

ANALYSIS OF THE STOCK MARKET USING COMPLEX NETWORKS AND MACHINE LEARNING

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Abstract

**ANALYSIS OF THE STOCK MARKET
USING COMPLEX NETWORKS
AND MACHINE LEARNING**

Lingjie Zhang

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Due to the complexity of financial market and the interconnectedness and interdependencies of industry sectors in the economy, the price returns of each coupling stocks might have certain underlying economic link. Such behaviours can hardly be explained by traditional financial models and theories. This thesis study on the construction and topological properties of US stock market with complex network theory. In order to determine the directions of edges in the stock network, we first used the machine learning technique to predict the Granger causalities of the price return series between all stock pairs while concluded with unsuccessful results. In addition, another method of using economical transactions of Economic Input-Output (EIO) from Bureau of Economic Analysis (BEA) is proposed. The constructed directed-unweighted stock network is partitioned in communities and compared with Erdős–Rényi (ER) random network and Watts-Strogatz (WS) small-world network with the same number of nodes and edges and the constructed directed-weighted stock network is compared with undirected-weighted stock network which is constructed by the method of correlation coefficient of stock price return series as previous researches conducted. Further, through analysing the topological properties including out-degree and out-strength distribution, efficiencies, betweenness centrality and clustering coefficient of both of the

directed stock networks, we find that the main topological properties such as small-world feature and power-law distribution of degrees are still exist as the conventional undirected stock networks follow. Suggestions towards financial market investment are provided based on the results of the study.

Declaration

No portion of the work referred to in this dissertation has been submitted in support of an application for another degree or qualification of this or any other university or other institute of learning.

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Contents

Chapter 1

Introduction

1.1 Motivation

Financial markets are complex systems, the interconnectedness and interdependencies of industrial sectors in the economy are highly inter-coupled with strong correlations with stock price fluctuations, i.e., the price returns of each coupling stocks underlying certain economic link, e.g. two companies that manufacture similar products, or both in one supply chain. Such behaviours can hardly be explained by traditional financial models and theories.

During recent times, weighted but undirected complex network models have been applied to study the correlations of stock prices. Prevailing approach is to use companies as nodes, and correlations between each pair of stock price time series, return time series, or fluctuation patterns as links. As a result, much of the previous researches have proved the represented complex networks of worldwide stock markets are scale-free and small-world [LLH07, CLL10]. However in theory, directed complex networks for the stock market can be achieved hence more potential information can be produced which is helpful for investment decisions and financial market supervisions.

For building an investment portfolio of stocks, one should consider not only about the irrelevancy on price or price return time series, but also about the irrelevancy on economical activities between firms and industries. Naturally and instinctively, we can depict the interactions of economical activities between stock-pairs as the directions of edges in the stock complex network, and the weights of the edges are still determined by the correlations of stock price return time series as many previous researches practised. Therefore, some guidance may be offered for investors to build more effective portfolio and market supervisors to avoid potential crisis according to the study of

directed stock complex network.

The goal of this thesis is to reveal the interactions of economical activities between companies and utilise them into the topological analysis and visualisation of constructed directed complex networks as so far no previous work has attempted to construct a directed network about stock markets. In addition, suggestions for stock market are provided according to the results and findings.

In addition to this approach, there was a goal of using machine learning techniques to predict the directions of stock complex network. However, these results were not as successful and conclusive as we expected. They are reported in the last chapter of this thesis as additional work complementing the core analysis of this thesis based on complex network theory.

1.2 Objectives and deliverables

The goal of this thesis is to construct a directed complex network using economical industrial transaction data and stock price data to depict the US stock market by means of topological properties analysis, community detection and visualisation. Same-sized directed Watt-Strogatz small-world network and random networks are generated for the purpose of comparison. This thesis will explore whether the conclusions are consistent with the undirected complex network researches.

Objectives produced:

- To normalise the Economic Input-Output (EIO) tables into matrices for setting thresholds.
- To generate a matrix of correlation coefficients for all stock-pairs.
- To set appropriate thresholds of correlation coefficient and normalised economical transactions.
- To construct directed-unweighted and directed-weighted stock price return networks.
- To study the topological properties of directed stock price return networks.
- To detect communities in the directed stock price return networks.

- To visualise the directed stock price return networks.
- To study the relationships between price return and betweenness centrality.
- To analyse the theoretical and practical contributions of findings.

Deliverables produced:

- Stock counts by industries.
- Matrix of EIO transaction flows.
- Heatmap of combinations of thresholds of directed demands and directed requirements flows and correlation coefficients.
- Two benchmarking networks: directed Watts-Strogatz (WS) small-world network and directed Erdős–Rényi (ER) random network.
- Directed-unweighted and directed-weighted stock network.
- Topological properties of studied networks.
- Community partition of directed-unweighted stock network.
- Bivariate distribution graphs about betweenness centrality and price return statistics.
- We plan to produce a research thesis to submit to a journal. We are thinking of journals like: *Physica A, Journal of Mathematical Finance, Journal of Applied Mathematical Finance, Applied Network Science*.

1.3 Proposed methodology

In this thesis we proposed a method to generate directed-unweighted complex network and directed-weighted complex network for stock market, especially for the US stock market in the year of 2016. Analysis of topological properties and comparison with benchmarking networks provide unique insights towards its continuity or uncontinuity features to conventional undirected stock networks in previous researches and its compositional structure.

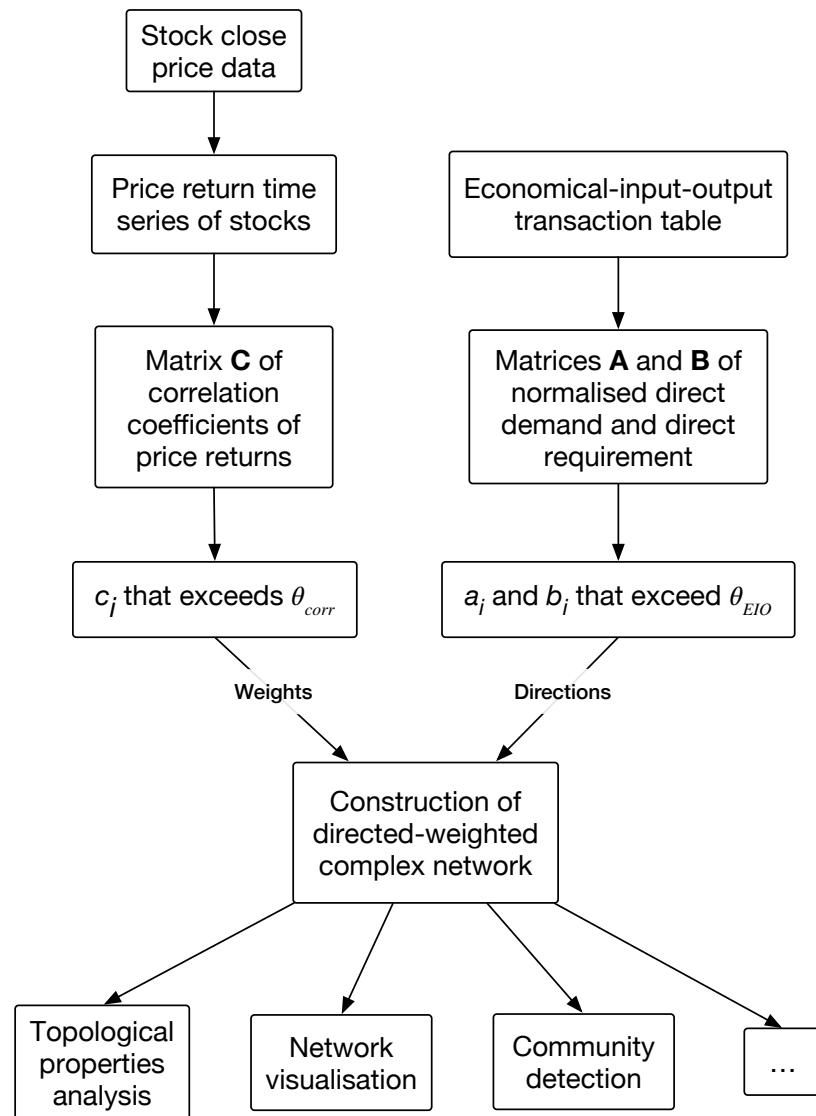


Figure 1.1: The methodology

1.4 Summary of results

While working on this thesis, the following achievements have been made that will be described in detail in this thesis:

- To calculate topological property values to study the properties of stock complex networks.
- To compare the directed-unweighted stock complex network with generated directed WS small-world network and directed ER random network.
- To apply community detection algorithm to find possible communities of the directed-unweighted stock complex network.
- To generate bivariate distributions between betweenness centralities and functions of stock daily return to find the potential relationships between them.

1.5 Outline of the thesis

The rest of this thesis is organised as follows. Chapter 2 discusses the development of quantified financial analysis for stock markets and the application of complex theories of complex networks towards stock markets. The subsequent chapters of methodologies introduce the critical analytical methods implemented in the research by this thesis. Detailed outcomes are then illustrated in chapter 7. Other results about the method of using machine learning techniques to help construct directed stock networks are presented in chapter 8. Finally, the findings and conclusions are discussed in chapter 9.

Chapter 2

Background and state of the art

2.1 Introduction

This chapter will introduce the development and literature review of quantitative finance, stock market investment, and the application of complex networks theory to the financial markets, especially to the stock markets.

2.2 Background

2.2.1 Historical review of quantitative finance and stock market investment

Quantitative finance combines mathematics, statistics, econometrics, machine learning and empirical finance to provide a solid analytical foundation for the analysis of financial issues, especially for the investments in financial markets such as stock, future, option and forex. The development of quantitative finance is the history of scholars trying to reveal the essential of the financial markets from rational behaviours to irrational, from organised to chaos, and from simple to complex. Until present day, the theoretical foundations of quantitative finance include efficient market theory, behavioural finance, asset allocation theory and chaos theory.

The revolutionary who pioneered the theory of asset allocation, Markowitz [Mar52] proposed the idea of efficient frontier and the mean-variance model, which established a clear mathematical definition of the two previously vague concepts of risk and return. Markowitz [Mar56] then presents the properties and formulas for efficient frontier and generalised it by allowing an arbitrary, possibly singular, covariance matrix [Mar59].

Tobin [Tob58] developed Markowitz's theory and added the concept of risk free assets. Sharp [Sha64] and Linter [Lin65] added two key assumptions based on the mean-variance model to enable the portfolio mean-variance valid, forming a capital asset pricing model (CAPM) with the support of economic theories. The CAPM believes that only non-dispersible systemic risks can be compensated off, while non-systematic risks can be eliminated by effectively decentralised investments. Investors could only assume systemic risks through decentralised investment. The systematic risk of a single security or portfolio can be characterised by beta, which represents the extent to which a single security or portfolio is affected by the overall market volatility. And later, Richard Michaud and Robert Michaud [MM98] addressed the information uncertainty in risk-return estimates by the invention of the Re-sampled Efficient portfolio.

Since the invention of the CAPM, worldwide scholars had been actively conducting empirical tests towards the practicality of the CAPM, while early results show that *beta* is able to explain the return movements of stock prices. However, in the late 1970s, some empirical studies on the CAPM began to show that a large part of the changes in the stock returns cannot be explained by *beta*, as anomalies about market return were increasingly found.

Researchers had proposed models and theories considering the individual stock features to explain such anomalies. For instance, Fama and French [Mer73, CR76] proposed a three-factor model based on the inter-temporal capital asset model (ICAPM) proposed by Merton [FF93] and the arbitrage pricing theory (APT) proposed by Cox et al. [FF96], which reveals a large part of the cross-section of the average return of stocks that cannot be explained by CAPM, can be explained using firm size, book-to-market equity ratio, and overall market return as regression factors.

Above asset allocation models based on expected return and risk mainly implement the analytical tools of statistics, time series analysis and financial econometrics. The underlying economic ideas were all derived from the rationality of investors. As such methods revolutionised the research of finance, huge lacunae were left striking by the asset allocation theory. For instance, the traditional models are limited in terms of volume. Further, individual investors still hold significantly few stocks in investment portfolios although the importance of diversification are emphasised by these theories. Lastly, expected returns do not seem to vary in the cross-section only due to the risk differentials across stocks.

As Subrahmanyam [Sub08] puts forward, traditional finance theories like asset allocation is limited in explaining issues including (1) the reasons of trading for individuals, (2) the performance of traders, (3) the ways for investors choosing portfolios, and (4) the reasons of returns varying across stocks other than risk. Hence, scholars began to explain financial market with psychology and behavioural economics.

Some typical studies on behavioural finance are related to overconfidence, self-attribution, loss aversion, and short-sale constraints. Daniel et al. [DHS98, DHS01], Barberis et al. [BSV98], and Hong and Stein [HS99] explain patterns using overconfidence and self-attribution. Overconfidence about private signals causes overreaction and therefore phenomena such as the book/market effect and long-run reversals., while self-attribution maintains overconfidence and allows prices to continue to overreact, creating momentum.

Loss aversion refers to tendency to prefer avoiding losses to acquiring equivalent gains for investors. In terms of modelling such behavioural biases, Barberis et al. [BHS01] and Barberis and Huang [BH01] attempt to incorporate the phenomenon of loss aversion into utility functions. Grinblatt and Han [GH05] argue that loss aversion can also help explain momentum. Scheinkman and Xiong [SX03] analyse the interaction of overconfidence and short-sale constraints. They show that agents with positive information may be tempted to buy overvalued assets because they believe they can sell that asset to agents with even more extreme beliefs.

From the studies about behavioural finance, it is clear that financial markets are complex systems which cannot be analysed with traditional statistical models such as linear regression. Therefore comparing with the method of psychology or behavioural economy, chaos can be another approach that interpret the "abnormal behaviour" of financial markets in a mathematical way.

The chaos theory for decades was one of the hottest research field in science, while it is rarely applied into finance, timid attempts are made to elucidate the possibilities and outline the limits of its application in finance [Sew08]. Klioutchnikov et al. [KSB17] expect that chaos theory is competitive and may well become a "convenient" theory of the financial market, because traditional finance does not take into account dynamics, while chaos theory is built on the dynamics of the system, which allows the theory to be brought closer to reality. Mandelbrot [MH04] studies the chaos of stock markets and finds that (1) the changes of stock prices do not strictly follow a normal or Gaussian distribution (2) stock prices show significant autocorrelation, which is

incompatible with efficient market theory (3) numerous random factors obscure historical facts. Therefore, the prediction of stock prices is conducted by fractal behaviour to which markets exhibit, and the fractal analysis results show difference from traditional methods. Other methods to predict stock prices based on the considerations of the resumption and wave propagation of events are conducted by Mandelbrot [Man83].

In the last two decades, the notion of complex networks as part of the complexity studies is actively and intensively investigated in the wide field of networks including financial networks. Therefore, next section will focus on complex networks theory and its applications on financial markets.

2.2.2 Theory of complex networks

A network is defined by a collection of nodes and edges between pairs of nodes. Nodes in large scale brain networks usually represent brain regions [RS10], while edges represent anatomical, functional, or effective connections, depending on the dataset.

Complex networks are the networks that have some or all of the properties from self-organisation, self-similarity, attractors, small-world and scale-free. A large number of complex systems that exist in nature or society can be described by a variety of networks. Since complex networks are the topological basis for the existence of a large number of complex systems, the research on complex networks is believed to help understand the critical problem of "why complex systems are complex".

A typical network consists of a number of nodes and edges which connect these nodes, where nodes are used to represent different individuals in the real system and edges are used to represent the relationships between individuals. In certain cases, a particular relationship is described as an edge between two nodes, otherwise, it is not connected. Two nodes with edge are considered as adjacent among the network.

For instance, the nervous system can be regarded as a network formed by a large number of nerve cells interconnected by nerve fibres [WS98]. The computer networks can be regarded as a network in which autonomously working computers are connected to each other through communication media such as optical cables, twisted pairs, coaxial cables, etc [WS98]. In addition, there are more complex networks like electric power networks [FFF99], social networks [WS98, HSW17, EMB02], etc.

The research of complex networks involves the knowledge and theoretical basis of many disciplines due to its cross-disciplinary and complex characteristics, especially for system science, statistical physics, mathematics, computer and information science. Commonly used analytical methods and tools for complex networks research include

graph theory, combinatorial mathematics, matrix theory, probability theory, stochastic process, optimisation theory and genetic algorithms. The main research methods for complex networks are based on the theories and methods of graph theory. However, in recent years, many concepts and methods of statistical physics have been successfully applied in the modelling and calculating of complex networks, such as statistical mechanics, self-organisation theory, critical and phase transition theory, seepage theory, etc. [AB02], such as the concept of network structure entropy, and its application of quantitative measure of the "order" of complex networks. The models of complex networks are widely used in numerous scientific areas.

It is acknowledged that most practical networks illustrate a structure of community [VKR03, New03], which refers to groups of nodes that have high inter-density of edges and low intra-density of edges among groups. It is a matter of common experience that stock market do divide into groups along lines of industry, stock price, revenue, P/E and so forth, and the phenomenon of assortativity discussed in chapter 7 certainly suggests that this might be the case.

Below are some frequently used topological properties and statistical features of complex networks:

- Average path length
- Clustering coefficient
- Degree (strength) and degree (strength) distribution
- Centrality
- Small-world
- Scale-free

Below are some common complex networks models:

- Regular network
- Random network
- Small-world network

- Scale-free network
- Self-similar network

The details of major topology and community features of complex networks will be presented in chapter 4 and the introduction of small-world and random networks will be presented in chapter 5.

2.2.3 Complex networks theory applied in Finance

While traditional stock pricing models still capture limited forms of financial behaviour, according to Johnson et al. [JJH⁺03], the premises of standard financial theory contradict the modern notion of financial markets are complex systems, by which many statistical niceties such as stationarity no longer can be taken for granted. Nevertheless, attempts to assess the prospects of the financial market from the perspective of complex networks theory expand the borders of its application and stimulate the development of new tools and methods of mathematical analysis.

Since the property of small-world and scale-free are respectively revealed by the research upon complex networks by Watts [WS98] and Barabási [BA99], the application of complex networks has been greatly promoted to each field including finance. Therefore, recent researches have implemented the complex networks theory to reveal the underlying factors of price movements in financial markets. Huang et al. [HZY09] implemented the threshold method to construct correlation network in A-Share stock market in China and studied the topological properties and topological stability of the stock correlation networks. Their statistical analysis of the degree distribution has revealed the power-law property of financial networks, and the networks display a topological robustness against random node failures, while they are also fragile under intentional attacks. Tabak et al. [TSC10] construct and investigate the stock market networks in Brazil with the minimum spanning tree which is based on the concept of ultrametricity, and implement the correlation matrix for a variety of stocks of distinctive industrial sectors. As a result, they find that stocks tend to cluster by sector. Kauê Dal'Maso Peron et al. [KDPdFCR12] also use the method of stock correlation matrices to analyse the topological properties and dynamic evolution of stock networks in New York Stock Exchange. Additionally they adopt the entropy-related measurement to quantify the robustness of the evolving financial market organisation. As a result, they verify the network topological organisation suffers strong variation during financial instabilities and the networks in such periods become less robust. Namaki et

al. [NSRJ11] utilised Random Matrix Theory (RMT) to specify the biggest eigenvector in the complex networks of price correlations, which reveals that the Tehran Stock Exchange correlation network is scale-free in a specific time interval. Li and Wang [LW07] construct a weighted network of Hang Seng index (HSI) from coarse-graining preprocess of HSI in Hong Kong stock market, where the nodes stand for patterns of HSI fluctuations and the edges represent the paths between nodes and weights of edges. They discover the some nodes have the highest betweenness centrality and are statistically changeless whether HSI fluctuations. Yu [Lon13] studied the evolution of gold price from a network perspective using the visibility network approach and shows that the series of gold price and gold price return are long-term correlated, fractal series with a power-law degree distribution of visibility graph network. Jiang and Zhou [JZ10] construct stock trading networks based on the order flow data of a stock with high-liquidity listed on Shenzhen Stock Exchange in China during a whole year, and find that the trading networks have power-law degree distributions and disassortative architectures. Chopra and Khanna [CK15] developed a framework which associates the economic input–output model with techniques for understanding interdependences and interconnectedness in the economy of US, based on complex networks theory. Its topological analysis for two networks suggests that the unweighted network exhibits small world properties, and the weighted network follows a power-law with an exponential cut-off. Boginski et al. [BBP05] identified cliques and independent groups among stock networks, which invents a new alternative data mining method to the classification of stocks. Chen et al. [CLSW15] studied the inter-stock and inter-industry effects towards stock returns based on APT and the topological properties of a complex network of correlations. They have found that the average centrality of the top 100 stocks tracks the GDP growth rate of China, hence, the degrees of connection between stocks in the stock market reflect the development of the real economy to some extent. Another finding is that stocks with smaller market capitalisation tend to be located in more central positions in networks. Brida [Bri02] proposed the approach by using symbolic-network model based on coarse graining and symbolisation for calculating the distance of stocks, which is illustrated to be effective to transform stock price time series into complex networks as well, and it does provide an advantageous attempt for analysing time series from the network perspective.

2.3 Summary

In this chapter a brief literature review and discussion about quantitative finance, stock market investment and applied complex networks theory have been presented. It can be seen that because of the less regulated price float and tremendously available data, the study of financial market complexity is mainly concentrated on stock data. However, it can also be seen that prevailing complex network approaches to analyse stock markets are almost all about investigating weighted or unweight but undirected networks. To our best knowledge, there is no previous work has attempted to construct a directed network so far.

Chapter 3

Pre-processing of stock market and industrial data

3.1 Introduction

This chapter will introduce the sources of economy data and stock data and the methods to pre-process these data in order to transform and normalise raw data for the further visualisation, construction of networks and topological analysis.

3.2 Data source

This thesis considers 1,418 stocks of listing US companies that were traded consecutively in the NYSE and NASDAQ stock market of US on the trading days from January 4, 2016 to December 30, 2016 and uses daily closing price during this period and the economical use table data from the Industry Economic Accounts (IEAs) of year 2016 in a summary-level of industrial sectors are collected from the official website of Bureau of Economic Analysis, US Department of Commerce [oEA18].

3.3 Economic Input-Output table

The Bureau of Economic Analysis (BEA) in the US publishes Economic Input-Output (EIO) tables each year, which are the transaction matrices of all purchases and sales between sectors in a certain industry group level of a year, i.e. depict how industries provide input to, and use output from, each other to produce Gross Domestic Product

(GDP).

This thesis uses the use table of 2016. Among the transaction matrix \mathbf{Z} there are Total Industry Input row \mathbf{I} at the bottom and the Total Industry Output column \mathbf{O} at the right are the statistics of total purchase by each sectors and total sales from each sectors respectively. The elements of the normalised direct demand matrix \mathbf{A} and the direct requirement matrix \mathbf{B} are:

$$a_{i,j} = -\log_{10} \frac{z_{i,j}}{I_j N_j}^{-1} \quad (3.1)$$

and

$$b_{i,j} = -\log_{10} \frac{z_{i,j}}{O_i N_i}^{-1} \quad (3.2)$$

respectively. N_i is the number of stocks in the industrial sector which stock i belongs to. Moreover, certain threshold values θ_{DD} and θ_{DR} are specified and a directed edge can be added between stock i and stock j if the value of $a_{i,j}$ is greater than θ_{DD} or the value of $b_{i,j}$ is greater than θ_{DR} .

3.4 Logarithmic return of stock prices

Logarithmic return of a stock in this thesis is calculated as the log of the close price of one day divided by the close price of the previous day, which is obtained from the following formula:

$$r_i(\tau) = \ln P_i(\tau) - \ln P_i(\tau - \Delta t) \quad (3.3)$$

As a proxy for the percentage change in the price, logarithmic return is symmetric and has mathematical conveniences for adding up or subtracting values on the log scale, which are useful for mathematical finance. Therefore, logarithmic return is the measure of price changes in this thesis.

3.5 Correlation coefficient

The correlation coefficient between two stocks is considered in terms of the matrix \mathbf{C} , as the following equation shows:

$$c_{i,j} = \frac{\langle r_i r_j \rangle - \langle r_i \rangle \langle r_j \rangle}{\sqrt{(\langle r_i^2 \rangle - \langle r_i \rangle^2)(\langle r_j^2 \rangle - \langle r_j \rangle^2)}} \quad (3.4)$$

where r denotes the return and the bracket indicates a temporal average over the period. Additionally, a certain threshold value θ_{corr} , $0 \leq \theta_{corr} \leq 1$ is specified, and a directed edge is qualified to be linked between stock i and stock j if the value of $c_{i,j}$ is greater than or equal to θ_{corr} .

3.6 Summary

In this chapter the data sources together with the pre-processing methods have been introduced. Hence, the table of economical data are converted into matrix and the stock price data are transformed to logarithmic return data and correlation coefficients for further analysis.

Chapter 4

Topological properties of directed complex networks

4.1 Introduction

Topological properties of stock complex network are the structural organisations of the interconnections of the system components, e.g., nodes, edges, and the directions and weights of edges, which are also referred to as "network architecture".

In the networks of real stock markets, there are numerous common recurring patterns of connections which have profound effects towards the way the complex financial systems behave. This chapter will introduce the critical topological properties implemented in this thesis.

4.2 Degree centrality and strength centrality

The degree of a node k represents the number of its neighbours. In directed network, out-degree k_{out} is the number of edges which start from the given node and end at others, while in-degree k_{in} is the number of edges which end at the given node and start from others. Thus, there is relationship between k_{in} and k_{out} :

$$k = k_{in} + k_{out}. \quad (4.1)$$

As one of the most widespread measures to calculate network centrality, degree centrality of a node can be described as the number of direct links that relate to a specific node [Fre78]. In terms of the directed stock price return network, this thesis

mainly focuses on the out-degree analysis on the nodes. Moreover, the strength centrality has generally been accumulated to the sum of weights of out-degrees to form the weighted networks. The equation of this measure is shown as bellow:

$$C_D^W(i) = \sum_j^N w_{ij} \quad (4.2)$$

where W represents the matrix of weighed adjacencies, and w_{ij} represents the weight of the link between node i and j .

4.3 Degree distribution and strength distribution

The degree distribution of stock price return network $p(k)$ can be defined as:

$$p_d(k) = \frac{N_k}{N}, \quad (4.3)$$

while N_k represents the number of nodes whose out-degree value is k . The distribution of strength has a similar definition:

$$p_s(w) = \frac{N_w}{N}, \quad (4.4)$$

while N_w represents the number of nodes whose strength value is w .

4.4 Average shortest path length

In a network, the distance between two nodes is the number of edges contained on the shortest path connecting the two nodes. The average path length of the network refers to the average distance of all pairs of nodes in the network. It indicates the degree of separation between nodes in the network and reflects the global characteristics of the network.

The average shortest path length of a directed network G is defined as the following equation:

$$l_G = \frac{1}{n(n-1)} \sum_{i,j \in V} d(i,j) \quad (4.5)$$

where V is the set of nodes of G .

4.5 Betweenness centrality

Other than strength, betweenness centrality [Fre77] can be used to determine the critical nodes among the entire network and to recognise the most associated firms in the chosen stock market. When it comes to weighted networks, betweenness centrality of a node is the sum of the weights in the fraction of all-pairs shortest paths that pass through this node, which can be described as the following equation:

$$C_B(v) = \sum_{s,t \in V} \frac{\sigma(s,t|v)}{\sigma(s,t)} \quad (4.6)$$

where V is the set of nodes, $\sigma(s,t)$ is the sum of weights of all-pairs shortest (s,t) -paths, and $\sigma(s,t|v)$ is the sum of weights of those paths passing through some node v other than s,t . If $s = t$, $\sigma(s,t) = 1$, and if $v \in s,t$, $\sigma(s,t|v) = 0$.

4.6 Clustering coefficient

The clustering coefficient of a node refers to the ratio of the number of connected edges between all of adjacent nodes of the node to the maximum number of possible edges between these adjacent nodes. The clustering coefficient of the network refers to the average of the clustering coefficients of all nodes in the network, which indicates the clustering of nodes in the network, i.e., the clustering characteristic of the network. It also means that how large is the possibility of two nodes are adjacent nodes if they are both adjacent nodes of a same node, which reflects the local characteristics of the network.

In a nutshell, clustering coefficient is a measure of the degree to which nodes in a network tend to cluster together. Concerning the clustering coefficient of the complex networks, it is defined as:

$$C_i = \frac{2E_i}{(k_i(k_i - 1))}, \quad (4.7)$$

where k_i is the degree of a given node v_i , E_i is the real existing edges among the nearest neighbour nodes of the given node v_i , and $k_i(k_i - 1)/2$ means the maximum possible edges existing between its nearest neighbours of the node v_i . Besides, the clustering coefficient of a node accounts for the extent to which the transmission relationship between the given node and its neighbours also exists between its neighbours,

and the clustering coefficient may be given by:

$$C = \frac{3 \times \text{number of triangles in the networks}}{\text{number of connected triples of nodes}}. \quad (4.8)$$

This measure gives an indication of the clustering in the whole network, and can be applied to both undirected and directed networks.

4.7 Efficiency

Network efficiency measures how efficient for information being conducted and exchanged in the network, which can help to determine whether the objective network shows small-world property. There are global and local efficiencies that on the different scale sizes [LM01].

4.7.1 Global efficiency

Global efficiency quantifies the conduction and exchange of information through out the entire network. The global efficiency of network \mathbf{G} is defined as:

$$E_{glob}(\mathbf{G}) = \frac{\sum_{i \neq j \in \mathbf{G}} \epsilon_{ij}}{N(N-1)} = \frac{1}{N(N-1)} \sum_{i \neq j \in \mathbf{G}} \frac{1}{d_{ij}} \quad (4.9)$$

In other words the global efficiency is calculated as the average of each inverse shortest path length among the entire network, hence it is inversely related to the average shortest path length.

4.7.2 Local efficiency

The local efficiency evaluates the resistance of a network towards node i and quantifies the conduction and exchange of information among its neighbours. It can also be regarded as the global efficiency computed on node neighborhoods. The local efficiency of node i in network \mathbf{G} is defined as:

$$E_{loc}(G, i) = \frac{1}{N} \sum_{i \in \mathbf{G}} E_{glob}(\mathbf{G}_i) \quad (4.10)$$

Therefore it can be seen that the local efficiency is related to the clustering coefficient, which can help recognise the property of small-world for a network.

4.8 Assortativity and degree correlations

The assortativity is a correlation coefficient between the degrees of all nodes on two opposite ends of an edge. A positive assortativity value indicates that nodes tend to link to other nodes with the same or similar degree.

The phenomenon of assortative [New02] mixing can be quantified by means of an assortative coefficient. Let E_{ij} be the number of edges in the network that connect a vertex of type i to one of type j , with $i, j = 1, \dots, n$, then similar in spirit to the adjacency matrix for vertices, these edges can be represented in the form of an edge incidence matrix \mathbf{E} , with elements E_{ij} . A normalized mixing matrix is defined as follows:

$$\mathbf{e} = \frac{\mathbf{E}}{\|\mathbf{E}\|}, \quad (4.11)$$

where $\|\mathbf{E}\|$ refers to the sum of the elements of the matrix \mathbf{E} . The entries e_{ij} in the normalized matrix represent the fraction of edges that connect vertices of types i and j , and satisfies the normalization condition,

$$\sum_{ij} e_{ij} = 1. \quad (4.12)$$

The assortativity coefficient r is then defined thus,

$$r = \frac{Tr(\mathbf{e}) - \|\mathbf{e}\|^2}{1 - \|\mathbf{e}\|^2}, \quad (4.13)$$

where $Tr(\mathbf{e})$ is the standard matrix trace—the sum of the diagonal elements e_{ii} . The value of the coefficient r lies in the range $-1 \leq r \leq 1$, where 1 represents a perfectly assortative network, 0 a randomly mixed one and -1 a perfectly disassortative network.

Since the degree is an important topological measure, degree correlations assume a significant amount of relevance as they can give rise to complicated network structural effects. The degree correlation can be computed using Eqn. 4.13, where the elements e_{ij} represent the fraction of edges that connect a vertex of degree i to that with degree j .

4.9 Modularity

Modularity stands for the difference between fraction of links that fall within communities and the expected fraction if links are randomly distributed [NG04]. This project introduces modularity as a measure to evaluate the connection strength between node pair within a group. Regarding to the industry where the stocks belong to, these stocks are divided into different groups hence modularity is used to measure the closeness of intra- and inter-group.

Two groups are combined to generate the modularity value while computing the closeness of two groups, as formula below shows:

$$Q = \frac{1}{2m} \sum_j \left[w_{ij} - \frac{k_i k_j}{2m} \right] \delta(c_i, c_j) \quad (4.14)$$

where c_i is the community to which node i is assigned, and k_i represents the degree of node i . The δ -function $\delta(u, v)$ is 1 if $u = v$ and 0 otherwise and $m = 0.5 \sum_{ij} w_{ij}$ is the sum of weights in the whole network.

4.10 Summary

In this chapter the critical topological properties for this thesis have been introduced. Corresponding properties will be calculated if they are applicable for the directed-unweighted or directed-weighted network during the empirical practice.

Chapter 5

Community detection for directed networks

5.1 Introduction

In this chapter, the basic theory and algorithm of community detection for directed networks will be introduced. It starts with the concepts of modularity score and modularity optimisation method. Then, it will be discussed the eigenvector and eigenvalue in a matrix for finding the optimal nodes assignments of communities. Finally, a practical algorithm will be illustrated.

5.2 Community detection algorithm

This thesis considers a theoretic concept of modularity-based community detection method for directed graphs to recognise natural faults occur in the stock network along which it partitions. Community detection is applied for further understanding to the overall pattern of economical and stock price relations of listed companies.

While there are many methods to identify communities in undirected graphs, the community detection method used in this thesis is for the directed networks proposed by Leicht and Newman [LN08], which based on modularity optimisation method. Modularity optimisation method identifies communities by maximizing the modularity Q , which is defined as:

$$Q = (\text{fraction of intra-community edges}) - (\text{expected fraction of such edges}) \quad (5.1)$$

It signifies that a community is figured when the number of edges inside the community is more than the expected number on the basis of chance. As a result, modularity-based community detection maximised intra-community density and minimised inter-community density. While the complexity of modularity optimisation is NP-complete problem, this thesis uses the spectral optimisation methodology, which finds the best partition of the directed US stock network by the following expression of Q :

$$Q = \frac{1}{m} \sum_{ij} \left[A_{ij} - \frac{k_i^{\text{in}} k_j^{\text{out}}}{m} \right] \delta_{c_i, c_j} \quad (5.2)$$

where A_{ij} is defined to be 1 if there is an edge from j to i and 0 otherwise. k_i is the in-degree for node i , k_j is the out-degree for node j , m is the total number of edges in the network. δ is the Kronecker delta symbol that is 1 if nodes i and j are in the same community, i.e., $C_i = C_j$, and 0 otherwise. Spectral optimisation technique for modularity maximisation assigns nodes to different communities based on the sign of the eigenvector, corresponding to the largest positive eigenvalue of the modularity matrix \mathbf{B} , whose elements are:

$$B_{ij} = A_{ij} - \frac{k_i^{\text{in}} k_j^{\text{out}}}{m} \quad (5.3)$$

This thesis applies the repeated bisection graph-partitioning algorithm in the cause of community detection according to Leicht and Newman [LN08]. This approach begins with partition the network in two and then repeating it while optimising for the maximum modularity score of the communities. A preferred partition of a network results in a higher modularity score, therefore the modularity Q is maximised over all possible partitions of the stock network to detect communities of listed companies.

The following algorithm describes the details about the partitioning process and maximising modularity score in community detection. The functions of calculating modularity and subdividing node group are called repeatedly over iterations until no further increment of the overall modularity score.

Algorithm 1 Community detection

```

1: procedure COMMUNITY( $G, nNode, nEdge, EntireModMat, EntireNodeSpace$ )
2:   procedure CALDELTAQ( $s, \mathbf{B}$ )
3:     return  $Q \leftarrow 1 / (4 * nNode) * s^T (\mathbf{B} + \mathbf{B}^T) s$ 
4:   procedure UPDCOMMUNITYASSIGNMENT( $NodeSpace, UpdAssign$ )
5:      $Mark1, Mark2 \leftarrow \max(Assignment) + 1, \max(Assignment) + 2$ 
6:     for each  $node \in NodeSpace$  do
7:       if  $node \in UpdAssign > 0$  then node of  $Assignment \leftarrow Mark1$ 
8:       if  $node \in UpdAssign < 0$  then node of  $Assignment \leftarrow Mark2$ 
9:     return  $Assignment$ 
10:    procedure SUBDIVIDECOMMUNITY( $\mathbf{B}$ )
11:       $SymmetricMatrix \leftarrow \mathbf{B} + \mathbf{B}^T$ 
12:       $eigv \leftarrow \text{eigenvector as } \max(\text{eigenvalues}) \text{ in } SymmetricMatrix$ 
13:      return  $\text{sign}(eigv)$ 
14:    procedure CALMODULARITY( $assignment$ )
15:      for each  $node1 \in \text{Nodes of } G$  do
16:        for each  $node2 \in \text{Nodes of } G$  do
17:          if  $assignment$  of  $node1 \leftarrow assignment$  of  $node2$  then
18:             $Q \leftarrow Q + HasEdge - (nIn(node1)) * (nOut(node2)) / (nEdge)$ 
19:      return  $Q / (nEdge)$ 
20:    procedure GENMODULARITYMATRIX( $NodeSpace, ModMat$ )
21:      for each  $node1 \in NodeSpace$  do
22:        for each  $node2 \in NodeSpace$  do
23:           $B \leftarrow HasEdge - (nIn(node1)) * (nOut(node2)) / nEdge$ 
24:          if Assignment of  $node1 = Assignment$  of  $node2$  then
25:            for each  $node \in NodeSpace$  do  $C \leftarrow C + HasEdge1 +$ 
26:             $HasEdge2 - (nIn(node1) * nOut(node) + nIn(node) * nOut(node1)) / nEdge$ 
27:    procedure INTERATEBISECTION( $ModMat, NodeSpace$ )
28:       $UpdAssign \leftarrow \text{SubdivideCommunity}(ModMat)$ 
29:       $DeltaQ \leftarrow \text{CalDeltaQ}(UpdAssign, ModMat)$ 
30:      if  $DeltaQ > 0$  then
31:         $Assignment \leftarrow \text{UpdCommunityAssignment}(NodeSpace, UpdAssign)$ 
32:        for each  $side \in \text{UpdCommunityAssignment}$  do
33:           $ModMat \leftarrow \text{GenModularityMatrix}(NodeSpace)$ 
34:           $\text{InterateBisection}(ModMat, NodeSpace)$ 
35:       $\text{InterateBisection}(EntireModMat, EntireNodeSpace)$ 
36:      return  $Assignment$ 

```

5.3 Summary

In this chapter, the basic theory and algorithm of community detection for directed networks have been introduced. This modularity-based community detection method allows us to produce more accurate partitioning of the directed network than the methods only for undirected networks.

Chapter 6

Benchmarking networks generation

6.1 Introduction

Numerous literatures support the idea that undirected stock networks have small-world features. It can be helpful to examine whether the directed one is a small-world network or not by comparing it with conventional and acknowledged random network and small-world networks. This chapter will introduce the directed forms of such two conventional and basic networks: Erdős–Rényi (ER) random network and Watts-Strogatz (WS) small-world network.

6.2 Directed Erdős–Rényi random network

To some extent, the regular network and the random network are two extremes while the complex network is between them. In random network, nodes are connected in a purely random manner, hence the resulting network is called a random network. If the nodes are wired in a self-organising manner, it will then evolve into a variety of different complex networks.

The Erdős–Rényi (ER) model [ER59] generates a graph that winded randomly between N nodes in the network with probability p . The degrees of nodes comply with a Poisson distribution, indicating that most nodes have approximately same number of edges.

Erdős and Rényi has found that as the number of edges M gradually increases from a small value, the random graph will evolve from a fragmented graph with many independent components to a fully connected one [Str01]. They demonstrate that there is a threshold of the probability p below which the property is rare and above which it

is almost certain for a number of topological properties. This transition is regarded as "phase change" due to the complex system that changes its state at some critical value of possibility p .

The algorithm for generating a standard ER random network with possibility p is depicted as below:

Algorithm 2 ErdosRenyiRandomNetwork

```

1: procedure GENERATERANDOMNETWORK( $nNodes$ ,  $p$ ,  $edges$ )
2:   Initialize:
3:      $G \leftarrow$  Directed graph with nodes in  $nNodes$ 
4:   for each  $e \in edges$  do
5:     if random number between 0 and 1  $< p$  then add edge  $e$  to  $G$ 
6:   return  $G$ 

```

6.3 Directed Watts-Strogatz small-world network

The nearest neighbour coupled regular network is highly clustered, but it is not a small-world network. On the other hand, the ER random network has a small average path length but without high clustering characteristics. Therefore, neither of these two types of network models can reproduce some important features of the real network, for most of the actual networks are neither completely regular nor completely random. As a transition from a fully regular network to a completely random network, Watts and Strogatz introduced a small-world network model called the WS small-world model [WS98].

In the complex networks theory, a network with both a small average path length and a large average clustering coefficient feature is called a small-world network. In the WS model, when the random reconnection probability p of the connected nodes is gradually increased from 0 to 1, it can be observed that the initial regular network will go through the following three phases: regular network, small-world network, and eventually random network.

This thesis uses an alternative method based on WS model [SW14]. Specify the number of nodes N , the mean degree K (assumed to be an even integer), and a special parameter β , satisfying $0 \leq \beta \leq 1$ and $N \gg K \gg \ln N \gg 1$, the model constructs an undirected graph with N nodes and $NK/2$ edges as the following algorithm depicts:

Algorithm 3 WattsStrogatzSmallWorldNetwork

```

1: procedure GENERATESMALLWORLDNETWORK( $nNodes, p0, beta$ )
2:    $Dmax \leftarrow nNodes \% 2$ 
3:    $R \leftarrow range from 1 to Dmax$ 
4:    $D \leftarrow$  circulant matrix of  $R/Dmax$ 
5:    $p \leftarrow beta * p0 + ((D \leq p0) * (1 - beta))$ 
6:    $A \leftarrow 1 * (\text{randomised matrix } p < p)$ 
7:   fill diagonal of matrix  $A$ 
8:   fill diagonal of matrix  $A$ 
9:    $G \leftarrow$  Directed graph corresponds to  $A$ 
10:  return  $G$ 

```

6.4 Summary

In this chapter, the directed forms of ER random network and WS small-world network have been introduced. Topologically both of the two kinds of networks have the phenomenon of "phase change" with the change of connection thresholds. In practice these two kinds of networks will be generated by the same number of nodes and edges, and their topological properties can be regarded as the benchmarks under certain circumstances to compare with the stock price return networks.

Chapter 7

Empirical study and results

7.1 Stock market description

There are totally 261 trading days in 2016 of US stock market, this thesis selects 1,418 stocks of listing US companies that were traded in all trading days in 2016. Table 7.1 lists the titles of 55 industrial sectors corresponding to the summary level of BEA industry codes as well as the number of stocks in each of them.

Industrial Sector Title	Stock Count
Banks, credit intermediation, and related activities	214
Computer and electronic products	173
Funds, trusts, and other financial vehicles	132
Insurance carriers and related activities	85
Chemical products	76
Utilities	64
Food and beverage and tobacco products	56
Fabricated metal products	52
Securities, commodity contracts, and investments	42
Broadcasting and telecommunications	42
Other retail	38
Machinery	36
Wholesale trade	33
Motor vehicles, bodies and trailers, and parts	32
Construction	30
Computer systems design and related services	27

Performing arts, spectator sports, museums, and related activities	27
Miscellaneous professional, scientific, and technical services	23
Petroleum and coal products	16
Paper products	15
Air transportation	14
Data processing, internet publishing, and other information services	14
Ambulatory health care services	12
Plastics and rubber products	12
Accommodation	12
Administrative and support services	11
Truck transportation	11
Rental and leasing services and lessors of intangible assets	10
Other transportation and support activities	9
Publishing industries, except internet (includes software)	8
Other transportation equipment	8
Support activities for mining	7
Other real estate	7
Miscellaneous manufacturing	7
Oil and gas extraction	6
Furniture and related products	6
Electrical equipment, appliances, and components	6
Rail transportation	5
Textile mills and textile product mills	5
Nonmetallic mineral products	5
Transit and ground passenger transportation	4
Waste management and remediation services	3
Hospitals	3
Wood products	3
Printing and related support activities	2
Motion picture and sound recording industries	2
Nursing and residential care facilities	2
Pipeline transportation	2
Primary metals	2
Apparel and leather and allied products	2
Other services, except government	1

Water transportation	1
Legal services	1
Social assistance	1
Mining, except oil and gas	1
Total	1,418

Table 7.1: Part of counts for US stocks by industry [SEC18]

It is not hard to see the composition of stock market are mainly dominated by the finance-related industry ("Banks, credit intermediation, and related activities", "Funds, trusts, and other financial vehicles", "Insurance carriers and related activities", "Securities, commodity contracts, and investments", etc.) and computer-related industry ("Computer and electronic products", "Computer systems design and related services", "Data processing, internet publishing, and other information services", "Electrical equipment, appliances, and components", etc.). The total numbers of finance-related industry and computer-related industry are over 473 and 220 respectively, which jointly take almost half of the number of total stocks. Therefore, it is necessary to use the formalised formula which divides the value by the number of stocks in its belonging industrial sector, punishing the connection from or to a node by the industry size, i.e., if a stock is in a large industry, it will need higher transaction flows to connect to other nodes in the network.

7.2 Networks construction

This thesis first generated matrices of normalised direct demand **A**, normalised direct requirement **B**, correlation coefficient **C** using formula 3.1, 3.2, and 3.4.

Figure 7.1 from normalised direct demand **A** and normalised direct requirement **B** illustrates that the transaction densities decrease as threshold of normalised direct requirement and normalised direct demand increase, and their patterns are very similar with the same inflection point at around $threshold = 0.136$ where the densities begin to decline. Therefore, the values of thresholds for normalised direct requirement and normalised direct demand are set to be equal, i.e., $\theta_{EIO} = \theta_{DD} = \theta_{DR}$, to filter the directed edges among the stock network.

Figure 7.2 shows the distribution of stock price correlation coefficients has a shape complies to the normal distribution. Most correlation coefficients are vary from -0.2 to 0.85 with the mean of 0.265 . Figure 7.3 also shows that the edge density drops

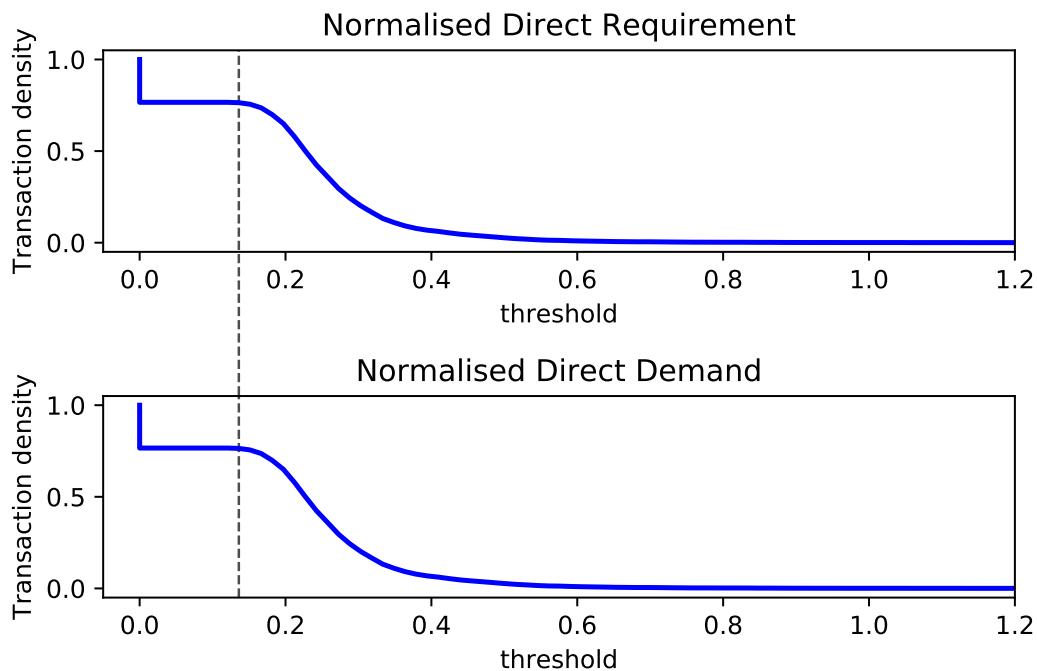


Figure 7.1: Transaction densities in EIO. The density of transactions drops vertically at the threshold of 0, which means nearly a quarter of values in the normalised direct demand matrix **A** and normalised direct requirement **B** are 0. Then the two densities both decrease from the point around 0.136, and overall they follow a same pattern.

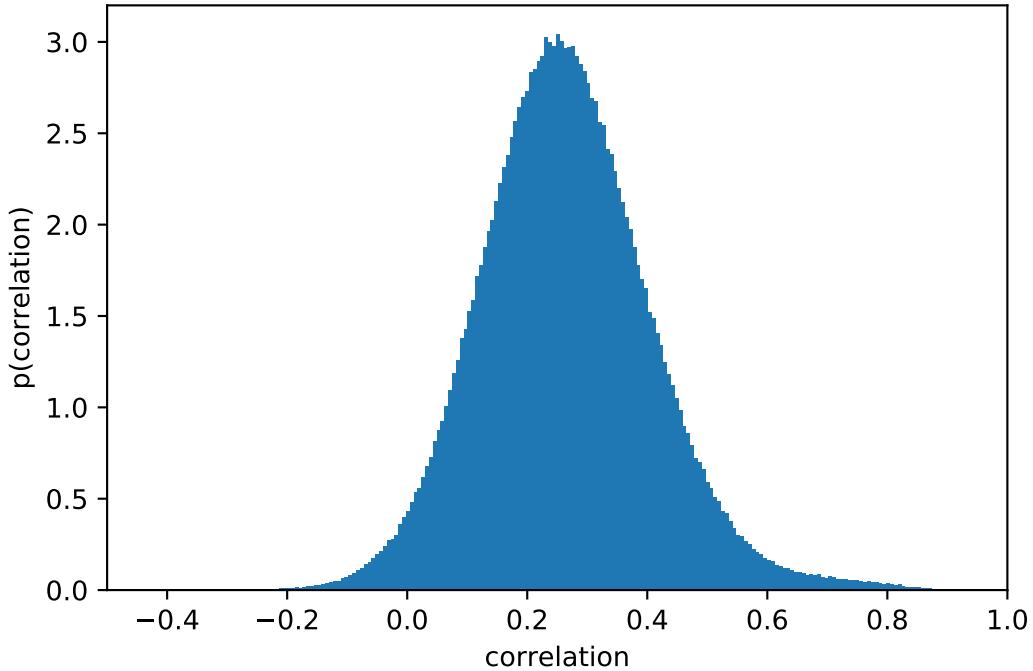


Figure 7.2: Correlation coefficient distribution of stock price return. The minimum and maximum are -0.687 and 0.977 and the mean is 0.265 . The distribution follows normal distribution.

dramatically as the correlation coefficient increases from 0 to 0.50. It implies that the prices of most stocks traded in NYSE and NASDAQ often fluctuate to the same direction, but the patterns are less similar to each other.

Figure 7.4 shows the number of directed edges remain at the conditions of different value combinations of $\{\theta_{EIO}, \theta_{corr}\}$. When both of the thresholds set to be minimal at their own value range, i.e., $\theta_{EIO} = 0$ and $\theta_{corr} = -1$, the number of directed edges is $N \times (N - 1) = 2,009,306$, while N indicates the total number of nodes, which is 1418. According to the figure 7.4, the number of edges will be less than 100,000, in which case the network has a density of lower than 5%, if $\theta_{EIO} \geq 0.3545$ or $\theta_{corr} \geq 0.5020$.

It is obvious that the larger values assigned to θ_{EIO} and θ_{corr} , the more significant will be for the weights and directions of the remaining edges. But if the network becomes too sparse, it can not be strongly or even weakly connected and there would be many independent cliques, hence the network becomes too inefficient to be a sensible network. As a result, this thesis selects the threshold-value-pair $\{\theta_{EIO} = 0.292, \theta_{corr} = 0.379\}$ to construct a directed-unweighted network and a directed-weighted network

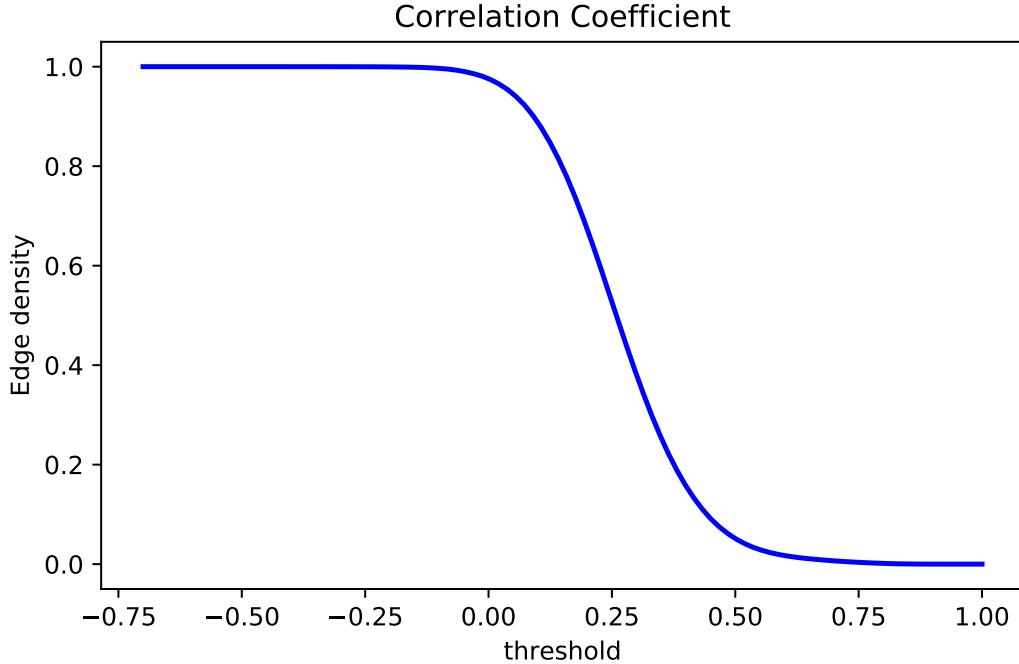


Figure 7.3: Edge density with correlation coefficient. The edge density drops dramatically as the correlation coefficient increases from 0 to 0.50.

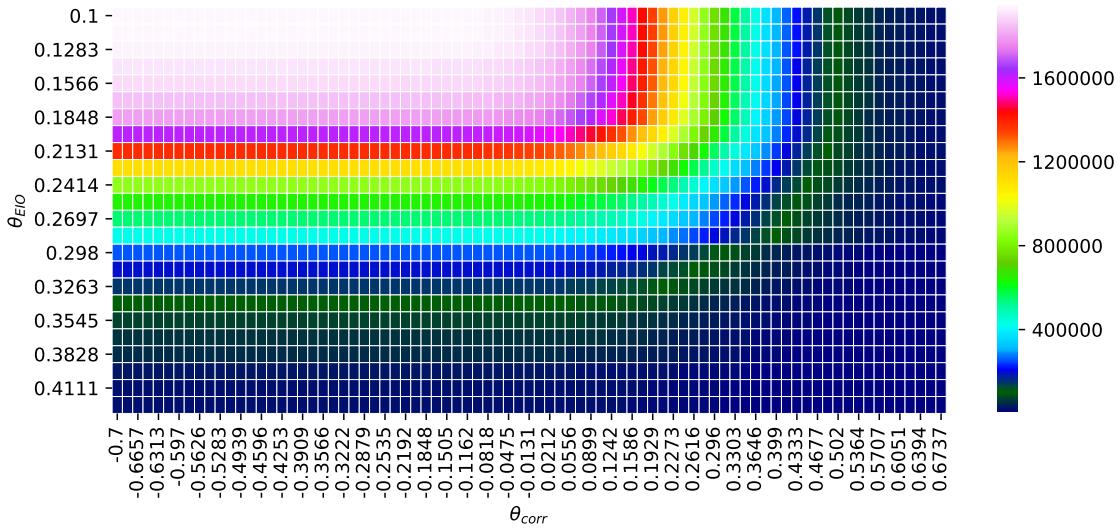


Figure 7.4: Heatmap of the numbers of directed edges per EIO-threshold and correlation-coefficient-threshold. The number of directed edges changes from the maximum to 0 as θ_{EIO} decreases from 0.10 to 0.45 and θ_{corr} increases from -0.70 to 0.68.

7.2. NETWORKS CONSTRUCTION

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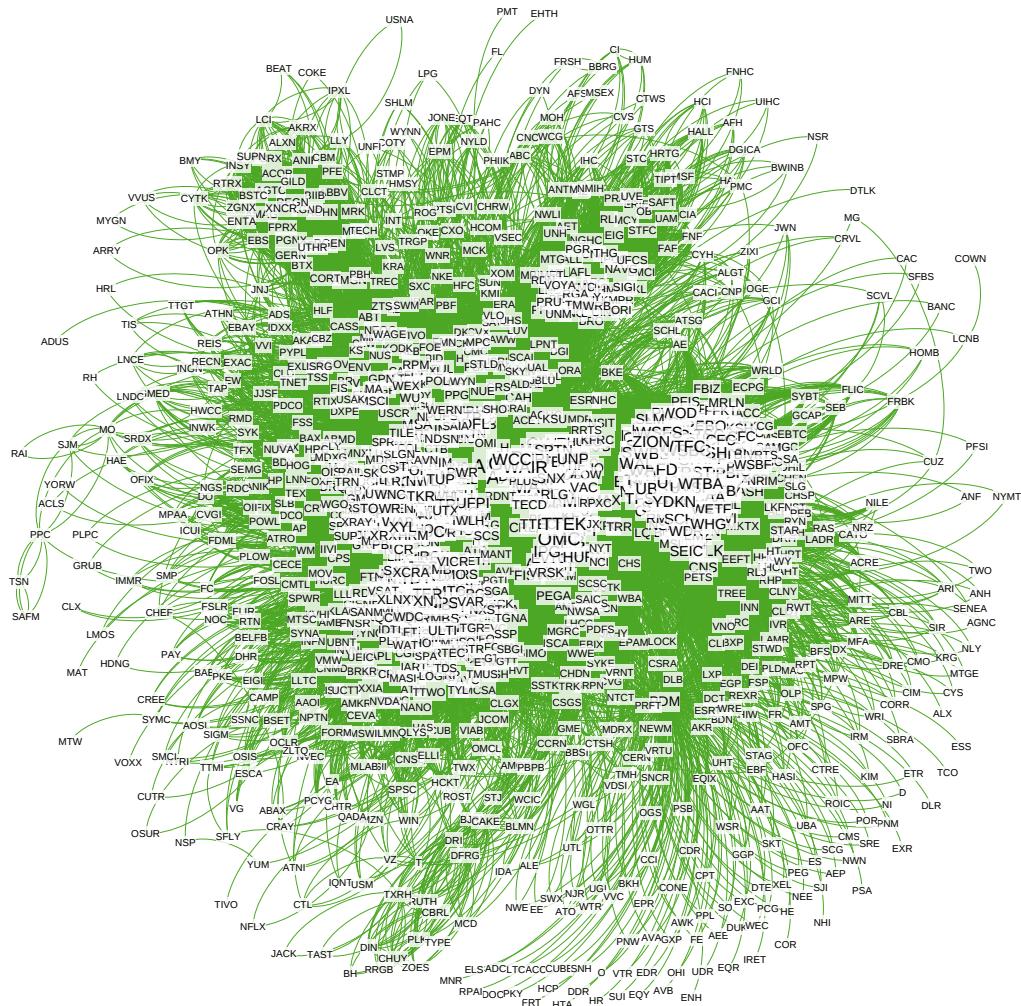


Figure 7.5: Visualisation of the directed-unweighted stock price return network. The stock codes are nodes and the clockwise rotations of edges are directions. Graph is generated by *Gephi* [BHJ09].

Directed networks	Stock price return	WS small-world	ER random
Number of nodes	1418	1418	1418
Number of edges	102051	102051	102051
Out-degree distribution	Power-law	Normal	Normal
Average out-degrees	143.94	143.94	143.94
Average path length	2.775	2.005	1.973
Clustering coefficient	0.4675	0.1367	0.05105
Global efficiency	0.2563	0.5161	0.5216
Local efficiency	0.6276	0.5027	0.4456
Assortativity	0.02004	-0.002180	0.001452

Table 7.2: Main properties of stock network, small-world network, and random network

for the 2016 US stock market. Figure 7.5 shows the visualisation of the directed-unweighted stock network.

7.3 Analysis of the directed-unweighted stock network

A directed WS small-world network and a directed ER random network with the same number of nodes and edges with the stock directed-unweighted network are generated according to algorithms 3 and 2. Table 7.2 compares the main topological properties of the three networks, which will be discussed together with some other measures in the following sections.

7.3.1 Power-law distribution

According to the table 7.2, the values of average out-degrees of directed stock network, WS small-world network and ER random network are exactly the same due to the identical numbers of nodes and edges, but in terms of the distributions of out-degrees, stock network is totally different from the others.

The distribution and P-P plots in figures 7.7 and 7.8 show clearly that the out-degree distributions of WS small-world network and ER random network fitted nicely to the normal distribution, because most degrees of nodes fall in the middle range, especially in the P-P plots, the sample data points are basically on the diagonal representing the theoretical normal distribution for both WS small-world network and ER random network. Nonetheless, figure 7.6a illustrates that for the stock price return network, only

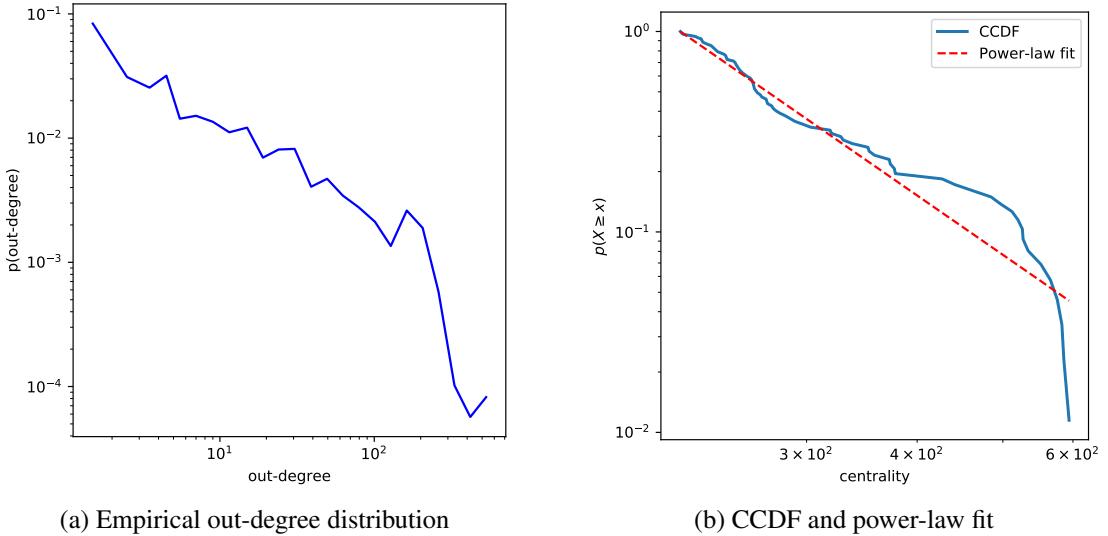


Figure 7.6: Out-degree distribution of directed stock price return network

a few number of nodes show higher out-degree, while most nodes are at the positions of low out-degree level. Statistical result shows the distribution of the directed stock price return network follows power-law distribution with the exponent of 4.057.

The discovered power-law distribution property reveals that in the aspect of degree the directed stock network shows the continuity with conventional undirected stock networks in previous studies. Therefore in general, most of the nodes have a small degree while a few modes have a higher degree for both directed and undirected stock networks.

7.3.2 Small-world property

Previous researches upon undirected stock networks have argued that they have small-world topologies. Such feature is also applied to the directed WS small-world network and ER random network, for the average path lengths of around 2, indicating that if we take any node in the network, it can be expected to reach any other nodes just through one node as the medium. For the directed stock network, the expectation number of medium nodes is 1.775, which can be also treated as a small number for network connectedness.

On the other hand, the global efficiency of the benchmarking networks are slightly higher than $1/l_G$ which are both around 0.5. It means that in physical terms the flow

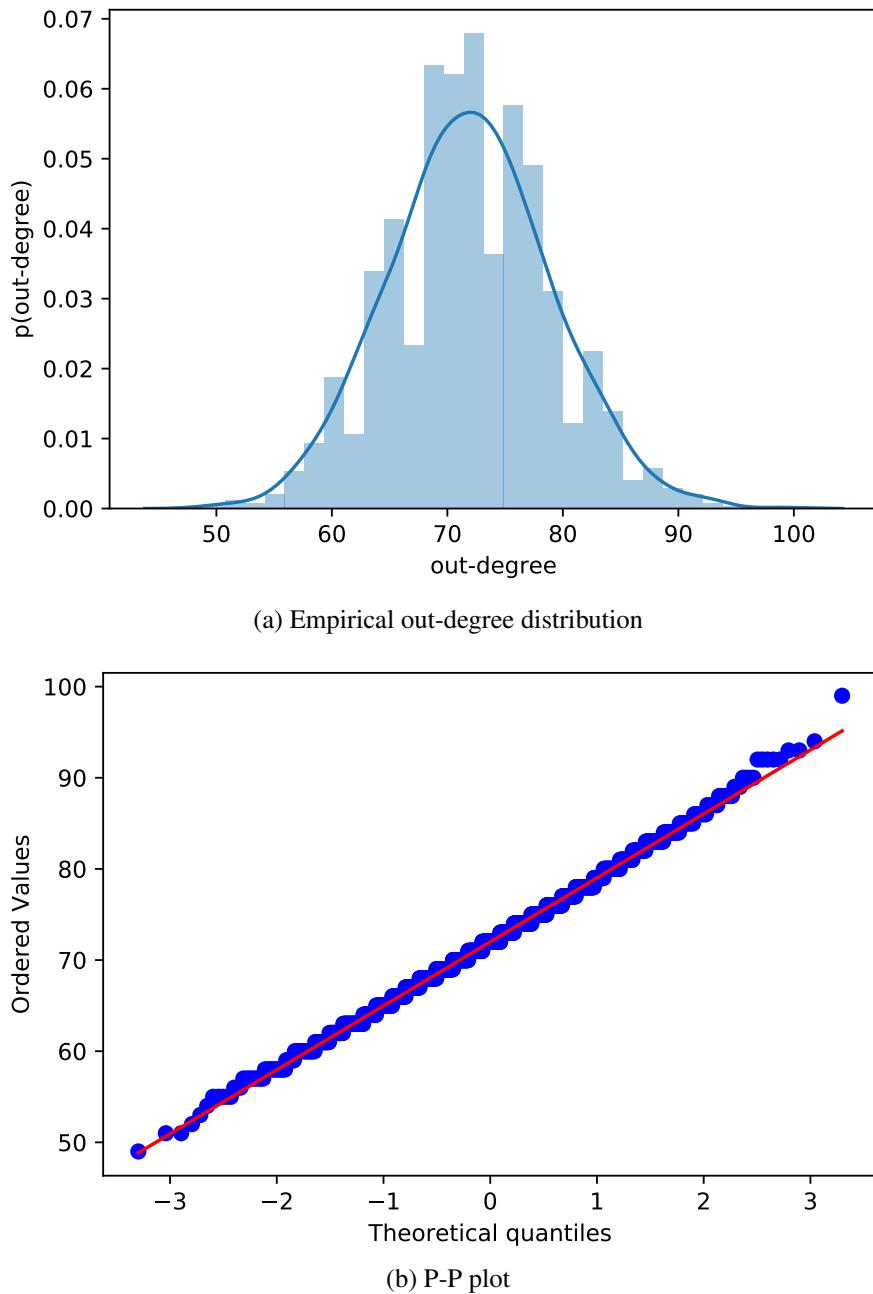


Figure 7.7: Out-degree distribution and P-P plot of small-world network

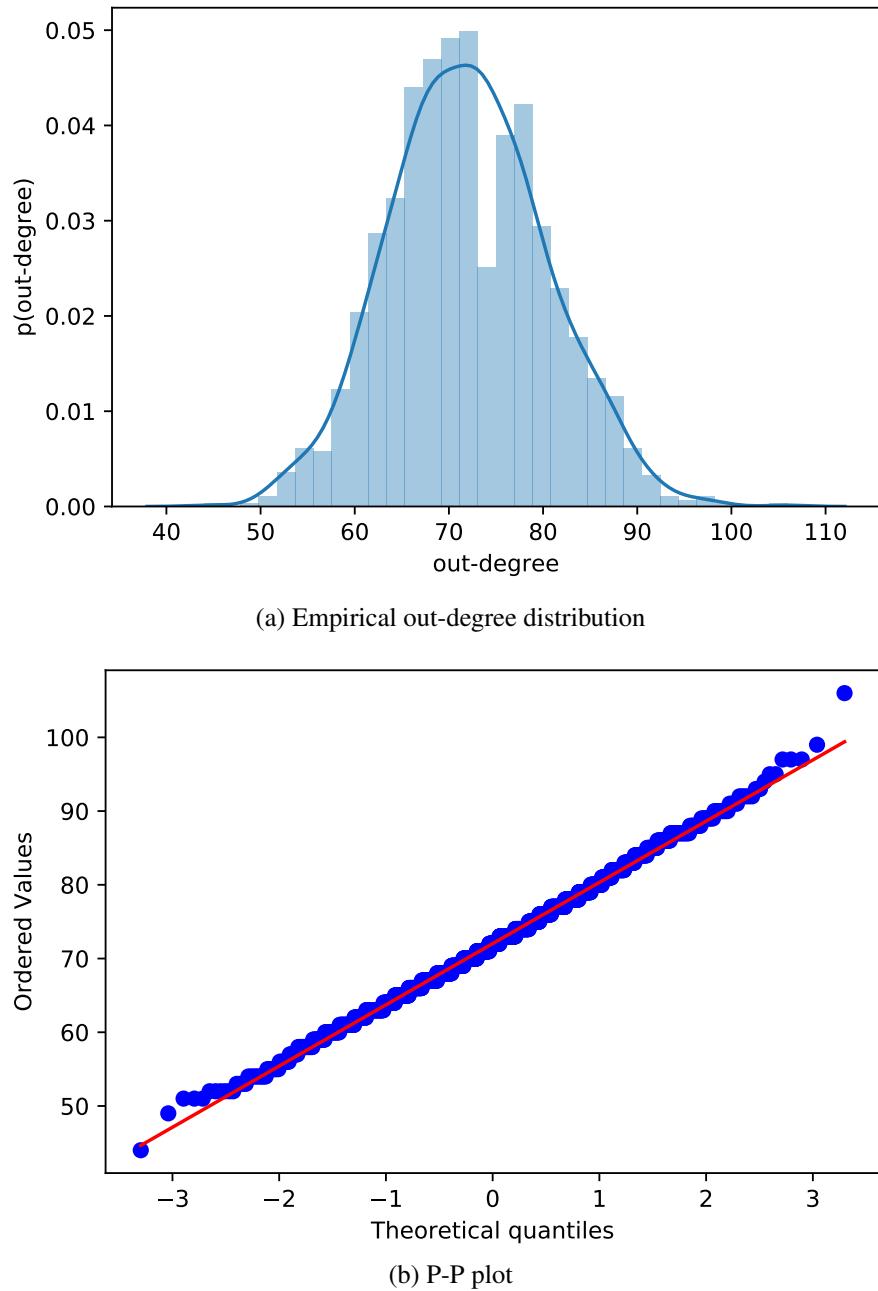


Figure 7.8: Out-degree distribution and P-P plot of random network

of information in these two networks is efficient, which is the behaviour of small-world networks. While as for the directed stock network, its global efficiency is less than $1/l_G$ which is 0.36. In essence, like directed WS small-world and ER random networks, directed stock network also has the small-world properties to some degree, while it is not efficient to exchange information across the network in the global scale.

7.3.3 Clustering feature

The directed ER random network shows no clustering feature because its clustering coefficient is close to zero (0.05105). For the directed WS small-world network, its clustering coefficient of 0.1367 shows slight clustering feature. While for the directed stock network, its clustering coefficient of 0.4675 is much higher, which shows a significant clustering feature. The indicator of local efficiency also supports this conclusion because it reveals the neighbours of a node in the directed stock network are more efficient when conducting information than the other two benchmarking networks, therefore the nodes in the stock network tend to cluster together in higher degree.

The assortativity values for the three networks are all non-significant, for the two benchmarking networks this corresponds to the aforementioned non-clustering feature and the normal distribution of degrees. However, for the stock network, the incredibly low assortativity together with the aforementioned power-law distribution of degrees indicate that the nodes in this network tend to connect to other nodes with high degrees.

7.3.4 Community structure of the directed-unweighted stock network

The larger value of clustering coefficient for stock network than the other two networks indicating that the nodes in stock network tend to cluster together. Therefore, communities of stock network will be identified implementing the *algorithm 1* for directed networks in this section. According to the composition of industrial sectors of each community, as figure 7.11 shows, the following five communities are identified: (1) Production (2) Finance (3) Livelihood (4) Insurance and chemical products (5) Utilities and financial vehicles.

The communities of production (purple) and livelihood (blue) are sparsely distributed while there are some large-sized nodes acting as hubs of the overall network. The hubs not only connect to the nodes of same communities, but also the externals.

These two communities are partially intertwined due to the high relevancy of production industry and livelihood industry.

Unlike the above two communities, it can be seen from figure 7.9 that the community of finance (green) is decentralised, i.e., there is no obvious hubs and the degrees of each node distribute evenly. It also has a very dense structure, connected closely inside and completely exclusive from other nodes or communities. This means the co-movements among financial stocks are incredibly strong and economically they rely tightly to each other.

The other two communities are more interesting because of their peculiar structural features. Every industrial sectors of individual stocks in community are identified to investigate the properties of the community of insurance and chemical products (yellow). As figure 7.10d illustrates and through the investigation, almost all firms in the upper and lower clusters are in the sectors of "chemical products" and "insurance carriers and related activities" respectively, while firms between the two big clusters, like "MCK" (McKesson) and "CAH" (Cardinal Health), are large medical supplier, pharmaceutical and healthcare service companies with high out-degrees to both of the two clusters. Apart from that, there are also a considerable number of links from the nodes in upper cluster to the hubs of chemical companies. Thus, it is reasonable to infer that the prices of medicines have significant influence to medical insurance industry, additionally the purchases of chemical products of pharmaceutical firms and the sales of chemical products have made pharmaceutical and chemical companies influence to each other.

Another investigation towards the community of utilities and financial vehicles (orange) is conducted by the same measure. As figure 7.10e illustrates, there is only one huge hub (PDM) which is the company "Piedmont Office Realty Trust" among the whole community while all the others are one-degree nodes located remotely. There are more links from the hub to the rest than the opposite direction, and also the weights of the former links are generally higher. The hub, "Piedmont Office Realty Trust", is a real estate investment trust company, and the rest in the community contains 59 "funds, trusts, and other financial vehicles" firms and 44 "utilities" firms. For a big realty trust enterprise, demand for financial trust business is extremely high, and its successes of investments upon real estates will promote the development of utilities companies. It depicts that the major realty trust enterprise alone has significant influence to all of these financial trust and utilities companies.

The result of detected communities focuses on the economical links of companies

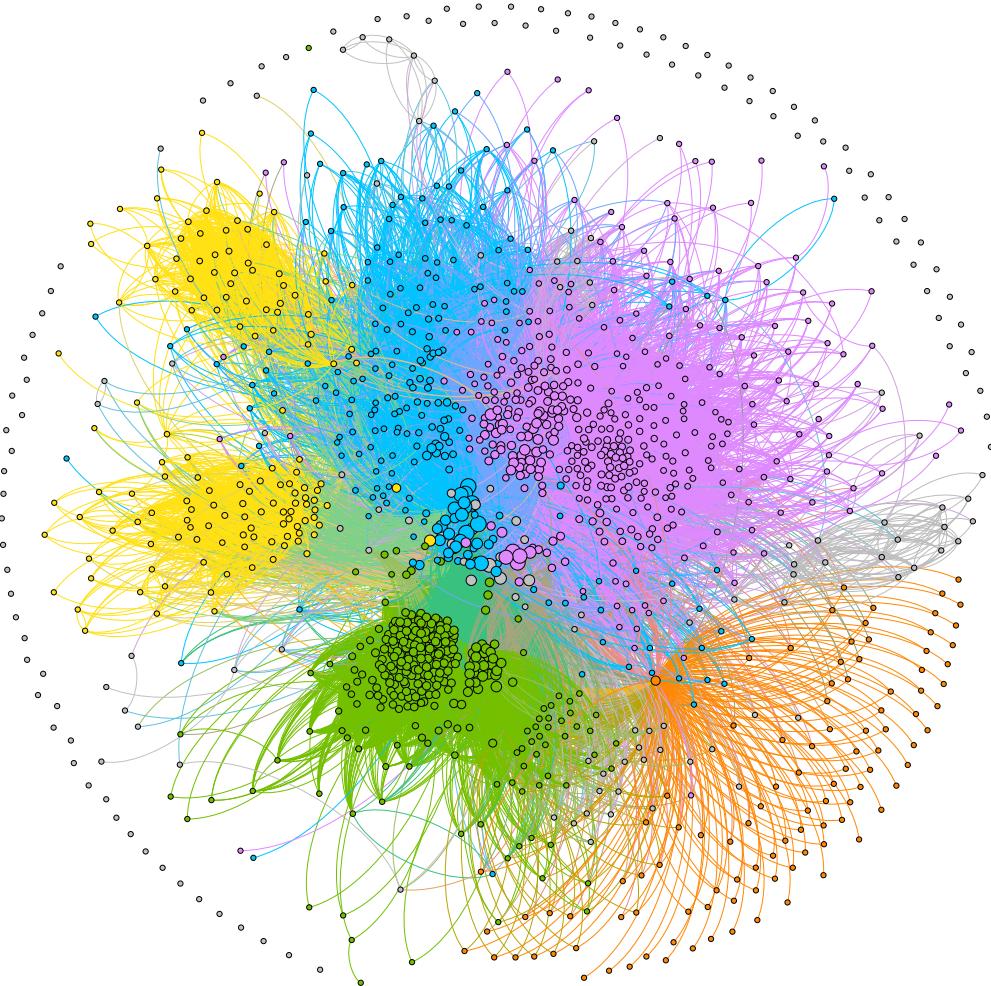


Figure 7.9: Community structure of the 2016 US stock price return network. Five distinct communities are detected represented by different colours of nodes. The direction of edge is clockwise. The size of nodes and thickness of edges are related to the value of degrees and weights. The grey nodes do not belong to any communities and most of them have zero degree. Graph is generated by *Gephi* [BHJ09].

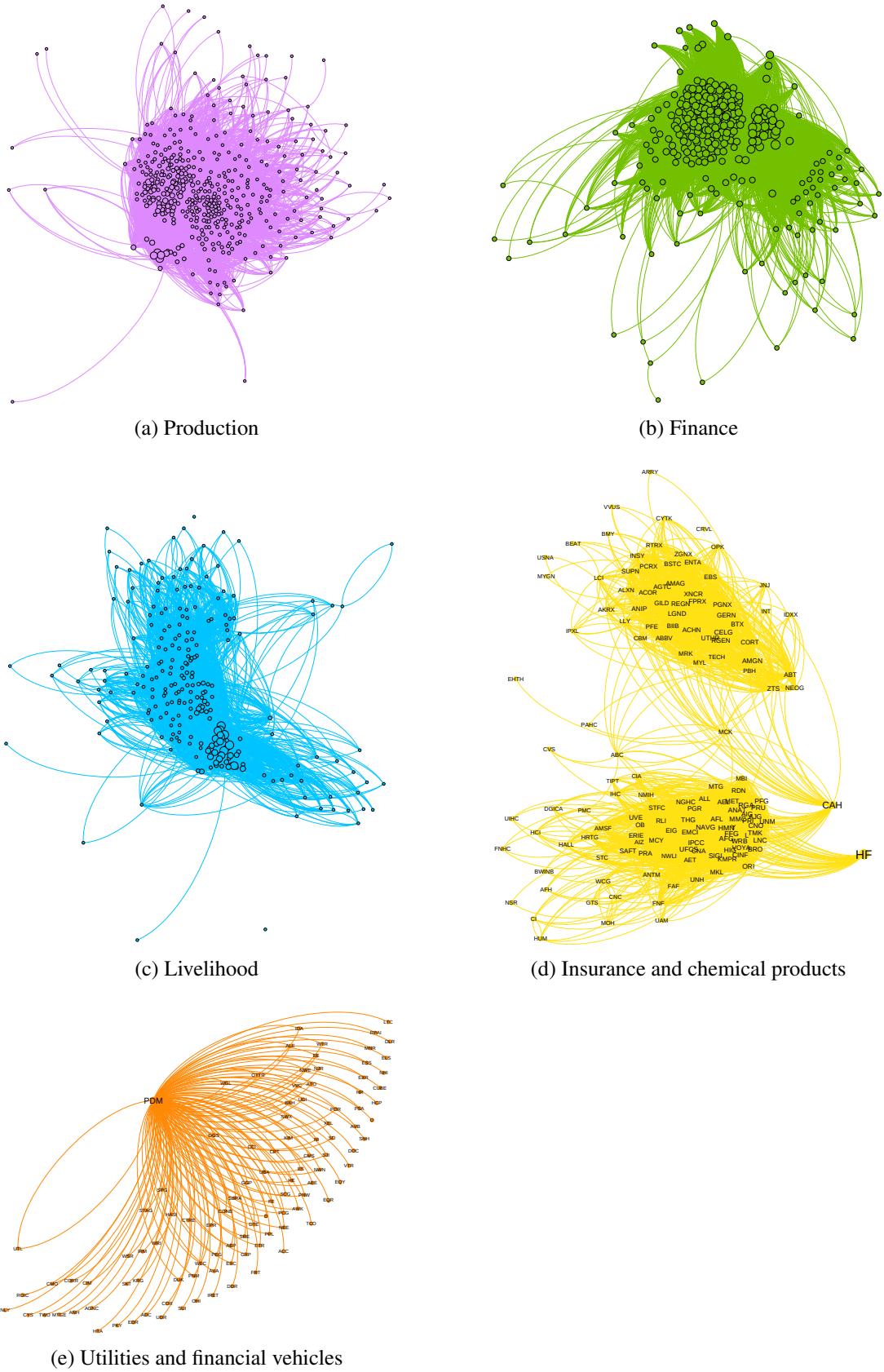


Figure 7.10: Community sole views of the directed stock network. Stock tickers are displayed for the sparsely distributed communities. Graphs are generated by *Gephi* [BHJ09].

and reveals their economical dependences and influences to each other. Through the structural features of each community, we find that the "financial" community is easily collapse inside due to the incredibly dense connections while the "utilities and financial vehicles" is also easy to collapse because the whole community relies prejudicially on few large companies and this may cause crisis if such companies are in troubles. Many stocks "production" are closely related to stocks in "livelihood" and "insurance and chemical products", while there is almost no connections between the stocks in "livelihood" and the stocks in "insurance and chemical products" and "utilities and financial vehicles", due to their economical activities with extremely few interactions.

According to the stacked bar chart in figure 7.11, almost all firms in the industrial sectors of "Computer and electronic products", "Construction", "Data processing, internet publishing, and other information services", "Electrical equipment, appliances, and components", "Machinery", "Motor vehicles, bodies and trailers, and parts", "Nonmetallic mineral products", "Other transportation equipment", "Waste management and remediation services", "Wood products" are partitioned into the community of production. For the financial community, it occupies "Federal Reserve banks, credit intermediation, and related activities" and "Securities, commodity contracts, and investments", while the community of utilities and financial vehicles contains more stocks in sectors of "Funds, trusts, and other financial vehicles" than finance. Stocks in livelihood community distribute evenly on general sectors.

7.4 Analysis of the directed-weighted stock network

A directed-weighted stock network is generated by adding the correlation coefficients in the matrix \mathbf{C} as weights to each existing directed edges from the directed-unweighted stock network. As the weighted form of the directed stock network that discussed in previous sections, this section will only focus on its features about the weights.

7.4.1 Topological properties on weighted networks

A conventional undirected-weight network is constructed independently and through the threshold of correlation coefficient we can adjust the number of undirected edges remain. When converting an undirected network to directed network, the number of edges are doubled because each undirected links are generated into two directed

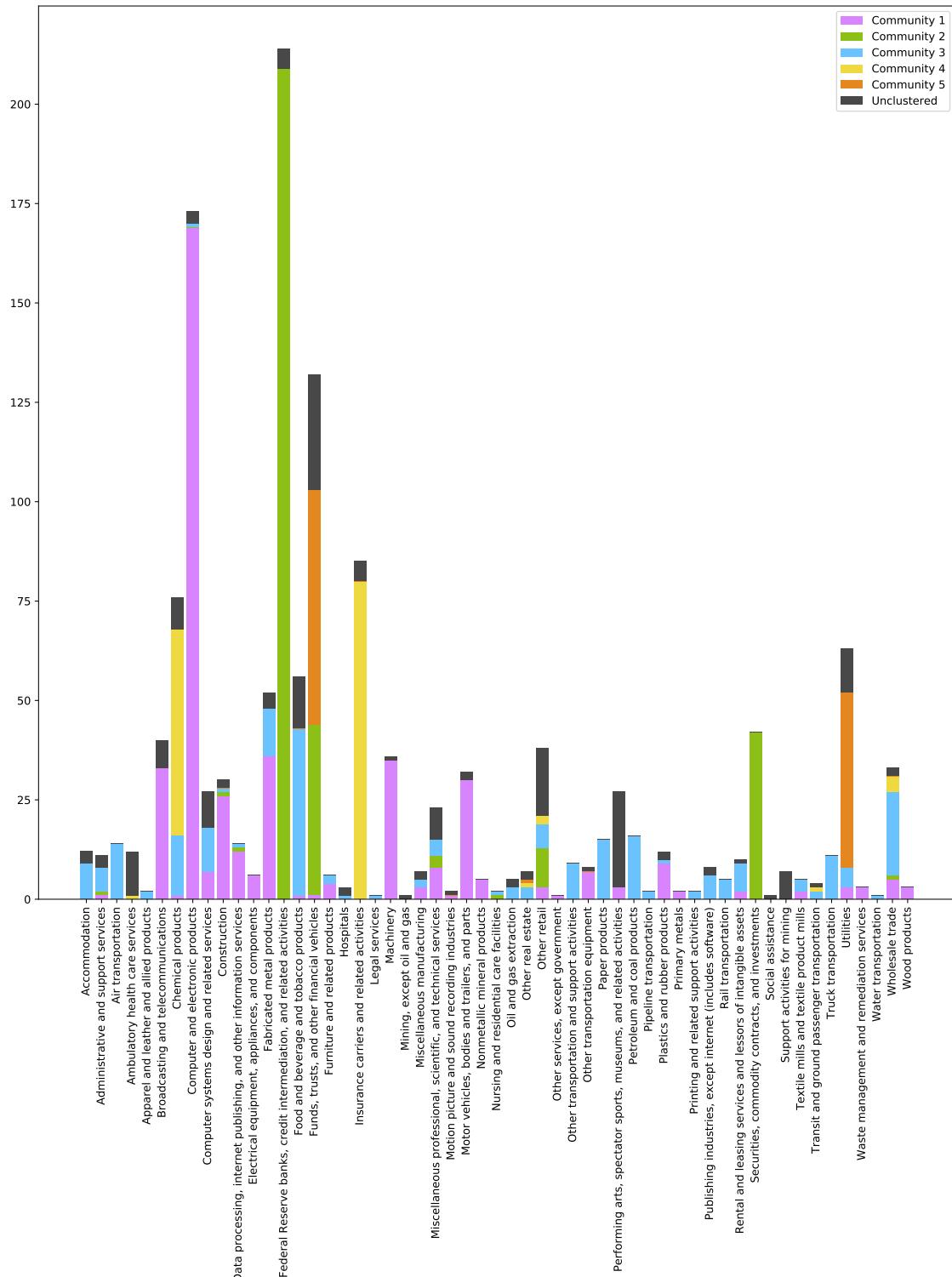


Figure 7.11: Stacked bar chart about the distribution of communities upon industrial sectors. Colours of stacks correspond to the colours of communities in figure 7.9 and figure 7.10, except the black stack indicating the nodes not belong to any communities. Sectors are arranged alphabetically.

Weighted stock network	Directed	Undirected
Number of nodes	1418	1418
Number of edges	102051	51037
Strength distribution	Power-law	Power-law
Average strength	40.89	42.31
Average betweenness centrality	0.0007440	0.0007464
Weighted assortativity	0.1244	0.06138

Table 7.3: Main topologies of weighted stock networks

links with opposite directions for remaining original network topological features unchanged. Same reason is applied for constructing the conventional undirected-weighted stock network with equivalent topologies with the directed stock network. Hence, table 7.3 compares the topological properties between them.

Like the directed-unweighted stock network, and also conventional weighted stock networks, the strength distribution of directed-weighted stock network follows power-law distribution as well. The average strength and betweenness centrality of the two weighted networks are close to each other. However interestingly, the directed-weighted stock network has significantly high assortativity other than directed-unweighted and conventional weighted networks. In certain cases, the degree may not be a good measure of the importance of the nodes, because of the equivalence of all connections. Nevertheless, some connections are of great importance. Therefore, the high value of weighted assortativity reveals that in the researched stock networks, nodes tend to be connected with other nodes with similar strength values rather than degree values, which means stocks tend to have relationships with other stocks with similar fluctuation in stock price return. As a result, correlation coefficient is an important factor for the behaviour of node connections.

7.4.2 Analysis on the relationships between price return and betweenness centrality

Figures 7.12 reveal the relationships between betweenness centralities and price returns of stocks. First, in figure 7.12a as much more nodes have low betweenness centrality values (lower than 0.001), and the cumulative sum of returns fall intensively in the range of $(-0.1, 0.6)$, while that of the nodes with high betweenness centrality values (higher than 0.001) also fall evenly in the same range. Therefore, there is no significant

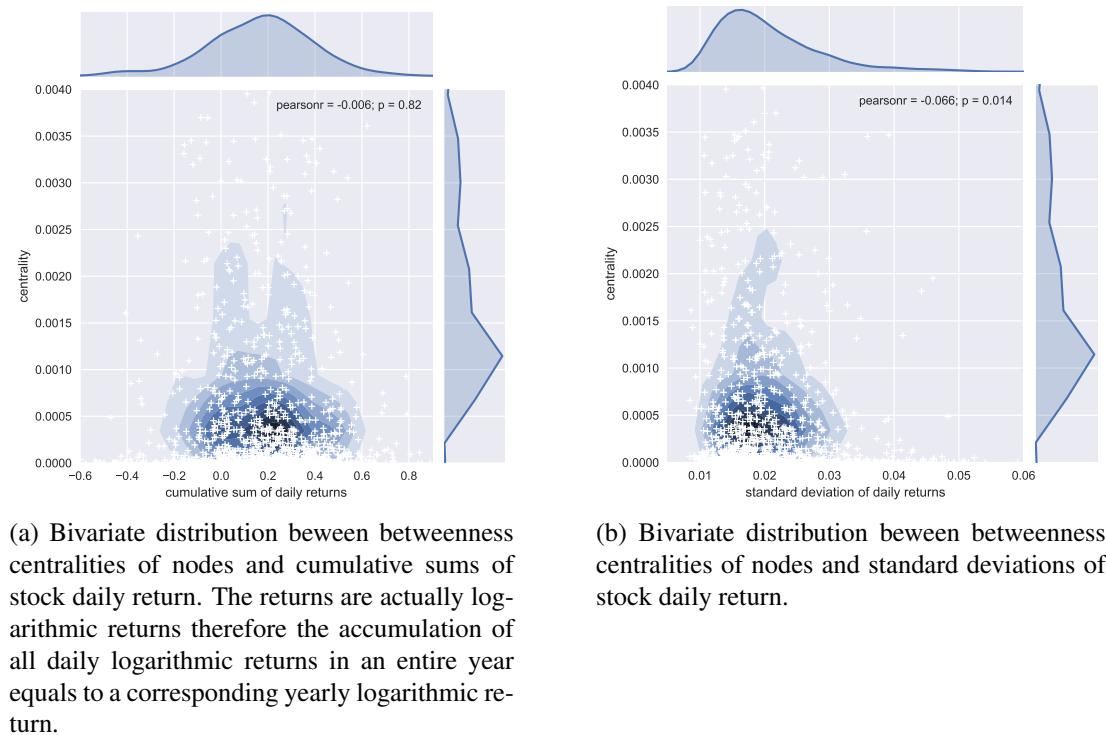


Figure 7.12: Bivariate distribution graphs about betweenness centrality and price return statistics.

difference between the expected return for stocks with different betweenness centrality values.

Second, according to the figure 7.12b, in spite of several outliers, as the betweenness centrality of nodes becomes higher, there will be a higher possibility of nodes tend to have low standard deviation of stock daily return. This indicates the hubs in the network have considerably stable return during the specified researched year among the whole stock market. The average standard deviation for all values of betweenness centrality remain similar because of the more frequent occurrences of outliers with higher betweenness centralities from the figure.

As a result, it is suggested to investors although choosing stocks with high centralities possibly will not bring a higher expected return for a portfolio, they have the functionality of reducing the overall risks and generating more stable returns, which is also a vital feature for stock investment.

Chapter 8

Other results

8.1 Introduction

Due to the complexity of financial market and the interconnectedness and interdependencies of industrial sectors in the economy, the price returns of each coupling stocks might have certain underlying economic link. Such behaviours can hardly be explained by traditional financial models and theories. This chapter attempts to combine machine learning techniques, individual stock features, and empirical data of Economic Input-Output (EIO) from Bureau of Economic Analysis (BEA) in the US to predict Granger causality of coupling US stocks. Limited Granger causalities are calculated as a small sample set compared to the target date set. Therefore a directed complex network is expected to be constructed. The generated directed stock network is planned to be analysed about its topological properties, stability and effects on individual stocks and industries. Suggestions towards financial market investment are expected to be provided based on the results in this study.

Financial data of listed companies and fundamental economical data are both available in each stock market and government websites. Efforts have been taken upon the researches such as the work of Patel et al. [PSTK15], which applied machine learning techniques to predict stock price movement, but most of them use correlations between stock price or return series, such measures are unable to provide direction information for building a directed graph of stock market. Granger causality test is one suitable measure but the computation is overwhelmingly complex so that no researchers have ever implemented this.

This chapter has probed into the feasibility of applying machine learning techniques helping to predict Granger causality based on samples of Granger causalities

that have been manually calculated. Here the word “predict” means estimation of some property that is not directly observed, rather than its common meaning of inferring something about the future. Unfortunately, over 3,000 listed companies yielding couples many orders of magnitude larger than the amount of sample data for human-beings can ever calculate. The scarcity of training data on these outcomes makes the application of machine learning techniques challenging.

This project overcome this challenge through a multi-step ”transfer learning” approach [PY⁺10], whereby a noisy but easily obtained proxy for sectoral association, the correlations of stock pairs, and fundamental indicators of listed companies are used to train a deep learning model. The model is then used to estimate Granger causalities based on very limited samples through a transferring process.

8.1.1 Motivation

Conducting Granger causality test between the price return series of all stock pairs is straightforward while not feasible due to the heavy-precondition for Granger causality test in time series analysis and the high time-complexity in computer programme, as this is an NP-hard problem. Hence, predicting Granger causality of the price return series of stock pairs using a training sample which contains manually calculated Granger causalities. However, compared to the large order of magnitude of total stock pairs, the realistic number of manually calculated Granger causalities are too less to be regarded as training samples. Enlightened by the recent work of Jean et al. (2016) which implements transfer learning and noisy proxy information performed unexpectedly well at predicting poverty, demonstrating that machine learning techniques are powerful to be applied in a setting with limited training data [JBX⁺16], therefore an exploration towards the directed network of stock market is motivated in this thesis, combines machine learning techniques, transfer learning, individual stock features, and empirical data of Economic Input-Output (EIO) from Bureau of Economic Analysis (BEA) in the US to predict Granger causalities of rest coupling US stocks. Therefore, the directed stock network is able to be constructed by considering predicted Granger causalities as the indicators of directions of edges.

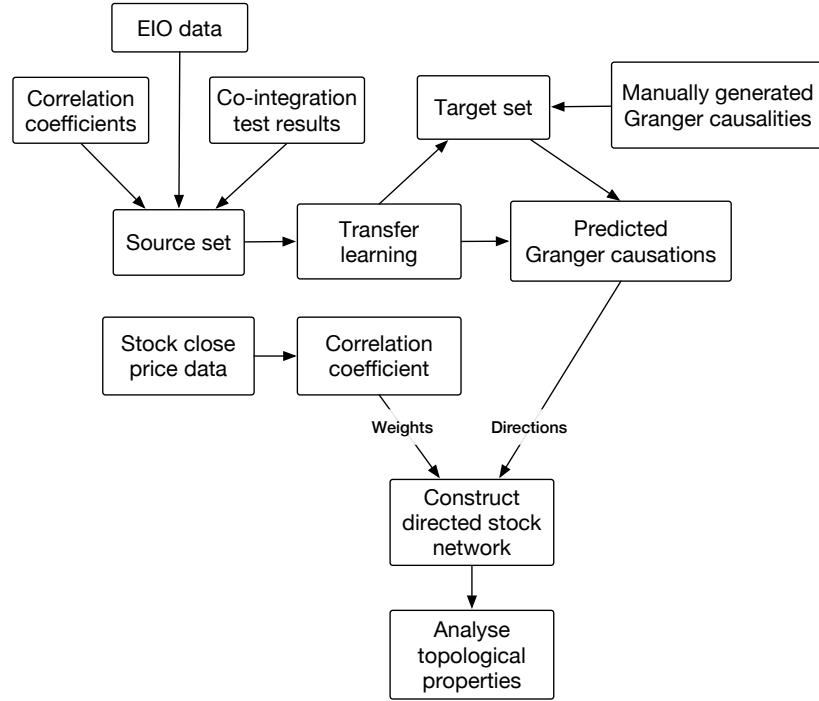


Figure 8.1: The methodology diagram of machine learning pathway

8.1.2 Objectives

The goal of the attempt in this chapter is to predict and reveal the Granger causality of price return series with machine learning techniques and utilise them into the construction and topological analysis of the directed stock network as so far no previous work has ever been attempted to construct a directed network of stock markets. While in hindsight this is not a successful attempt, conclusion will be drawn according to the results of prediction.

8.2 Methodology

8.2.1 Technical challenges in the pre-processing for network construction

A preliminary correlation matrix is generated for the co-integration test of two price return time series. Bivariate Granger causality test is heavy on the precondition of time series analysis and its time-complexity in computer programme is polynomial, as the amount of all coupling stock pair is $n(n - 1)/2$, while n is the number of stocks. There

are over 3,000 companies listing in NASDAQ, hence there should be millions of times for Granger causality tests and pre-process time series analyses to run in the computer programmes in order to construct the directed stock network.

However, in this chapter, machine learning techniques are applied to predict the precedence relations, i.e., predicted Granger causalities of every possible US stock pairs, based on a limited amount of actual Granger causalities calculated as training set. In addition to the fundamental indicators such as market capitalisation, P/B ratio, P/E ratio, etc., public empirical data of EIO are also implemented into the entire machine learning prediction process. Stocks are divided into industrial groups according to the summary level defined in the BEA. Transfer learning technique is applied as well and will be introduced in section 8.2.3. In addition, learning performances of each models are compared based on their predicting performances according to the ROC analysis.

8.2.2 Granger causality test

Granger causality test [Gra69] provides an asymmetrical measure for testing precedence relationship between two time series. The leitmotiv inside is that a time series can be described and analysed through a time-delayed auto-regressive model. Granger causality test tests whether the difference of a prediction to the time series from another time series through a multi-variate auto-regressive model is able to improve the prediction of the current behaviour of the time series, as the following forms illustrates:

$$x_t = \sum_{i=1}^{\infty} a_i x_{t-i} + c + \varepsilon_t \quad (8.1)$$

$$x_t = \sum_{i=1}^{\infty} a_i x_{t-i} + \sum_{j=1}^{\infty} b_j y_{t-j} + c' + \varepsilon'_t \quad (8.2)$$

Calculate the f-statistic using the following equation, the Granger causality is not significant if f-statistic is greater than the f-value:

$$F = \frac{(ESS_R - ESS_{UR})/q}{ESS_{UR}/(n-k)} \quad (8.3)$$

8.2.3 Transfer learning and ANN model

The most common and basic assumptions for the sampling of machine learning are: (1) the training sample and the test sample are both independent and identically distributed; (2) there must be enough available training samples [Ras04]. However, as aforementioned reasons in this chapter, the application of machine learning in stock market to predict Granger causalities is hard to satisfy these assumptions.

Transfer learning with existing knowledge to solve only one small target area labelled sample data even without data of learning problems, fundamentally relaxes the basic assumptions of conventional machine learning. Transfer learning can migrate the models which are applicable to big data sets to small data sets, identify the commonality of different problems, and then transfer the generalised model on customised data sets to achieve customised transfer objectives.

The initial set of parameters of ANN model that is trained in this thesis has 3 layers of neurons and 10 nodes in each layers. The activation function for each nodes is rectified linear unit (ReLU) [HSM⁺00], as the below expression shows:

$$f(x) = x^+ = \max(0, x) \quad (8.4)$$

During the training process, Adagrad optimiser [DHS11] with the learning rate of 0.01 are applied.

As the methodology diagram 8.1 illustrates, since only hundreds of times of Granger causality tests and the pre-works such as co-integration tests can be conducted towards randomly selected stock pairs within a reasonable period of time, the ANN model cannot be directly trained to predict Granger causalities of the rest stock pairs. According to the basic assumptions, there must be enough training samples.

For solving the scarcity of sample, this thesis applies the transfer learning approach and builds the source set for pre-training with EIO data, co-integration test data, stock fundamental data and correlation coefficient data which is regarded as the proxy for Granger causalities. The parameters of ANN model will be fine-tuned during the following optimisation stage, until an satisfying prediction accuracy for correlation coefficients is achieved.

In the first step of the transfer learning precess, the 3-layer ANN model previously trained is fine-tuned through the source set to predict Granger causalities given the corresponding EIO data and a small set of manually calculated Granger causality results. We treat this step of the transfer learning approach as a classification problem, of

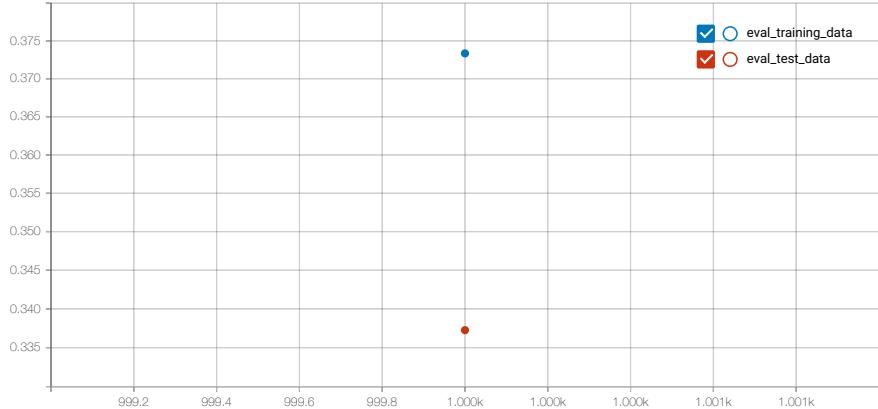
which the three classes of stock network directions correspond to forward, backward, and neutral. Given a stock pair $[A, B]$, a forward class corresponding to the price return fluctuation preceding direction from stock A to B and vice versa, while a neutral class indicates that there is no significant price return fluctuation preceding influence between stock A and B .

8.3 Results

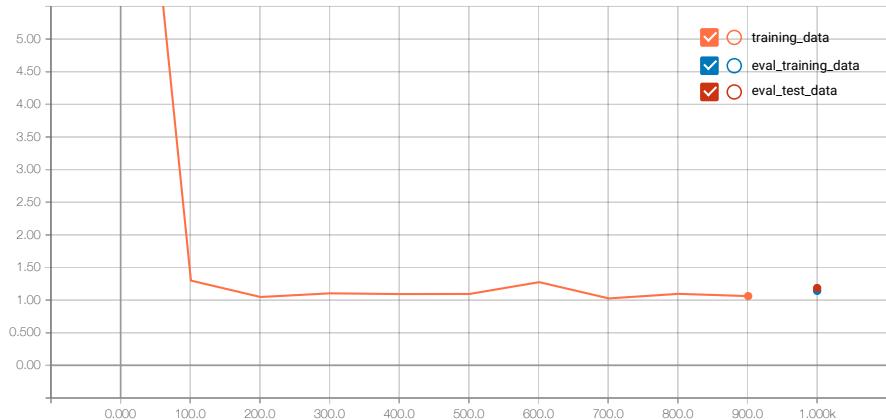
Figure 8.2a illustrates the results of accuracy under the circumstance of the initial ANN model, i.e., with 3 neuron layers and 10 nodes in each layer. Since the accuracy of prediction towards the correlation coefficients in training set and test set are around 0.374 and 0.337 respectively, the performance are even worth than random guess which should be 0.333 as there are three distinctive classes. The cross-entropy loss is calculated by using softmax cross entropy [AAB⁺15], and the average loss is calculated by loss divided by the batch size which is 50 set in the computer programme. According to the figure 8.2b and figure 8.2c, as more sample data input to the ANN model through iterations, the cross-entropy loss and average cross-entropy loss gradually decrease until the asymptotic lines of 50 and 1, which indicate the random-guess prediction. Similar results applied to all parameter combinations through the model optimisation approach of grid search.

8.4 Conclusion

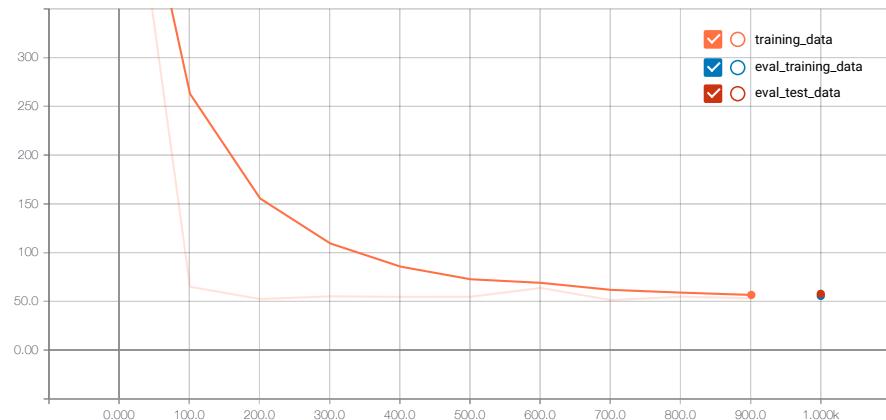
The machine learning pathway of the edge direction approach has been briefly presented. As a result, the underperformed outcomes in the first step of transfer learning indicate that the subsequent processes could not be performed. This thesis considers that the predictive patterns to the Granger causality beneath the data of stock price return correlation coefficients, stock fundamental and economical transactions are insignificant and therefore a new pathway of using direct demand and direct requirement from EIO data is explored as the main content of this thesis presents.



(a) Accuracy. The prediction accuracy upon training set and test set are 37.4% and 33.7% respectively for the trained ANN model during the first stage of transfer learning.



(b) Average cross-entropy loss. As more iterations process, the average loss converge to the value of 1, which is equivalent to the performance of random guess approach.



(c) Cross-entropy loss. Equals to the average loss multiply by the batch size 50.

Figure 8.2: Performance of prediction. Graphs are generated by *TensorBoard* [AAB⁺15].

Chapter 9

Conclusions and future work

9.1 Summary of results

This thesis constructed and studied the directed complex networks of US stock market in the year of 2016. From another perspective apart from the methodology presented in this thesis, the construction of the studied directed-weighted network can be also regarded as a network that removed the edges of stock-pairs that are weak in economical transactions and added the directions of edges of stock-pairs by the significance of direct demand or direct requirement from a conventional undirected-weighted stock network.

The essence of introducing the direction of edges is to uplift the difficulty for nodes to connect. Although the new kind of thresholds are based on the fundamental situations of stocks, other than the technical situations of the threshold of correlation coefficient, since the characteristics of topology properties have not changed significantly from conventional stock networks according to the preliminary research in this thesis, we can infer that the new fundamental edge thresholds have similar effect with the technical edge threshold. Furthermore, it does provide an advantageous horizon to elicit more potentially useful information contained in the edge directions. From the new horizon, this thesis is able to analyse on a higher dimensionality — topological property research and community detection with methods for directed networks which utilised the feature of edge directions. The resulting features of power-law and small-world for directed stock complex networks show continuity with the results in undirected stock complex networks researches. The study on community detection suggests "livelihood" and "production" are the most dominant and influential sectors in the stock market and the "finance" sector has extremely strong internal connections.

The partitioned communities are highly related with the economical activities among industries and indicate the potential cascading impact from a collapse of a specific firm or sector. The theoretical and practical contributions of aforementioned findings have been discussed.

9.2 Future work

In terms of future work, stock complex networks during a longer range of years can be generated and compared in together, the periods correspond to bull, bear, and stable market can be recognised and categorised for more critical analysis. According to Papadopoulos et al. (2012), the degrees of sub-networks of any power-law networks are not power-law distributed[PKS⁺12], hence for a strict demonstration of the power-law distribution for the degrees in stock networks, all stocks in the stock market should be considered in the best-case scenario, but also possible for financial market research. Additionally, more novel and advanced methods for determining the directions of edges to construct the directed complex networks of stock markets are expected to be proposed and implemented.

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Appendix A

Python code

The code files of this entire research is available to download on GitHub [Zha18].

A.1 stock_network.py

```
from __future__ import division
import logging
import logging.config
import sys, csv, time, requests, statsmodels, math
from sklearn.linear_model import LinearRegression
from statsmodels.tsa.stattools import coint, adfuller, grangercausalitytests
import statsmodels.api as sm
from scipy import stats
import scipy.special
from scipy.stats import describe
from scipy.linalg import circulant
from contextlib import contextmanager
from datetime import datetime, timedelta
from dateutil.parser import parse
import collections
import random
import scipy.stats as ss
import seaborn as sns
import matplotlib.pyplot as plt
from matplotlib.lines import Line2D
import matplotlib as mpl
import pylab
import powerlaw
import networkx as nx
from networkx.algorithms import community
import pandas as pd
import numpy as np
from core import SendEmail, ROOTPATH, sri_SP500_log_return, sri_SP500_close
from preprocess_stocks import lst_tickers_stp, LENTCKR, LENTRGL, df_codes_and_title, DICT_STP, getIndustryCodeByStockCode
sns.set(color_codes=True)
data_dir = ROOTPATH + r'/Codes'

def genPureDirectedGraph(theta_1, theta_2, mat_1, mat_2):
    G = nx.DiGraph()
    G.add_nodes_from(lst_tickers_stp)
    for i in lst_tickers_stp:
        matidx_i = EIO.industry_BEA_code_list.index(
            df_codes_and_title.loc[i, 'BEA'])
        for j in lst_tickers_stp:
            if i != j:
                matidx_j = EIO.industry_BEA_code_list.index(
                    df_codes_and_title.loc[j, 'BEA'])
                a = mat_1[matidx_i, matidx_j]
                b = mat_2[matidx_i, matidx_j]
                if a > 0.0 and a > theta_1:
                    G.add_edge(i, j)
                if b > 0.0 and b > theta_2:
```

```

        G.add_edge(j, i)
    return G

def genWDGraphFromPureDirectedGraph(PGD, return_list, threshold=-1):
    G = nx.DiGraph()
    G.add_nodes_from(lst_tickers_stp)
    for n, nbrs in PGD.adj.items():
        S1 = return_list[n]
        for nbr, eattr in nbrs.items():
            S2 = return_list[nbr]
            corr = S1.corr(S2)
            if corr >= threshold: G.add_edge(n, nbr, corr=corr)
    return G

def genPartCorrGraph(UGD):
    G = nx.DiGraph()
    G.add_nodes_from(lst_tickers_stp)
    for n, nbrs in UGD.adj.items():
        for nbr, eattr in nbrs.items():
            G.add_edge(n, nbr, weight=eattr['corr'])
    return G

def genEntCorrGraph():
    G = nx.Graph()
    G.add_nodes_from(lst_tickers_stp)
    for i in range(LENTCKR):
        S1 = df_stock_abr[lst_tickers_stp[i]]
        for j in range(i+1, LENTCKR):
            S2 = df_stock_abr[lst_tickers_stp[j]]
            G.add_edge(i, j, weight=S1.corr(S2))
    return G

def rmvEdgeAttrOfGraph(WG):
    G = WG.copy()
    for n, nbrs in G.adj.items():
        for nbr, eattr in nbrs.items():
            if 'corr' in eattr: del eattr['corr']
    return G

def rmvIndepNodesFromGraph(WholeG):
    G = WholeG.copy()
    for n in WholeG.nodes():
        if WholeG.degree(n) == 0: G.remove_node(n)
    return G

def _distance_matrix(L):
    Dmax = L/2

    D = list(range(Dmax+1))
    D += D[-2+(L%2):0:-1]

    return circulant(D)/Dmax

def _pd(d, p0, beta):
    return beta*p0 + (d <= p0)*(1-beta)

def watts_strogatz(L, p0, beta, directed=False, rngseed=1):
    rng = np.random.RandomState(rngseed)

    d = _distance_matrix(L)
    p = _pd(d, p0, beta)

    if directed:
        A = 1*(rng.random_sample(p.shape) < p)
        np.fill_diagonal(A, 0)
    else:
        upper = np.triu_indices(L, 1)

        A = np.zeros_like(p, dtype=int)
        A[upper] = 1*(rng.rand(len(upper[0])) < p[upper])
        A.T[upper] = A[upper]

    return A

dct_title_amt = dict(df_codes_and_title['Title'].value_counts())
dct_BEA_amt = dict(df_codes_and_title['BEA'].value_counts())

def genEIODirectMatrix(directType, tradeoff = True, to_log = True):
    global dct_title_amt
    global EIO_industry_title_list
    industry_list = EIO_industry_title_list
    EIO_direct_matrix = np.matrix(
        np.zeros(
            (len(industry_list),

```

```

        len(industry_list)),
        dtype=np.float64)
if directType is 'requirements':
    for i in range(len(industry_list)):
        for j in range(len(industry_list)):
            if EIO_matrix[i, j] > 0:
                m = np.float64(EIO_matrix[i, j]) / EIO_matrix[-1, j]
                if tradeoff and industry_list[i] in dct_title_amt:
                    m /= dct_title_amt[industry_list[i]]
                EIO_direct_matrix[i, j] = logarise(m) if to_log else m
elif directType is 'demands':
    for i in range(len(industry_list)):
        for j in range(len(industry_list)):
            if EIO_matrix[i, j] > 0:
                m = np.float64(EIO_matrix[i, j]) / EIO_matrix[i, -1]
                if tradeoff and industry_list[j] in dct_title_amt:
                    m /= dct_title_amt[industry_list[j]]
                EIO_direct_matrix[i, j] = logarise(m) if to_log else m
else: return None
return EIO_direct_matrix

def getAllMatrixContent(mat):
    arr = []
    for m in mat:
        arr = np.append(arr, np.array(m)[0])
    return arr

def getNonzeroMatrixContent(mat):
    arr = []
    for m in mat:
        ar_m = np.array(m)[0]
        ar_m = ar_m[ar_m!=0]
        arr = np.append(arr, ar_m)
    return arr

def genEdgeDensity(lst, bins=100):
    theta_thresholds = np.linspace(np.floor(min(lst)*10.0)/10.0, np.ceil(max(lst)*10.0)/10.0, bins)
    edge_densities = []
    n = 0
    LENLST_FLOAT = np.float(len(lst))
    for theta in theta_thresholds:
        n += 1
        edge_densities.append(sum(corr >= theta for corr in lst)/LENLST_FLOAT)
    return theta_thresholds, edge_densities

def logarise(n): return 0.0 if n == 0 else -1.0/np.log10(n)

def combineThresholds(thresholds_1, thresholds_2, mat_1, mat_2):
    LENMAT = mat_1.shape[0]
    df = pd.DataFrame(
        index=range(len(thresholds_1)*len(thresholds_2)),
        columns=['theta_DR', 'theta_DD', 'no_directions'])
    idx = 0
    for t1 in thresholds_1:
        exceeded = False
        for t2 in thresholds_2:
            cnt = 0
            if not exceeded:
                for i in range(LENMAT):
                    for j in range(LENMAT):
                        a = mat_1[i, j]
                        b = mat_2[i, j]
                        if (a > 0.0 and a > t1) or (b > 0.0 and b > t2):
                            cnt += 1
                if cnt == 0: exceeded = True
            df.iloc[idx, :] = [t1, t2, cnt]
            idx += 1
    return df

def combineThresholdsOfEIOAndCorrForAmtOfEdges(thresholds_eio, thresholds_corr, FG):
    global lst_tickers_stp
    df = pd.DataFrame(
        index=range(len(thresholds_eio)*len(thresholds_corr)),
        columns=['theta_EIO', 'theta_corr', 'no_edges'])
    idx = 0
    numrow = 0
    for t1 in thresholds_eio:
        exceeded = False
        for t2 in thresholds_corr:
            cnt = 0
            if not exceeded:
                for n, nbrs in FG.adj.items():
                    for nbr, eattr in nbrs.items():
                        if ('direct_requirement' in eattr and eattr['direct_requirement'] > t1) or

```

```

        ('direct_demand' in eattr and (eattr['direct_demand'] > t1)):
            if eattr['corr'] > t2: cnt += 1
        if cnt == 0: exceeded = True
        df.iloc[idx,:] = [t1, t2, cnt]
        idx += 1
    numrow += 1
return df

def combineThresholdsOfEIOAndCorrForIsWeaklyConnected(thresholds_eio, thresholds_corr, FG):
    global lst_tickers_stp
    df = pd.DataFrame()
    index=range(len(thresholds_eio)*len(thresholds_corr)),
    columns=['EIO', 'corr', 'is_weakly_connected'])
    idx = 0
    for t1 in thresholds_eio:
        for t2 in thresholds_corr:
            G = nx.DiGraph()
            G.add_nodes_from(lst_tickers_stp)
            for n, nbrs in FG.adj.items():
                for nbr, eattr in nbrs.items():
                    if ('direct_requirement' in eattr and eattr['direct_requirement'] > t1) or
                       ('direct_demand' in eattr and (eattr['direct_demand'] > t1)):
                        if eattr['corr'] > t2: G.add_edge(n, nbr)
            G = rmvInDepNodesFromGraph(G)
            if G.number_of.nodes() > 0:
                is_weakly_c = nx.is_weakly_connected(G)
                df.iloc[idx,:] = [t1, t2, is_weakly_c]
            else:
                df.iloc[idx,:] = [t1, t2, False]
            idx += 1
    return df

def continueCombineThresholdsOfEIOAndCorrForIsWeaklyConnected(thresholds_eio, thresholds_corr, FG, start_point):
    global df
    i = 0
    idx = start_point
    cnt = 0
    for t1 in thresholds_eio:
        for t2 in thresholds_corr:
            if i < start_point:
                i += 1
                continue
            G = nx.DiGraph()
            G.add_nodes_from(lst_tickers_stp)
            for n, nbrs in FG.adj.items():
                for nbr, eattr in nbrs.items():
                    if ('direct_requirement' in eattr and eattr['direct_requirement'] > t1) or
                       ('direct_demand' in eattr and (eattr['direct_demand'] > t1)):
                        if eattr['corr'] > t2: G.add_edge(n, nbr)
            G = rmvInDepNodesFromGraph(G)
            if G.number_of.nodes() > 0:
                is_weakly_c = nx.is_weakly_connected(G)
                df.iloc[idx,:] = [t1, t2, is_weakly_c]
            else:
                df.iloc[idx,:] = [t1, t2, False]
            idx += 1
        cnt += 1

FILE_EIO_2016 = ROOTPATH + '/Source/lx1/EIO_2016.csv'
EIO_matrix = np.matrix(np.genfromtxt(open(FILE_EIO_2016, 'rb'), delimiter=',', skip_header=2))
EIO_industry_BEAs_code_list = list(pd.read_csv(FILE_EIO_2016, nrows=0).columns)[-2]
EIO_industry_title_list = list(pd.read_csv(FILE_EIO_2016, skiprows=1).columns)[-2]
FILE_STOCK_ABR = ROOTPATH + '/Source/DF_STOCK_ABR.csv'
df_stock_abr = pd.read_csv(FILE_STOCK_ABR).set_index('Date')
df_stock_normal_return = pd.DataFrame(index=df_stock_abr.index, columns=df_stock_abr.columns)
for i in DICT_STP: df_stock_normal_return[i] = DICT_STP[i]['log_return']

EIO_direct_requirements_matrix = genEIODirectMatrix('requirements', tradeoff=True, to_log=True)
EIO_direct_demands_matrix = genEIODirectMatrix('demands', tradeoff=True, to_log=True)

ar_all_DR_Mat = getAllMatrixContent(EIO_direct_requirements_matrix)
ar_all_DD_Mat = getAllMatrixContent(EIO_direct_demands_matrix)

ar_all_DR_trans = [i for i in ar_all_DR_Mat]
ar_all_DD_trans = [i for i in ar_all_DD_Mat]

theta_thresholds_DR_all, edge_densities_DR_all = genEdgeDensity(ar_all_DR_trans, 100)
theta_thresholds_DD_all, edge_densities_DD_all = genEdgeDensity(ar_all_DD_trans, 100)

ar_nonzero_DR_Mat = getNonzeroMatrixContent(EIO_direct_requirements_matrix)
ar_nonzero_DD_Mat = getNonzeroMatrixContent(EIO_direct_demands_matrix)

ar_nonzero_DR_trans = [i for i in ar_nonzero_DR_Mat]
ar_nonzero_DD_trans = [i for i in ar_nonzero_DD_Mat]

```

```

theta_thresholds_DR, edge_densities_DR = genEdgeDensity(ar_nonzero_DR_trans, 100)
theta_thresholds_DD, edge_densities_DD = genEdgeDensity(ar_nonzero_DD_trans, 100)

b1 = np.append(1.0, edge_densities_DR.all)
b1[1] = b1[2]
b2 = np.append(0, theta_thresholds_DR.all)

x_dashline = 0.136
fig = plt.figure()
ax = fig.add_subplot(2,1,1)
ax.set_xlabel('threshold')
ax.set_ylabel('Transaction-density')
ax.set_xlim(left=-0.05, right=1.2)
ax.set_title('Normalised-Direct-Requirement', fontsize='large')
dashed_line = Line2D([x_dashline, x_dashline], [-1.05, 1.05], linestyle = '--',
    linewidth = 1, color = [0.3,0.3,0.3], zorder = 1, transform = ax.transData)
ax.lines.append(dashed_line)
ax.plot(b2, b1, color='blue', lw=2)
ax = fig.add_subplot(2,1,2)
ax.set_xlabel('threshold')
ax.set_ylabel('Transaction-density')
ax.set_title('Normalised-Direct-Demand', fontsize='large')
dashed_line = Line2D([x_dashline, x_dashline], [-0.05, 1.05], linestyle = '--',
    linewidth = 1, color = [0.3,0.3,0.3], zorder = 1, transform = ax.transData)
ax.lines.append(dashed_line)
ax.set_xlim(left=-0.05, right=1.2)
ax.plot(b2, b1, color='blue', lw=2)
fig.tight_layout()

df_combined_thresholds = combineThresholds(
    theta_thresholds_DR,
    theta_thresholds_DD,
    EIO_direct_requirements_matrix,
    EIO_direct_demands_matrix)

pt = df_combined_thresholds.pivot_table(index='theta_DR', columns='theta_DD', values='no_directions', aggfunc=np.sum)
f, ax = plt.subplots(figsize = (10, 4))
sns.heatmap(pt.iloc[:30,:20], cmap='rainbow', linewidths = 0.05, ax = ax)
ax.set_title('Amounts_of_directions_per_DR-threshold_and_DD-threshold')
ax.set_xlabel('theta_DD')
ax.set_ylabel('theta_DR')

def genFullGraph(stock_return_df):
    global lst_tickers_stp
    global EIO_industry_BEAT_code_list
    global EIO_direct_requirements_matrix
    G = nx.DiGraph()
    G.add_nodes_from(lst_tickers_stp)
    for i in lst_tickers_stp:
        matidx_i = EIO_industry_BEAT_code_list.index(df_codes_and_title.loc[i, 'BEA'])
        S1 = stock_return_df[i]
        for j in lst_tickers_stp:
            if i != j:
                matidx_j = EIO_industry_BEAT_code_list.index(df_codes_and_title.loc[j, 'BEA'])
                if EIO_direct_requirements_matrix[matidx_i, matidx_j] > 0:
                    G.add_edge(i, j, direct_requirement = EIO_direct_requirements_matrix[matidx_i, matidx_j])
                if EIO_direct_demands_matrix[matidx_j, matidx_i] > 0:
                    G.add_edge(i, j, direct_demand = EIO_direct_demands_matrix[matidx_j, matidx_i])
            if G.has_edge(i, j): G.add_edge(i, j, corr=S1.corr(stock_return_df[j]))
    return G

FullG = genFullGraph(df_stock_normal_return)
direct_requirements_CN = []
direct_demands_CN = []
for n, nbrs in FullG.adj.items():
    for nbr, eattr in nbrs.items():
        if 'direct_requirement' in eattr.keys():
            direct_requirements_CN.append(eattr['direct_requirement'])
        if 'direct_demand' in eattr.keys():
            direct_demands_CN.append(eattr['direct_demand'])

corr_coeff_CN = []
for n, nbrs in FullG.adj.items():
    for nbr, eattr in nbrs.items():
        corr_coeff_CN.append(eattr['corr'])

plt.hist(corr_coeff_CN, density=1, bins=260, histtype='bar')
plt.axis([-0.5, 1, 0, 3.2])
plt.xlabel('correlation')
plt.ylabel('p(correlation)')

describe(corr_coeff_CN)

```

```

corr_mean = np.mean(corr_coef_CN)
corr_std = np.std(corr_coef_CN)
corr_coef_CN_00 = [(i - corr_mean)/corr_std for i in corr_coef_CN]

stats.probplot(corr_coef_CN, dist='norm', plot=pylab)
pylab.show()

sm.qqplot(np.array(corr_coef_CN_00), line='45')
pylab.show()

ss.kstest(corr_coef_CN_00, 'norm')

theta_thresholds_corr, edge_densities_corr = genEdgeDensity(corr_coef_CN, 100)

fig = plt.figure()
ax = fig.add_subplot(1,1,1)
ax.set_xlabel('threshold')
ax.set_ylabel('Edge-density')
ax.set_title('Correlation_Coefficient', fontsize='large')
ax.plot(theta_thresholds_corr, edge_densities_corr, color='blue', lw=2)
fig.tight_layout()

recalc = False
npzfile_name = data_dir + '/pt_cteac_0719.npz'
pt_cteac = None
if recalc == True:
    df = pd.DataFrame(
        index=range(len(theta_thresholds_DR)*len(theta_thresholds_corr)),
        columns=['EIO', 'corr', 'is_weakly_connected'])
    continueCombineThresholdsOfEIOAndCorrForIsWeaklyConnected(
        theta_thresholds_DR, theta_thresholds_corr, FullG, 0)
    df_cteac = df.copy()
    pt_cteac = df_cteac.pivot_table(
        index = 'EIO', columns='corr',
        values = 'is_weakly_connected', aggfunc=np.sum)
    outfile = open(npzfile_name, 'wb')
    np.savez(outfile, ar_cteac=pt_cteac, col=pt_cteac.columns, ind=pt_cteac.index)
    outfile.close()
else:
    infile = open(npzfile_name, 'rb')
    npzfile = np.load(infile)
    infile.close()
    ar_cteac = npzfile['ar_cteac']
    pt_cteac = pd.DataFrame(ar_cteac)
    pt_cteac.columns = npzfile['col']
    pt_cteac.index = npzfile['ind']

f, ax = plt.subplots(figsize = (10, 4))
sns.heatmap(pt_cteac.iloc[5:50,20:90], cmap='rainbow', linewidths = 0.05, ax = ax)
ax.set_title('Amounts_of_directions_per_DR-threshold_and_DD-threshold')
ax.set_xlabel('corr')
ax.set_ylabel('EIO');

recalc = True
npzfile_name = data_dir + '/pt_toeacfaoe_0719.npz'
pt_toeacfaoe = None
if recalc == True:
    df_toeacfaoe = combineThresholdsOfEIOAndCorrForAmtOfEdges(
        theta_thresholds_DR, theta_thresholds_corr, FullG)
    pt_toeacfaoe = df_toeacfaoe.pivot_table(
        index = 'theta_EIO', columns='theta_corr',
        values = 'no.edges', aggfunc=np.sum)
    outfile = open(npzfile_name, 'wb')
    np.savez(outfile, ar_toeacfaoe=pt_toeacfaoe,
             col=pt_toeacfaoe.columns, ind=pt_toeacfaoe.index)
    outfile.close()
else:
    infile = open(npzfile_name, 'rb')
    npzfile = np.load(infile)
    infile.close()
    ar_toeacfaoe = npzfile['ar_toeacfaoe']
    pt_toeacfaoe = pd.DataFrame(ar_toeacfaoe)
    pt_toeacfaoe.columns = npzfile['col']
    pt_toeacfaoe.index = npzfile['ind']

pt_toeacfaoe.index = [round(i, 4) for i in pt_toeacfaoe.index]
pt_toeacfaoe.columns = [round(i, 4) for i in pt_toeacfaoe.columns]

f, ax = plt.subplots(figsize = (10, 4))
sns.heatmap(pt_toeacfaoe.iloc[:24,:81], cmap='gist_ncar', linewidths = 0.05, ax = ax)
ax.set_xlabel(r'$\theta_{corr}$')
ax.set_ylabel(r'$\theta_{EIO}$');

threshold_eio = 0.29225

```

```

threshold_corr = 0.378705
DiUnwtG = genPureDedirectedGraph(
    threshold_eio,
    threshold_eio,
    EIO_direct_requirements_matrix,
    EIO_direct_demands_matrix)

G = genWDGraphFromPureDirectedGraph(DiUnwtG, df_stock_normal_return, threshold_corr)
nonodes = G.number_of_nodes()
noedges = G.number_of_edges()
DiG_pureedge = rmvEdgeAttrOfGraph(G)
DiG_connected = rmvIndepNodesFromGraph(DiG_pureedge)

def genConventionalGraph(theta, return_list):
    global LENTCKR
    global lst_tickers_stp
    G = nx.Graph()
    G.add_nodes_from(lst_tickers_stp)
    for i in range(LENTCKR):
        T1 = lst_tickers_stp[i]
        S1 = return_list[T1]
        for j in range(i+1, LENTCKR):
            T2 = lst_tickers_stp[j]
            S2 = return_list[T2]
            corr = S1.corr(S2)
            if corr > theta: G.add_edge(T1, T2, corr=corr)
    return G

G_conv = genConventionalGraph(0.4983, df_stock_normal_return)
G_conv.number_of_edges()

data = [d for n, d in G.out_degree()]
plt.hist(data, density=1, bins=50, histtype='bar');
fit = powerlaw.Fit(data)
fit.distribution_compare('power-law', 'lognormal')

fig4 = fit.plot_ccdf(linewidth = 2)
fit.power_law.plot_ccdf(ax = fig4, color = 'r', linestyle = '--');
fig4.set_xlabel('centrality')
fig4.set_ylabel('$p(X \geq x)$')
fig4.legend(('CCDF', 'Power-law fit'))
set_size(4,4,fig4)

data = [d for n, d in G_rd.out_degree()]
plt.hist(data, density=1, bins=50, histtype='bar');

stats.probplot([d for n, d in G_rd.out_degree()], dist='norm', plot=pylab)

fig = sns.distplot([d for n, d in G_rd.out_degree()])
fig.set_xlabel('out-degree')
fig.set_ylabel('p(out-degree)')

data = [d for n, d in G_ws.mat.out_degree()]
plt.hist(data, density=1, bins=50, histtype='barstacked');

data = [d for n, d in G_ws.mat.out_degree() if d > 0]
powerlaw.plot.pdf(data, linear_bins = False, color = 'b');

fig = plt.figure()
ax = fig.add_subplot(1,1,1)
data = [d for n, d in G.out_degree() if d > 0]
powerlaw.plot.pdf(data, linear_bins = False, color = 'b')
ax.set_xlabel('out-degree')
ax.set_ylabel('p(out-degree)')
set_size(4,4,ax)

data = [d for n, d in G.in_degree() if d > 0]
powerlaw.plot.pdf(data, linear_bins = False, color = 'b');

data = [d for n, d in G.degree() if d > 0]
powerlaw.plot.pdf(data, linear_bins = False, color = 'b');

p0 = np.average([i[1] for i in G.out_degree()])/(nonodes-1)
ws_mat = watts_strogatz(L=nonodes, p0=p0, beta=0.5, directed=True)
G_ws_mat=nx.from_numpy_matrix(ws_mat, create_using=nx.DiGraph())
G_ws_mat.number_of_edges()

p = noedges / nonodes / (nonodes-1)
G_rd = nx.generators.gnp_random_graph(nonodes, p=p, directed=True)
G_rd.number_of_edges()

def calGlobalEfficiency(G, lst_nodes, N):
    shortest_path = nx.shortest_path(G)
    acc = 0.0

```

```

for i in lst_nodes:
    for j in lst_nodes:
        if i != j and (j in shortest_path[i]):
            acc += 1.0/(len(shortest_path[i][j])-1)
return acc/N/(N-1)

def calLocalEfficiency(G):
    UndiG = G.to_undirected()
    lst_nodes = G.nodes()
    acc = 0.0
    for i in lst_nodes:
        nodes_g = list(UndiG[i])
        n = len(nodes_g)
        if n > 0:
            acc += calGlobalEfficiency(G.subgraph(nodes_g), nodes_g, n)
    return acc/G.number_of_nodes()

calGlobalEfficiency(DiG_connected, G.number_of_nodes())
calGlobalEfficiency(G_ws_mat)
callLocalEfficiency(G)

def detectCommunityForDirectedGraph(G):
    lst_node = list(G.nodes)
    NONODES = G.number_of_nodes()
    NOEDGES = G.number_of_edges()
    NOIINDEGREES = G.in_degree()
    NOOUTDEGREES = G.out_degree()
    overall_asgn = [(0, 0)] * NONODES

    def getNodeSpace(node_space, upd_asgn, val):
        return [node_space[i] for i in range(len(upd_asgn)) if upd_asgn[i] == val]

    def interateBisection(mod_mat, node_space, generation_mark):
        nonlocal G
        nonlocal overall_asgn
        upd_asgn = subdivideCommunities(mod_mat)

        if len(np.unique(upd_asgn)) == 1: return
        delta_Q = calDeltaQ(upd_asgn, mod_mat)
        if delta_Q < 0: return
        node_space_1 = getNodeSpace(node_space, upd_asgn, -1)
        if len(node_space_1) == 0: return
        updCommunityAssignment(node_space_1, upd_asgn, generation_mark)
        mod_mat_1 = genGeneralisedModularityMatrix(node_space_1)
        interateBisection(mod_mat_1, node_space_1, generation_mark+1)
        node_space_2 = getNodeSpace(node_space, upd_asgn, 1)
        if len(node_space_2) == 0: return
        updCommunityAssignment(node.space_2, upd_asgn, generation_mark)
        mod_mat_2 = genGeneralisedModularityMatrix(node.space_2)
        interateBisection(mod_mat_2, node.space_2, generation_mark+1)
    return

    def genGeneralisedModularityMatrix(node_space):# Subgraph
        nonlocal G
        nonlocal lst_node
        nonlocal NOEDGES
        nonlocal NOIINDEGREES
        nonlocal NOOUTDEGREES
        nonlocal overall_asgn
        LENNODESPECE = len(node_space)
        mod_mat = np.matrix(np.zeros((LENNODESPECE, LENNODESPECE), dtype=np.float64))
        for i in range(LENNODESPECE):
            tckr_i = lst_node[node_space[i]]
            for j in range(LENNODESPECE):
                tckr_j = lst_node[node_space[j]]
                Bij = G.has_edge(tckr_j, tckr_i) - NOIINDEGREES[tckr_i] * NOOUTDEGREES[tckr_j] / NOEDGES
                if overall_asgn[node_space[i]] == overall_asgn[node_space[j]]:
                    Ck = 0.0
                    for k in node_space:
                        tckr_k = lst_node[k]
                        Ck += G.has_edge(tckr_k, tckr_i) + G.has_edge(tckr_i, tckr_k) - (NOINDEGREES[tckr_i] * NOOUTDEGREES[tckr_k] + NOINDEGREES[tckr_k] * NOOUTDEGREES[tckr_i]) / NOEDGES
                    mod_mat[i, j] = Bij - Ck / 2.0
                else: mod_mat[i, j] = Bij
        return mod_mat

    def updCommunityAssignment(node_space, upd_asgn, generation_mark):
        nonlocal overall_asgn
        global asgn_history
        inreval_1 = 0
        inreval_2 = 0
        lst_gener_asgn = []
        for asgn in overall_asgn:
            if asgn[0] == generation_mark:
                lst_gener_asgn.append(asgn[1])

```

```

for i in range(len(node_space)):
    if i not in lst_gener_asgn:
        inreval_1 = i
        break
if upd_asgn.count(1) == 0: inreval_2 = inreval_1
else:
    for i in range(len(node_space)):
        if i not in lst_gener_asgn:
            inreval_2 = i
            break
    for i in range(len(node_space)):
        if upd_asgn[i] == 1: overall_asgn[node_space[i]] = (generation_mark, inreval_1)
        if upd_asgn[i] == -1: overall_asgn[node_space[i]] = (generation_mark, inreval_2)
        asgn_history.append(overall_asgn.copy())

def subdivideCommunities(mod_mat):
    sym_mat = mod_mat + mod_mat.T
    w, v = np.linalg.eigh(sym_mat)
    eigv = v[:, len(w)-1]
    return [np.sign(v.tolist()[0][0]) for v in eigv]

def calDirectedGraphModularity(assignment):
    nonlocal G
    nonlocal lst_node
    nonlocal NONODES
    nonlocal NOEDGES
    nonlocal NOINDEGREES
    nonlocal NOOUTDEGREES
    Q = 0.0
    for i in range(NONODES):
        for j in range(NONODES):
            if assignment[i] == assignment[j]:
                Q += G.has_edge(lst_node[j], lst_node[i]) - NOINDEGREES[lst_node[i]] * NOOUTDEGREES[lst_node[j]] / NOEDGES
    return Q / NOEDGES

def calDeltaQ(upd_asgn, Bg):
    nonlocal NOEDGES
    sg = np.matrix(upd_asgn)
    return 0.25/NOEDGES*np.dot(np.dot(sg, (Bg+Bg.T)), sg.T)[0,0]

MODMAT = np.matrix(np.zeros((NONODES, NONODES), dtype=np.float64))
for i in range(NONODES):
    for j in range(NONODES):
        MODMAT[i, j] = G.has_edge(lst_node[j], lst_node[i]) - NOINDEGREES[lst_node[i]] * NOOUTDEGREES[lst_node[j]] / NOEDGES
interateBisection(MODMAT, list(np.arange(NONODES)), 1)
return overall_asgn, calDirectedGraphModularity(overall_asgn)

def calModularity(assignment):
    global G
    global lst_node
    global NONODES
    global NOEDGES
    global NOINDEGREES
    global NOOUTDEGREES
    Q = 0.0
    for i in range(NONODES):
        for j in range(NONODES):
            if assignment[i] == assignment[j]:
                Q += G.has_edge(lst_node[j], lst_node[i]) - NOINDEGREES[lst_node[i]] * NOOUTDEGREES[lst_node[j]] / NOEDGES
    return Q / NOEDGES

lst_node = list(G.nodes())
NONODES = G.number_of_nodes()
NOEDGES = G.number_of_edges()
NOINDEGREES = G.in_degree()
NOOUTDEGREES = G.out_degree()

over_best_asgn = [0] * len(lst_tickers_stp)
for i in range(len(lst_tickers_stp)):
    over_best_asgn[i] = int(G.node[lst_tickers_stp[i]]['community'])

best_asgn = over_best_asgn.copy()
origin_mod = calModularity(best_asgn)
for i in range(len(best_asgn)):
    asgn = best_asgn[i]
    for uniq in uniq_asgn:
        if asgn != uniq:
            best_asgn[i] = uniq
            new_mod = calModularity(best_asgn)
            if new_mod > origin_mod:
                origin_mod = new_mod
                asgn = uniq
            else: best_asgn[i] = asgn

```

```

lst_tckr_nonzero = [i[0] for i in G.degree if i[1]>0]
rdmchosen_tickers = np.random.choice(lst_tckr_nonzero, 1, replace=False)
nonzerodeg_subG = G.subgraph(lst_tckr_nonzero).copy()

asgn.history = []
overall_asgn, modularity = detectCommunityForDirectedGraph(nonzerodeg_subG)

stp_group_tckr_index = sri_overall_asgn[sri_overall_asgn == v_c.index[0]].index.tolist()
stp_group_tckr = [lst_tickers_stp[i] for i in stp_group_tckr_index]
stp_group_indcode = getIndustryCodeByStockCode(stp_group_tckr, code_type='Title')
sri_community_1 = pd.Series(stp_group_indcode).value_counts()
stp_group_tckr_index = sri_overall_asgn[sri_overall_asgn == v_c.index[1]].index.tolist()
stp_group_tckr = [lst_tickers_stp[i] for i in stp_group_tckr_index]
stp_group_indcode = getIndustryCodeByStockCode(stp_group_tckr, code_type='Title')
sri_community_2 = pd.Series(stp_group_indcode).value_counts()
stp_group_tckr_index = sri_overall_asgn[sri_overall_asgn == v_c.index[2]].index.tolist()
stp_group_tckr = [lst_tickers_stp[i] for i in stp_group_tckr_index]
stp_group_indcode = getIndustryCodeByStockCode(stp_group_tckr, code_type='Title')
sri_community_3 = pd.Series(stp_group_indcode).value_counts()
stp_group_tckr_index = sri_overall_asgn[sri_overall_asgn == v_c.index[3]].index.tolist()
stp_group_tckr = [lst_tickers_stp[i] for i in stp_group_tckr_index]
stp_group_indcode = getIndustryCodeByStockCode(stp_group_tckr, code_type='Title')
sri_community_4 = pd.Series(stp_group_indcode).value_counts()
stp_group_tckr_index = sri_overall_asgn[sri_overall_asgn == v_c.index[4]].index.tolist()
stp_group_tckr = [lst_tickers_stp[i] for i in stp_group_tckr_index]
stp_group_indcode = getIndustryCodeByStockCode(stp_group_tckr, code_type='Title')
sri_community_5 = pd.Series(stp_group_indcode).value_counts()

stp_group_tckr_index = []
for i in range(5,11): stp_group_tckr_index += sri_overall_asgn[sri_overall_asgn == v_c.index[i]].index.tolist()
stp_group_tckr = [lst_tickers_stp[i] for i in stp_group_tckr_index]
stp_group_indcode = getIndustryCodeByStockCode(stp_group_tckr, code_type='Title')
sri_community_6 = pd.Series(stp_group_indcode).value_counts()

uniq.ind = np.unique(df_codes_and_title.Title)

lst_community_1 = []
lst_community_2 = []
lst_community_3 = []
lst_community_4 = []
lst_community_5 = []
lst_community_6 = []
for ind in uniq.ind:
    if ind in sri_community_1.index: lst_community_1.append(sri_community_1[ind])
    else: lst_community_1.append(0)
    if ind in sri_community_2.index: lst_community_2.append(sri_community_2[ind])
    else: lst_community_2.append(0)
    if ind in sri_community_3.index: lst_community_3.append(sri_community_3[ind])
    else: lst_community_3.append(0)
    if ind in sri_community_4.index: lst_community_4.append(sri_community_4[ind])
    else: lst_community_4.append(0)
    if ind in sri_community_5.index: lst_community_5.append(sri_community_5[ind])
    else: lst_community_5.append(0)
    if ind in sri_community_6.index: lst_community_6.append(sri_community_6[ind])
    else: lst_community_6.append(0)

lst2_sector = [None] * len(uniq.ind)
for i in range(len(uniq.ind)):
    lst2_sector[i] = []
    if uniq.ind[i] in sri_community_1.index: lst2_sector[i].append(sri_community_1[uniq.ind[i]])
    else: lst2_sector[i].append(0)
    if uniq.ind[i] in sri_community_2.index: lst2_sector[i].append(sri_community_2[uniq.ind[i]])
    else: lst2_sector[i].append(0)
    if uniq.ind[i] in sri_community_3.index: lst2_sector[i].append(sri_community_3[uniq.ind[i]])
    else: lst2_sector[i].append(0)
    if uniq.ind[i] in sri_community_4.index: lst2_sector[i].append(sri_community_4[uniq.ind[i]])
    else: lst2_sector[i].append(0)
    if uniq.ind[i] in sri_community_5.index: lst2_sector[i].append(sri_community_5[uniq.ind[i]])
    else: lst2_sector[i].append(0)
    if uniq.ind[i] in sri_community_6.index: lst2_sector[i].append(sri_community_6[uniq.ind[i]])
    else: lst2_sector[i].append(0)

idx = np.arange(6)
plt.figure(figsize=(15,15))

colors = list(dict(mpl.colors.BASE.COLORS, **mpl.colors.CSS4.COLORS).values())
idx = np.arange(6)
plt.figure(figsize=(10,10))
p = []
for i in range(len(uniq.ind)):
    bottom = [0] * 6
    for j in range(i): bottom = [a+b for a, b in zip(bottom, np.array(lst2_sector[j]))]
    p.append(plt.bar(idx, lst2_sector[i], bottom=bottom, color=colors[np.random.randint(len(colors))]))
plt.xticks(idx, ['C1', 'C2', 'C3', 'C4', 'C5', 'Others'])

```

```

idx = np.arange(len(uniq.ind))
plt.figure(figsize=(15,15))
p1 = plt.bar(idx, lst.community_1, color=(0.85, 0.5176, 1))
p2 = plt.bar(idx, lst.community_2, bottom=lst.community_1, color=(0.553, 0.753, 0.0863))
p3 = plt.bar(idx, lst.community_3,
             bottom = np.array(lst.community_1) + np.array(lst.community_2), color = (0.4157, 0.7608, 1))
p4 = plt.bar(idx, lst.community_4,
             bottom = np.array(lst.community_1) + np.array(lst.community_2) + np.array(lst.community_3), color = [0.937255,0.851,0.253])
p5 = plt.bar(idx, lst.community_5,
             bottom = np.array(lst.community_1) + np.array(lst.community_2)+np.array(lst.community_3) +
             np.array(lst.community_4), color = [0.898,0.5294,0.1294])
p6 = plt.bar(idx, lst.community_6,
             bottom = np.array(lst.community_1) + np.array(lst.community_2) + np.array(lst.community_3) +
             np.array(lst.community_4) + np.array(lst.community_5), color = [0.283,0.2823,0.282])
plt.xticks(idx, uniq.ind, rotation=90)
plt.legend((p1[0], p2[0], p3[0], p4[0], p5[0], p6[0]), ('Community_1', 'Community_2',
'Community_3', 'Community_4', 'Community_5', 'Unclustered'));

A.2 ml_transfer.py

import sys, csv, time, requests, statsmodels, math
from datetime import datetime, timedelta
from core import LocateIdx, Polygonal, Triangular, ROOTPATH, DROPLIST, df_source
from preprocess_stocks import lst_tickers_stp, LENTCKR, LENTRGL
from sampling_granger import lst_rdm_pair, srs_res_sample
import tensorflow as tf
from sklearn.model_selection import StratifiedKFold, KFold, train_test_split
from sklearn.metrics import mean_squared_error
from sklearn.utils import shuffle
from sklearn.base import clone
import networkx as nx
import pandas as pd
import numpy as np

skfolds = StratifiedKFold(n_splits=3, random_state=42)
kf = KFold(n_splits=3, shuffle = True)

df_sample = pd.DataFrame(columns=df_source.columns)
for rdm_pair in lst_rdm_pair:
    idx = LocateIdx(rdm_pair[0], rdm_pair[1], num_of_obj=LENTCKR)
    df_sample = df_sample.append(df_source.iloc[idx,:])
df_sample = df_sample.reset_index(drop=True)
for i in range(len(srs_res_sample)):
    if srs_res_sample[i] == -1:
        srs_res_sample[i] = 2
df_sample['causality'] = srs_res_sample
df_sample['corr_lbl'] = 0
cnt = 0
sri_corr = df_sample['corr']
for i in range(len(sri_corr)):
    if sri_corr[i] > 0.8:
        df_sample.loc[i,'corr_lbl'] = 1
    elif sri_corr[i] > 0.5:
        df_sample.loc[i,'corr_lbl'] = 1
dnn_rgs.fit(x=X_train, y=y_train, batch_size=50, steps=40000)

corr_lbl = tf.feature_column.numeric_column('corr_lbl')
coint_pvalue = tf.feature_column.numeric_column('coint_pvalue')
ieas = tf.feature_column.numeric_column('ieas')
pricetorevenue = tf.feature_column.numeric_column('pricetorevenue')
marketcap = tf.feature_column.numeric_column('marketcap')
pricetobook = tf.feature_column.numeric_column('pricetobook')
pricetoearnings = tf.feature_column.numeric_column('pricetoearnings')
beta = tf.feature_column.numeric_column('beta')

model_dir = ROOTPATH + r'/Stock_CN/ml_model_data/ann_01.csv'
deep_columns = [
    coint_pvalue,
    ieas,
    pricetorevenue,
    marketcap,
    pricetobook,
    pricetoearnings,
    beta
]
estimator = tf.estimator.DNNRegressor(
    model_dir=model_dir,
    feature_columns=deep_columns,

```

```

hidden_units=[10,10],
n_classes=3
)

col.indpd = ['ieas', 'pricetorevenue', 'marketcap', 'pricetobook', 'pricetoearnings', 'beta']
col.tgdpd = 'corr'

df_sample_sf1 = shuffle(df_sample).reset_index(drop=True)
arr_uniq_lbl = np.unique(df_sample['causality'])
lst_res_sample = list(df_sample['causality'])
lst_uniq_lbl_cnt = []
for i in range(len(arr_uniq_lbl)):
    lst_uniq_lbl_cnt.append(lst_res_sample.count(i))
for i in range(len(lst_uniq_lbl_cnt)):
    for j in range(lst_uniq_lbl_cnt[i]-min(lst_uniq_lbl_cnt)):
        df_sample_sf1 = df_sample_sf1.drop(df_sample_sf1[df_sample_sf1['causality']==i].iloc[0].name)

df_sample_sf1 = shuffle(df_sample_sf1).reset_index(drop=True)
df_sample_sf1_a = df_sample_sf1.loc[:2403,:].reset_index(drop=True)
df_sample_sf1_b = df_sample_sf1.loc[2403:,:].reset_index(drop=True)
X_train = df_sample_sf1_a.loc[:, col.indpd].reset_index(drop=True)
y_train = df_sample_sf1_a.loc[:, col.tgdpd].reset_index(drop=True)
X_eval = df_sample_sf1_b.loc[:, col.indpd].reset_index(drop=True)
y_eval = df_sample_sf1_b.loc[:, col.tgdpd].reset_index(drop=True)

train_input_fn = tf.estimator.inputs.numpy_input_fn({
    'ieas': X_train['ieas'],
    'pricetorevenue': X_train['pricetorevenue'],
    'marketcap': X_train['marketcap'],
    'pricetobook': X_train['pricetobook'],
    'pricetoearnings': X_train['pricetoearnings'],
    'beta': X_train['beta'],
},
y_train, batch_size=50,
num_epochs=None, shuffle=True
)

test_input_fn = tf.estimator.inputs.numpy_input_fn({
    'ieas': X_train['ieas'],
    'pricetorevenue': X_train['pricetorevenue'],
    'marketcap': X_train['marketcap'],
    'pricetobook': X_train['pricetobook'],
    'pricetoearnings': X_train['pricetoearnings'],
    'beta': X_train['beta'],
},
y_train, batch_size=50,
num_epochs=40000, shuffle=False
)

eval_input_fn = tf.estimator.inputs.numpy_input_fn({
    'ieas': X_eval['ieas'],
    'pricetorevenue': X_eval['pricetorevenue'],
    'marketcap': X_eval['marketcap'],
    'pricetobook': X_eval['pricetobook'],
    'pricetoearnings': X_eval['pricetoearnings'],
    'beta': X_eval['beta'],
},
y_eval, batch_size=50,
num_epochs=40000, shuffle=False
)

estimator.train(input_fn=train_input_fn, steps=1000)

train_metrics = estimator.evaluate(input_fn=test_input_fn, name='training_data')
eval_metrics = estimator.evaluate(input_fn=eval_input_fn, name='test_data')

df_source_sf1_3 = df_source_sf1.iloc[int(len(df_source_sf1)/2)+10001:int(len(df_source_sf1)/2+10050)].reset_index()
X_pred = df_source_sf1_3.loc[:, ['ieas', 'coint.pvalue']]
y_pred = df_source_sf1_3.loc[:, 'corr']

pred_input_fn = tf.estimator.inputs.numpy_input_fn({
    'ieas': X_pred['ieas'],
    'pricetorevenue': X_pred['pricetorevenue'],
    'marketcap': X_pred['marketcap'],
    'pricetobook': X_pred['pricetobook'],
    'pricetoearnings': X_pred['pricetoearnings'],
    'beta': X_pred['beta'],
},
num_epochs=40000, shuffle=False
)

test_pred = estimator.predict(input_fn=pred_input_fn)

```