was the majority type, corresponding to a mean proportion of 0.003 across populations. By contrast, in 913 cases the majority types had  $L_{\text{bound}}$  with close to an even share between literal (454) and pragmatic types (459), corresponding to a mean proportion of about .48 taken together.



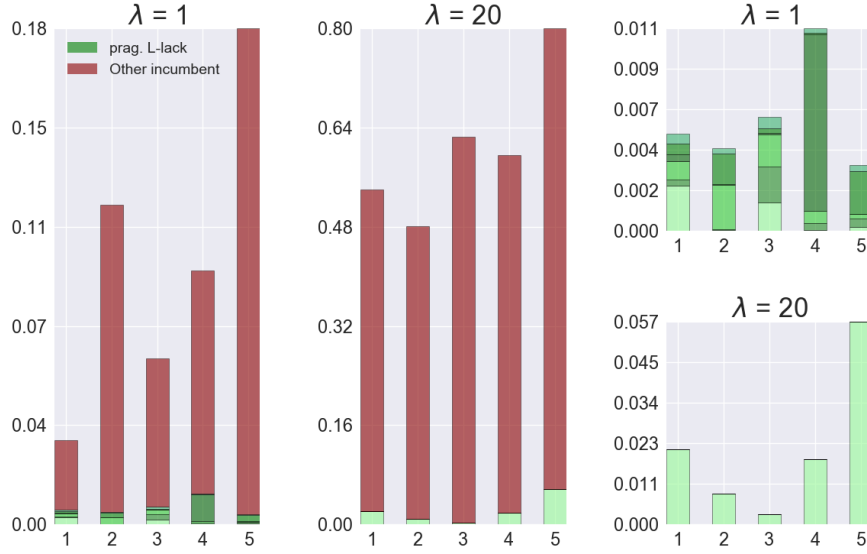


Figure 2: Stacked proportion of pragmatic  $L_{\text{lack}}$ -style types and majority types, when other than pragmatic  $L_{\text{lack}}$ , in 5 independent populations after 50 generations under only a pressure for communicative success. The right-most plots zoom in on only the proportion of target types. [TB: change plot to maj. type]

### 3.2.2 Iterated learning only

The effect of iterated learning without a pressure for communicative success using either posterior sampling ( $l = 1$ ) or a stronger tendency towards posterior maximization ( $l = 15$ ) is shown in Figure 3 together with the prior over types. The prior shows that while users of  $L_{\text{lack}}$  are not the most favored by the inductive bias (compared, e.g., to  $L_{\text{all}}$ ) they are nevertheless more advantaged than others, such as  $L_{\text{bound}}$ , in virtue of the relatively simple semantics they conventionalize (see Section 3.1.2). Crucially,  $L_{\text{lack}}$  enables its users to convey each state with a single message when combined with pragmatic reasoning provided sufficiently high  $\lambda$ . This makes it less likely to be confused with other types if the learning data is not too sparse ( $k \geq 5$ ). Put differently, learners have a higher propensity to infer pragmatic  $L_{\text{lack}}$  when the teacher’s type produces very similar data, such as when using  $L_{\text{bound}}$ . Moreover,  $L_{\text{lack}}$  is also less likely to be confused with types with different observable behavior because its pragmatic use approximates a one-to-one form-meaning mapping. As a consequence, a stronger propensity to maximize the posterior increases their proportion in the population.

However, in contrast to a pressure only for communicative success with high  $\lambda$  (see Figure 2), learnability alone does not succeed in selecting for a single prevalent type. Indeed, all six target

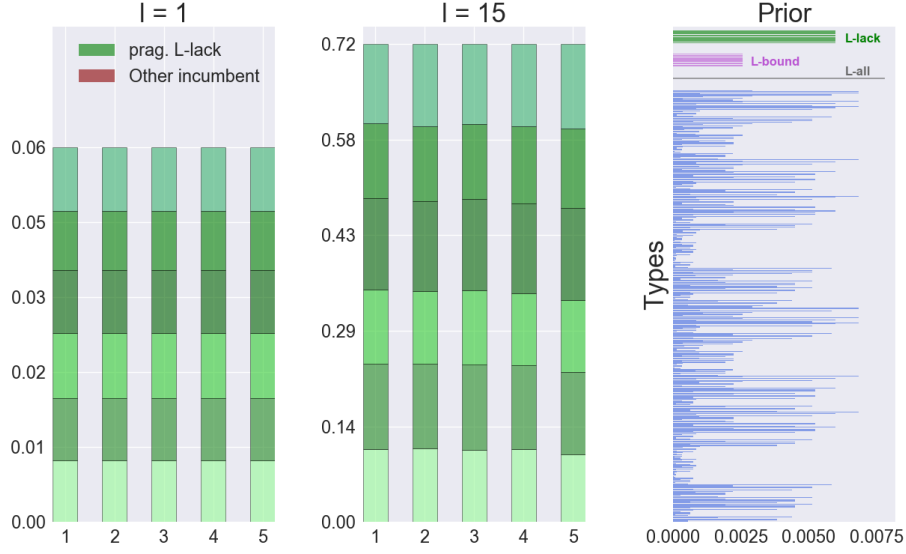


Figure 3: Stacked proportion of pragmatic  $L_{\text{lack}}$ -style types and majority types, when other than pragmatic  $L_{\text{lack}}$ , in 5 independent populations after 50 generations under only a pressure for learnability ( $\lambda = 20, k = 5$ ). The types' prior probability is shown in the right-most plot. [MF: explain the topmost part of the right plot?!] [TB: and change to maj. type in plot]

types tend to coexist at roughly equal proportion. Each is passed on to the next generation with the same faithfulness and, differently from a pressure for communicative success, they do not stand in competition with each other. In 1000 independent populations with  $\lambda = 20$  all majority types were target types, with each reaching approximately the same proportion of users in the population. As with a pressure only for communicative success, low values of  $\lambda$  make the differences in observable behavior across types less pronounced and therefore reflect the learners' inductive bias more faithfully, favoring functionally deficient but a priori preferred types such as those that use  $L_{\text{all}}$ . A pressure for learnability alone may consequently lead to a spread of communicatively suboptimal types that are easier to learn. In the extreme, when  $l = 1$  and  $\lambda = 1$  all of 1000 independent populations had users of  $L_{\text{all}}$  as majority types.

### 3.2.3 Combining pressures of communicative success and learnability

Pressures for communicative success or learnability are not sufficient on their own to have a single target type dominate the population. When pressured for communicative success, the slight communicative advantage of  $L_{\text{bound}}$  users leads to its prevalence. When pressured for learnability, pragmatic  $L_{\text{lack}}$  is promoted over functionally similar but semantically more complex

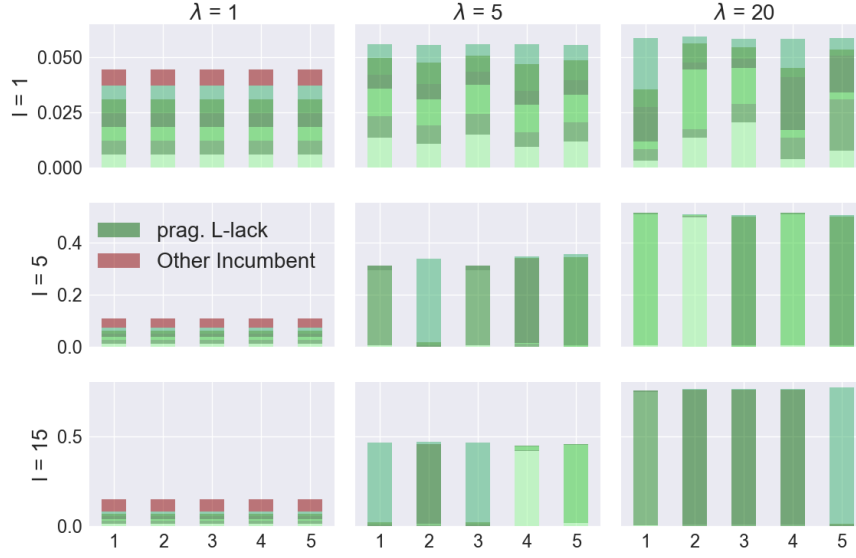


Figure 4: Stacked proportion of pragmatic  $L_{\text{lack}}$ -style types and majority types, when other than pragmatic  $L_{\text{lack}}$ , in 5 independent populations after 50 generations under both pressures ( $k = 5$ ).  
[TB: change plot to maj. types]

alternatives such as  $L_{\text{bound}}$ . However, learnability alone does not foment the propagation of a single target type across the population.

Figure 4 illustrates the combined effects of both pressures for a sample of  $\lambda$  and  $l$  values. These results show that an inductive learning bias for simpler semantics in tandem with functional pressure can lead to the selection of a single target type. The proportion of a single majority target type increases with  $\lambda$  and  $l$ . Pressure for communicative success magnifies the effects of iterated learning and dampens the proliferation of types of a kind that are equal in expressivity *and* learnability. A pressure towards learnability favors the transmission of simpler semantics and thereby selects for pragmatic language use.

As before, low  $\lambda$  and  $l$  lead to the prevalence of communicatively suboptimal types that are a priori favored, such as  $L_{\text{all}}$ . An increase in  $\lambda$  leads to the selection of target types but does not lead to monomorphic populations if learners sample from the posterior. Finally, a combination of high  $\lambda$  and  $l$  leads to increasing proportions of a single majority target type. The difference between the mean of the highest pragmatic  $L_{\text{lack}}$ -like type in 1000 independent populations and the highest proportion of other types across  $\lambda$  and  $l$  values is shown in Figure 5.

As for the effect of the sequence length  $k$  not mentioned so far, it influences populations in a predictable way: small values lead to more heterogeneous populations that reflect the learner's

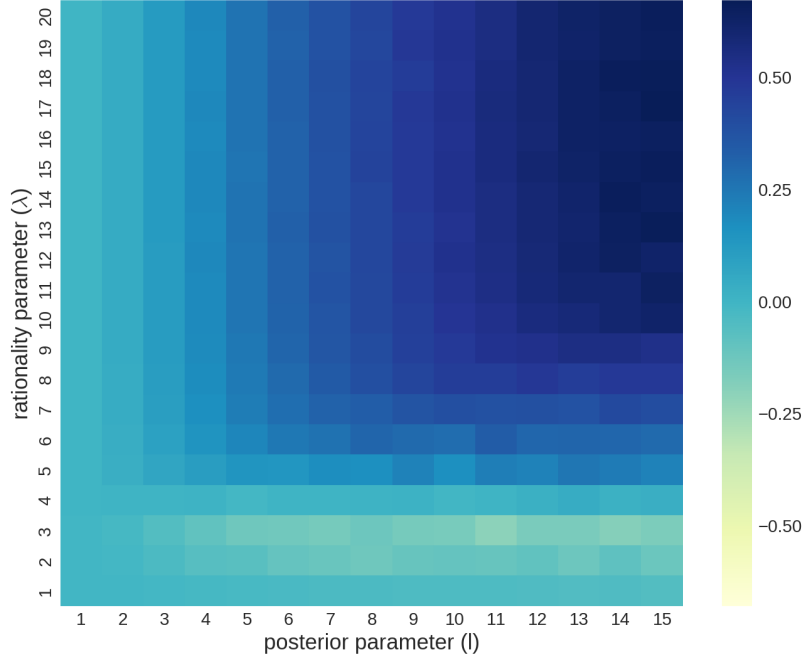


Figure 5: Difference between mean proportion of highest pragmatic  $L_{\text{lack}}$  type and highest other type in 1000 independent populations after 50 generations under both pressures ( $k = 5$ ). [MF: the coloring is not that easy to decipher here; would a two-dimensional surface be possible and look better?]

prior more faithfully. This is due to the fact that the likelihood that a small sequence was produced by any type is relatively uniform (modulo prior). By contrast, larger values increasingly allow learners to differentiate types with different signaling behaviors.

To recapitulate, other than the involvement of pressure on both communicative success and learnability, the resulting proportion of pragmatic  $L_{\text{lack}}$  speakers primarily hinges on three factors. First, the degree, captured by  $\lambda$ , to which agents try to maximize communicative success from their own subjective point of view. Second, the inductive bias, which leads learners to prefer simpler over more complex semantic representations in acquisition. Lastly, the learning behavior, captured by parameter  $l$ , where approximating a MAP strategy magnifies the effects of the learning bias in tandem with replication.

In summary, target types, which represent the majority view of scalar implicatures, can come to dominate the population if three assumptions are met: (i) language is pressured toward both communicative success and learnability; (ii) pragmatic language use is an option; (iii) learners

prefer simpler over more complex lexical representations and exhibit a tendency towards the acquisition of the type that best explains the learning data.

## 4 General discussion

The approach introduced here combines game theoretic models of functional pressure towards efficient communication (Nowak and Krakauer 1999), effects of transmission perturbations on (iterated) language learning (Griffiths and Kalish 2007), probabilistic speaker and listener types of varied degrees of pragmatic sophistication (Frank and Goodman 2012, Franke and Jäger 2014) as well as reasoning about unobservable lexical representations (Bergen et al. 2012; 2016). This allows a conceptual investigation of the co-evolution of conventional meaning and pragmatic language use. Main contributions of the model are (i) its modular separation of communicative success and learnability on evolutionary trajectories, (ii) the characterization of language learning as a joint inference over pragmatic behavior and lexical meaning, and (iii) the possibility to trace the co-evolution of conventional semantics and pragmatic use.

With respect to (i), Kirby et al. (2015) propose a comparable model of the interaction between a lexicon’s expressivity and its learnability. One of its main differences to our proposal lies in the former force exerting pressure only in the production of learning data. The pressure towards communicative success within a population central to replication is absent. Put differently, we consider a pressure for mutual understanding that may indirectly select for expressive types, i.e., those that can convey states unequivocally, whereas Kirby et al. only consider the bearing that the latter ability has on the production of learnable data. We see two main reasons for considering communicative success rather than expressivity, and to only considering it in learning. First, learnability alone can lead to the acquisition of functionally defective languages, as showcased by  $L_{all}$  (cf. Kirby et al. 2008, Silvey et al. 2014, and Fay and Ellison 2013 for review of laboratory results). Second and more importantly, types may be equally expressive but their performance as means of information transfer crucially depends not only on themselves but on the population they find themselves in (cf. the competition of types of a kind in Figure 4 and their lack of competition in Figure 3). That is, we contend that having an expressive lexicon that generates learnable data does not in itself capture a type’s arguably central communicative function of transferring information to peers. Under this view, a type’s expressiveness is secondary to its ability to communicate successfully. Acquiring a maximally expressive type is of little use when it is not understood in its population.

The main result of our case study is that types that correspond to the majority view of scalar implicatures (scalar readings are non-lexicalized pragmatic enrichments) can come to dominate a population. This can happen under the assumption that simpler semantic representations are

more likely to be learned (cf. Chater and Vitányi 2003). Pragmatic language use can be recruited indirectly by a preference for simpler lexical concepts. Under this view, semantics and pragmatics play a synergic role: pragmatic use allows maintenance of simpler concepts; pressure towards representational simplicity indirectly promotes pragmatic over literal language use. As a consequence, iterated transmission and use of language lead to a regularization that may explain the lack of lexicalization of systematic pragmatic enrichments.

While the results of this case study are interesting, they also raise a number of critical issues. First of all, while many favorable parameter settings exist which lead to a prevalence of target types, other types are usually represented in non-negligible proportions. This may just be a technical quirk of the mutator step. But there is a related issue of empirical importance. Several experimental studies on scalar implicatures suggest that participants can be classified as either semantic or pragmatic users of, in particular, *some* (e.g. Bott and Noveck 2004, Nieuwland et al. 2010, Degen and Tanenhaus 2015). The former consistently accept *some* where *all* would be true as well, the latter do not. Interestingly, in our simulations when a target type is the majority type an inflated proportion of the population uses compatible lexica with a lexicalized upper bound. Particularly in those parameter settings where the prior influences the outcome less. In other words, we do find a tendency toward a similar co-existence of semantic and pragmatic types. Whether this analogy has any further explanatory value is an interesting path for future exploration. [TB: I some qualifications. While it is indeed true that  $L_{\text{bound}}$ 's proportion is inflated relative to other types in the hypothesis space, it is never the second most prolific type (which is what the above hopefully is not taken to suggest, otherwise it should be changed). As is to be expected,  $L_{\text{bound}}$  fares best when  $l$  is low and  $\lambda$  is high. Even then, it usually ranks around 5-th with a mean proportion of its kind of about 0.01 – 0.05. As  $l$  increases, it gets pushed back. Second or third place are usually instead literal  $L_{\text{lack}}$  or types that lexicalize “all”, “not all” and “none”. In short; yes, there is a inflated proportion but only compared to the whole population. Other particular types are usually more prolific. This is very likely due to the strong prior disadvantage of  $L_{\text{lack}}$ . In light of this I'm uncertain whether we want to keep this paragraph as is. I tend towards 'yes' but let me know if you think otherwise.]

Another important issue that is not addressed in the model are potential costs associated with pragmatic reasoning. Here, we simply assumed that literal and pragmatic reasoning strategies exist from the start and are equally costly to apply. In contrast, empirical results suggest that the computation of a scalar implicature may involve additional cognitive effort (e.g. Breheny et al. 2006, Neys and Schaeken 2007, Huang and Snedeker 2009, Tomlinson Jr. et al. 2013). Extensions of the model presented here to include processing costs for pragmatic language use would be interesting future work. It seems plausible that effects of reasoning cost may trade off with the frequency with which a given scalar expression is used. It may be that frequently

drawn scalar implicatures lexicalize to avoid cost, whereas infrequent ones are derived on-line to avoid more complex lexical concepts during acquisition. Such a prediction would lend itself to empirical testing in line with a recent interest in differences between various scalar implicature triggers (van Tiel et al. 2016).

Our case study could be criticized as follows: all it shows is that scalar implicatures do not lexicalize because upper bounds are dispreferred concepts. This criticism would be too superficial and highly unjust. Dispreferred lexical concepts can thrive under evolutionary selection. Lexicalized upper-bounds can dominate a population because they may boost communicative efficiency. But they do not have to. Moreover, even without selective pressure for communicative efficiency, it is not the case that necessarily the types that are most likely *a priori* will dominate. The dynamics of iterated learning are not that trivial. Iterated learning does not necessarily promote the *a priori* more likely type, but tends to promote a type  $t$  based on a gradient of how many other types might likely mutate into  $t$ , so to speak. Taken together, without an explicit model of the interaction between pressure for efficiency and learnability, it is far from trivial to judge whether or when preferred or dispreferred concepts can be adaptive. This is why a major contribution of this paper is the arrangement of many different ingredients into a joined model of the co-evolution of lexical meaning and pragmatic use.

What is more, it is not that we just assumed a prior disadvantage of lexicalized upper bounds. We tried to motivate and formalize a general assumption about concepts' complexity with a concrete, albeit provisional proposal. The specification of a learning bias in terms of a "grammar of concepts" can and should be seen critically, however. Much depends on the primitives of such a grammar. For instance, the concept "none or all" is the most complex in Table 2. But consider adding a primitive operation on sets  $A \smile B$  which is true if and only if  $\neg(A \cap B \neq \emptyset \wedge A \neq \emptyset)$ . The concept "none or all" would then be one of the simplest. Clearly, further research, empirical and conceptual, into the role of representational complexity, processing costs and learning biases is needed. The model here makes a clear and important contribution nonetheless: it shows how simplicity of concepts can interact with use and evolutionary selection to show that without pragmatic language users we would not see simpler concepts emerge in what may be a natural way. Future work should also include the possibility that conceptual simplicity may itself be a notion that is subject to evolutionary pressure (cf. Thompson et al. 2016).

Finally, our case study should not be interpreted as a proposal for a definite explanation of how scalar implicatures evolved. Other factors should be considered eventually even if they will lead to much more complex modeling. One such factor is the observation that non-lexicalized upper bounds allow a broader range of applicability, e.g., when the speaker is not certain as to whether *all* is true. This may suggest an alternative argument for why upper-bounded meanings do not conventionalize based on functional criteria only: should contextual cues provide enough

information to the hearer to identify whether a bound is intended to be conveyed pragmatically, then this is preferred over expressing it overtly through longer expressions, e.g., by saying *some but not all* explicitly. Importantly, although morphosyntactic disambiguation may be dispreferred due to its relative length and complexity (Piantadosi et al. 2012), it allows speakers to enforce an upper-bound and override contextual cues that might otherwise mislead the hearer. In a nutshell, this explanation posits that scalar implicatures fail to lexicalize because, all else being equal, speakers prefer to communicate as economically as possible and pragmatic reasoning enables them to do so. What this alternative explanation does not explain is why functional pressure does not lead to the emergence of different, equally costly lexical items to express different knowledge states of the speaker. Looking at pressure from learnability might come in again. The present work made a first start and gave a framework for exploring exactly these issues systematically.

## 5 Conclusion

The cultural evolution of meaning is influenced by intertwined pressures. We set out to investigate this process by putting forward a model that combines a pressure toward successful information transfer with perturbations that may arise in the transmission of linguistic knowledge in acquisition. Its objects of selection and replication are pairs of lexical meanings and patterns of language use. This allows the model to trace the interaction between conventional meaning and pragmatic use. Additionally, it takes the challenge serious of neither semantics nor pragmatics being directly observable. Instead, learners need to infer these unobservables from overt data that results from their combination. These components and their mutual influence were highlighted in a case study on the lack of lexical upper-bounds in weak scalar expressions that showed that, when pressured for learnability and communicative success, the former force drives for simpler semantic representations inasmuch as pragmatics can compensate for lack of expressivity in use. That is, the relative learning advantage of simpler semantics in combination with functional pressure in use may offer an answer to why natural languages fail to lexicalize systematic pragmatic inferences. And, more broadly, to a division of labor between semantics and pragmatics.

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## A notes

- [MF: The text frequently uses the term “expressivity” and “pressure for/towards expressivity”. I have mixed feelings about this. First of all, I don’t know what “expressivity” really is. It seems to relate to a lexicon: how much information can the lexicon convey about the states. But we do not model selection of expressivity, but selection of communicative success relative to the population state. The difference is very pronounced: there can be several maximally expressive lexica with huge differences in their communicative success or expected utility for a given population state. We only indirectly select for expressivity, and we don’t necessarily select for expressivity of a lexicon. ...It may be that “expressivity” is very much Edinburgh terminology where exactly the picture of communication success in the current population is missing. I might be wrong though. Possibly, we should introduce this distinction (with this terminology) and use it also in the general discussion to relate our work to those articles from the iterated-learning community that bring in some pressure for “expressivity” but not communicative efficiency (if that is what they do, I don’t know?).]