Problem 1

Prove whether the following languages are regular or not.

A Strings over the alphabet $\Sigma = \{0, ..., 9, \#\}$ that contain the substring $c\#^c c$ where $c \in \{0, ..., 9\}$.

This language is regular - this can be proven by constructing a regular expression that recognizes the language. (Notation Note: The string $\#^n$ is the string consisting of # repeated n times. Example: $\#^3 = \#\#\#$)

$$\bigcup_{r \in \{0, \dots, 9\}} \Sigma^*(r \#^r r) \Sigma^*$$
$$= \Sigma^*(00) \Sigma^* + \Sigma^*(1 \# 1) \Sigma^* + \dots + \Sigma^*(9 \#^9 9) \Sigma^*$$

B Strings over the alphabet $\Sigma = \{0, ..., 9, \#\}$ of the form $\langle n \rangle \#^n$ where n is a sequence of digits interpreted as a decimal number.

This language is not regular - this can be proven using fooling sets.

C Strings over the alphabet $\Sigma = \{0, ..., 9, \#\}$ that have the same 3 characters repeated in two places. This language is **not** regular - this can be proven using fooling sets.