$$\begin{bmatrix} u\left(e_{0}^{2}+e_{1}^{2}-e_{2}^{2}-e_{3}^{2}\right)+v\left(-2e_{0}e_{3}+2e_{1}e_{2}\right)+w\left(2e_{0}e_{2}+2e_{1}e_{3}\right)\\ u\left(2e_{0}e_{3}+2e_{1}e_{2}\right)+v\left(e_{0}^{2}-e_{1}^{2}+e_{2}^{2}-e_{3}^{2}\right)+w\left(-2e_{0}e_{1}+2e_{2}e_{3}\right)\\ -qw+rv+\frac{f_{Ex}+f_{cppcx}+f_{cppfx}+f_{cpscx}+f_{cpsfx}+gm\left(-2e_{0}e_{2}+2e_{1}e_{3}\right)}{m}\\ pw-ru+\frac{f_{Ex}+f_{cppcx}+f_{cppfy}+f_{cpscy}+f_{cpsfy}+gm\left(2e_{0}e_{1}+2e_{2}e_{3}\right)}{m}\\ -pv+qu+\frac{f_{Ex}+f_{cppcx}+f_{cppfz}+f_{cpscx}+f_{cpsfz}+gm\left(e_{0}^{2}-e_{1}^{2}-e_{2}^{2}+e_{3}^{2}\right)}{m}\\ \frac{e_{0}p}{2}+\frac{e_{2}r}{2}-\frac{e_{3}q}{2}\\ \frac{e_{0}q}{2}-\frac{e_{1}r}{2}+\frac{e_{3}p}{2}\\ \frac{e_{0}r}{2}+\frac{e_{1}q}{2}-\frac{e_{2}p}{2}\\ -\frac{J_{xx}pr-J_{zz}pr}{J_{xx}}+\frac{-f_{cppcz}-f_{cppfz}+f_{cpscz}+f_{cpsfz}}{J_{yy}}\\ -\frac{J_{xx}pr-J_{zz}pr}{J_{yy}}+\frac{f_{Ey}r_{Ex}+f_{cppcy}+f_{cppfx}-f_{cppfy}-f_{cpscx}+f_{cpscy}-f_{cpsfx}-f_{cpsfy}}{J_{zz}} \end{bmatrix}$$

References:

https://www.intechopen.com/chapters/64567