

Learning biases may prevent lexicalization of pragmatic inferences

A case study combining iterated (Bayesian) learning and functional selection

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Main methodological contribution

- interaction of: (replicator mutator dynamics)
 - fitness-relative replication (replicator dynamics)
 - iterated learning (mutator dynamics)
- learners perform joint-inference:
 - type of pragmatic behavior
RSA-style probabilistic types (Frank & Goodman 2012)
 - lexical meaning
LOT-style learning biases (Piantadosi et al. under review)

Case study on scalar implicatures

- model shows prevalence of:
 - Gricean pragmatic use
 - non-lexicalized upper-bounds

· M. C. Frank and N. D. Goodman. **Predicting pragmatic reasoning in language games.**
Science, 336(6084):998–998, 2012

· Steven T. Piantadosi, Joshua B. Tenenbaum, and Noah D. Goodman. **Modeling the acquisition of quantifier semantics: a case study in function word learnability, under review**

The semantics-pragmatics distinction

Semantics

Literal meaning (truth-conditional)

Pragmatics

Information beyond literal meaning (e.g. defeasible inferences)

Scalar inferences

(1) $\langle \text{some}, \text{many}, \text{most}, \text{all} \rangle$

a. All students came to class

→ **Some** students came to class

b. Some students came to class

\rightsquigarrow **Not all** students came to class

(2) $\langle \text{may}, \text{should}, \text{must} \rangle$

(3) $\langle \text{one}, \text{two}, \text{three}, \dots \rangle$

(4) $\langle \text{or}, \text{and} \rangle$

(5) ...

The use of a less informative expression when a more informative one could have been used* can license a defeasible inference that stronger alternatives do not hold

*The hearer assumes the speaker to be knowledgeable and cooperative

· Laurence R. Horn. *On the Semantic Properties of Logical Operators in English*.

Indiana University Linguistics Club, Bloomington, IN, 1972

· Gerald Gazdar. *Pragmatics, Implicature, Presupposition and Logical Form*.

Academic Press, New York, 1979

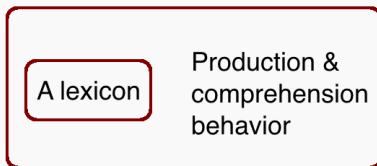
· Paul Grice. *Logic and conversation*.

In *Studies in the Ways of Words*, chapter 2, pages 22–40. Harvard University Press, Cambridge, MA, 1975

1. Why are (pragmatically inferred) upper-bounds of weak(er) alternatives not part of semantics?
2. What justifies semantic structure in light of pragmatic enrichment?

Model

Components I: Probabilistic (pragmatic) language users



A player's type

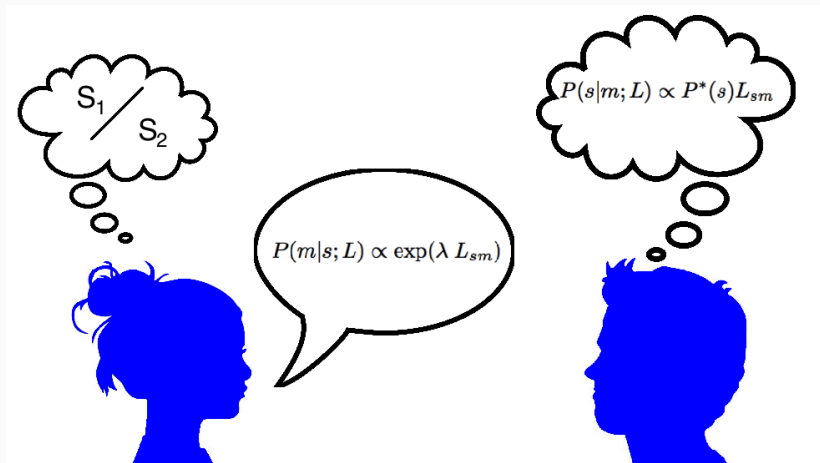
- Anton Benz, Gerhard Jäger, Robert Van Rooij, and Robert Van Rooij, editors. *Game theory and pragmatics*. Springer, 2005
- Leon Bergen, Roger Levy, and Noah D Goodman. *Pragmatic reasoning through semantic inference*. *Semantics and Pragmatics*, 2016
- M. C. Frank and N. D. Goodman. *Predicting pragmatic reasoning in language games*. *Science*, 336(6084):998–998, 2012
- Michael Franke and Gerhard Jäger. *Pragmatic back-and-forth reasoning*. *Semantics, Pragmatics and the Case of Scalar Implicatures.*, pages 170–200, 2014

- s_1 : Bill read some but not all books
- s_2 : Bill read all books

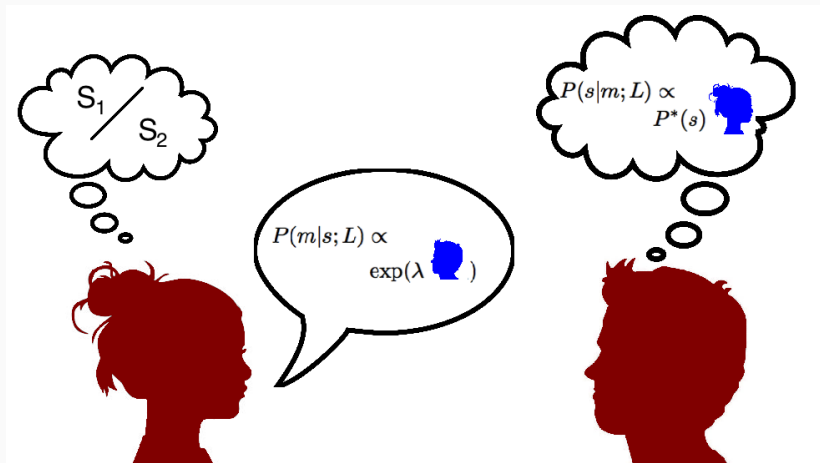
$$L_{\text{lack}} = \begin{array}{cc} & m_{\text{all}} & m_{\text{some}} \\ \begin{array}{c} s_1 \\ s_2 \end{array} & \left(\begin{array}{cc} 0 & 1 \\ 1 & 1 \end{array} \right) \end{array}$$

$$L_{\text{bound}} = \begin{array}{cc} & m_{\text{all}} & m_{\text{some}} \\ \begin{array}{c} s_1 \\ s_2 \end{array} & \left(\begin{array}{cc} 0 & 1 \\ 1 & 0 \end{array} \right) \end{array}$$

Literal behavior



Pragmatic behavior



Components II: Cultural transmission

Two competing pressures:

1. Communicative efficiency

... as replicator dynamics; \dot{x}

2. Learnability

... iterated Bayesian learning
as mutator dynamics; Q

Replicator-mutator dynamics

$$\hat{x} = \dot{x} \cdot Q$$

· Thomas L. Griffiths and Michael L. Kalish. **Language evolution by iterated learning with bayesian agents.** *Cognitive Science*, 31(3):441–480, 2007

· M. A. Nowak and D. C. Krakauer. **The evolution of language.** *Proceedings of the National Academy of Sciences*, 96(14):8028–8033, 1999

Functional pressure (replicator dynamics); $\dot{x}_i = \frac{x_i f_i}{\Phi}$

- Population of types x

x_i is the proportion of t_i in x

- Fitness of type i

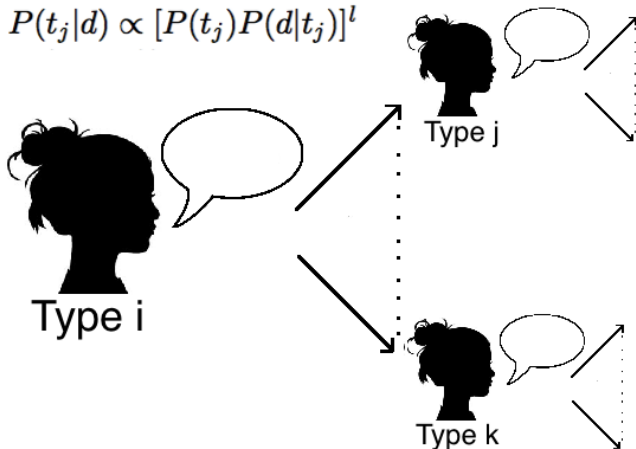
$$f_i = \sum_j x_j U(x_i, x_j)$$

- Average fitness in the population

$$\Phi = \sum_i x_i f_i$$

Iterated learning (mutator dynamics)

$$Q_{ij} \propto \sum_d P(d|t_i) P(t_j|d)$$
$$P(t_j|d) \propto [P(t_j)P(d|t_j)]^l$$



Analysis

Lexica, signaling behavior & types

Lexica subset

$$L_{\text{tautology}} = \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} \quad L_{\text{bound}} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \quad L_{\text{lack}} = \begin{pmatrix} 0 & 1 \\ 1 & 1 \end{pmatrix}$$

Signaling behavior

Literal or *pragmatic*

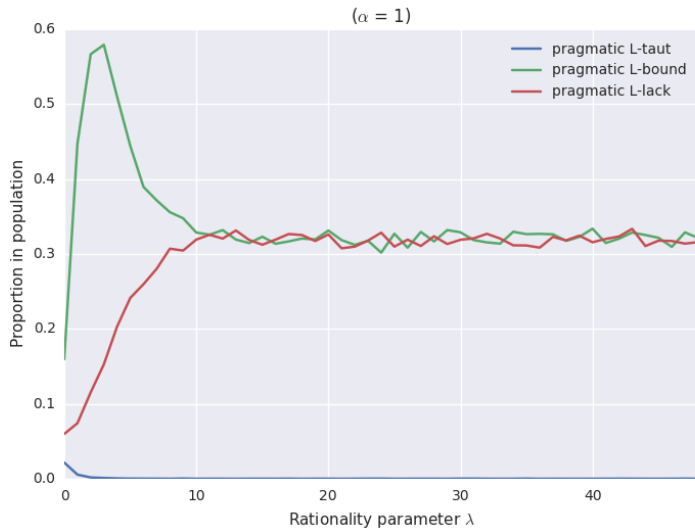
Types

12 types (2 behaviors \times 6 lexica)

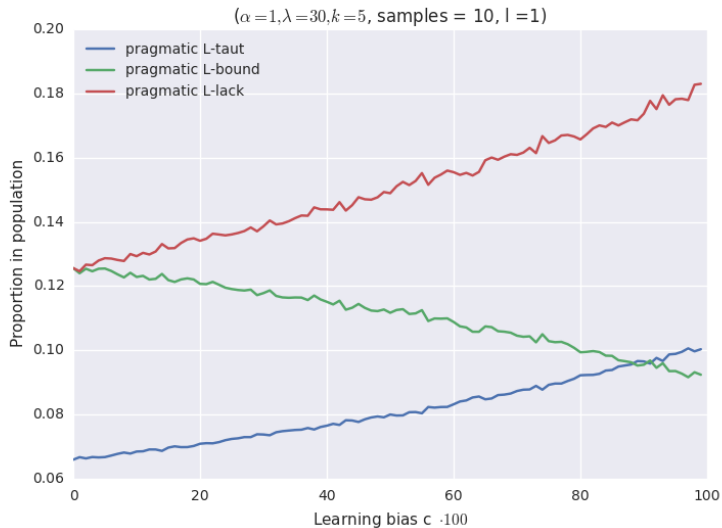
What factors lead to the selection of L_{lack} -like semantics?

parameter	explanation	locus
$c \in [0, 1]$	learning bias for upper-bound lack	$P(t_i)$
$l \geq 1$	sampling to MAP	$[P(t_i)P(d t_i)]^l$
$\lambda \geq 1$	rationality parameter	$\exp(\lambda R_{n-1}(s m; L))$
$k = d $	datum length	$P(d t_j)P(t_i d)$
$ D $	data produced per parent type	$P(d t_j)P(t_i d)$

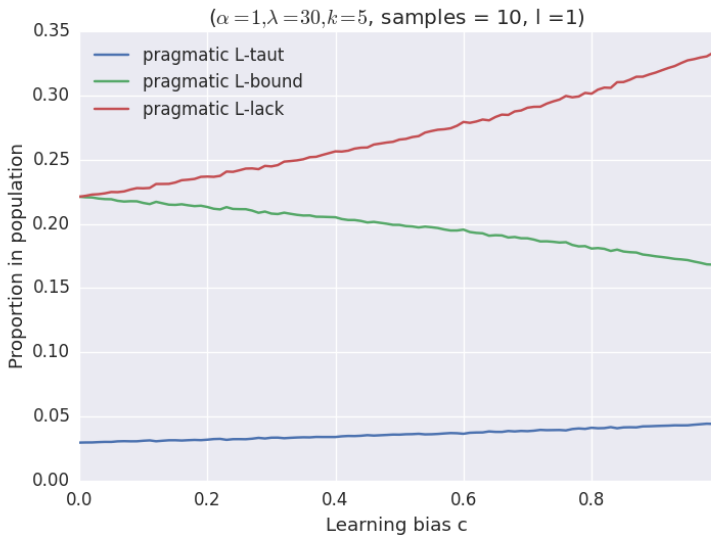
Expressivity only



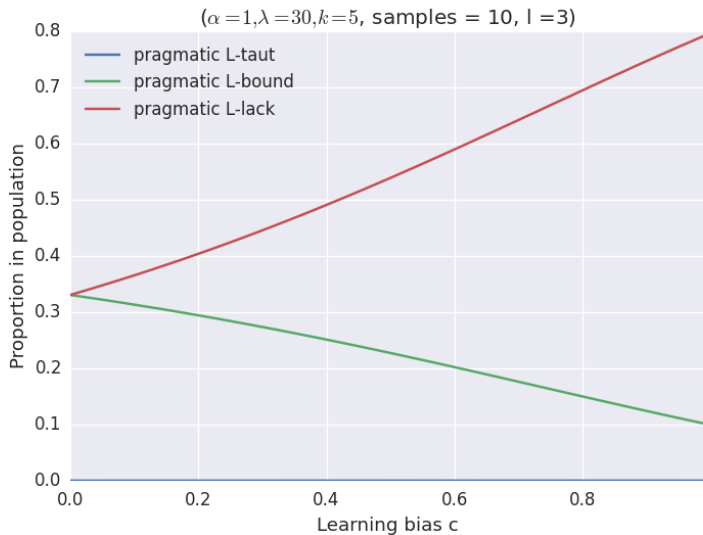
Learnability only



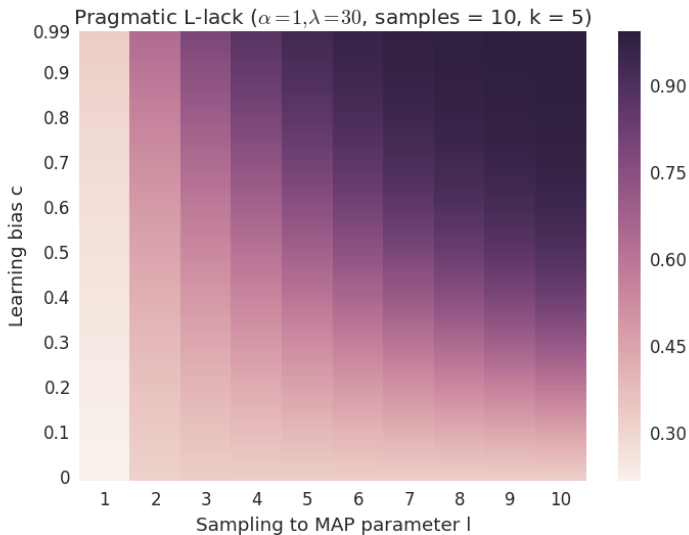
Expressivity and learnability



Effect of prior with higher posterior maximization



Prior and posterior



Concluding remarks: Application

- Learnability steers language towards simpler semantics
 - Pragmatics compensates for potential loss in expressivity
- } Lack of semantic upper-bounds

Provided

- Some degree of rationality in learning & choice

Selection, learning, pragmatic use & lexical meaning

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References I

- [BJVRVR05] Anton Benz, Gerhard Jäger, Robert Van Rooij, and Robert Van Rooij, editors.
Game theory and pragmatics.
Springer, 2005.
- [BLG16] Leon Bergen, Roger Levy, and Noah D Goodman.
Pragmatic reasoning through semantic inference.
Semantics and Pragmatics, 2016.
- [FG12] M. C. Frank and N. D. Goodman.
Predicting pragmatic reasoning in language games.
Science, 336(6084):998–998, 2012.
- [FJ14] Michael Franke and Gerhard Jäger.
Pragmatic back-and-forth reasoning.
Semantics, Pragmatics and the Case of Scalar Implicatures., pages 170–200, 2014.
- [Gaz79] Gerald Gazdar.
Pragmatics, Implicature, Presupposition and Logical Form.
Academic Press, New York, 1979.
- [GK07] Thomas L. Griffiths and Michael L. Kalish.
Language evolution by iterated learning with bayesian agents.
Cognitive Science, 31(3):441–480, 2007.
- [Gri75] Paul Grice.
Logic and conversation.
In *Studies in the Ways of Words*, chapter 2, pages 22–40. Harvard University Press, Cambridge, MA, 1975.

References II

- [Hor72] Laurence R. Horn.
On the Semantic Properties of Logical Operators in English.
Indiana University Linguistics Club, Bloomington, IN, 1972.
- [HS03] Josef Hofbauer and Karl Sigmund.
Evolutionary game dynamics.
Bulletin of the American Mathematical Society, 40(04):479–520, 2003.
- [NK99] M. A. Nowak and D. C. Krakauer.
The evolution of language.
Proceedings of the National Academy of Sciences, 96(14):8028–8033, 1999.
- [PTGew] Steven T. Piantadosi, Joshua B. Tenenbaum, and Noah D. Goodman.
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