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The magical file to quickly get a solution to a problem encountered before without searching the Internet.

## Trigonometry

### Cosine → Sine Conversion

$$\cos(\theta - 90) = \sin(\theta)$$

$$\sin(\theta + 90) = \cos(\theta)$$

## RLC Circuit Analysis

### Impedance of Series Circuit :

$$Z^2 = R^2 + (X_L - X_C)^2$$

Impedance of Inductor :  $X_L = 2\pi fL$

Impedance of Capacitor :  $X_C = \frac{1}{2\pi fC}$

### Leading/Lagging Component

- **ELI** the **ICE** man
- Voltage Leads Current in Inductor Circuit.
- Current Leads Voltage in Capacitor Circuit.

### Reactive Power

$$Q = VI \sin(\theta)$$

- Resistive Load :  $Q_L = I^2 X_L$
- Capacitive Load :  $Q_C = I^2 X_C$

### Phase Relationships

$$S = P + jQ = VI \cos(\theta) + jVI \sin(\theta) = VI \angle \theta$$

- Real Power :  $P = VI_{in}$  - Reactive Power :  $Q = VI_{out}$  - Apparent Power :  $S = \sqrt{Q^2 + P^2}$

## Signal Analysis

### Aliasing

Example :

$$x_a(t) = 3 \cos(600\pi t) + 2 \cos(1800\pi t)$$

- Sampling Frequency : 1000 Hz
- Aliasing : Sampling frequency  $\leq 2F$

Frequencies in Resulting Discrete-time signal : -  $f_1 = \frac{F_1}{F_s} = \frac{300}{1000} = 0.3$  cycles/sample -  $f_2 = \frac{F_2}{F_s} = \frac{900}{1000} = 0.9$  cycles/sample

$f_2$  appearing as  $f_2^{\text{alias}} = 0.9 - 1 = -0.1$  cycles/sample

- $f_2 = \frac{F_2}{F_s} = \frac{900}{1000} = 0.9$  cycles/sample

### Power and Energy of Signal

#### Energy

$$E = \sum_{n=-\infty}^{\infty} |x(n)|^2$$

#### Power

$$P = \lim_{N \rightarrow \infty} \frac{1}{2N+1} \sum_{n=-N}^N |x(n)|^2$$

For  $x(n) = A \cos(2\pi f n + \phi)$  :

$$P = \frac{A^2}{2}$$

### Impulse Response

1. System Equation
2. Impulse Response
3. Characteristic Equation from Poles
4. General Form
5. Impulse Response from General Form

Example :

$$y(n) = 0.25y(n-1) + \frac{1}{8}y(n-2) + x(n) - x(n-1)$$

$$\text{Impulse Response : } h(n) = 0.25h(n-1) + \frac{1}{8}h(n-2) + \delta(n) - \delta(n-1)$$

$$\text{Characteristic Equation : } \lambda^2 - 0.25\lambda - 0.125 = 0 \quad \lambda_1 = 0.5, \lambda_2 = -0.25$$

$$\text{General Form : } h(n) = c_1(0.5)^n + c_2(-0.25)^n \text{ for } n \geq 1$$

From Impulse Response :

$$h(0) = 1, h(1) = -0.75, h(2) = -0.0625$$

From General Form :

$$n = 1 : 0.5c_1 - 0.25c_2 = -0.75$$

$$n = 2 : 0.25c_1 - 0.0625c_2 = -0.0625$$

$$c_1 = -\frac{2}{3}, c_2 = \frac{5}{3}$$

Impulse Response from General Form :

$$h(n) = (-2/3)(0.5)^n + (5/3)(-0.25)^n \text{ for } n \geq 0$$

### Steady-state response

Example :

$$x(n) = 2 \cos(0.1\pi n)u(n)$$

$$H(z) = \frac{1 - 0.5z^{-1}}{1 - \frac{1}{12}z^{-1} + \frac{1}{12}z^{-2}}$$

1. Frequency Response.  $H(jw) = H(z)|_{z \equiv e^{jw}} = 1.0332 \times e^{0.358j}$
2. Fundamental Frequency.  $w_0 = 0.1\pi$
3. Substitute Fundamental Frequency into Frequency Response.
4. Steady-state Response.  $y(n) = 2 \times 1.0332 \times \cos(0.1\pi n + 0.358)u(n)$

### Zero-state Step Response

The step response is the system's output when the input is  $u(n)$ .

### Zero-input Response

- Poles of the system.

$$y_{zi} = [A(p_1)^n + B(p_2)^n]u(n)$$

### Stability of a System

Determine if the poles of the system are within the unit circle.

### Initials and Final Values of Causal Signal

- Signal is causal

### Initial Value

$$\lim_{z \rightarrow \infty} z^{-1} = 0$$

### Final Value

$$\lim_{z \rightarrow 1} z^{-1} = 1$$

### Statistical Calculations

#### Mean

$$\mu = E[X] = \int_{-\infty}^{\infty} xp(x)dx$$

### Mean Square

$$\mu = E[X^2] = \int_{-\infty}^{\infty} x^2 p(x) dx$$

### Variance

$$Var[X] = E[X^2] - \mu^2$$

### Standard Deviation

$$\sigma = \sqrt{Var[X]}$$

### Quantisation Noise

$$\Delta = \frac{x_{max} - x_{min}}{L}$$

**Variance of Quantisation Noise** Signal Power is also equal to Quantisation Noise variance.

$$P_{signal} = \delta^2 = \Delta/12$$

### Signal to Quantisation-Noise Ratio

$$SQNR = \frac{P_{signal}}{P_{noise}} = L^2$$

### Autocorrelation Sequence

$$r_{xx}(l) = \sum_{n=-\infty}^{\infty} x(n)x(n-l)$$

With number sequences :

$$x(n) = \{1, 2, 1, 1\}$$

- Do multiplication with

$$\begin{array}{r} \begin{array}{cccc} 1 & 2 & 1 & 1 \\ 1 & 1 & 2 & 1 \end{array} \quad \backslash \backslash \text{ Inverted } x(n) \\ \hline \begin{array}{ccccccc} & & 1 & 2 & 1 & 1 & \\ & 2 & 4 & 2 & 2 & 0 & \\ 1 & 2 & 1 & 1 & 0 & 0 & \\ 1 & 2 & 1 & 1 & 0 & 0 & 0 \end{array} \\ \hline 1 & 3 & 5 & 7 & 5 & 3 & 1 \end{array}$$

### Communication System

Information Source -> Input Transducer -> Transmitter -> Channel -> Receiver -> Output Transducer -> Sink

Source Encoder -> Channel Encoder -> Modulator

Demodulator -> Channel Decoder -> Source Decoder

## Instantaneous Frequency

Example :

$$x(t) = 2 \cos(2\pi 10t + 10\pi t^2)$$

Instantaneous Frequency :

$$f(t) = \frac{1}{2\pi} \frac{d(2\pi 10t + 10\pi t^2)}{dt} = 10 + 10t$$

**VCO** Instantaneous Frequency :

$$f(t) = f_c + k_f m(t)$$

## AM Modulation

Amplitude of AM Signal :

$$A_{max} = A_C(1 + \mu)$$

$$A_{min} = A_C(1 - \mu)$$

$$A_m = A_C \times \mu$$

Example :

$$x_c(t) = A_c[1 + \mu x(t)] \cos(w_c t)$$

Assuming that  $\mu < 1$ .

- Transmitted Power =  $P_t = \langle x_c^2(t) \rangle$
- Power in Message Signal =  $P_x = \langle x^2(t) \rangle$

Find an expression for transmitted power in terms of message power and modulation index.

Substitute expression for transmitted power :

$$P_t = \frac{1}{2} A_c^2 \langle 1 + 2\mu x(t) + \mu^2 x^2(t) \rangle + \frac{1}{2} A_c^2 \langle [1 + \mu x(t)]^2 \cos(2w_c t) \rangle$$

- Time average of a constant is the same.
- Twice the carrier frequency component was removed
- Message Signal has no DC Component  $\langle x(t) \rangle = 0$

$$P_t = \frac{1}{2} A_c^2 (1 + \mu^2 P_x) = \frac{1}{2} A_c^2 + \frac{1}{2} A_c^2 \mu^2 P_x$$

- First term is unmodulated carrier power  $\mu = 0$
- Second term is power in carrier plus the signal
- Significant percentage of power resides in the carrier and conveys no information.

## FM Modulation

### FM Modulation Index

$$\mu_f = \frac{A_m k_f}{f_m}$$

- $A_m k_f \leftarrow$  Maximum Frequency Deviation,  $f_{max}$
- Narrowband FM,  $\mu_f \ll 1$

Example :

VCO has sensitivity constant of  $3kHz/V$  and free running frequency of  $1MHz$ . Input to VCO is tone signal with peak amplitude equal to  $2V$  and frequency  $4kHz$ . Output signal is FM. Calculate modulation index of the output FM Signal.

$$\begin{aligned} f_c &= 1 \times 10^6 \quad k_f = 3 \times 10^3 \quad f(t) = f_c + k_f m(t) \\ m(t) &= A_m \cos(2\pi f_m t) = 2 \cos(2\pi \times 4000t) \\ f_{max} &= k_f \max\{|m(t)|\} = 3 \times 10^3 \times 2 = 6 \times 10^3 Hz \\ \mu_f &= \frac{6kHz}{4kHz} = 1.5 \end{aligned}$$

### Narrowband FM Magnitude Spectrum :

$$e(t) \approx A_c \cos(w_c t) - A_c \mu_f \sin(w_m t) \sin(w_c t)$$

$$e(t) \approx A_c \cos(w_c t) - \frac{A_c \mu_f}{2} \cos(w_c - w_m)t + \frac{A_c \mu_f}{2} \cos(w_c + w_m)t$$

Example :

Draw a double-sided magnitude spectrum for the Narrowband FM signal.

$$e(t) = 10 \cos[2\pi 10^7 t + 0.2 \cos(2\pi 10^4 t)]$$

- $\mu_f = 0.2$

$$e(t) = A_c \cos(2\pi 10^7 t) - A_c \mu_f \cos(2\pi 10^4 t) \sin(2\pi 10^7 t)$$

- Carrier Signal has amplitude of 5 and two side-bands which are message signals with amplitude of 0.5

### Wideband FM

$$\begin{aligned} e(t) &= A_c J_n(\mu_f) \cos(w_c t) \\ &+ \sum_{n \text{ even}}^{\infty} A_c J_n(\mu_f) [\cos(w_c + n w_m)t + \cos(w_c - n w_m)t] \\ &+ \sum_{n \text{ odd}}^{\infty} A_c J_n(\mu_f) [\cos(w_c + n w_m)t - \cos(w_c - n w_m)t] \end{aligned}$$

- FM spectrum has carrier frequency line and **infinite** number of side-band lines at  $f_c \pm n f_m$ .
- Lines equally spaced by  $f_m$ .
- Odd-order lower side-band lines reversed in phase.
- $J_n(\mu_f)$  obtained from the Bessel Function Values table.

## Bessel Function Values Table

Modulation index	Carrier	Side-band 1	Side-band 2	Side-band 3	Side-band 4	Side-band 5	Side-band 6	Side-band 7	Side-band 8	Side-band 9	Side-band 10	Side-band 11	Side-band 12	Side-band 13	Side-band 14	Side-band 15	Side-band 16
0.00	1.00																
0.25	0.98	0.12															
0.5	0.94	0.24	0.03														
1.0	0.77	0.44	0.11	0.02													
1.5	0.51	0.56	0.23	0.06	0.01												
2.0	0.22	0.58	0.35	0.13	0.03												
2.41	0.00	0.52	0.43	0.20	0.06	0.02											
2.5	-0.05	0.50	0.45	0.22	0.07	0.02	0.01										
3.0	-0.26	0.34	0.49	0.31	0.13	0.04	0.01										
4.0	-0.40	-0.07	0.36	0.43	0.28	0.13	0.05	0.02									
5.0	-0.18	-0.33	0.05	0.36	0.39	0.26	0.13	0.05	0.02								
5.53	0.00	-0.34	-0.13	0.25	0.40	0.32	0.19	0.09	0.03	0.01							
6.0	0.15	-0.28	-0.24	0.11	0.36	0.36	0.25	0.13	0.06	0.02							
7.0	0.30	0.00	-0.30	-0.17	0.16	0.35	0.34	0.23	0.13	0.06	0.02						
8.0	0.17	0.23	-0.11	-0.29	-0.10	0.19	0.34	0.32	0.22	0.13	0.06	0.03					
8.65	0.00	0.27	0.06	-0.24	-0.23	0.03	0.26	0.34	0.28	0.18	0.10	0.05	0.02				
9.0	-0.09	0.25	0.14	-0.18	-0.27	-0.06	0.20	0.33	0.31	0.21	0.12	0.06	0.03	0.01			
10.0	-0.25	0.04	0.25	0.06	-0.22	-0.23	-0.01	0.22	0.32	0.29	0.21	0.12	0.06	0.03	0.01		
12.0	0.05	-0.22	-0.08	0.20	0.18	-0.07	-0.24	-0.17	0.05	0.23	0.30	0.27	0.20	0.12	0.07	0.03	0.01

### Modulated Signal Example :

Carrier given by  $c(t) = 10 \cos(2\pi f_c t)$ . Message Signal  $\cos(20\pi t)$ . The message is used to frequency modulate the carrier with  $k_f = 50$ . Find expression for modulated signal, determine how many harmonics selected to contain 99% of modulated power.

From message signal :

$$f_m = 10 \text{ Hz}$$

Modulated Signal :

$$\begin{aligned}
 e(t) &= A \cos(2\pi f_c t + 2\pi k_f \int_{-\infty}^t \cos(20\pi \tau) d\tau) \\
 &= 10 \cos(2\pi f_c t + \frac{100\pi}{20\pi} \sin(20\pi t)) \\
 &= 10 \cos(2\pi f_c t + 5 \sin(20\pi t))
 \end{aligned}$$

Modulation index :

$$\mu_f = 5$$

FM Modulated Signal :

$$e(t) = 10 \cos(2\pi f_c t + 5 \sin(20\pi t))$$

Total Power :

$$P = \frac{A^2}{2} = 100/2 = 50$$



Spectral lines are at  $f_c \pm 10n$  - How many of the lines contain 99% of the total power.

General FM Signal Spectrum :

$$e(t) = A_c J_n(\mu_f) \cos(w_c t) + \sum_{n \text{ even}}^{\infty} A_c J_n(\mu_f) [\cos(w_c + nw_m)t + \cos(w_c - nw_m)t] + \sum_{n \text{ odd}}^{\infty} A_c J_n(\mu_f) [\cos(w_c + nw_m)t - \cos(w_c - nw_m)t]$$

- $A_c = 10$  and  $\mu_f = 5$
- Power in carrier line  $\frac{A_c J_0(\mu_f))^2}{2} = \frac{100 J_0^2(5)}{2}$

Value of  $k$  such that at least 99% of power is covered :

$$\sum_{n=-k}^k \frac{100 J_0^2(5)}{2} \geq 0.99P$$

- $k = 6$
- Significant spectral lines at  $f_c \pm 10k$ ,  $k = 1, \dots, 6$
- Effective bandwidth =  $120Hz$  ( $60Hz$  on both sides of carrier)

### Bandwidth of FM Signals

- Bandwidth of FM signal depends on  $f_m$  and  $\mu_f$

**Carson's Rule** : 98% of total power is contained in bandwidth.

$$B_c = 2(\mu_f + 1)W$$

- Modulation Index,  $\mu_f$
- Bandwidth of message signal,  $W$

Example :

$$m(t) = 10 \text{sinc}(10^4 t)$$

Determine transition bandwidth of FM modulated signal with  $k_f = 4000$ .

$$m(t) = \frac{10}{10^4 t} \sin(10^4 \pi t)$$

- Sinc function can be converted to sine function.
- Bandwidth,  $W = 5000Hz$

$$f_{max} = k_f \max\{|m(t)|\} = 4000 \times 10 = 40kHz$$

$$\mu_f = \frac{f_{max}}{W} = \frac{40k}{5k} = 8$$

$$B_c = 2(8 + 1)5k = 90kHz$$

## Information Measure

### Entropy Example

Source = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10}

$$P(1)=P(6)=P(7)=P(10)=1/16$$

$$P(2)=P(3)=P(4)=P(5)=P(8)=P(9)=2/16$$

$$\begin{aligned} \text{Entropy} &= 4 \times -\frac{1}{16} \log_2 \frac{1}{16} + 6 \times -\frac{2}{16} \log_2 \frac{2}{16} \\ &= 3.25 \text{ bits} \end{aligned}$$

### Source Coding Example

% Source has alphabet = {A B C D}

$$P(A)=0.25, \quad P(B)=0.5, \quad P(C)=0.125, \quad P(D)=0.125$$

Encoder 1 : - Encode 4 elements into 2 bits

Element	Bit
A	00
B	01
C	10
D	11

Encoder 2 : - Account Probabilities

Element	Bit
A	10
B	0
C	110
D	111

### Source Rate

$$R = \frac{H}{T}$$

- H, Entropy
- T, Time

### Noiseless Channel Capacity

$$C = 2B \log_2 M$$

$$C = B \log_2 \left(1 + \frac{S}{N}\right)$$

- B, Bandwidth
- M, Level Signalling
- C, Channel Capacity

## Signal-to-Noise Ratio (SNR)

$$SNR = \frac{P_x}{P_n}$$

$$SNR_{db} = 10 \log_{10} SNR$$

## Quantisation

### Uniform Quantisation

Step Size :

$$\Delta = \frac{(x_{max} - x_{min})}{L}$$

- $L = 2^n$ , Number of discrete levels

$$Eq(l) = |x - q_l| \quad q_l = x_{min} + \Delta/2 + l \times \Delta$$

Accuracy :

$$\text{Accuracy} = \frac{E}{D}$$

Maximum Quantisation Error :

$$E = \frac{\Delta}{2}$$

Bit Rate :

$$R = f_s \times n$$

### $\mu$ -Law Warping/Unwarping

Sample Compressing (Warping) + Uniform Quantisation + Sample Expanding (Unwarping)

$\mu$ -Law Warping :

$$F(x) = x_{max} \frac{\ln(1 + \mu[\frac{|x|}{x_{max}}])}{\ln(1 + \mu)} \cdot \text{sgn}(x)$$

$\mu$ -Law Unwarping :

$$\hat{x} = F^{-1}(F(x)) = \frac{x_{max}}{\mu} [(1 + \mu)^{\frac{|F(x)|}{x_{max}}} - 1] \cdot \text{sgn}(F(x))$$

## Encoding

Type of Encoding	Characteristics
Unipolar	Only 1s and 0s
NRZ-L	Positive voltage mean 0 Negative voltage mean 1
NRZ-I	Transition when next bit is 1
RZ	Positive, Negative and 0 Change to 0 and Positive for 1 and Negative for 0
Manchester	Low -> High represents 1 High -> Low represents 0
Differential Manchester	Transition at beginning means 0 No transition means 1

## Raised Cosine Pulse Shaping

Bandwidth :

$$B_{RC} = \frac{1 - \alpha}{2T}$$

Efficiency :

$$E_{RC} = \frac{2}{1 - \alpha}$$

## Pulse Shaping

Type of Pulse Shaping	Characteristics
Nyquist	Problems :- Time duration long- Ideal Synchronisation Required
Raised Cosine	Reduce Intersymbol Interference (ISI)

## Matched Filtering

Matched Filter :

$$H(f) = K \frac{S^*(f)}{P_n(f)} e^{-j2\pi f t_0}$$

Impulse Response :

$$h(t) = Cs(t_0 - t)$$

- Known signal played backward and translated by  $t_0$
- Autocorrelation function maximum when perfectly aligned

Power Spectral Density of White Noise :

$$P_n(f) = \frac{N_0}{2}$$

Probability of bit error :

$$P_e < \frac{e^{-E_b/N_0}}{2\sqrt{\pi E_b/N_0}}$$

- $E_b$ , Transmitted signal energy per bit
- $N_0$ , Noise spectral density
- $\frac{E_b}{N_0}$  proportional to SNR

## Equalisation

- Equalising Filter to minimise ISI
- Two types :
  - Zero Forcing Equaliser
  - MMSE Equaliser

## Digital Modulation

$$a \cos(2\pi f_c t + \theta)$$

Binary Shift Keyring	Characteristics
Frequency Shift Keyring	Carrier Frequency of signal changed to represent 1,0
Amplitude Shift Keyring	Amplitude of signal changed to represent 1,0
Phase Shift Keyring	Phase of signal changed to represent 1,0

M-ary Digital Modulation	Characteristics
Quadrature PSK	Four phased used, represented by dibit
M-ary Quadrature Amplitude Modulation	Combines ASK and PSK
Differential PSK	Encode information in phase difference

### Discrete Time Fourier Transform (DTFT)

DTFT :

$$X(jw) = \sum_{n=-\infty}^{\infty} x[n]e^{-jwn}$$

IDTFT :

$$x[n] = \frac{1}{2\pi} \int_{w=-\pi}^{\pi} X(jw)e^{jwn}dw$$

### Discrete Fourier Transform (DFT)

DFT :

$$X[k] = \sum_{n=0}^{N-1} x[n]e^{-j\frac{2\pi k}{N}n}$$

IDFT:

$$X[n] = \frac{1}{N} \sum_{k=0}^{N-1} X[k]e^{j\frac{2\pi k}{N}n}$$

### Geometric Series

$$\sum_{n=0}^{N-1} a^n = \frac{1 - a^{N-1+1}}{1 - a}$$

### Circular Convolution

Time domain Method :

$$y(m) \equiv \sum_{n=0}^{N-1} x_1(n)x_2((m-n)_N)$$

DFT and IDFT Method :

1. Find DFT's of the input sequences
2. Product of the two DFT's
3. Inverse DFT

Example :

$$x_1(n) = \{1, 3, 5, 7\}$$

$$x_2(n) = \{2, 4, 6, 8\}$$

$$X_1(k) = 1 + 3W_4^k + 5W_4^{2k} + 7W_4^{3k}$$

$$X_2(k) = 2 + 4W_4^k + 6W_4^{2k} + 8W_4^{3k}$$

$$\text{Product of two DFT, } Y(k) = X_1(k)X_2(k) = 84 + 92W_4^k + 84W_4^{2k} + 60W_4^{3k}$$

$$\text{Inverse DFT, } y(n) = 84, 92, 84, 60$$

### Direct Form Realisation

Transfer Function :

$$H(z) = \frac{Y(z)}{X(z)}$$

- Top portion is non-recursive
- Bottom portion is recursive

Cascade Form :

$$H(z) = CH_1(z)H_2(z)$$

- Splitting the two fractions into different direct form II
- Multiply by the constant at the end

Parallel Form :

- Partial Fraction Decomposition to get different terms
- Each term is a sub-system by itself
- Sums after computation within each sub-system

## AVR Programming

### Common Items

#### Pointer Register Locations

Pointer Register	HEX	DEC	BIN
X-Register Low Byte	1A	26	11010
X-Register High Byte	1B	27	11011
Y-Register Low Byte	1C	28	11100
Y-Register High Byte	1D	29	11101
Z-Register Low Byte	1E	30	11110
Z-Register High Byte	1F	31	11111

### AVR Addressing Mode

Addressing Mode	Example
I/O Direct Addressing	IN r8, SPL
Immediate Addressing	ANDI r16, 0x0D
Data Direct Addressing	STS 0x00AA, r2
Data Indirect Addressing (no +/-)	ST Y, r13
Data Indirect Addressing with Post-Increment	ST Y+, r28
Data Indirect Addressing with Pre-Decrement	LD r15, -X
Data Indirect Addressing with Displacement	LDD Z+1, r21