Final Report

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Introduction

As human populations are rising across the world, so is the proportion of people that live in urban areas. Estimates from the *UN World Urbanization Prospects* (2018) indicate that over 4.2 billion people (55% of the global population) currently live in urban areas, and by 2050, an additional 2.5 billion people (68% of the global population) could be living in urban areas. More people living in urban areas calls for more space-, cost-, and energy-efficient systems of transportation as an alternative to cars. One such promising transportation alternative is the implementation of bicycle sharing programs.

Bicycle sharing programs are transportation schemes that allow individuals to rent bicycles on a short-term basis for either a set rate or for free. Most bicycle sharing programs have many computer-controlled bicycle rack "hubs" dispersed across a city that keep bikes locked and release them for use when a user enters the appropriate information/payment from a station or an app (Figure 1). A user can then ride the bike and return it to any other bicycle hub that is part of the same program. Many cities across the world have begun implementing bicycle sharing programs, including Chapel Hill, which has a Tar Heel Bikes sharing system¹. Systems like these provide convenient, inexpensive, and eco-friendly transportation options for individuals residing in a city.



Figure 1: A 'hub' of bicycles belonging to the Santander Cycles system in London. SOPA Images/Lightrocket via Getty Images

Successful implementations of bike sharing programs depend on proper management of these systems. It is important for a bike sharing program to provide a stable supply of rental bikes to its population so its users feel that they can rely on the system for their transportation needs. The analysis of bike sharing data allows for a better understanding of the demand of rental bikes in a city, which, in turn, can help inform a city about how to provide appropriate supplies of rental bikes for its population. For our project, we were interested in predicting the number of bikes rented within a given bike sharing system given information about weather,

 $^{^{1}}$ https://move.unc.edu/bike/bikeshare/

time of day, and date. We were also interested in assessing the most important variables for predicting bike rental counts. To answer these questions, we fit and evaluated a negative binomial generalized mixed model, a conditional inference tree, and a random forest model, using data from three publicly available bike sharing demand datasets.

The first dataset we use is a London bike sharing demand dataset downloaded from Kaggle² and provided by Transport for London³. This dataset contains hourly bike rental count observations over two years, from Jan 04 2015 - Jan 03 2017. The first full consecutive year of data was used as the training set in the analysis, and the second full consecutive year of data was held out as a test set.

The second dataset we use is a Seoul bike sharing demand dataset downloaded from the UCI Machine Learning Repository⁴ and provided by the Seoul Metropolitan Government⁵. This dataset contains hourly bike rental counts over one year, from Dec 1 2017 - Nov 30 2018. This was used as an independent test set. The third dataset we use is a Washington, D.C. bike sharing demand dataset downloaded from Kaggle⁶ and provided by Capital Bikeshare⁷. This dataset contains hourly bike rental counts over two years, from Jan 01 2011 - Dec 31 2012. This was used as an independent test set.

Each dataset contained hourly observations of bike rental count data. To simplify our analysis, we chunked the hourly data into three time blocks: [0:00 - 8:00), [8:00 - 16:00), and [16:00 - 24:00). Additionally, because temperature and humidity can be correlated with time of day, we chose to use the maximum and minimum daily temperature and humidity measurements for each 8-hour data point in order to avoid any issues of colinearity.

We created an R package named bikeSharing that includes methods for training and evaluating the negative binomial glmm and random forest models, as well as the processed source data from all three sets.

The below code can be used to install the package and load the package library. The zipped package source data, bikeSharing_1.0.0.tar.gz can be found in the Github repository for our project⁸.

```
if(!require("bikeSharing", quietly = TRUE))
  install.packages("package/bikeSharing_1.0.0.tar.gz", repos = NULL)
library(bikeSharing)
```

Once the package is loaded, the bike sharing data from all three sets becomes easily accessible through the variable names london, seoul, and dc. To directly load them into the R environment, one can simply run:

```
data("london", "seoul", "dc")
```

All three datasets contain bike rental count data as well as 11 additional weather-, time-, and date-related variables that were used as predictors in our models:

- Hour chunk (00:00 8:00, 8:00-16:00, 16:00-24:00)
- Weekend status (Yes/No)
- Holiday status (Yes/No)
- Season (Winter, Spring, Summer, Autumn)
- Minimum daily temperature (C)
- Maximum daily temperature (C)
- Minimum daily humidity (%)
- Maximum daily humidity (%)
- Wind speed (m/s)
- Presence of any rain or snow (Yes/No)
- Date (mm-dd)

The way that these variables are used within our models will be further described in the Methods section. For all of the analyses performed, the london dataset was divided into training and testing sets, where the

 $^{^2} https://www.kaggle.com/datasets/hmavrodiev/london-bike-sharing-dataset$

³https://cycling.data.tfl.gov.uk

⁴https://archive.ics.uci.edu/ml/datasets/Seoul+Bike+Sharing+Demand

⁵https://data.seoul.go.kr

⁶https://www.kaggle.com/datasets/marklvl/bike-sharing-dataset

⁷https://ride.capitalbikeshare.com/system-data

 $^{^8 \}rm https://github.com/brookefelsheim/bios735-group1$

training set contained all "Year 1" data (Jan 04 2015 - Jan 03 2016), and the testing set contained all "Year 2" data (Jan 04 2016 - Jan 03 2017).

```
london_train <- london[london$Year == "Year 1",]
london_test <- london[london$Year == "Year 2",]</pre>
```

Methods

Negative Binomial Generalized Linear Mixed Model

Let y_{ij} be the number of bikes rented at hour chunk j of day i. Thus i ranges from 1 to 365, and j ranges from 1 to 3, corresponding to hour chunks [00:00 - 8:00, 8:00-16:00, 16:00-24:00]. We assume that the number of bikes rented for a given hour chunk within a specific day follows a negative binomial distribution, so $Y_{ij} \sim NB(\mu_{ij}, \theta)$ using the Hilbe parameterization, so:

$$P(Y_{ij} = y_{ij} | \mu_{ij}, \theta) = \frac{\Gamma(y_{ij} + \theta)}{\Gamma(y_{ij} + 1)\Gamma(\theta)} \left(\frac{\theta}{\theta + \mu_{ij}}\right)^{\theta} \left(\frac{\mu_{ij}}{\theta + \mu_{ij}}\right)^{y_{ij}}$$
(1)

The mean of y_{ij} for each day i at hour chunk j is μ_{ij} , which we assume follows a negative binomial generalized linear mixed model with a random intercept. Thus it is determined from the following model:

$$\log(\mu_{ij}) = x_{ij}^T \beta + b_i \tag{2}$$

Let $x_{ij} = (1, I(HourChunk_{ij} = [8,16)), I(HourChunk_{ij} = [16,24)), Weekend_i, Holiday_i, I(Season_i = Spring), I(Season_i = Summer), I(Season_i = Winter), Min_Temperature_i, Max_Temperature_i, Min_Humidity_i, Max_Humidity_i, Wind_Speed_{ij}, Rain_or_Snow_{ij})^T.$

HourChunk_{ij} is a categorical variable corresponding to the hour chunk j of day i, with the reference hour chunk being [0:00,8:00), Weekend_i is a binary variable with 1 if day i is a weekend, 0 if it is not, Holiday_i is a binary variable with 1 if day i is a holiday, 0 if it is not. Season_i is a categorical variable corresponding to which season day i is in, with the reference season being Autumn. The Min_Temperature_i and Max_Temperature_i are the minimum and maximum temperature of day i, respectively. Similarly, The Min_Humidity_i and Max_Humidity_i are the minimum and maximum humidity of day i, respectively. Wind_Speed_{ij} is the average wind speed of hour chunk j of day i. Rain_or_Snow_i is a binary variable with 1 if during day i hour chunk j there is any rain or snow, 0 if there is not. Thus $\beta = (\beta_0, \beta_1, \beta_2, \beta_3, \beta_4, \beta_5, \beta_6, \beta_7, \beta_8, \beta_9, \beta_{10}, \beta_{11}, \beta_{12}, \beta_{13})'$.

In Equation (2), b_i is the unobserved random effect that the day i has on the number of rented bikes at any given hour chunk. It is assumed that $b_i \sim N(0, \sigma_{\gamma}^2)$.

Thus, of interest is the estimate θ , β , and σ_{γ}^2 . Equations 1 and 2 can be combined to obtain the following likelihood equation for a given day (i).

$$L(\theta, \beta, \sigma_{\gamma}^{2} | \mathbf{y}, \mathbf{b}) = \prod_{i=1}^{365} \prod_{j=1}^{3} p(y_{ij}) = \prod_{i=1}^{365} \left(\prod_{j=1}^{3} f(y_{ij} | \mu_{ij}) \right) f(b_{i} | \sigma_{\gamma}^{2})$$
(3)

Since the random effects b_i are unobservable, this means they must be integrated out of the above expression to obtain the likelihood, so:

$$L(\theta, \beta, \sigma_{\gamma}^{2} | \mathbf{y}, \mathbf{b}) = \prod_{i=1}^{365} \left[\int \left(\prod_{j=1}^{3} f(y_{ij} | \mu_{ij}) \right) f(b_{i} | \sigma_{\gamma}^{2}) db_{i} \right]$$

$$= \prod_{i=1}^{365} \left[\int \prod_{j=1}^{3} \frac{\Gamma(y_{ij} + \theta)}{\Gamma(y_{ij} + 1)\Gamma(\theta)} \left(\frac{\theta}{\theta + e^{x_{ij}^T \beta + b_i}} \right)^{\theta} \left(\frac{e^{x_{ij}^T \beta + b_i}}{\theta + e^{x_{ij}^T \beta + b_i}} \right)^{y_{ij}} \frac{1}{\sqrt{2\pi\sigma_{\gamma}^2}} \exp\left(-\frac{b_i^2}{2\sigma^2} \right) db_i \right]$$

So thus, the log likelihood is found to be

$$l(\theta, \beta, \sigma_{\gamma}^{2}) = \sum_{i=1}^{365} log \left[\int \prod_{j=1}^{3} \frac{\Gamma(y_{ij} + \theta)}{\Gamma(y_{ij} + 1)\Gamma(\theta)} \left(\frac{\theta}{\theta + e^{x_{ij}^{T}\beta + b_{i}}} \right)^{\theta} \cdot \left(\frac{e^{x_{ij}\beta + b_{i}}}{\theta + e^{x_{ij}\beta + b_{i}}} \right)^{y_{ij}} \frac{1}{\sqrt{2\pi\sigma_{\gamma}^{2}}} \exp\left(-\frac{b_{i}^{2}}{2\sigma_{\gamma}^{2}} \right) db_{i} \right]$$

$$(4)$$

We will use MCEM algorithm to solve the problem and use Metropolis Hastings Algorithm with a random walk to sample the random effects b_i for the i-th day. Let $Y_i = (y_{i1}, y_{i2}, y_{i3})^T$. The density function for b_i given $Y_i, \beta, \theta, \sigma_{\gamma}^2$ is:

$$P(b_{i}|Y_{i},\theta,\beta,\sigma_{\gamma}^{2}) \propto P(Y_{i}|b_{i},\theta,\beta,\sigma_{\gamma}^{2}) \cdot P(b_{i}|\sigma_{\gamma}^{2})$$

$$\propto \prod_{j=1}^{3} \left(\frac{\theta}{\mu_{ij}+\theta}\right)^{\theta} \cdot \left(\frac{\mu_{ij}}{\mu_{ij}+\theta}\right)^{y_{ij}} \cdot \exp\left(-\frac{b_{i}^{2}}{2\sigma_{\gamma}^{2}}\right)$$

$$\propto \sum_{j=1}^{3} \left[(y_{ij}\log\mu_{ij} - (y_{ij}+\theta)\log(\mu_{ij}+\theta)) - \frac{b_{i}^{2}}{2\sigma_{\gamma}^{2}} \right]$$
(5)

Here is our Metropolis Hastings Algorithm with a random walk: Step 1: Let b_i^* be generated by $b_i^* = b^{(t)} + \epsilon$, where $\epsilon \sim U(-a, a)$. And we need to do parameter tuning on a to to achieve around 20%-35% acceptance rate for optimal efficiency. Step 2: Compute the Metropolis–Hastings ratio $R(b_i^{(t)}, b_i^*)$ where

$$R(b_i^{(t)}, b_i^*) = \frac{f(y_{ij}|\phi, b_i^*)f(b^*|\sigma^2)}{f(y_{ij}|\phi, b_i^{(t)})f(b^{(t)}|\sigma^2)}$$

Step 3: Pick the new value for $b_i^{(t+1)}$ such that

$$b_i^{(t+1)} = \begin{cases} b_i^* \text{with probability} \min(R(b_i^{(t)}, b_i^*), 1) \\ b_i^{(t)} \text{otherwise.} \end{cases}$$

Step 4: Set t=t+1 and return to step 1.

Also we will use Nelder-Mead in the M-step because it does not require 1st or 2nd derivatives and it is robust.

```
[1] -10009.51
Maximizing -- use negfn and neggr
Iter: 1 Qf: -10009.508 s2gamma: 0.139693 Intercept: 8.288
Hour_Chunks[8,16):1.515 Hour_chunks[16,24): 1.426 Is_weekend:-0.258
Is_holiday:-0.445 SeasonSpring:0.007 SeasonSummer:0.020 SeasonWinter:-0.289
Min temp: 0.006 Max temp: -0.005 Min humidity: -0.000 Max humidity: 0.000
Wind speed: -0.002 Rain or snow: -0.200 theta: 10.380 eps: 0.989990
[1] -9927.993
Maximizing -- use negfn and neggr
Iter: 2 Qf: -9927.993 s2gamma: 0.115304 Intercept: 8.288
Hour_Chunks[8,16):1.492 Hour_chunks[16,24): 1.385 Is_weekend:-0.253
Is_holiday:-0.404 SeasonSpring:0.056 SeasonSummer:0.093 SeasonWinter:-0.264
Min_temp:0.003 Max_temp:-0.003 Min_humidity:0.000 Max_humidity:-0.001
Wind_speed: 0.001 Rain_or_snow: -0.183 theta: 12.726 eps: 0.008144
[1] -9837.183
Maximizing -- use negfn and neggr
Iter: 3 Qf: -9837.183 s2gamma: 0.081402 Intercept: 8.219
Hour Chunks [8,16):1.529 Hour chunks [16,24): 1.414 Is weekend:-0.272
Is_holiday:-0.392 SeasonSpring:0.035 SeasonSummer:0.099 SeasonWinter:-0.242
Min temp: 0.008 Max temp: -0.004 Min humidity: -0.001 Max humidity: -0.000
Wind_speed:0.000 Rain_or_snow:-0.192 theta:14.086 eps:0.009147
[1] -9763.714
Maximizing -- use negfn and neggr
Iter: 4 Qf: -9763.714 s2gamma: 0.070620 Intercept: 8.291
Hour_Chunks[8,16):1.547 Hour_chunks[16,24): 1.424 Is_weekend:-0.298
Is holiday:-0.388 SeasonSpring:0.023 SeasonSummer:0.089 SeasonWinter:-0.221
Min_temp:0.013 Max_temp:-0.005 Min_humidity:-0.002 Max_humidity:-0.000
Wind_speed:-0.006 Rain_or_snow:-0.174 theta:16.304 eps:0.007468
[1] -9692.282
Maximizing -- use negfn and neggr
Iter: 5 Qf: -9692.282 s2gamma: 0.059093 Intercept: 8.240
Hour_Chunks[8,16):1.517 Hour_chunks[16,24): 1.397 Is_weekend:-0.308
Is_holiday:-0.360 SeasonSpring:0.015 SeasonSummer:0.092 SeasonWinter:-0.228
Min_temp:0.013 Max_temp:-0.001 Min_humidity:-0.003 Max_humidity:-0.000
Wind speed: -0.001 Rain or snow: -0.174 theta: 17.007 eps: 0.007316
[1] -9655.907
Maximizing -- use negfn and neggr
Iter: 6 Qf: -9655.907 s2gamma: 0.054342 Intercept: 8.222
Hour_Chunks[8,16):1.516 Hour_chunks[16,24): 1.405 Is_weekend:-0.312
Is_holiday:-0.361 SeasonSpring:0.003 SeasonSummer:0.099 SeasonWinter:-0.219
Min temp: 0.013 Max temp: -0.000 Min humidity: -0.003 Max humidity: -0.000
Wind_speed:-0.002 Rain_or_snow:-0.174 theta:17.768 eps:0.003753
[1] -9624.324
Maximizing -- use negfn and neggr
Iter: 7 Qf: -9624.324 s2gamma: 0.047064 Intercept: 8.208
Hour_Chunks[8,16):1.528 Hour_chunks[16,24): 1.409 Is_weekend:-0.322
Is_holiday:-0.383 SeasonSpring:-0.007 SeasonSummer:0.109 SeasonWinter:-0.221
Min_temp:0.014 Max_temp:-0.000 Min_humidity:-0.003 Max_humidity:-0.000
Wind_speed:-0.006 Rain_or_snow:-0.172 theta:18.032 eps:0.003271
[1] -9601.023
Maximizing -- use negfn and neggr
Iter: 8 Qf: -9601.023 s2gamma: 0.040836 Intercept: 8.171
Hour_Chunks[8,16):1.525 Hour_chunks[16,24): 1.407 Is_weekend:-0.328
Is holiday: -0.398 SeasonSpring: -0.009 SeasonSummer: 0.111 SeasonWinter: -0.205
```

```
Min_temp: 0.016 Max_temp: 0.001 Min_humidity: -0.004 Max_humidity: 0.000
Wind_speed:-0.007 Rain_or_snow:-0.173 theta:17.536 eps:0.002421
[1] -9579.64
Maximizing -- use negfn and neggr
Iter: 9 Qf: -9579.640 s2gamma: 0.038947 Intercept: 8.160
Hour Chunks[8,16):1.529 Hour chunks[16,24): 1.415 Is weekend:-0.325
Is holiday: -0.387 SeasonSpring: -0.011 SeasonSummer: 0.110 SeasonWinter: -0.194
Min_temp: 0.016 Max_temp: 0.001 Min_humidity: -0.004 Max_humidity: 0.000
Wind speed: -0.009 Rain or snow: -0.178 theta: 18.146 eps: 0.002227
[1] -9566.678
Maximizing -- use negfn and neggr
Iter: 10 Qf: -9566.678 s2gamma: 0.035977 Intercept: 8.140
Hour_Chunks[8,16):1.534 Hour_chunks[16,24): 1.417 Is_weekend:-0.332
Is_holiday:-0.381 SeasonSpring:-0.015 SeasonSummer:0.106 SeasonWinter:-0.190
Min_temp:0.017 Max_temp:0.001 Min_humidity:-0.004 Max_humidity:0.000
Wind_speed:-0.011 Rain_or_snow:-0.180 theta:18.152 eps:0.001353
[1] -9558.14
Maximizing -- use negfn and neggr
Iter: 11 Qf: -9558.140 s2gamma: 0.034944 Intercept: 8.185
Hour Chunks [8,16):1.539 Hour chunks [16,24): 1.426 Is weekend:-0.345
Is_holiday:-0.400 SeasonSpring:-0.017 SeasonSummer:0.100 SeasonWinter:-0.182
Min temp: 0.019 Max temp: 0.001 Min humidity: -0.005 Max humidity: 0.000
Wind_speed:-0.013 Rain_or_snow:-0.178 theta:17.895 eps:0.000892
[1] -9550.829
Maximizing -- use negfn and neggr
Iter: 12 Qf: -9550.829 s2gamma: 0.033988 Intercept: 8.221
Hour_Chunks[8,16):1.534 Hour_chunks[16,24): 1.421 Is_weekend:-0.347
Is_holiday:-0.401 SeasonSpring:-0.018 SeasonSummer:0.101 SeasonWinter:-0.182
Min_temp:0.019 Max_temp:0.001 Min_humidity:-0.005 Max_humidity:0.000
Wind_speed:-0.014 Rain_or_snow:-0.177 theta:17.985 eps:0.000765
[1] -9545.979
Maximizing -- use negfn and neggr
Iter: 13 Qf: -9545.979 s2gamma: 0.034305 Intercept: 8.276
Hour_Chunks[8,16):1.535 Hour_chunks[16,24): 1.423 Is_weekend:-0.341
Is holiday: -0.392 SeasonSpring: -0.033 SeasonSummer: 0.096 SeasonWinter: -0.186
Min_temp:0.019 Max_temp:0.000 Min_humidity:-0.005 Max_humidity:-0.000
Wind speed: -0.014 Rain or snow: -0.174 theta: 18.295 eps: 0.000508
[1] -9541.885
Maximizing -- use negfn and neggr
Iter: 14 Qf: -9541.885 s2gamma: 0.033014 Intercept: 8.282
Hour Chunks[8,16):1.522 Hour chunks[16,24): 1.412 Is weekend:-0.342
Is holiday: -0.389 SeasonSpring: -0.045 SeasonSummer: 0.088 SeasonWinter: -0.190
Min temp: 0.019 Max temp: 0.000 Min humidity: -0.006 Max humidity: 0.000
Wind_speed:-0.013 Rain_or_snow:-0.186 theta:18.380 eps:0.000429
[1] -9538.622
Maximizing -- use negfn and neggr
Iter: 15 Qf: -9538.622 s2gamma: 0.032616 Intercept: 8.321
Hour_Chunks[8,16):1.531 Hour_chunks[16,24): 1.411 Is_weekend:-0.346
Is_holiday:-0.399 SeasonSpring:-0.046 SeasonSummer:0.074 SeasonWinter:-0.183
Min_temp:0.020 Max_temp:0.000 Min_humidity:-0.006 Max_humidity:-0.000
Wind_speed:-0.014 Rain_or_snow:-0.181 theta:18.497 eps:0.000342
[1] -9534.839
Maximizing -- use negfn and neggr
Iter: 16 Qf: -9534.839 s2gamma: 0.032440 Intercept: 8.334
```

```
Hour Chunks [8,16):1.536 Hour chunks [16,24): 1.414 Is weekend:-0.343
Is_holiday:-0.391 SeasonSpring:-0.046 SeasonSummer:0.077 SeasonWinter:-0.182
Min temp: 0.020 Max temp: 0.000 Min humidity: -0.006 Max humidity: -0.000
Wind_speed:-0.014 Rain_or_snow:-0.175 theta:18.442 eps:0.000397
[1] -9531.502
Maximizing -- use negfn and neggr
Iter: 17 Qf: -9531.502 s2gamma: 0.031958 Intercept: 8.335
Hour Chunks[8,16):1.537 Hour chunks[16,24): 1.412 Is weekend:-0.346
Is holiday: -0.401 SeasonSpring: -0.047 SeasonSummer: 0.078 SeasonWinter: -0.182
Min_temp:0.020 Max_temp:0.000 Min_humidity:-0.006 Max_humidity:-0.000
Wind_speed:-0.013 Rain_or_snow:-0.172 theta:18.532 eps:0.000350
[1] -9526.663
Maximizing -- use negfn and neggr
Iter: 18 Qf: -9526.663 s2gamma: 0.031245 Intercept: 8.339
Hour_Chunks[8,16):1.535 Hour_chunks[16,24): 1.410 Is_weekend:-0.346
Is_holiday:-0.405 SeasonSpring:-0.050 SeasonSummer:0.078 SeasonWinter:-0.180
Min_temp:0.020 Max_temp:0.000 Min_humidity:-0.006 Max_humidity:-0.000
Wind speed: -0.013 Rain or snow: -0.174 theta: 18.638 eps: 0.000508
[1] -9525.671
Maximizing -- use negfn and neggr
Iter: 19 Qf: -9525.671 s2gamma: 0.030310 Intercept: 8.340
Hour Chunks [8,16):1.527 Hour chunks [16,24): 1.405 Is weekend:-0.347
Is_holiday:-0.415 SeasonSpring:-0.052 SeasonSummer:0.073 SeasonWinter:-0.177
Min temp: 0.021 Max temp: 0.001 Min humidity: -0.007 Max humidity: -0.000
Wind speed: -0.012 Rain or snow: -0.179 theta: 18.449 eps: 0.000104
[1] -9523.732
Maximizing -- use negfn and neggr
Iter: 20 Qf: -9523.732 s2gamma: 0.029895 Intercept: 8.338
Hour_Chunks[8,16):1.528 Hour_chunks[16,24): 1.410 Is_weekend:-0.344
Is_holiday:-0.401 SeasonSpring:-0.052 SeasonSummer:0.074 SeasonWinter:-0.177
Min_temp:0.020 Max_temp:0.001 Min_humidity:-0.007 Max_humidity:-0.000
Wind_speed:-0.013 Rain_or_snow:-0.179 theta:18.310 eps:0.000204
[1] -9518.461
Maximizing -- use negfn and neggr
Iter: 21 Qf: -9518.461 s2gamma: 0.029774 Intercept: 8.343
Hour_Chunks[8,16):1.531 Hour_chunks[16,24): 1.411 Is_weekend:-0.342
Is holiday: -0.393 SeasonSpring: -0.053 SeasonSummer: 0.074 SeasonWinter: -0.176
Min_temp:0.020 Max_temp:0.001 Min_humidity:-0.007 Max_humidity:-0.000
Wind speed: -0.013 Rain or snow: -0.177 theta: 18.560 eps: 0.000553
[1] -9520.844
Maximizing -- use negfn and neggr
Iter: 22 Qf: -9520.844 s2gamma: 0.029349 Intercept: 8.348
Hour Chunks[8,16):1.533 Hour chunks[16,24): 1.415 Is weekend:-0.340
Is_holiday:-0.399 SeasonSpring:-0.063 SeasonSummer:0.067 SeasonWinter:-0.177
Min_temp:0.020 Max_temp:0.001 Min_humidity:-0.007 Max_humidity:-0.000
Wind_speed:-0.014 Rain_or_snow:-0.177 theta:18.519 eps:0.000250
[1] -9520.354
Maximizing -- use negfn and neggr
Iter: 23 Qf: -9520.354 s2gamma: 0.029582 Intercept: 8.353
Hour_Chunks[8,16):1.534 Hour_chunks[16,24): 1.415 Is_weekend:-0.337
Is_holiday:-0.393 SeasonSpring:-0.064 SeasonSummer:0.067 SeasonWinter:-0.179
Min temp: 0.020 Max temp: 0.001 Min humidity: -0.007 Max humidity: -0.000
Wind_speed:-0.014 Rain_or_snow:-0.176 theta:18.422 eps:0.000051
There were 22 warnings (use warnings() to see them)
```

str(glmm_fit)

```
##
  List of 7
##
    $ beta
                : num [1:14] 8.353 1.534 1.415 -0.337 -0.393 ...
    $ s2gamma
##
                : num 0.0296
##
    $
      theta
                 num 18.4
##
    $ eps
                 num 5.15e-05
     qfunction: num -9520
##
     day_ranef: num [1:365] 0.0653 -0.398 -0.5165 -0.2612 -0.0374 ...
##
      iter
                : num 23
```

Machine learning models

Next, we applied two machine learning methods to predict the bike count. The first model we used is a conditional inference tree. In traditional partitioning, all possible splits are investigated to find the best split, which results in overfitting and selection. The conditional inference tree embeds the partition step with a permutation test, thereby enabling this method to be robust to covariates of different scales. Furthermore, it is capable of stopping when no significant correlation exists between the covariates and the response (Hothorn, Hornik, and Zeileis 2006). We emplyed the ctree function in the partykit to fit the conditional inference tree.

We visualized the three layer conditional inference tree in order to verify the relationship between bike count and variables (Figure 2). It is apparent that people tend to rent fewer bikes between midnight and 8 am. Maximum temperatures and humidity also affect bike rental rates. The splits that are employed in the conditional reference tree provide well reasoned explanations of the data structure, which means high accuracy predictions are made.

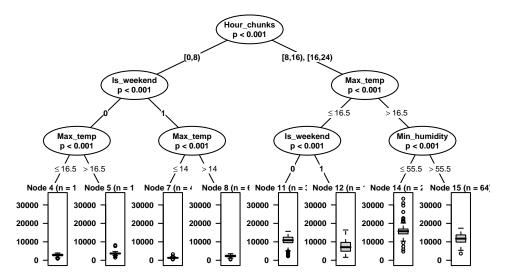


Figure 2: Three layer conditional inference tree

A random forest model was then applied to predict the number of bikes that would be rented. Random forest is composed of many decision trees as opposed to a single tree, resulting in a more accurate result. Incorporating the randomness allows random forest to protect against overfitting and can be applied more effectively to other data sets. The disadvantage of the random forest is its computational complexity. To fit the random forest, we created a method train_random_forest() within our bikeSharing R package that leverages the train() function within the caret R package. The optimal tuning parameter mtry was determined using a 5-fold cross validation. We visualized a random selected tree.

```
rf_fit <- train_random_forest(data = london_train)</pre>
```

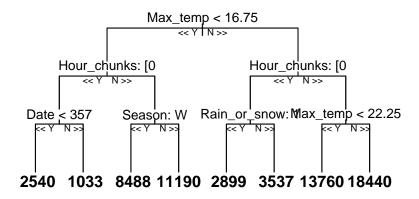


Figure 3: A random selected tree in the trained random forest model

Random forest sample trees share similar splits with conditional inference trees (Figure 3). The estimated bike rental count is much higher in the hour chunks that are not 0-8am. Additionally, the estimated count is high when the temperature is more than 22.25 degrees.

Variable Importance in machine learning models

To investigate which variables affect the prediction most, we calculate the importance of the variables in the conditional inference tree and the random forest. In conditional inference tree, we calculated the mean decrease in accuracy when deleting a variable (Table 1).

| Table 1: Mean | decrease | in | accuracy | of | variables | ${\rm in}$ | the cond | itional |
|----------------|----------|----|----------|----|-----------|------------|----------|---------|
| inference tree | | | | | | | | |

| Variable | Mean decrease in accuracy |
|--------------|---------------------------|
| Hour_chunks | 42292743.475 |
| Max_temp | 7305786.627 |
| Is_weekend | 2819028.041 |
| Rain_or_snow | 1622451.011 |
| Min_humidity | 1014266.239 |
| Season | 905987.474 |
| Max_humidity | 184868.121 |
| Wind_speed | 35027.139 |
| Is_holiday | 25815.318 |
| Date | 3737.395 |

In random forest, we calculate the increase in MSE when deleting a variable (Figure 4). The code to do this was implemented as a function plot_rf_importance in the bikeSharing R package.

```
plot_rf_importance(london_train)
```

The top important variables of the conditional inference tree and random forest are similar. The hour chunk is the most important variable in both models. Additionally, the maximum temperature has a significant impact on the model prediction. Additional details of the variables are discussed in the discussion section. We further compare the performance of random forest and conditional inference tree using the second year bike renting data in London. Conditional inference tree results in a $R^2 = 0.81$ and random forest has $R^2 = 0.91$. Due the similarity in these two models, we selected random forest tree in the further comparison.

Results

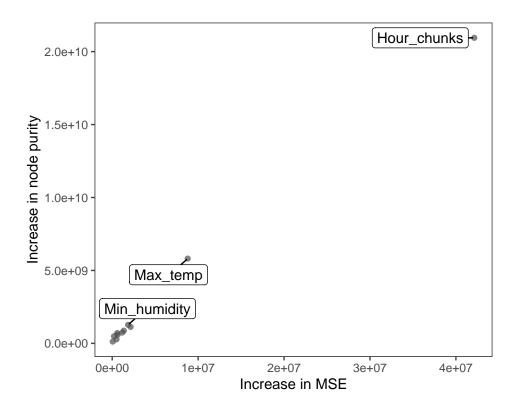
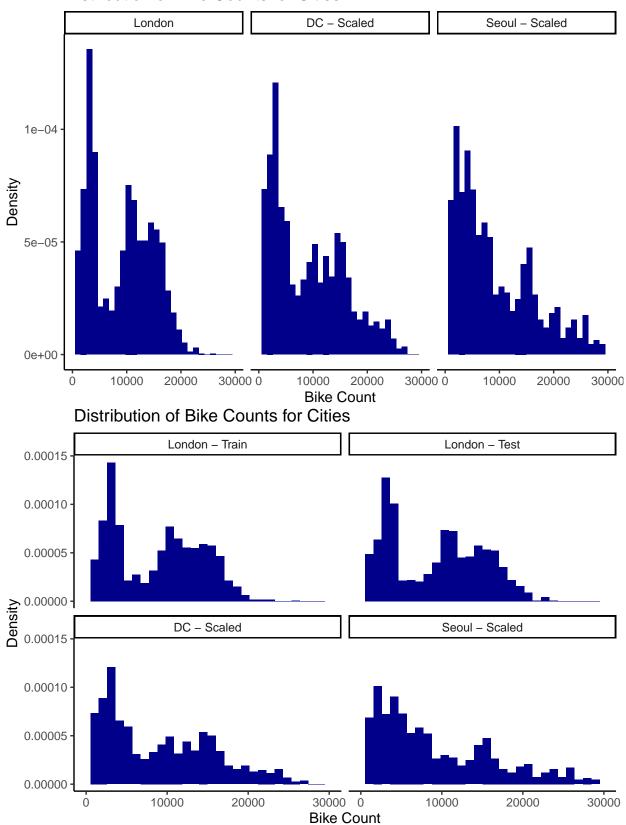


Figure 4: Feature importance in the random forest model

```
## 1 845.741 605.217 0.521788
glmm_model_fit(glmm_fit, seoul, scale_to_reference_mean = "yes",
               reference = london)
##
         RMSE
                   MAE
## 1 3519.413 2719.021 0.4999935
rf_model_fit(rf_fit, london_train, scale_to_reference_mean = "no",
             reference = london)
##
         RMSE
                   MAE
## 1 752.2336 471.5412 0.9822717
rf_model_fit(rf_fit, london_test, scale_to_reference_mean = "no",
             reference = london)
##
        RMSE
                 MAE
## 1 1789.24 1191.32 0.9084533
rf_model_fit(rf_fit, dc, scale_to_reference_mean = "yes",
             reference = london)
##
         RMSE
                   MAE
                              R2
## 1 664.5474 492.4647 0.6737107
rf_model_fit(rf_fit, seoul, scale_to_reference_mean = "yes",
             reference = london)
##
         RMSE
                   MAE
                              R2
## 1 3163.613 2479.835 0.5658297
```

Distribution of Bike Counts for Cities



[1] 9286.037

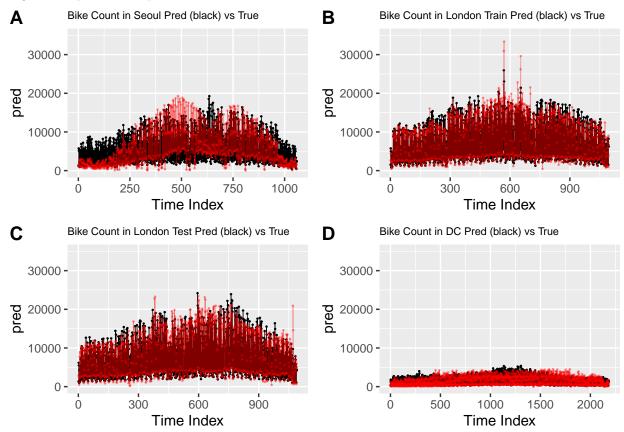
[1] 8913.796

Discussion and Conclusion

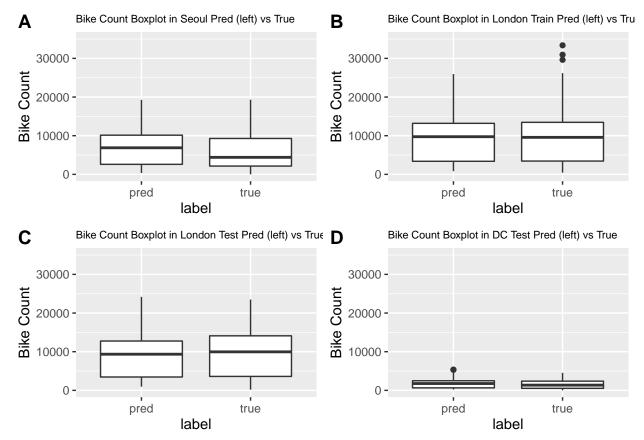
In conclusion, factors including hours, holidays, min temperature, max temperature, min humidity, max humidity, average wind speed and presence of rain/snow all have inference on the number of bike rented in the three cities. Hours from 4pm to midnight have the largest effect on the number of bike rented. Hours from 8am to 4pm, winter season, rain/snow also have large impact on the bike rent count. Random Forest have better prediction result on all the training and testing data, compared to the results of GLMM.

In addition to the conclusion above, we also have some findings that need to discuss more. The RMSE for Seoul is much larger than that in the other two cities. The results on the test dataset are much worse than in the training dataset. This may imply that our model may have some limitations across cities. The possible reason is that in our model, we only considered the effects of days, hours and weather on the bike count but did not take information about cities into consideration (e.g. population, GDP), which may cause bias in prediction.

To get a better understanding on how our model predict on the sequences of bike count in different dataset, we plotted out the predicted bike count and the ground truth for each of the four datasets. Below is the longitudinal plots of the predicted bike count and the true bike count in the three cities.



To understand the bias and variance of our prediction results, we also drew the boxplots of predicted bike count and the true bike count of the four datasets. The plots are shown below:



Overall, our result is consistent with the published research by Sylwia et al. (2021) in "Impact of environment on bicycle travel demand-Assessment using bikeshare system data". In their study, they used the data from the bike sharing system in Cracow, Polan and conducted an ordinal least square regression model to analyze the effect of daily air temperature, daily rainfall, public holidays, and school holidays on the daily number of bike rented from bike sharing system. Their study result indicated that weather conditions, especially air temperature and daily rainfall, have large impact on the number of bike sharing system, which is consistent with ours result. Compared to their research, our study further found that the maximum temperature and the minimum humidity have more impact on the bike count. We did not restrict our study on daily level but cut one day into different hour chunks and found that different hour chunks in one day can also have large effect on the number of bike rented from bike sharing system.

Reference

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Sylwia P., Mariusz K., Carmelo D (2021). "Impact of environment on bicycle travel demand—Assessment using bikeshare system data." Sustainable Cities and Society, 67, [102724]. https://doi.org/10.1016/j.scs.2021.102724

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