

Q1: Show that $8n^2 - 5n + 7 = O(n^3)$

Q2: Determine whether each of these functions is bounded by $O(n)$. Say yes or no.

a) $f(n) = 3$

b) $f(n) = n^2 + n + 12$

c) $f(n) = 17n + 7$

d) $f(n) = 15n \log n$

Q3: Arrange the following functions in ascending order of growth rate.

$$f(n) = (1.5)^n + 50$$

$$f(n) = n^{100} + n^3 \log n$$

$$f(n) = (\log n)^3$$

$$f(n) = \sqrt{n} \log n$$

$$f(n) = 10^n$$

$$f(n) = n^{99} + n^{98}$$

$$f(n) = (n!)^2$$

Q4: Solve the following recurrences using Master Theorem

a. $T(n) = 4T(n/2) + n^2$

b. $T(n) = 2T(n/4) + n$

Q5: In the divide and conquer closest pair of points, we sorted the coordinates (x or y). Once sorted, are we ready to start computing distances?

Q6: You are given an $n \times n$ grid representing a maze, where:

- 1 represents an open path.
- 0 represents a wall.
- The starting position is at the top-left corner (0,0).
- The goal is to reach the bottom-right corner (n-1, n-1).

Write a **backtracking function** that finds a path from the start to the goal and prints the path taken.

Example Input:

```
int maze[4][4] = {  
    {1, 0, 1, 1},  
    {1, 1, 1, 0},  
    {0, 1, 0, 1},  
    {1, 1, 1, 1}  
};
```

Expected Output (One Possible Path):

$(0,0) \rightarrow (1,0) \rightarrow (1,1) \rightarrow (2,1) \rightarrow (3,1) \rightarrow (3,2) \rightarrow (3,3)$

Q7: B – Tree

Insertion example: Insert key 68, please show your steps. The degree of the B-Tree is $t = 2$

