

```
In [1]: #pip install seaborn
        #pip install astropy
        #pip install intersect
```

```
In [2]: from astropy.io import fits
        import numpy as np
        import matplotlib.pyplot as plt
        import pandas as pd
        import glob
        from datetime import datetime, timedelta
        from sklearn.linear_model import LinearRegression
        from intersect import intersection
        from PIL import Image
```

```
In [3]: """
        Methodology:
        loop through timestamps of skyprobe measurements, for each one find a timestamp
        minute as well as an ASIVA image with a timestamp within +/- 1 minute.
        output a csv file with 5 columns as follows:
        1 - skyprobe timestamp
        2 - Skyprobe attenuation
        3 - telescope Az
        4 - Telescope Alt
        5 - ASIVA Image Filename
        """
```

```
Out[3]: '\nMethodology:\nloop through timestamps of skyprobe measurements, for each
one find a timestamp in the telescope data within +/- 1 \nminute as well as
an ASIVA image with a timestamp within +/- 1 minute. \noutput a csv file wi
th 5 columns as follows:\n1 - skyprobe timestamp\n2 - Skyprobe attenuation
\n3 - telescope Az\n4 - Telescope Alt\n5 - ASIVA Image Filename\n'
```

```
In [4]: """File Parsing:
        Skyprobe Data:
        Column 1: Time in UNIX EPOCH
        Column 4: Zeropoint (Attenuation)

        Telescope Data:
        Column 1: Time in UNIX Epoch
        Column 2: Alt
        Column 3: Az

        ASIVA Images:
        naming example: asiva202301251900.png
        naming format: asivaYYYYMMDDHHMM
        HH in military time
        """
```

```
Out[4]: 'File Parsing:\nSkyprobe Data:\nColumn 1: Time in UNIX EPOCH\nColumn 4: Zer
opoint (Attenuation)\n\nTelescope Data:\nColumn 1: Time in UNIX Epoch\nColu
mn 2: Alt\nColumn 3: Az\n\nASIVA Images:\nnaming example: asiva20230125190
0.png\nnaming format: asivaYYYYMMDDHHMM\nHH in military time\n'
```

```
In [5]: DF_skyprobe = pd.read_csv("skyprobe_data.csv", low_memory=False)
DF_skyprobe.columns = ['Time', 'skip1', 'skip2', 'attenuation', 'skip3', 'sk
DF_skyprobe = DF_skyprobe.drop(columns = ['skip1', 'skip2', 'skip3', 'skip4'
DF_telescope = pd.read_csv("tcs_data.csv", low_memory=False)
DF_telescope.columns = ['Time', 'Alt', 'Az', 'skip']
DF_telescope = DF_telescope.drop(columns = ['skip'])
DF = pd.merge_asof(DF_skyprobe, DF_telescope, on = "Time", direction="neares
DF = DF.dropna()
print(DF.head)
```

```
<bound method NDFrame.head of
Az
0      1274851510      0.107  89.8103  279.5074
1      1274851809      0.155  67.7496  80.3481
2      1274851870      0.144  67.7496  80.3481
3      1274851929      0.559  67.7496  80.3481
4      1274851989      0.121  67.7496  80.3481
...      ...
2125491  1694792290     -0.108  64.9583  48.1660
2125492  1694792350      0.151  64.9213  48.1046
2125493  1694792407     -0.183  64.8382  48.1806
2125494  1694792470      0.004  65.0426  47.9788
2125495  1694793600      0.004  64.9767  48.1581
```

```
[1647649 rows x 4 columns]>
```

```
In [13]: #we now have a combined dataset of skyprobe data with corresponding Alt and
#Now we need to find ASIVA images with close timestamps and add the filename

folder = "../images"
filenames = []
timestamps = []
for file in glob.glob(folder + '/*.png'):
    filedate = file.split('/')[2].split('asiva')[1].split('.')[1:-2]
    time = datetime.strptime(filedate, '%Y%m%d%H%M') + timedelta(hours=10)
    timestamp = datetime.timestamp(time)
    filenames.append(file)
    timestamps.append(int(timestamp))
#convert filedate/time to UNIX. Add 10 hours for converting HST to UTC
DF_ASIVA = pd.DataFrame(timestamps)
DF_ASIVA.columns = ["Time"]
DF_ASIVA["filenames"] = filenames
DF_ASIVA = DF_ASIVA.sort_values(by="Time")
print(DF_ASIVA.head)
```

	<bound method NDFrame.head of	Time	filenam
es			
1409	1674727200	../images/asiva202301251900.png	
1442	1674727260	../images/asiva202301251901.png	
1251	1674727320	../images/asiva202301251902.png	
1208	1674727380	../images/asiva202301251903.png	
868	1674727440	../images/asiva202301251904.png	
...	
247	1687974900	../images/asiva202306280355.png	
75	1687974960	../images/asiva202306280356.png	
107	1687975020	../images/asiva202306280357.png	
2742	1687975080	../images/asiva202306280358.png	
2701	1687975140	../images/asiva202306280359.png	

[2999 rows x 2 columns]>

```
In [7]: #perform another merge_asof to add asiva filenames to the main dataframe
DF = pd.merge_asof(DF, DF_ASIVA, on = "Time", direction="nearest", tolerance=10)
DF = DF.dropna()
DF = DF.reset_index()
print(DF.head)
```

	<bound method NDFrame.head of	index	Time	attenuation	Alt
Az \					
0	1581249 1675601947	0.092 32.4534	321.3330		
1	1581250 1675602000	0.092 32.4534	321.3330		
2	1581251 1675602006	0.095 32.4534	321.3330		
3	1581252 1675602007	0.095 32.4534	321.3330		
4	1581253 1675602187	0.103 31.4518	321.3330		
..		
882	1616383 1687964890	-0.021 56.4768	142.2442		
883	1616384 1687964950	-0.001 57.4772	142.2442		
884	1616385 1687965010	-0.027 57.4772	143.2486		
885	1616386 1687965067	-0.084 57.4772	143.2486		
886	1616387 1687965130	-0.018 57.4772	143.2486		

	filenames
0	../images/asiva202302042200.png
1	../images/asiva202302042200.png
2	../images/asiva202302042200.png
3	../images/asiva202302042200.png
4	../images/asiva202302042203.png
..	...
882	../images/asiva202306280108.png
883	../images/asiva202306280109.png
884	../images/asiva202306280110.png
885	../images/asiva202306280111.png
886	../images/asiva202306280112.png

[887 rows x 6 columns]>

```
In [8]: ## Code from https://scipython.com/blog/direct-linear-least-squares-fitting-
## Posted by: christian on 9 Aug 2021

def fit_ellipse(x, y):
    """
```

Fit the coefficients a, b, c, d, e, f , representing an ellipse described by the formula $F(x, y) = ax^2 + bxy + cy^2 + dx + ey + f = 0$ to the provided arrays of data points $x=[x_1, x_2, \dots, x_n]$ and $y=[y_1, y_2, \dots, y_n]$.

Based on the algorithm of Halir and Flusser, "Numerically stable direct least squares fitting of ellipses".

```
#####

D1 = np.vstack([x**2, x*y, y**2]).T
D2 = np.vstack([x, y, np.ones(len(x))]).T
S1 = D1.T @ D1
S2 = D1.T @ D2
S3 = D2.T @ D2
T = -np.linalg.inv(S3) @ S2.T
M = S1 + S2 @ T
C = np.array([(0, 0, 2), (0, -1, 0), (2, 0, 0)], dtype=float)
M = np.linalg.inv(C) @ M
eigval, eigvec = np.linalg.eig(M)
con = 4 * eigvec[0] * eigvec[2] - eigvec[1]**2
ak = eigvec[:, np.nonzero(con > 0)[0]]
return np.concatenate((ak, T @ ak)).ravel()

def cart_to_pol(coeffs):
    #####

    Convert the cartesian conic coefficients, (a, b, c, d, e, f), to the
    ellipse parameters, where  $F(x, y) = ax^2 + bxy + cy^2 + dx + ey + f = 0$ .
    The returned parameters are  $x_0, y_0, ap, bp, e, \phi$ , where  $(x_0, y_0)$  is the
    ellipse centre;  $(ap, bp)$  are the semi-major and semi-minor axes,
    respectively;  $e$  is the eccentricity; and  $\phi$  is the rotation of the semi
    major axis from the x-axis.

    #####

    # We use the formulas from https://mathworld.wolfram.com/Ellipse.html
    # which assumes a cartesian form  $ax^2 + 2bxy + cy^2 + 2dx + 2fy + g = 0$ .
    # Therefore, rename and scale b, d and f appropriately.
    a = coeffs[0]
    b = coeffs[1] / 2
    c = coeffs[2]
    d = coeffs[3] / 2
    f = coeffs[4] / 2
    g = coeffs[5]

    den = b**2 - a*c
    if den > 0:
        raise ValueError('coeffs do not represent an ellipse: b^2 - 4ac must
            ' be negative!')

    # The location of the ellipse centre.
    x0, y0 = (c*d - b*f) / den, (a*f - b*d) / den
```

```

num = 2 * (a*f**2 + c*d**2 + g*b**2 - 2*b*d*f - a*c*g)
fac = np.sqrt((a - c)**2 + 4*b**2)
# The semi-major and semi-minor axis lengths (these are not sorted).
ap = np.sqrt(num / den / (fac - a - c))
bp = np.sqrt(num / den / (-fac - a - c))

# Sort the semi-major and semi-minor axis lengths but keep track of
# the original relative magnitudes of width and height.
width_gt_height = True
if ap < bp:
    width_gt_height = False
    ap, bp = bp, ap

# The eccentricity.
r = (bp/ap)**2
if r > 1:
    r = 1/r
e = np.sqrt(1 - r)

# The angle of anticlockwise rotation of the major-axis from x-axis.
if b == 0:
    phi = 0 if a < c else np.pi/2
else:
    phi = np.arctan((2.*b) / (a - c)) / 2
    if a > c:
        phi += np.pi/2
if not width_gt_height:
    # Ensure that phi is the angle to rotate to the semi-major axis.
    phi += np.pi/2
phi = phi % np.pi

return x0, y0, ap, bp, e, phi

def get_ellipse_pts(params, npts=100, tmin=0, tmax=2*np.pi):
    """
    Return npts points on the ellipse described by the params = x0, y0, ap,
    bp, e, phi for values of the parametric variable t between tmin and tmax

    """

    x0, y0, ap, bp, e, phi = params
    # A grid of the parametric variable, t.
    t = np.linspace(tmin, tmax, npts)
    x = x0 + ap * np.cos(t) * np.cos(phi) - bp * np.sin(t) * np.sin(phi)
    y = y0 + ap * np.cos(t) * np.sin(phi) + bp * np.sin(t) * np.cos(phi)
    return x, y

```

In []:

In [9]:

```

"""
Now need to find the location within each ASIVA image and save a 12x12 kernel
along with a corresponding attenuation value
Azimuth.fits gives f(x,y) = Az    -- from an (x,y) pair in an ASIVA image give
Altitude.fits gives g(x,y) = Alt   -- from an (x,y) pair in an ASIVA image give

```

I want to construct:

$f^{-1}(Az) = (x,y)$ -- from an Az value input give a set of (x,y) on an ASIVA im
 $g^{-1}(Alt) = (x,y)$ -- from an Alt value input give a set of (x,y) on an ASIVA

I then want to find the intersection between f^{-1} and g^{-1} -- that's where I'
,,,,,

#These indices have azimuth values that want to form vertical lines, doesn't

```
#DF = DF.reset_index()
```

```
problems = [73, 74, 75, 76, 819]
```

```
DF = DF.drop(index=problems)
```

```
hdl_az = fits.open("azimuth.fits")
```

```
hdl_alt = fits.open("altitude.fits")
```

```
az_image = hdl_az[0].data
```

```
alt_image = hdl_alt[0].data
```

```
vals = DF[['Az', 'Alt']]
```

```
i = 0
```

```
kernel_locs = []
```

```
for index, row in vals.iterrows():
```

```
    #print(i)
```

```
    #if(i not in problems):
```

```
        Az = np.float32(row[0])
```

```
        Alt = np.float32(row[1])
```

```
        az_locs = list(zip(*np.where(abs(az_image - Az) <= 2)))
```

```
        alt_locs = list(zip(*np.where(abs(alt_image - Alt) <= 0.5)))
```

```
        #Plot Alt data and get regression model for ellipse
```

```
        y, x = zip(*alt_locs)
```

```
        x = np.array(x)
```

```
        y = np.array(y)
```

```
        plt.scatter(x, y, color="r")
```

```
        coeffs_ellipse = fit_ellipse(x, y)
```

```
        x0, y0, ap, bp, e, phi = cart_to_pol(coeffs_ellipse)
```

```
        x_e, y_e = get_ellipse_pts((x0, y0, ap, bp, e, phi), npts=1000)
```

```
        plt.plot(x_e, y_e, linewidth=4)
```

```
        #Plot Az data and get regression model for line
```

```
        y, x = zip(*az_locs)
```

```
        x = np.array(x)
```

```
        y = np.array(y)
```

```
        midx = np.mean(x)
```

```
        plt.scatter(x, y, color="y")
```

```
        x_r = x.reshape((-1, 1))
```

```
        model = LinearRegression().fit(x_r, y)
```

```
        coeffs_line = [model.coef_, model.intercept_]
```

```
        x_pred = np.linspace(0, x0, len(y_e)).reshape((-1, 1))
```

```
        y_pred = model.predict(x_pred)
```

```
        plt.plot(x_pred.reshape((-1, 1)), y_pred)
```

```
        #find the intersection point between the linear and elliptical models.
```

```
        x_loc, y_loc = intersection(x_pred, y_pred, x_e, y_e)
```

```
        #idx = np.argwhere(np.diff(np.sign(y_e - y_pred))).flatten()
```

```
        #x_loc = x_pred[idx]
```

```
        #y_loc = y_pred[idx]
```

```
        x_loc = int(x_loc[0])
```

```
        y_loc = int(y_loc[0])
```

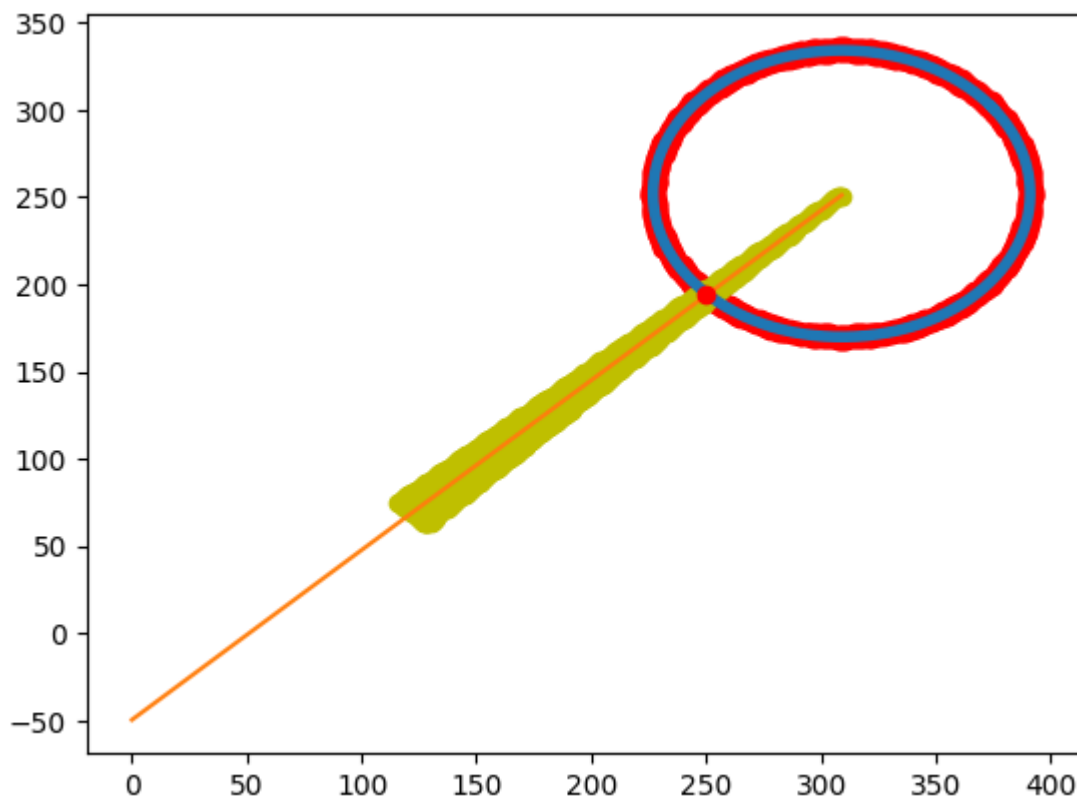
```
        kernel_locs.append((x_loc, y_loc))
```

```

if(i == 67):
    plt.plot(x_loc, y_loc, 'ro')
    plt.show()
    i += 1
    plt.clf()

DF["Kernel_Location"] = kernel_locs
print(DF.head)
hdul_az.close()
hdul_alt.close()

```



```

/Library/Frameworks/Python.framework/Versions/3.7/lib/python3.7/site-packages/ipykernel_launcher.py:85: RuntimeWarning: divide by zero encountered in double_scalars
/Library/Frameworks/Python.framework/Versions/3.7/lib/python3.7/site-packages/ipykernel_launcher.py:85: RuntimeWarning: divide by zero encountered in double_scalars
/Library/Frameworks/Python.framework/Versions/3.7/lib/python3.7/site-packages/ipykernel_launcher.py:85: RuntimeWarning: divide by zero encountered in double_scalars

```

	<bound method NDFrame.head of		index	Time	attenuation	Alt
Az \						
0	1581249	1675601947	0.092	32.4534	321.3330	
1	1581250	1675602000	0.092	32.4534	321.3330	
2	1581251	1675602006	0.095	32.4534	321.3330	
3	1581252	1675602007	0.095	32.4534	321.3330	
4	1581253	1675602187	0.103	31.4518	321.3330	
..	
882	1616383	1687964890	-0.021	56.4768	142.2442	
883	1616384	1687964950	-0.001	57.4772	142.2442	
884	1616385	1687965010	-0.027	57.4772	143.2486	
885	1616386	1687965067	-0.084	57.4772	143.2486	
886	1616387	1687965130	-0.018	57.4772	143.2486	

	filenames	Kernel_Location
0	../images/asiva202302042200.png	(220, 435)
1	../images/asiva202302042200.png	(220, 435)
2	../images/asiva202302042200.png	(220, 435)
3	../images/asiva202302042200.png	(220, 435)
4	../images/asiva202302042203.png	(219, 437)
..
882	../images/asiva202306280108.png	(251, 370)
883	../images/asiva202306280109.png	(253, 367)
884	../images/asiva202306280110.png	(255, 368)
885	../images/asiva202306280111.png	(255, 368)
886	../images/asiva202306280112.png	(255, 368)

[882 rows x 7 columns]>

<Figure size 640x480 with 0 Axes>

```
In [12]: """
The format of DF is now 6 columns as follows:
1 - skyprobe timestamp
2 - Skyprobe attenuation
3 - telescope Az
4 - Telescope Alt
5 - ASIVA Image Filename
6 - (x, y) position of the skyprobe measurement in the corresponding ASIVA i

I now need to parse through each filename in the dataframe and extract a ker
location

"""
size = 6
images = DF[["filenames", "Kernel_Location", "attenuation"]]
image_kernel_filenames = []
image_kernel_attenuations = []
for index, row in images.iterrows():
    filename = row[0]
    attenuation = row[2]
    oldimagename = filename.split('../images/')[1].split('.png')[0]
    loc = row[1]
    im = Image.open(filename)
    x = loc[0]
    y = loc[1]
    imk = im.crop((x-size, y-size, x+size, y+size))
```



```

newfilename = oldimagename + "_12x12" + ".png"
image_kernel_filenames.append(newfilename)
image_kernel_attenuations.append(attenuation)
imk.save('../kernels/' + newfilename)
if(attenuation > 0.2):
    #also sample around the target location
    offset = int(size)
    xs = [x-offset, x-offset/2, x, x+offset/2, x+offset]
    ys = [y-offset, y-offset/2, y, y+offset/2, y+offset]
    for x_pos in xs:
        for y_pos in ys:
            if(x_pos != x or y_pos != y):
                imk = im.crop((x_pos-size, y_pos-size, x_pos+size, y_pos+size))
                newfilename = oldimagename + "_12x12" + "_" + str(x_pos) + str(y_pos) + ".png"
                image_kernel_filenames.append(newfilename)
                image_kernel_attenuations.append(attenuation)
                imk.save('../kernels/' + newfilename)

#write CSV file containing kernel filenames and corresponding attenuations

attenuations = pd.DataFrame(image_kernel_attenuations)
attenuations.columns = ["attenuation"]
attenuations["filename"] = image_kernel_filenames
attenuations.to_csv("../kernels/attenuations.csv")

```

In []: *# demonstrate example kernels and attenuation values.*