OSSE

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| : %py | ylab inline | |
| #%r | $matplotlib\ qt$ | |
| imp | port sk_dsp_comm.sigsys as ss | |
| imp | port sk_dsp_comm.digitalcom as dc | |
| imp | port scipy.signal as signal | |
| imp | port rs_fec_conv.fec_conv as rs_fec | |
| imp | port sk_dsp_comm.fec_conv as fec | |
| imp | port numpy as np | |
| fro | om numpy.random import randint | |
| imp | port matplotlib.pyplot as plt | |
| fro | om IPython.display import Audio, display | |
| fre | om IPython.display import Image, SVG | |

```
[2]: pylab.rcParams['savefig.dpi'] = 100 # default 72
     \#pylab.rcParams['figure.figsize'] = (6.0, 4.0) \# default (6,4)
     #%config InlineBackend.figure_formats=['png'] # default for inline viewing
     #%config InlineBackend.figure_formats=['svg'] # SVG inline viewing
     %config InlineBackend.figure_formats=['pdf'] # render pdf figs for LaTeX
```

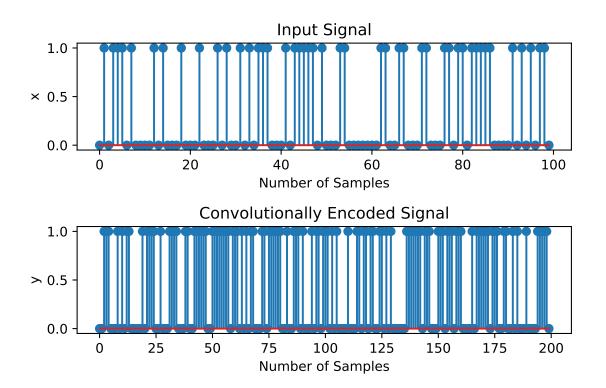
conv_encoder and viterbi_decoder

Function Comparison

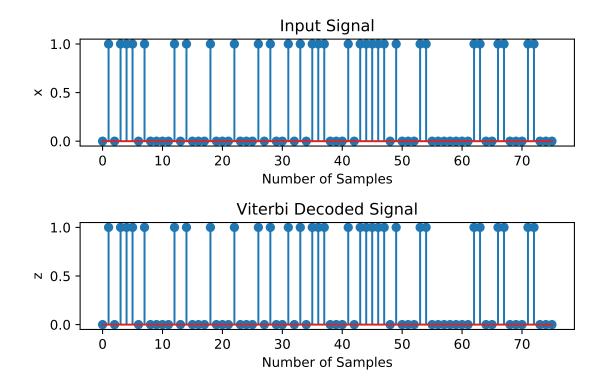
Compare the outputs of the convolutional encoder and viter idecoder between Python and Rust functions.

```
[3]: # Generate random data
     N = 100
     x = randint(0,2,N)
     # Initialize fec_conv object with either G length 2 or 3
     # depth = 10
     # G = ('111', '101')
     # depth = 25
     \# G = ('111111', '11011', '10101')
     depth = 25
     G = ('1111001', '1011011')
     cc1 = rs fec.fec conv(G,depth)
     # Encode with shift register starting state of '0000'
     state = ''
     for i in range(len(G[0]) - 1):
         state += '0'
     # Convolutionally Encode Signal
     y,state = cc1.conv_encoder(x,state)
     # Plot input signal
     subplot(211)
     stem(x, use_line_collection=True)
     xlabel('Number of Samples')
     ylabel('x')
     title('Input Signal')
     # Plot convolutionally encoded signal
     subplot(212)
     stem(y, use_line_collection=True)
     xlabel('Number of Samples')
     ylabel('y')
     title('Convolutionally Encoded Signal')
     tight_layout()
     savefig('conv_enc.png')
```

Rate 1/2 Object



```
[4]: # Viterbi decode
     z = cc1.viterbi_decoder(y.astype(int), 'hard', 3)
     z
     # Plot input signal
     subplot(211)
     # stem(x[:11], use_line_collection=True)
     stem(x[:-(depth-1)], use_line_collection=True)
     xlabel('Number of Samples')
     ylabel('x')
     title('Input Signal')
     # xlim([0,10])
     # Plot viterbi decoded signal
     subplot(212)
     stem(z, use_line_collection=True)
     xlabel('Number of Samples')
     ylabel('z')
     title('Viterbi Decoded Signal')
     # xlim([0,10])
     tight_layout()
     savefig('viterbi_dec.png')
```



Code length 3. Rate 1/2

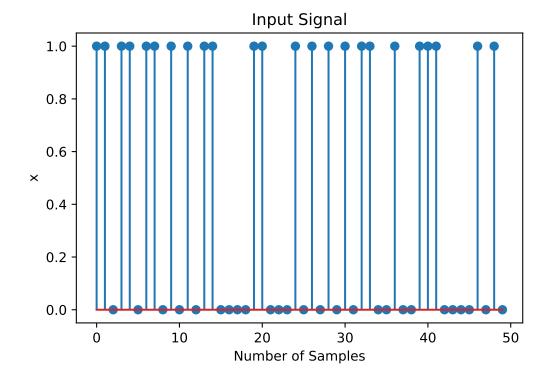
```
[5]: # Python
     N = 50
     x = randint(0,2,N)
     depth = 10
     G = ('111', '101')
     cc1 = fec.fec_conv(G,depth)
     # Encode with shift register starting state of '0000'
     state1 = ''
     for i in range(len(G[0]) - 1):
         state1 += '0'
     y1,state1 = cc1.conv_encoder(x,state1)
     # Viterbi decode
     z1 = cc1.viterbi_decoder(y1.astype(int), 'hard', 3)
     # print results
     print(y1)
     print(state1)
     print(z1)
```

```
[1. 1. 0. 1. 0. 1. 0. 0. 0. 1. 0. 1. 0. 0. 0. 1. 0. 1. 0. 1. 0. 0. 0. 0.
     1. 0. 0. 0. 0. 1. 0. 1. 1. 1. 0. 0. 0. 1. 1. 0. 1. 0. 1. 1. 1. 0. 0.
     1. 1. 1. 0. 0. 0. 1. 0. 0. 0. 1. 0. 0. 0. 1. 0. 0. 0. 0. 1. 0. 1. 1. 1.
     1. 1. 1. 0. 1. 1. 1. 1. 0. 1. 1. 0. 0. 1. 1. 1. 0. 0. 0. 0. 0. 1. 1. 1. 0.
     0. 0. 1. 0.]
    01
    [1. 1. 0. 1. 1. 0. 1. 1. 0. 1. 0. 1. 0. 1. 1. 0. 0. 0. 0. 1. 1. 0. 0. 0.
     1. 0. 1. 0. 1. 0. 1. 0. 1. 1. 0. 0. 1. 0. 0. 1. 1.]
[6]: # Rust
     N = 50
     \#x = randint(0,2,N)
     depth = 10
     G = ('111', '101')
     cc2 = rs_fec.fec_conv(G,depth)
     # Encode with shift register starting state of '0000'
     state2 = ''
     for i in range(len(G[0]) - 1):
         state2 += '0'
     y2,state2 = cc2.conv_encoder(x,state2)
     # Viterbi decode
     z2 = cc2.viterbi_decoder(y2.astype(int), 'hard', 3)
     # print results
     print(y2)
     print(state2)
     print(z2)
    Rate 1/2 Object
    [1. 1. 0. 1. 0. 1. 0. 0. 0. 1. 0. 1. 0. 0. 0. 1. 0. 1. 0. 1. 0. 1. 0. 0. 1. 0. 0.
     1. 0. 0. 0. 0. 1. 0. 1. 1. 1. 0. 0. 0. 1. 1. 0. 1. 0. 1. 1. 1. 0. 0.
     1. 1. 1. 0. 0. 0. 1. 0. 0. 0. 1. 0. 0. 1. 0. 0. 0. 1. 0. 0. 1. 1. 1. 1.
     1. 1. 1. 0. 1. 1. 1. 1. 0. 1. 1. 0. 0. 1. 1. 1. 0. 0. 0. 0. 1. 1. 1. 0.
     0. 0. 1. 0.7
    01
    [1. 1. 0. 1. 1. 0. 1. 1. 0. 1. 0. 1. 0. 1. 1. 0. 0. 0. 0. 0. 1. 1. 0. 0. 0.
     1. 0. 1. 0. 1. 0. 1. 0. 1. 1. 0. 0. 1. 0. 0. 1. 1.]
    Plot the outputs from Rust and Python.
[7]: # plot input
     stem(x, use_line_collection=True)
     xlabel('Number of Samples')
     ylabel('x')
```

Rate 1/2 Object

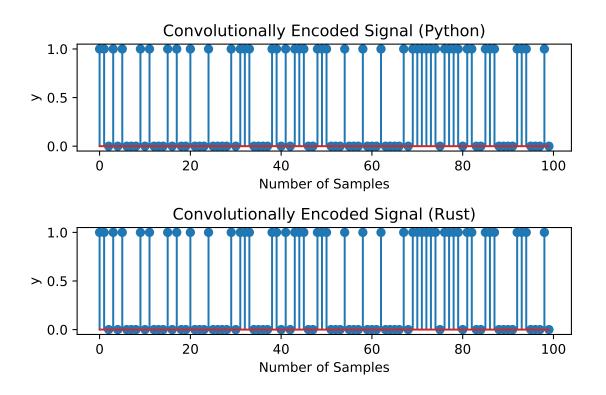
```
title('Input Signal')
```

[7]: Text(0.5, 1.0, 'Input Signal')



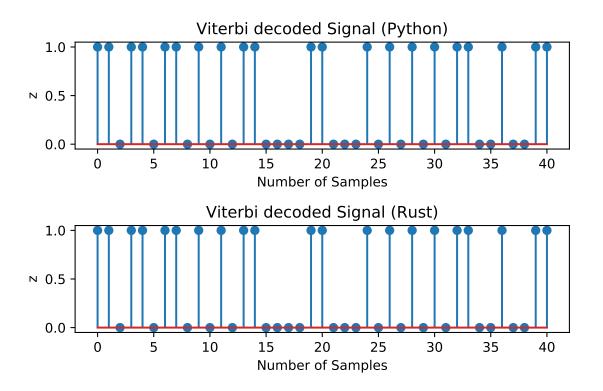
```
[8]: # plot conv encoded signal
    subplot(211)
    stem(y1, use_line_collection=True)
    xlabel('Number of Samples')
    ylabel('y')
    title('Convolutionally Encoded Signal (Python)')

subplot(212)
    stem(y2, use_line_collection=True)
    xlabel('Number of Samples')
    ylabel('y')
    title('Convolutionally Encoded Signal (Rust)')
    tight_layout()
```



```
[9]: # plot viterbi decoded signals
subplot(211)
stem(z1, use_line_collection=True)
xlabel('Number of Samples')
ylabel('z')
title('Viterbi decoded Signal (Python)')

subplot(212)
stem(z2, use_line_collection=True)
xlabel('Number of Samples')
ylabel('z')
title('Viterbi decoded Signal (Rust)')
tight_layout()
```



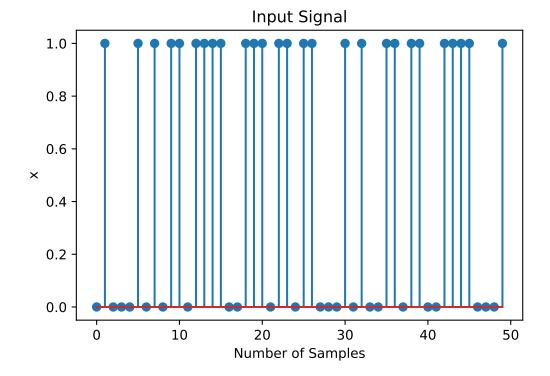
Code length 5. Rate 1/3

```
[10]: # Python
      N = 50
      x = randint(0,2,N)
      depth = 25
      G = ('111111', '11011', '10101')
      cc1 = fec.fec_conv(G,depth)
      # Encode with shift register starting state of '0000'
      state1 = ''
      for i in range(len(G[0]) - 1):
          state1 += '0'
      y1,state1 = cc1.conv_encoder(x,state1)
      # Viterbi decode
      z1 = cc1.viterbi_decoder(y1.astype(int), 'hard', 3)
      # print results
      print(y1)
      print(state1)
      print(z1)
```

```
Rate 1/3 Object
     [0.\ 0.\ 0.\ 1.\ 1.\ 1.\ 1.\ 1.\ 0.\ 1.\ 0.\ 1.\ 1.\ 1.\ 0.\ 0.\ 0.\ 0.\ 1.\ 1.\ 0.\ 0.\ 1.\ 0.
     0. 0. 0. 1. 0. 1. 1. 1. 1. 0. 0. 1. 0. 0. 0. 0. 0. 0. 1. 1. 0. 1. 0.
     0. 1. 0. 1. 0. 0. 1. 1. 0. 1. 1. 0. 1. 0. 0. 1. 0. 1. 0. 1. 0. 0. 0.
     1. 0. 0. 1. 0. 0. 0. 0. 1. 0. 0. 0. 1. 1. 0. 0. 1. 0. 0. 1. 1. 0.
     0. 1. 0. 0. 0. 0. 1. 0. 0. 0. 1. 1. 1. 0. 0. 1. 1. 1. 0. 0. 0. 0. 0.
      1. 0. 0. 0. 1. 1. 1. 1. 0. 1. 1. 0. 1. 0. 0. 0. 0. 1. 0. 0. 1. 0. 0.
     0. 0. 1. 0. 0. 0.]
     0. 1.7
[11]: # Rust
     N = 50
     \#x = randint(0,2,N)
     depth = 25
     G = ('111111', '11011', '10101')
     cc2 = rs_fec.fec_conv(G,depth)
     # Encode with shift register starting state of '0000'
     state2 = ''
     for i in range(len(G[0]) - 1):
         state2 += '0'
     y2,state2 = cc2.conv_encoder(x,state2)
     # Viterbi decode
     z2 = cc2.viterbi_decoder(y2.astype(int), 'hard', 3)
     # print results
     print(y2)
     print(state2)
     print(z2)
     Rate 1/3 Object
     0. 0. 0. 1. 0. 1. 1. 1. 1. 0. 0. 1. 0. 0. 0. 0. 0. 0. 1. 1. 0. 1. 0.
     0. 1. 0. 1. 0. 0. 1. 1. 0. 1. 1. 0. 1. 0. 0. 1. 0. 1. 0. 1. 0. 0. 0.
      1. 0. 0. 1. 0. 0. 0. 0. 1. 0. 0. 0. 1. 1. 0. 0. 1. 0. 0. 1. 1. 0.
     0. 1. 0. 0. 0. 0. 1. 0. 0. 0. 1. 1. 1. 0. 0. 1. 1. 1. 0. 0. 0. 0. 0.
      1. 0. 0. 0. 1. 1. 1. 1. 0. 1. 1. 0. 1. 0. 0. 0. 1. 0. 0. 1. 0. 0. 1. 0. 0.
     0. 0. 1. 0. 0. 0.]
     1000
     [0.\ 1.\ 0.\ 0.\ 0.\ 1.\ 0.\ 1.\ 0.\ 1.\ 1.\ 0.\ 1.\ 1.\ 1.\ 1.\ 0.\ 0.\ 1.\ 1.\ 1.\ 1.\ 0.\ 1.\ 1.\ 1.
     0. 1.]
```

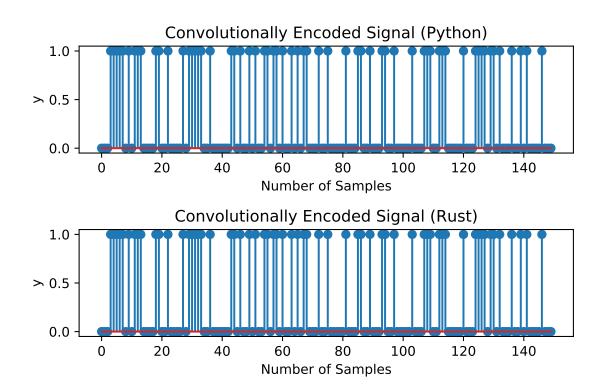
```
[12]: # plot input
stem(x, use_line_collection=True)
xlabel('Number of Samples')
ylabel('x')
title('Input Signal')
```

[12]: Text(0.5, 1.0, 'Input Signal')



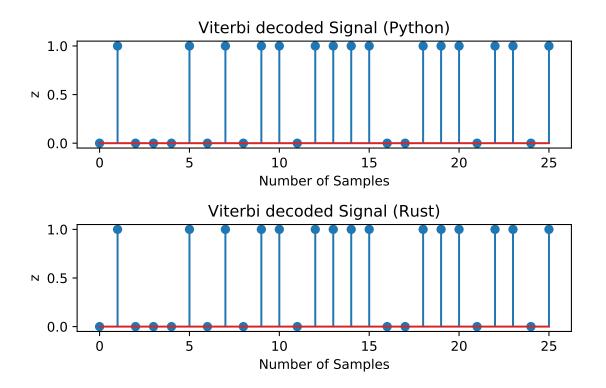
```
[13]: # plot conv encoded signal
    subplot(211)
    stem(y1, use_line_collection=True)
    xlabel('Number of Samples')
    ylabel('y')
    title('Convolutionally Encoded Signal (Python)')

subplot(212)
    stem(y2, use_line_collection=True)
    xlabel('Number of Samples')
    ylabel('y')
    title('Convolutionally Encoded Signal (Rust)')
    tight_layout()
```



```
[14]: # plot viterbi decoded signals
    subplot(211)
    stem(z1, use_line_collection=True)
    xlabel('Number of Samples')
    ylabel('z')
    title('Viterbi decoded Signal (Python)')

subplot(212)
    stem(z2, use_line_collection=True)
    xlabel('Number of Samples')
    ylabel('z')
    title('Viterbi decoded Signal (Rust)')
    tight_layout()
```

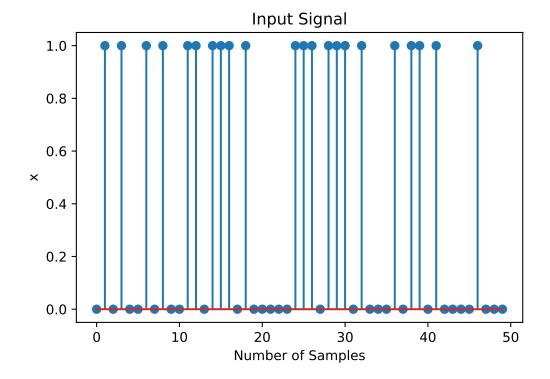


Code length 7. Rate 1/2

```
[15]: # Python
      N = 50
      x = randint(0,2,N)
      depth = 25
      G = ('1111001', '1011011')
      cc1 = fec.fec_conv(G,depth)
      # Encode with shift register starting state of '0000'
      state1 = ''
      for i in range(len(G[0]) - 1):
          state1 += '0'
      y1,state1 = cc1.conv_encoder(x,state1)
      # Viterbi decode
      z1 = cc1.viterbi_decoder(y1.astype(int), 'hard', 3)
      # print results
      print(y1)
      print(state1)
      print(z1)
```

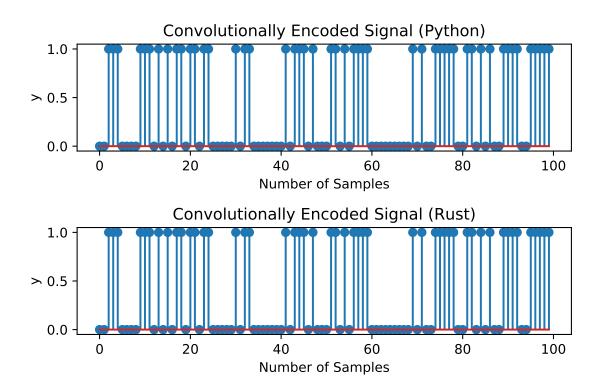
```
Rate 1/2 Object
    [0.\ 0.\ 1.\ 1.\ 1.\ 0.\ 0.\ 0.\ 1.\ 1.\ 1.\ 0.\ 1.\ 0.\ 1.\ 0.\ 1.\ 0.\ 1.\ 0.\ 1.
     1. 0. 0. 0. 0. 1. 0. 1. 1. 0. 0. 0. 0. 0. 0. 1. 0. 1. 1. 1. 0. 1.
     0. 0. 0. 1. 1. 0. 1. 0. 1. 1. 1. 1. 0. 0. 0. 0. 0. 0. 0. 0. 0. 1. 0. 1.
     0. 0. 1. 1. 1. 1. 0. 0. 1. 1. 0. 1. 0. 1. 0. 1. 1. 1. 1. 1. 0. 0. 1.
     1. 1. 1. 1.]
    000100
     [0. 1. 0. 1. 0. 0. 1. 0. 1. 0. 1. 1. 0. 1. 1. 1. 0. 1. 1. 0. 0. 0. 0. 0.
[16]: # Rust
     N = 50
     \#x = randint(0,2,N)
     depth = 25
     G = ('1111001', '1011011')
     cc2 = rs_fec.fec_conv(G,depth)
     # Encode with shift register starting state of '0000'
     state2 = ''
     for i in range(len(G[0]) - 1):
         state2 += '0'
     y2,state2 = cc2.conv_encoder(x,state2)
     # Viterbi decode
     z2 = cc2.viterbi_decoder(y2.astype(int), 'hard', 3)
     # print results
     print(y2)
     print(state2)
     print(z2)
    Rate 1/2 Object
    1. 0. 0. 0. 0. 1. 0. 1. 1. 0. 0. 0. 0. 0. 0. 1. 1. 1. 1. 0. 1.
     0. 0. 0. 1. 1. 0. 1. 0. 1. 1. 1. 1. 0. 0. 0. 0. 0. 0. 0. 0. 0. 1. 0. 1.
     0. 0. 1. 1. 1. 1. 0. 0. 1. 1. 0. 1. 0. 1. 0. 1. 1. 1. 1. 1. 0. 0. 1.
     1. 1. 1. 1.]
    000100
    1. 1.]
[17]: # plot input
     stem(x, use line collection=True)
     xlabel('Number of Samples')
     vlabel('x')
     title('Input Signal')
```

[17]: Text(0.5, 1.0, 'Input Signal')



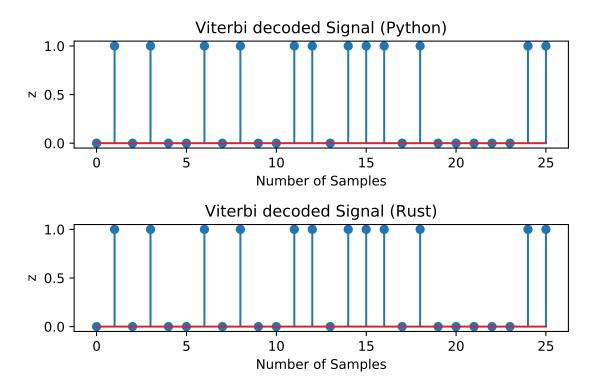
```
[18]: # plot conv encoded signal
    subplot(211)
    stem(y1, use_line_collection=True)
    xlabel('Number of Samples')
    ylabel('y')
    title('Convolutionally Encoded Signal (Python)')

subplot(212)
    stem(y2, use_line_collection=True)
    xlabel('Number of Samples')
    ylabel('y')
    title('Convolutionally Encoded Signal (Rust)')
    tight_layout()
```



```
[19]: # plot viterbi decoded signals
    subplot(211)
    stem(z1, use_line_collection=True)
    xlabel('Number of Samples')
    ylabel('z')
    title('Viterbi decoded Signal (Python)')

subplot(212)
    stem(z2, use_line_collection=True)
    xlabel('Number of Samples')
    ylabel('z')
    title('Viterbi decoded Signal (Rust)')
    tight_layout()
```



The Rust and Python match for convolutionally encoding and viter idecoding.

Timing Comparison

The Python versions of conv_encoder and viterbi_decoder functions are compared with the Rust versions of the functions with respect to time.

Code length 3. Rate 1/2

```
[]: %%timeit
# Python
N = 100
x = randint(0,2,N)

depth = 10
G = ('111','101')

cc1 = fec.fec_conv(G,depth)

# Encode with shift register starting state of '0000'
state1 = ''
for i in range(len(G[0]) - 1):
    state1 += '0'
y1,state1 = cc1.conv_encoder(x,state1)
```

```
# Viterbi decode
z1 = cc1.viterbi_decoder(y1.astype(int), 'hard', 3)
```

Code length 5. Rate 1/3

```
[]: %%timeit
    # Python
    N = 100
    x = randint(0,2,N)

depth = 25
    G = ('11111','11011','10101')

cc1 = fec.fec_conv(G,depth)

# Encode with shift register starting state of '0000'
state1 = ''
for i in range(len(G[0]) - 1):
    state1 += '0'
    y1,state1 = cc1.conv_encoder(x,state1)

# Viterbi decode
z1 = cc1.viterbi_decoder(y1.astype(int), 'hard', 3)
```

```
N = 100
#x = randint(0,2,N)

depth = 25
G = ('11111','11011','10101')

cc2 = rs_fec.fec_conv(G,depth)

# Encode with shift register starting state of '0000'
state2 = ''
for i in range(len(G[0]) - 1):
    state2 += '0'
y2,state2 = cc2.conv_encoder(x,state2)

# Viterbi decode
z2 = cc2.viterbi_decoder(y2.astype(int), 'hard', 3)
```

Code length 7. Rate 1/2

```
[]: %%timeit
# Rust
N = 100
#x = randint(0,2,N)

depth = 25
G = ('1111001','1011011')
```

```
cc2 = rs_fec.fec_conv(G,depth)

# Encode with shift register starting state of '0000'
state2 = ''
for i in range(len(G[0]) - 1):
    state2 += '0'
y2,state2 = cc2.conv_encoder(x,state2)

# Viterbi decode
z2 = cc2.viterbi_decoder(y2.astype(int), 'hard', 3)
```

20 bits

Python: 3.81 ms \pm 126 µs per loop (mean \pm std. dev. of 7 runs, 100 loops each)

Rust: 696 $\mu s \pm 44.8 \,\mu s$ per loop (mean \pm std. dev. of 7 runs, 1000 loops each)

The convolutional encoder and viter idecoder functions built in Rust run significantly 5 times faster than the pure Python functions.

Viterbi BER Simulation

Function Comparison

```
[20]: # Python
      # Soft decision rate 1/2 simulation
      N_bits_per_frame = 100000
      EbNO = 4
      total_bit_errors = 0
      total_bit_count = 0
      cc1 = fec.fec_conv(('11101','10011'),25)
      # Encode with shift register starting state of '0000'
      state = '0000'
      while total_bit_errors < 100:</pre>
          # Create 100000 random 0/1 bits
          x = randint(0,2,N_bits_per_frame)
          y,state = cc1.conv_encoder(x,state)
          # Add channel noise to bits, include antipodal level shift to [-1,1]
          yn_soft = dc.cpx_AWGN(2*y-1,EbN0-3,1) # Channel SNR is 3 dB less for rate 1/
       →2
          yn_hard = ((np.sign(yn_soft.real)+1)/2).astype(int)
          z = cc1.viterbi_decoder(yn_hard, 'hard')
          # Count bit errors
          bit_count, bit_errors = dc.bit_errors(x,z)
          total bit errors += bit errors
```

```
total_bit_count += bit_count
         print('Bits Received = %d, Bit errors = %d, BEP = %1.2e' %\
              (total_bit_count, total_bit_errors,\)
               total_bit_errors/total_bit_count))
     print('Bits Received = %d, Bit errors = %d, BEP = %1.2e' %\
           (total_bit_count, total_bit_errors,\
           total_bit_errors/total_bit_count))
    Rate 1/2 Object
    kmax = 0, taumax = 0
    Bits Received = 99976, Bit errors = 875, BEP = 8.75e-03
    **************
    Bits Received = 99976, Bit errors = 875, BEP = 8.75e-03
[21]: # Rust
     # Soft decision rate 1/2 simulation
     N_bits_per_frame = 100000
     EbNO = 4
     total_bit_errors = 0
     total_bit_count = 0
     cc1 = rs_fec.fec_conv(('11101','10011'),25)
     # Encode with shift register starting state of '0000'
     state = '0000'
     while total_bit_errors < 100:</pre>
         # Create 100000 random 0/1 bits
         x = randint(0,2,N_bits_per_frame)
         y,state = cc1.conv_encoder(x,state)
         # Add channel noise to bits, include antipodal level shift to [-1,1]
        yn_soft = dc.cpx_AWGN(2*y-1,EbN0-3,1) # Channel SNR is 3 dB less for rate 1/
      →2
         yn_hard = ((np.sign(yn_soft.real)+1)/2).astype(int)
         z = cc1.viterbi_decoder(yn_hard, 'hard')
         # Count bit errors
         bit_count, bit_errors = dc.bit_errors(x,z)
         total_bit_errors += bit_errors
         total_bit_count += bit_count
         print('Bits Received = %d, Bit errors = %d, BEP = %1.2e' %\
              (total_bit_count, total_bit_errors,\
               total_bit_errors/total_bit_count))
     print('Bits Received = %d, Bit errors = %d, BEP = %1.2e' %\
```

```
(total_bit_count, total_bit_errors,\
  total_bit_errors/total_bit_count))
```

The two simulations provide similar BERs althought since they are using random inputs for each loop the results are not exactly the same.

Timing Comparison

```
[22]: %%timeit
      # Python
      # Soft decision rate 1/2 simulation
      N_bits_per_frame = 100000
      EbNO = 4
      total_bit_errors = 0
      total_bit_count = 0
      depth = 10
      G = ('111', '101')
      # depth = 25
      \# G = ('111111', '11011', '10101')
      # depth = 25
      \# G = ('1111001', '1011011')
      cc1 = fec.fec_conv(G, depth)
      # Encode with shift register starting state of '0000'
      state = ''
      for i in range(len(G[0]) - 1):
          state += '0'
      while total_bit_errors < 100:</pre>
          # Create 100000 random 0/1 bits
          x = randint(0,2,N_bits_per_frame)
          y,state = cc1.conv_encoder(x,state)
          # Add channel noise to bits, include antipodal level shift to [-1,1]
          yn_soft = dc.cpx_AWGN(2*y-1,EbNO-3,1) # Channel SNR is 3 dB less for rate 1/
          yn_hard = ((np.sign(yn_soft.real)+1)/2).astype(int)
          z = cc1.viterbi_decoder(yn_hard, 'hard')
```

```
# Count bit errors
   bit count, bit_errors = dc.bit_errors(x,z)
   total_bit_errors += bit_errors
   total_bit_count += bit_count
   print('Bits Received = %d, Bit errors = %d, BEP = %1.2e' %
         (total_bit_count, total_bit_errors,\)
         total_bit_errors/total_bit_count))
print('Bits Received = %d, Bit errors = %d, BEP = %1.2e' %
     (total_bit_count, total_bit_errors,\
      total_bit_errors/total_bit_count))
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1132, BEP = 1.13e-02
******************
Bits Received = 99991, Bit errors = 1132, BEP = 1.13e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1315, BEP = 1.32e-02
******************
Bits Received = 99991, Bit errors = 1315, BEP = 1.32e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1122, BEP = 1.12e-02
***************
Bits Received = 99991, Bit errors = 1122, BEP = 1.12e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1219, BEP = 1.22e-02
******************
Bits Received = 99991, Bit errors = 1219, BEP = 1.22e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1303, BEP = 1.30e-02
******************
Bits Received = 99991, Bit errors = 1303, BEP = 1.30e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1347, BEP = 1.35e-02
***************
Bits Received = 99991, Bit errors = 1347, BEP = 1.35e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1218, BEP = 1.22e-02
```

```
Rate 1/2 Object
     kmax = 0, taumax = 0
     Bits Received = 99991, Bit errors = 1316, BEP = 1.32e-02
     **************
     Bits Received = 99991, Bit errors = 1316, BEP = 1.32e-02
     42.5 \text{ s} \pm 2.08 \text{ s} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
[23]: %%timeit
      # Rust
      # Soft decision rate 1/2 simulation
      N_bits_per_frame = 100000
      EbNO = 4
      total_bit_errors = 0
      total_bit_count = 0
      depth = 10
      G = ('111', '101')
      # depth = 25
      \# G = ('111111', '11011', '10101')
      # depth = 25
      \# G = ('1111001', '1011011')
      cc1 = rs_fec.fec_conv(G, depth)
      # Encode with shift register starting state of '0000'
      state = ''
      for i in range(len(G[0]) - 1):
          state += '0'
      while total_bit_errors < 100:</pre>
          # Create 100000 random 0/1 bits
          x = randint(0,2,N_bits_per_frame)
          y,state = cc1.conv_encoder(x,state)
          # Add channel noise to bits, include antipodal level shift to [-1,1]
         yn_soft = dc.cpx_AWGN(2*y-1,EbN0-3,1) # Channel SNR is 3 dB less for rate 1/
       →2
          yn_hard = ((np.sign(yn_soft.real)+1)/2).astype(int)
          z = cc1.viterbi_decoder(yn_hard, 'hard')
          # Count bit errors
          bit_count, bit_errors = dc.bit_errors(x,z)
          total_bit_errors += bit_errors
          total_bit_count += bit_count
          print('Bits Received = %d, Bit errors = %d, BEP = %1.2e' %\
```

Bits Received = 99991, Bit errors = 1218, BEP = 1.22e-02

```
(total_bit_count, total_bit_errors,\
         total_bit_errors/total_bit_count))
print('Bits Received = %d, Bit errors = %d, BEP = %1.2e' %
     (total_bit_count, total_bit_errors,\
      total_bit_errors/total_bit_count))
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1224, BEP = 1.22e-02
***************
Bits Received = 99991, Bit errors = 1224, BEP = 1.22e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1344, BEP = 1.34e-02
******************
Bits Received = 99991, Bit errors = 1344, BEP = 1.34e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1342, BEP = 1.34e-02
******************
Bits Received = 99991, Bit errors = 1342, BEP = 1.34e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1186, BEP = 1.19e-02
***************
Bits Received = 99991, Bit errors = 1186, BEP = 1.19e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1339, BEP = 1.34e-02
******************
Bits Received = 99991, Bit errors = 1339, BEP = 1.34e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1436, BEP = 1.44e-02
*******************
Bits Received = 99991, Bit errors = 1436, BEP = 1.44e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1202, BEP = 1.20e-02
***************
Bits Received = 99991, Bit errors = 1202, BEP = 1.20e-02
Rate 1/2 Object
kmax = 0, taumax = 0
Bits Received = 99991, Bit errors = 1209, BEP = 1.21e-02
*******************
```

Bits Received = 99991, Bit errors = 1209, BEP = 1.21e-02 633 ms \pm 12.4 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)

100000 bits

Python: 1min 20s \pm 3.82 s per loop (mean \pm std. dev. of 7 runs, 1 loop each)

Rust: $2.73 \text{ s} \pm 135 \text{ ms}$ per loop (mean \pm std. dev. of 7 runs, 1 loop each)

The convolutional encoder and decoder functions built in Rust run faster than the Python versions. The time to process the Viterbi decoder runs about 30 times faster.