

E²M²: Ecological and Epidemiological Modeling in Madagascar

Data and Models

Centre ValBio

Ranomafana National Park, Madagascar

13 – 20 January, 2019

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Lecture contributions from:

Tanjona Ramiadantso

Steve Bellan



International Clinics on Infectious
Disease, Dynamics, & Data



International Clinics on Infectious
Disease, Dynamics, & Data

**MMED: *Clinic on the
Meaningful Modeling of
Epidemiological Data***

May-June 2019, Cape Town,
South Africa





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**DAIDD: *Clinic on Dynamical
Approaches to Infectious
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December 2019, Florida, USA





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**South African Center for
Epidemiological Modeling
and Analysis (SACEMA),
Director**

Dr. Juliet Pulliam
University of Stellenbosch

ICI3D, Program Director

Dr. Steve Bellan
University of Georgia



International Clinics on Infectious
Disease, Dynamics, & Data

www.ici3d.org

Goals for this lecture

- To explain what we're doing here

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- To define “science”

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- To introduce the “E” in E^2M^2

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 - Epidemiology

All course materials are available at:

https://carabrook.github.io/E2M2/E2M2_2019.html

Saturday: R Bootcamp

- Intro to R Studio
- Exploring and Visualizing Data in R
- For-loops, Functions, and If-Else Statements

Sunday: Travel

Monday: "Dealing with Data"

- Data and Models
- Student introductions & presentations
- Linear regression & simple stats
- Basic statistical modeling in R
- Formulating research questions

Tuesday: "Deeper Thinking About Data"

- Dynamical Fever
- Intro to Mixed Modeling
- Mixed modeling in R
- Study Design and Data Collection
- Refining research questions for modeling

Thursday: "Fitting Models to Data"

- Model Fitting in Practice – the Basic Concept
- Introduction to Occupancy Modeling
- Intro to Spatial Modeling
- Occupancy modeling in R
- Epidemic Cards
- Model Fitting with Epidemic Cards
- Model Telephone

Friday: "Refining Your Work"

- Intro to Network Modeling
- Model Selection and Comparison
- Modeling Vector-Borne Disease
- Final research plans

Saturday: "Putting it All in Perspective"

- Modeling in Practice: The Lifecycle of a Modeling Project
- Research snapshots

Sunday: Travel

Monday: "Sharing Your Work"

- Final student presentations

● Programming

● Data

● Models

● Research Development

What is science?

the **systematic observation** of natural events and conditions in order to **discover facts** about them and to **formulate laws and principles** based on these facts.

– *Academic Press Dictionary of Science & Technology*

Observations and Laws and Principles

Data and Models

Data

Models

$$\frac{\partial^2 \psi}{\partial t^2} = \Delta \psi, \quad \psi(x,0) = \sqrt{1 - \frac{y^2}{c^2}}, \quad \psi(x,t) = \frac{1}{2} \left[e^{-\frac{|x|}{c}} + e^{-\frac{|x|+2ct}{c}} \right]$$
$$x_1 + x_2 = 5, \quad x_1(x_1-1) = x_2^2, \quad x_1 = 2, \quad x_2 = 3$$
$$E = \frac{1}{2} m v^2 = \frac{1}{2} m (v_x^2 + v_y^2) = \frac{1}{2} m (x_1^2 + x_2^2)$$
$$A^2 + B^2 = C^2, \quad \sum_{i=1}^n \frac{\partial^2 \psi_i}{\partial t^2} - C_i^2 \frac{\partial^2 \psi_i}{\partial x^2} = 0$$
$$\sum_{i=1}^n \frac{\partial^2 \psi_i}{\partial x^2} = \frac{1}{2} \frac{\partial^2}{\partial t^2} \sum_{i=1}^n \psi_i^2 = \frac{1}{2} \frac{\partial^2}{\partial t^2} (C^2)$$
$$C^2 = x_1^2 + x_2^2$$

Data and Models

Data

- What is data?

Data and Models



- What is **data**?
 - Backbone of science

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Data vs. Models

- What is **data**?
 - Backbone of science
 - **Evidence** to support a **claim**

Data or not data?

Data

- 19

Data or not data?

Data

- 19
- 19 = total number of fingers and toes



Data

Data or not data?

- 19
- 19 = total number of fingers and toes
- 19 = total number of fingers and toes of Andry Rajoelina



Data or not data?

- 19
- 19 = total number of fingers and toes
- 19 = total number of fingers and toes of Andry Rajoelina
- This is a fact. It becomes **data** when we use it to support a **claim**.

There is a negative correlation between the number of years someone has served as president of Madagascar and their total number of fingers and toes.

Data or not data?

Data

- 5, 11, 27



Data

Data or not data?

- 5, 11, 27
- 5, 11, 27 = respective # of children belonging to Amy, Christian, & Ben



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Amy, Christian, & Ben are the names of tenrecs at Duke Lemur Center



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This is data to support the claim:

Tenrecs have high fecundity rates.



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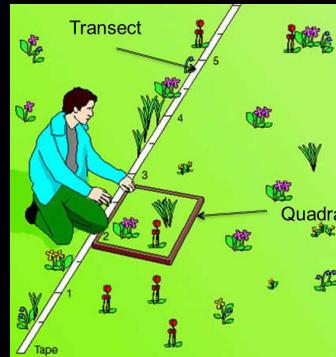
What is **data**?

- Backbone of science
- Evidence to support a claim
- A relationship between at least two variables
 - x: explanatory, control, driver, independent variable(s)
 - y: response, dependent variable(s)
- x and y should be clearly defined
 - with respect to the question!

Data: Sources of x and y

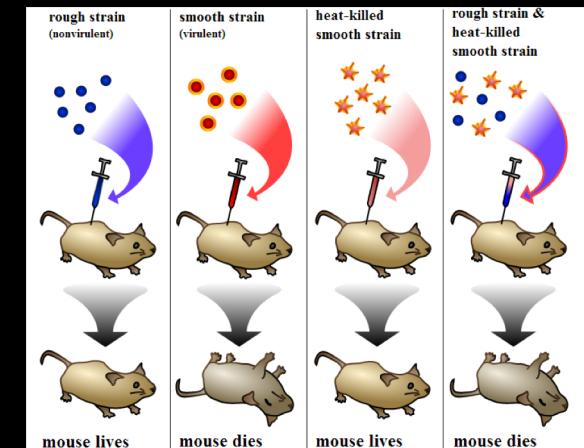
Observational

- Just measure x and y



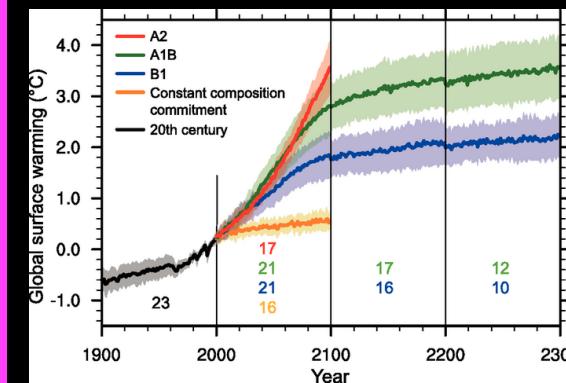
Experimental

- Interfere with x or the relationship between x and y



Simulated

- Create a relationship between x and y



Empirical data



Data: Types

Numerical

Categorical



Data: Types

Numerical

- A variable is numerical when you can transform it with mathematical operation
- Examples?

Categorical



Data: Types

Numerical

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- Integer, real number, multi-dimensional number

Categorical



Data: Types

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Categorical

- A variable is categorical when it is not numerical but a categorical can be numerical?
- Examples?



Data: Types

Numerical

- A variable is numerical when you can transform it with mathematical operation
- Examples:
- Integer, real number, multi-dimensional number

Categorical

- A variable is categorical when it is not numerical but a categorical can be numerical?
- Examples:
- Colors, (blood) types, species name



Data

Data: Things to consider

- Data acquisition



Data

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 - Impossible, example?

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- Measurement errors



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- Data quality and quantity
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 - Example: monetary cost, human effort -> power analysis, sampling design etc.
- Reproducibility
- Measurement errors
 - Examples?

Data and Models

Data

Models

$$\frac{\partial^2 \varphi}{\partial t^2} = \Delta \varphi, \quad \theta = \sqrt{1 - \frac{y^2}{t^2}}$$
$$x+3=5 \quad x(x-1)=x^2-1$$
$$E = -\frac{1}{r} - \frac{1}{2} \ln x \quad j = y_x \quad g = 52 - x^2 + y^2$$
$$A^2 + B^2 = C^2 \quad \sum_{i=1}^n \frac{\partial^2 v_{i,j}}{\partial t^2} - C_j^2 \frac{\partial^2 v_{i,j}}{\partial x^2} = 0$$
$$\sum_{i=1}^n -\frac{1}{2} \frac{\partial^2}{\partial t \partial x} C_j^2 v_{i,j} = 0$$
$$C(x) = x^2 N - 3(\pi)$$

Data vs. Models

- What is a model?

Models

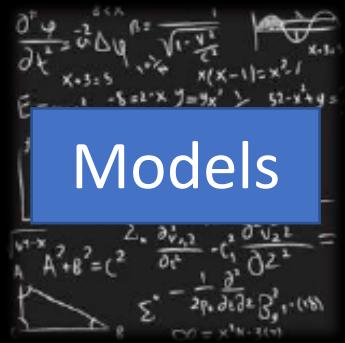
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the **systematic observation** of natural events and conditions in order to **discover facts** about them and to **formulate laws and principles** based on these facts.

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Laws and Principles

- A theory = a **declaration** to explain a phenomenon
 - Logical and falsifiable
- A model = an **abstract representation** of a phenomenon
- A hypothesis = a **testable declaration** that is derived from a theory



Theory, Models, Hypotheses

Theory

Model

Hypothesis

General

Specific

$$\frac{\partial^2 \psi}{\partial t^2} - \nabla^2 \Delta \psi = \frac{1}{c^2} \frac{\partial^2 \psi}{\partial x^2}$$
$$x+5=5 \quad x(x-1)=x^2-1$$
$$E=mc^2 \quad -S=k \cdot x \quad J=qx^2 \quad S=4\pi r^2$$
$$\sum_{i=1}^{N+1} A_i + B_i = C_i^2 \quad \frac{\partial^2 V_{12}}{\partial t^2} - c_1^2 \frac{\partial^2 V_{12}}{\partial x^2} =$$
$$\sum_{i=1}^N -\frac{1}{2\rho_i} \frac{\partial^2 \psi}{\partial x^2} B_i^2 \quad C_i^2 = x^2 h - 2(x)$$


Models: many types

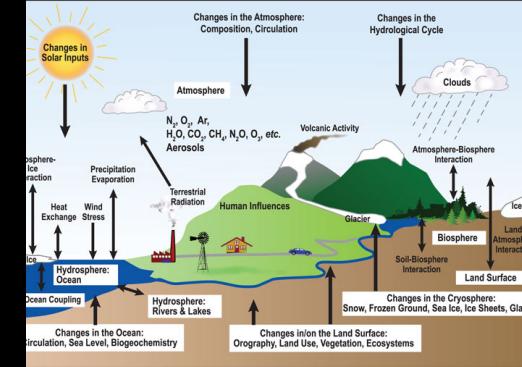
Human



Car



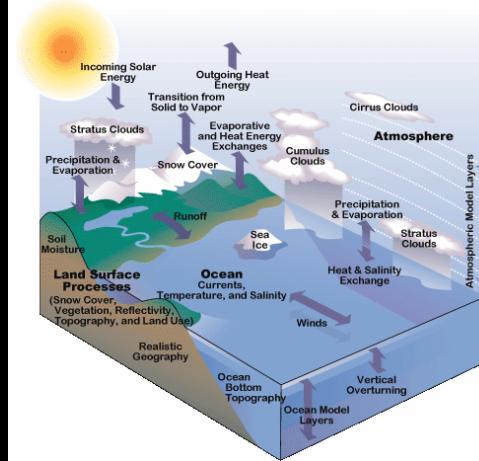
Ecosystem



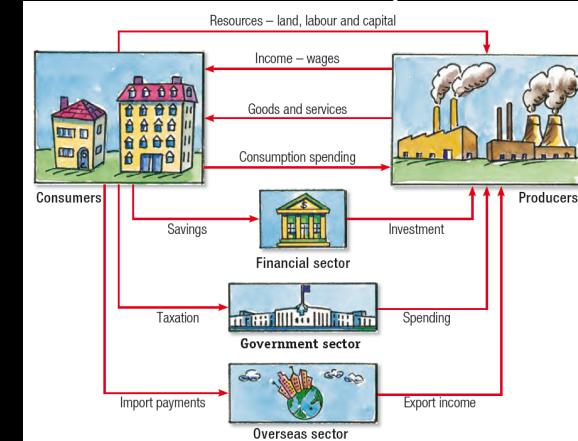
Ecology & Evolution



Climate



Economy



$$\frac{\partial^2 \psi}{\partial t^2} - c^2 \nabla^2 \psi = \frac{1}{\epsilon^2} \psi$$
$$x+5=5 \quad x(x-1)=x^2-1$$
$$E = \dots + \frac{1}{2} k x^2 - \frac{1}{2} k x^2 = 0$$
$$y = g(x) = \dots$$
$$\sum_{i=1}^{N+1} \frac{\partial^2 \psi_{i,1}}{\partial t^2} - \frac{1}{c_1^2} \frac{\partial^2 \psi_{i,2}}{\partial z^2} =$$
$$\sum_{i=1}^{N+1} -\frac{1}{2\rho_i} \frac{\partial^2 \psi_{i,2}}{\partial z^2} \delta_{i,j}^2 = \dots$$
$$\psi(z) = \dots$$

Models

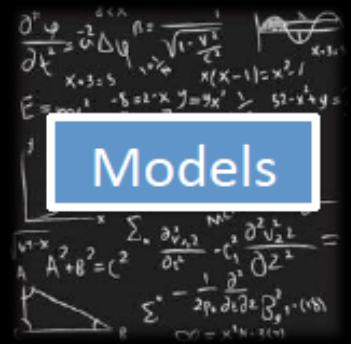
- When you make a **model**,
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elements that you feel are most important
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- Generally, we try to make **models**
that can reproduce real-world data



$$\frac{\partial^2 \psi}{\partial t^2} = \frac{c^2}{\epsilon_0} \nabla^2 \psi$$
$$x+5=5 \quad x(x-1)=x^2-1$$
$$E = mc^2 \quad -S = k \cdot x \quad J = qx^2 \quad 52 - 4^2 y =$$
$$\sum_{i=1}^{N+1} \frac{\partial^2 V_{i,i}}{\partial t^2} - C_1 \frac{\partial^2 V_{2,2}}{\partial t^2} =$$
$$\sum_{i=1}^{N+1} -\frac{1}{2\rho_i} \frac{\partial^2}{\partial x^2} \tilde{V}_i^2 + C_2 = x^2 N + 2(\gamma)$$

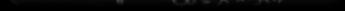
Models



- When you make a **model**,
you include the
elements that you feel are most important
to explain a phenomenon.
- Generally, we try to make **models**
that can reproduce real-world **data**
- In E²M², we distinguish between **statistical** and
mechanistic models

Statistical vs. Mathematical Model

The choice depends on the research question!

$$\frac{\partial^2 \psi}{\partial t^2} - \frac{1}{c^2} \Delta \psi = \frac{1}{\epsilon^2} \delta(x-t)$$
$$x+5=5 \quad x(x-1)=x^2-1$$
$$E = \dots$$
$$A^2 + B^2 = C^2$$
$$\sum_{i=1}^{N+1} \frac{\partial^2 \psi_{i,2}}{\partial t^2} - \frac{1}{c_1^2} \frac{\partial^2 \psi_{2,2}}{\partial z^2} =$$
$$\sum_{i=1}^N -\frac{1}{2\rho_i} \frac{\partial^2 \psi_{i,2}}{\partial z^2} \delta_g^2$$
$$C^2 = x^2 + z^2$$


Models

Statistical Models

- Goal: To rigorously assess the strength of relationship between x and y
 - Find a significant relationship using a p-value as a measure of relationship strength
 - Statistical models can demonstrate correlations.

The image shows a chalkboard with various mathematical calculations and formulas. In the top right corner, there is a blue rectangular box with the word "Models" written in white. The chalkboard contains the following text and equations:

$\frac{\partial^2 \psi}{\partial t^2} = -2 \Delta \psi$ $\Rightarrow \psi = \frac{1}{\sqrt{1 + \frac{|x|^2}{t^2}}}$

$x \cdot 3 = 5$ $x(x-1) = x^2 - 1$

$E = \dots$ $-S = k \cdot x$ $y = g(x)$ $52 - 4^2 y =$

$\sum_{i=1}^{N+1} \frac{\partial^2 \psi_{i,2}}{\partial t^2} - \frac{\partial^2 \psi_{1,2}}{\partial x^2} =$

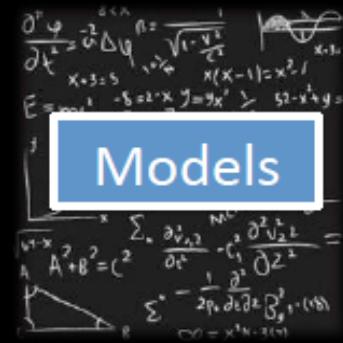
$A^2 + B^2 = C^2$ $\sum_{i=1}^{N+1} \frac{\partial^2 \psi_{i,2}}{\partial x^2} =$

$\sum_{i=1}^{N+1} -\frac{\partial^2 \psi_{i,2}}{\partial x^2} \frac{\partial^2 \psi_{i,2}}{\partial t^2} =$

$C^2 = x^2 N + 1 \cdot (y)$

Statistical Models

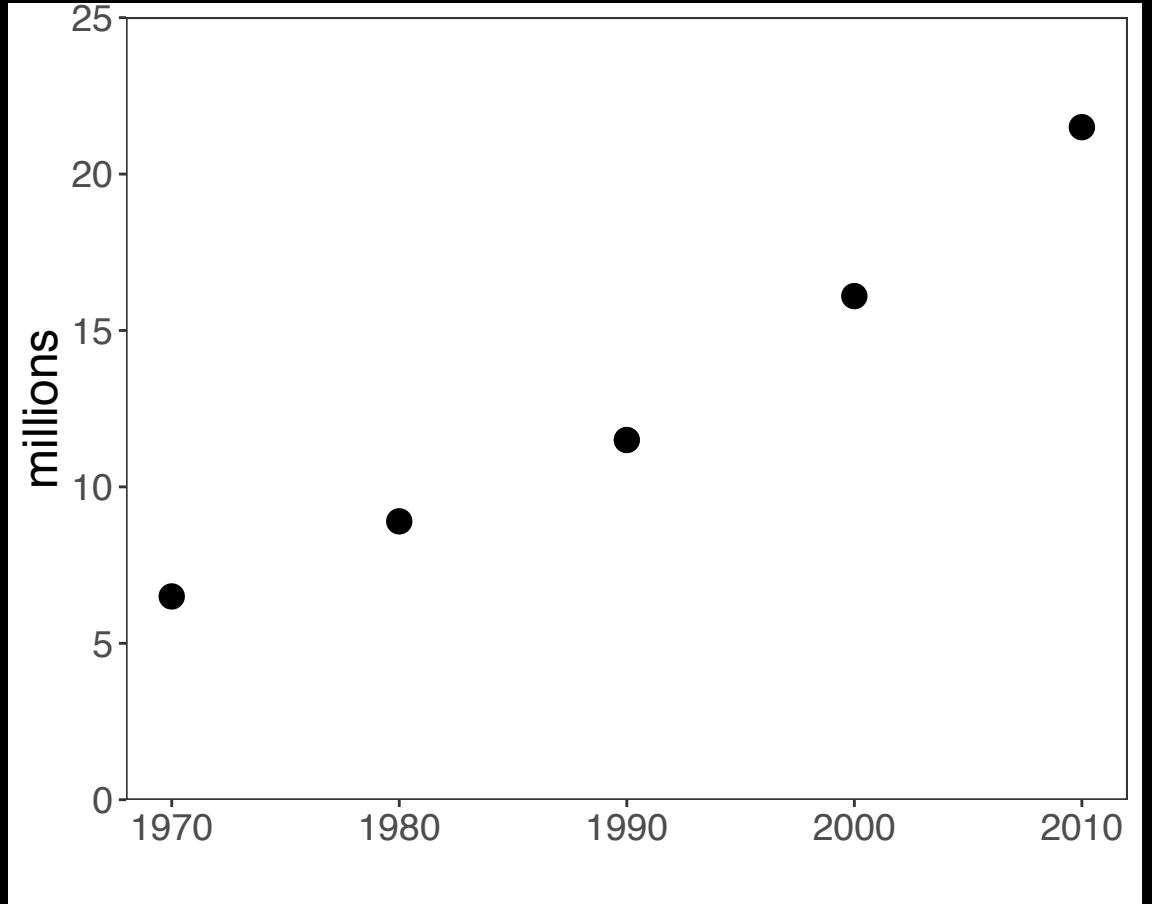
- Goal: To rigorously assess the strength of relationship between x and y (describe **patterns**)
 - Find a significant relationship using a p-value as a measure of relationship strength
 - Statistical models can demonstrate correlations.
- Steps:
 1. Formulate a research question
 2. Formulate a hypothesis
 3. Develop a model to demonstrate your hypothesis.
 4. Collect **data (required!!!)**
 5. Evaluate hypothesis with appropriate statistical tools
 - t-test, Chi-square, ANOVA
 - Ordination (PCA)
 - Regression (LM, GLM, GLMM, GAM)



1. Example Question: What is the trajectory Malagasy population size through time?

Models

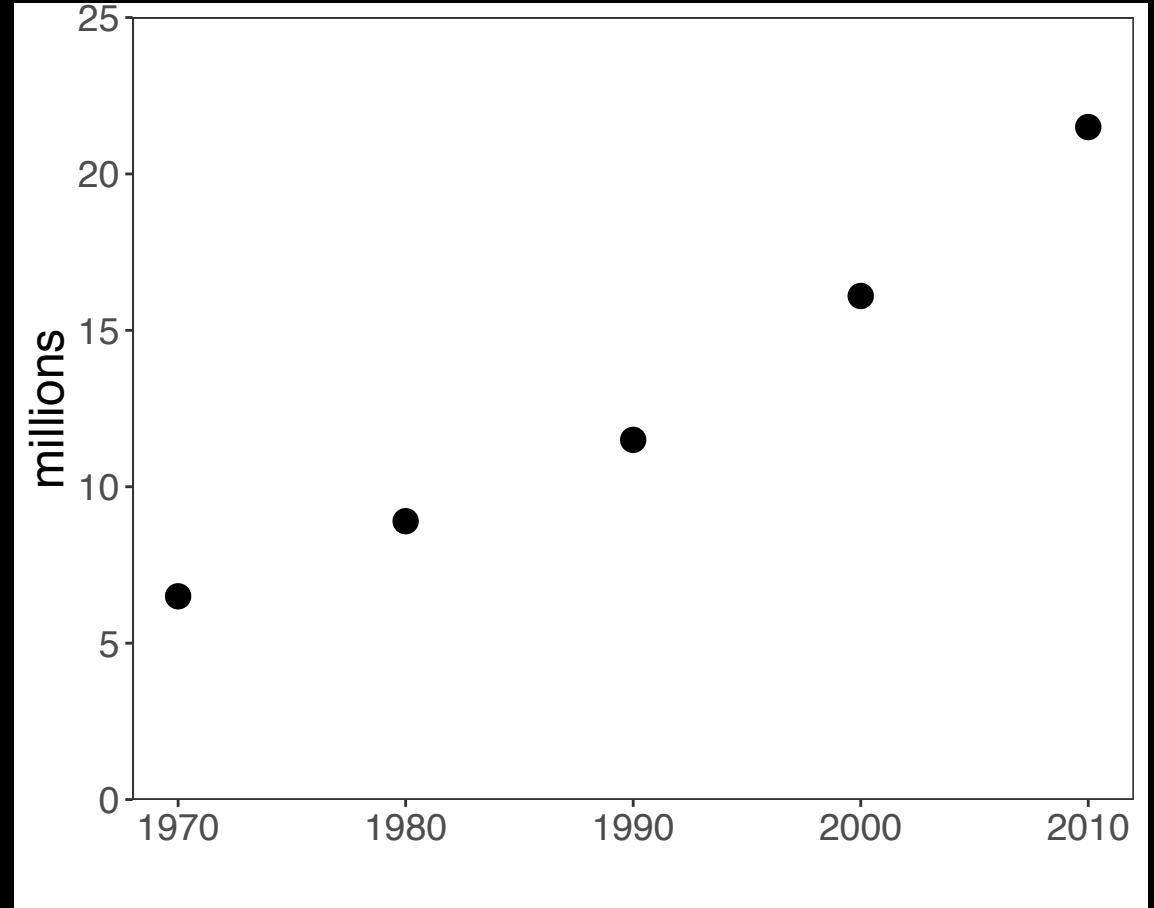
$$\frac{\partial^2 \Psi}{\partial t^2} = -2 \Delta \Psi \quad (\text{if } \Psi = \sqrt{1 - \frac{r^2}{t^2}})$$
$$x+3=5 \quad x(x-1)=x^2-1$$
$$E = m c^2 \quad -5 = 2 \cdot x \quad j = 9 x^2 \quad 52 - 4 x^2 y =$$
$$A^2 + B^2 = C^2 \quad \sum_{i=1}^{N+1} \frac{\partial^2 \Psi_i}{\partial t^2} = -C_1 \frac{\partial^2 \Psi}{\partial t^2}$$
$$\sum_{i=1}^{N+1} -\frac{\partial^2}{\partial t^2} \Psi_i = -\frac{\partial^2}{\partial t^2} \Psi$$
$$C(t) = x^2 h + 2(\gamma)$$



Source: World Bank

1. Example Question: What is the trajectory of Malagasy population size through time?

2. Hypothesis: Malagasy population size increases with time



Source: World Bank

Models

$$\frac{\partial^2 \Psi}{\partial t^2} = -2 \Delta \Psi \quad (\text{if } \Psi = \sqrt{1 - \frac{t^2}{T^2}})$$
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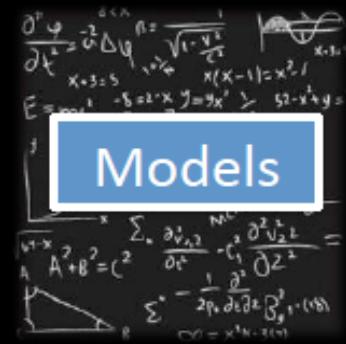
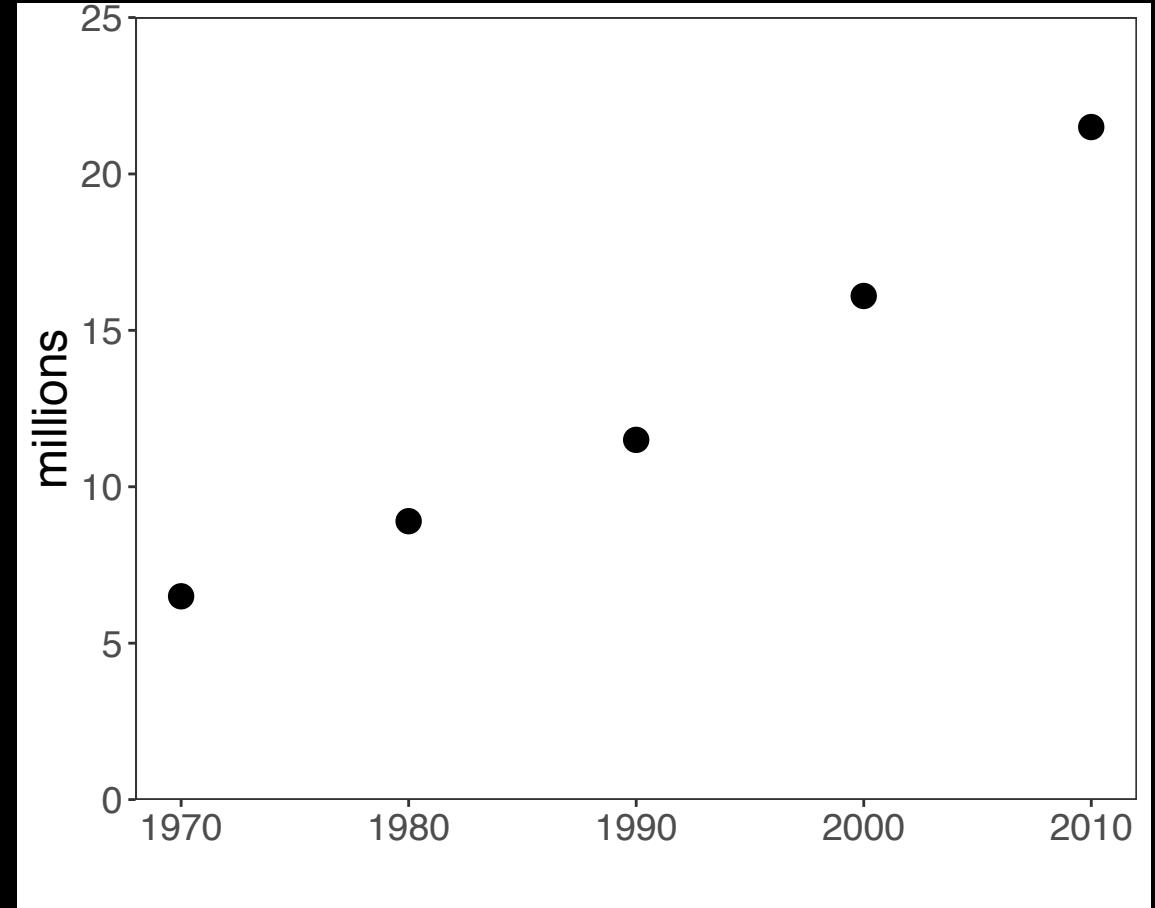
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2. Hypothesis: Malagasy population size increases with time

3. Statistical Model:

$$y = mx + b$$

Linear Regression



Source: World Bank

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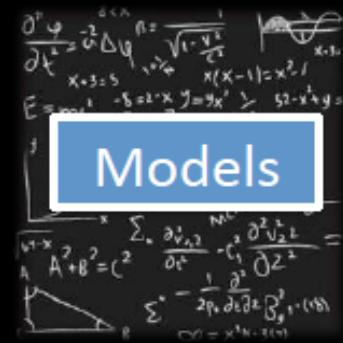
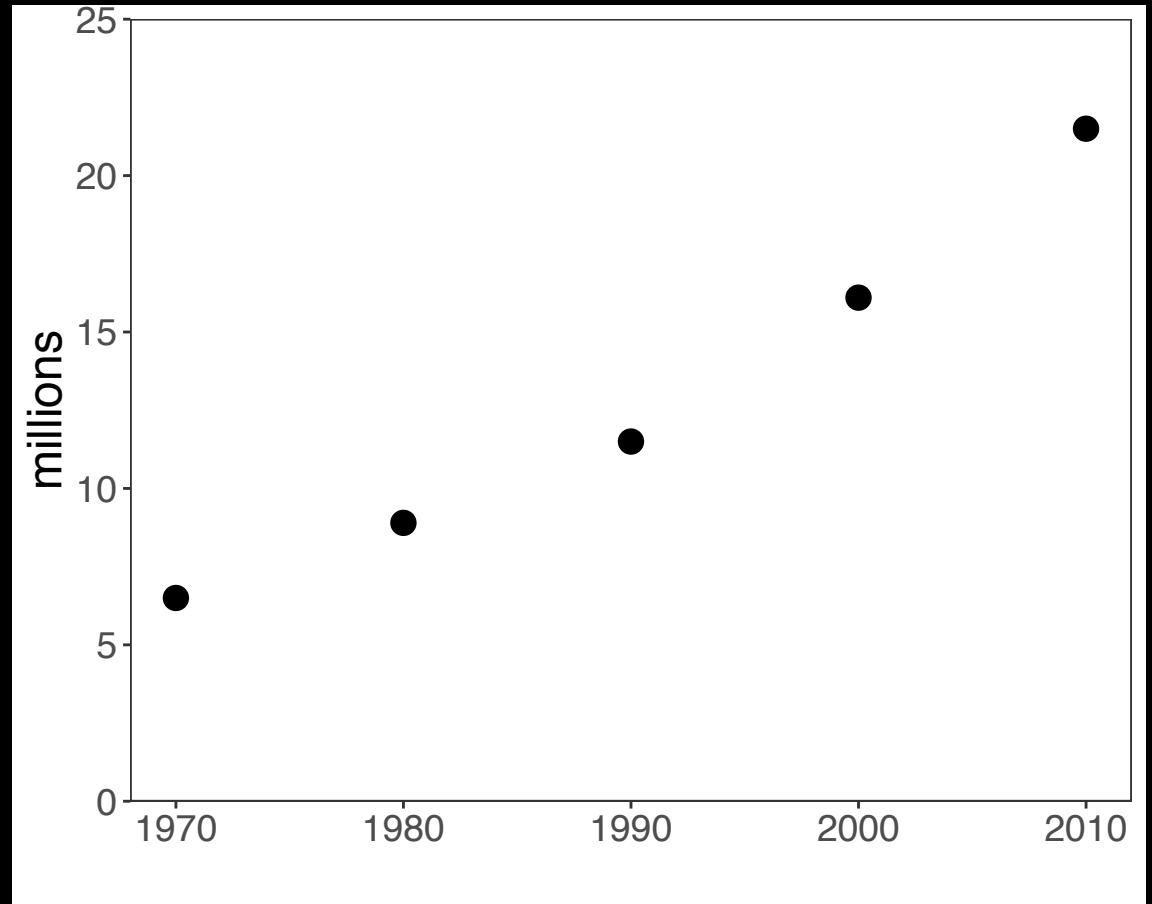
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4. Data:



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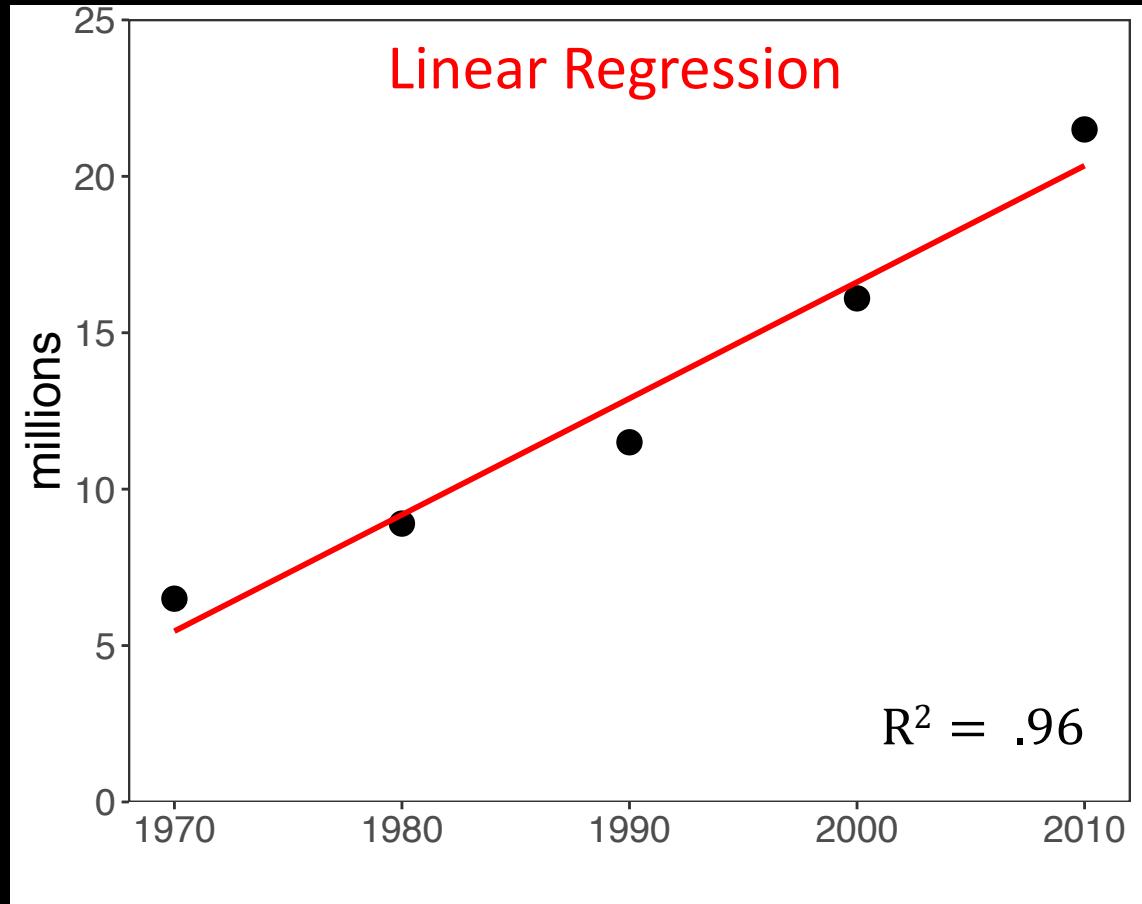
$$y = mx + b$$

5. Evaluation

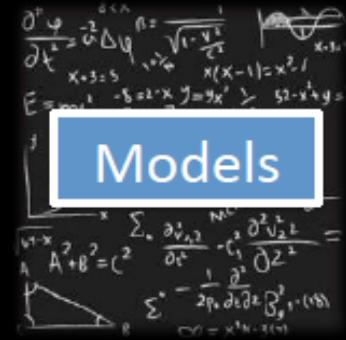
$$m = .372 \text{ million}$$

$$p = .003$$

4. Data:

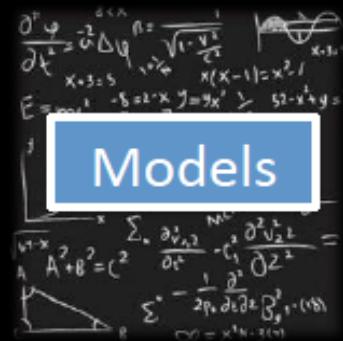


What can we conclude from this fitted model?



Source: World Bank

1. Example Question: What is the trajectory of Malagasy population size through time?



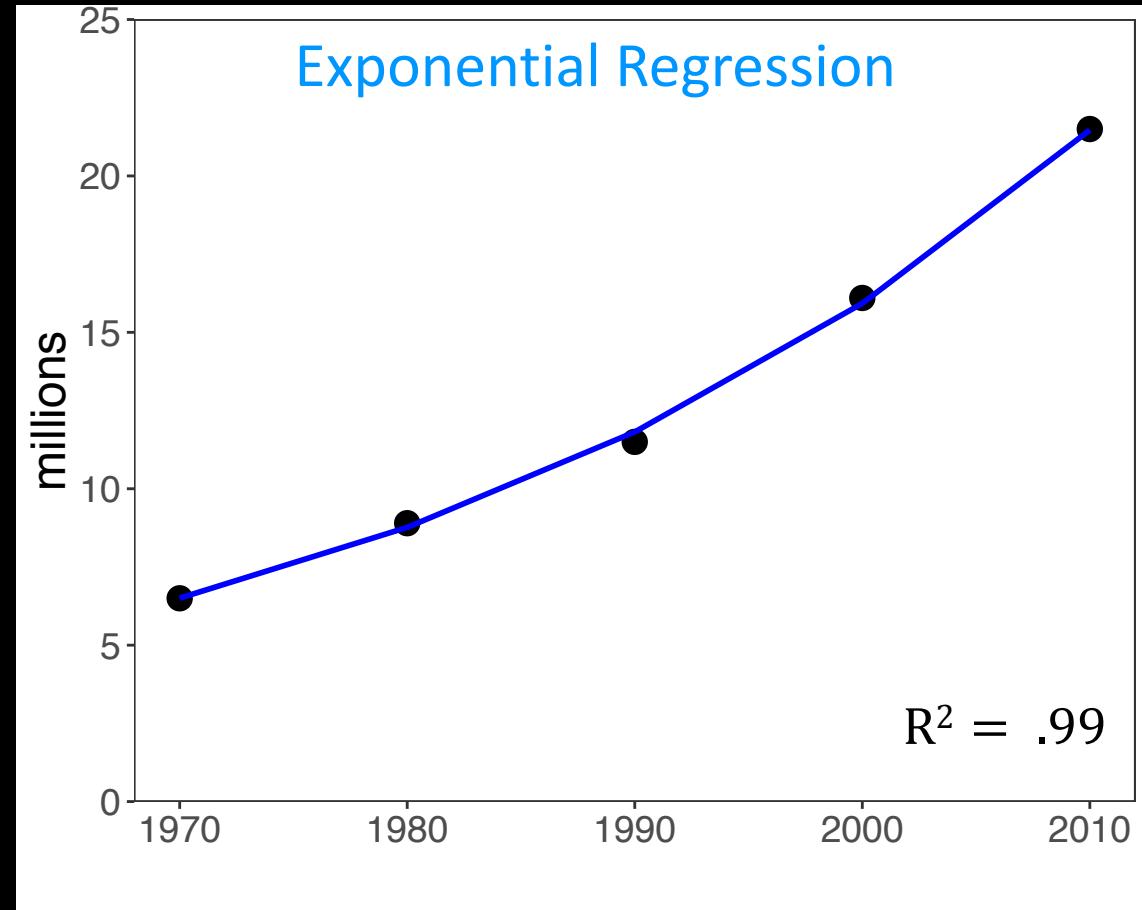
7. Adapt your model and re-evaluate:

$$y = e^{mx+b}$$

Exponential Regression

$$m = 0.029 \text{ mil.}$$

$$p < .001$$



What can we conclude from this fitted model?

Source: World Bank

Statistical Models: Beware!

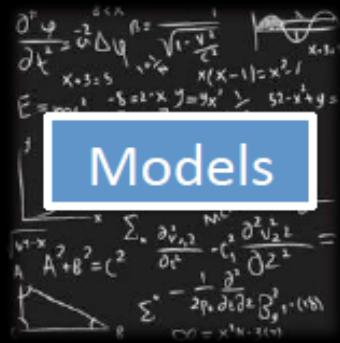
- Statistical models and tests are based on specific assumptions
 - data normally distributed
 - y and y' independent
 - etc.

A blackboard filled with mathematical notation, including:
 $\frac{\partial^2 \psi}{\partial t^2} = \frac{1}{t^2}$, $\psi(t) = \sqrt{1 - \frac{1}{t^2}}$, $x_1 + x_2 = 5$, $x(x-1) = x^2 - 1$, $E = \dots$, $-5 = x \cdot x' \Rightarrow y = yx' \Rightarrow 52 - y^2 =$
 $\sum_{i=1}^{N+1} \frac{\partial^2 \psi_{i,1}}{\partial t^2} - \frac{1}{t^2} \frac{\partial^2 \psi_{i,2}}{\partial t^2} =$
 $A^2 + B^2 = C^2$, $\sum_{i=1}^n \frac{\partial^2 \psi_{i,1}}{\partial t^2} \frac{\partial^2 \psi_{i,2}}{\partial t^2} =$
 $\sum_{i=1}^n -\frac{1}{t^2} \frac{\partial^2 \psi_{i,1}}{\partial t^2} \frac{\partial^2 \psi_{i,2}}{\partial t^2} =$
 $C^2 = x^2 n - 2 \cdot 52$

Models

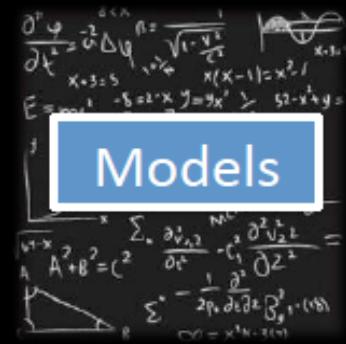
Statistical Models: Beware!

- Statistical models and tests are based on specific assumptions
 - data normally distributed
 - y and \hat{y} independent
 - etc.
- Assessing a model means you need to make sure the assumptions are not violated.



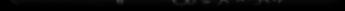
Statistical Models: Beware!

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- There are so many statistical models...



Statistical vs. Mathematical Model

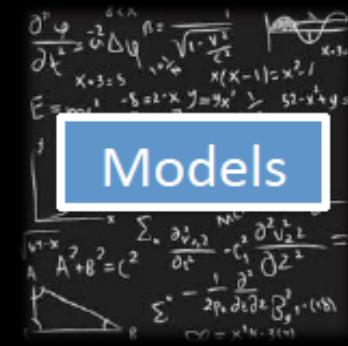
The choice depends on the research question!

$$\frac{\partial^2 \psi}{\partial t^2} - \frac{1}{c^2} \Delta \psi = \frac{1}{\epsilon^2} \delta(x-t)$$
$$x+5=5 \quad x(x-1)=x^2-1$$
$$E = \dots$$
$$A^2 + B^2 = C^2$$
$$\sum_{i=1}^{N+1} \frac{\partial^2 \psi_{i,2}}{\partial t^2} - \frac{1}{c_1^2} \frac{\partial^2 \psi_{2,2}}{\partial z^2} =$$
$$\sum_{i=1}^N -\frac{1}{2\rho_i} \frac{\partial^2 \psi_{i,2}}{\partial z^2} \delta_g^2$$
$$C^2 = x^2 + z^2$$


Models

Mechanistic Models

- Goal: To demonstrate the **processes** that underlie a relationship between x and y
 - Find a significant relationship using a p-value as a measure of relationship strength
 - Mechanistic models can demonstrate causation.
- Steps:
 1. Formulate a research question
 2. Formulate a hypothesis
 3. Develop a model to demonstrate your hypothesis.
 4. Collect **data** (for certain questions)
 5. Evaluate the extent to which your model-simulated data matches that from the real world.

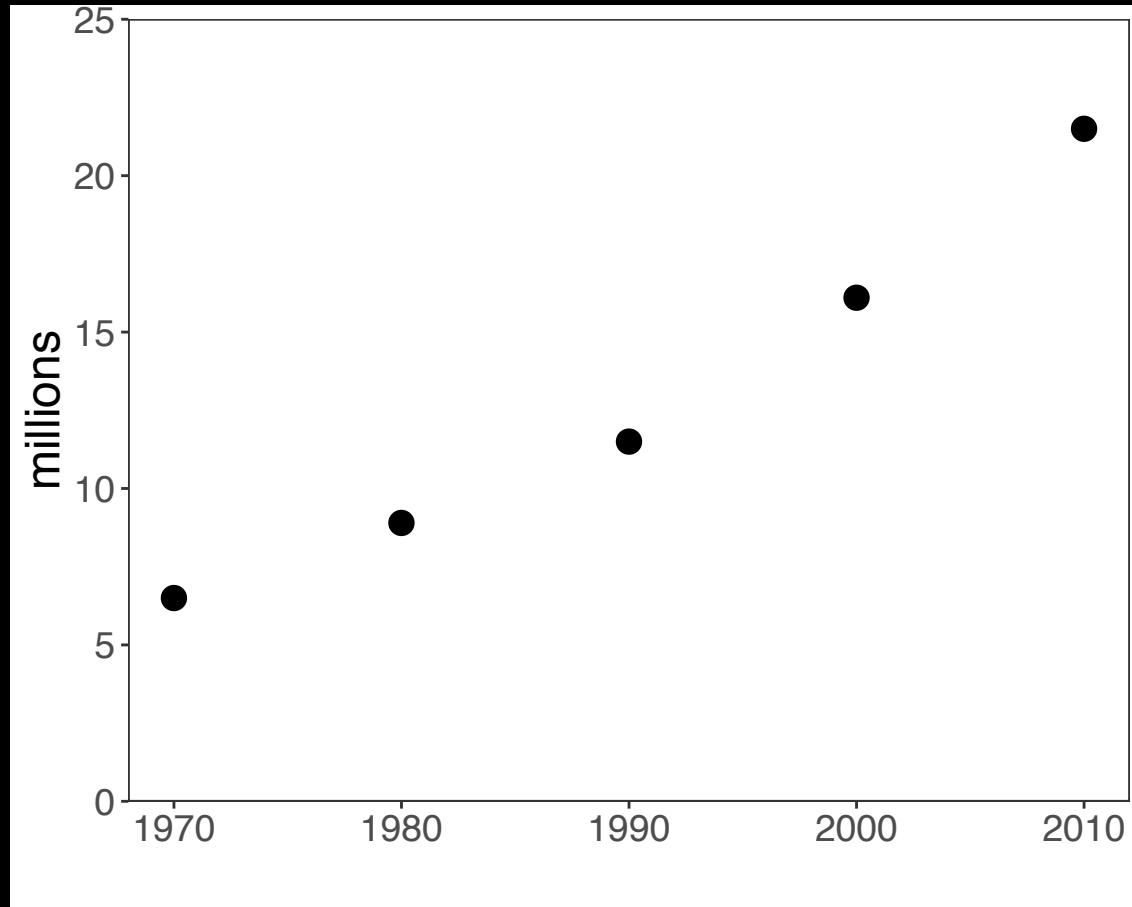


1. Example Question: How does Malagasy population size change with time?

2. Hypothesis: Malagasy population size increases because people are having children.

Can you think of an alternative hypothesis?

4. Data:

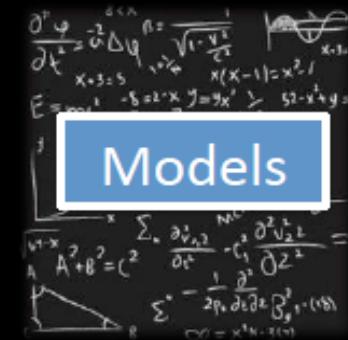


Source: World Bank

Models

$$\frac{\partial^2 \Psi}{\partial t^2} = \frac{\partial^2 \Delta \Psi}{\partial x^2} \quad (\text{1}) = \frac{1}{\sqrt{1 - \frac{y^2}{c^2}}} \quad x(x-1) = x^2 - 1 \\ E = \frac{1}{2} c^2 \cdot 1 - \frac{1}{2} x^2 \cdot x^2 = \frac{1}{2} c^2 - \frac{1}{2} x^4 \quad \frac{1}{2} c^2 - \frac{1}{2} x^4 = \\ \sum_{n=1}^{\infty} \frac{\partial^2 \Psi_n}{\partial t^2} = \frac{\partial^2 \Psi_1}{\partial t^2} - \frac{1}{2} \frac{\partial^2 \Psi_2}{\partial t^2} = \\ A + B^2 = C^2 \quad \frac{\partial^2 \Psi_1}{\partial t^2} - \frac{1}{2} \frac{\partial^2 \Psi_2}{\partial t^2} = \\ \sum_{n=1}^{\infty} \frac{\partial^2 \Psi_n}{\partial t^2} = \frac{1}{2} \frac{\partial^2 \Psi_1}{\partial t^2} + \frac{1}{2} \frac{\partial^2 \Psi_2}{\partial t^2} = \\ C^2 = x^4 n + 1/2$$

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2. Hypothesis: Malagasy population size increases because people are having children.

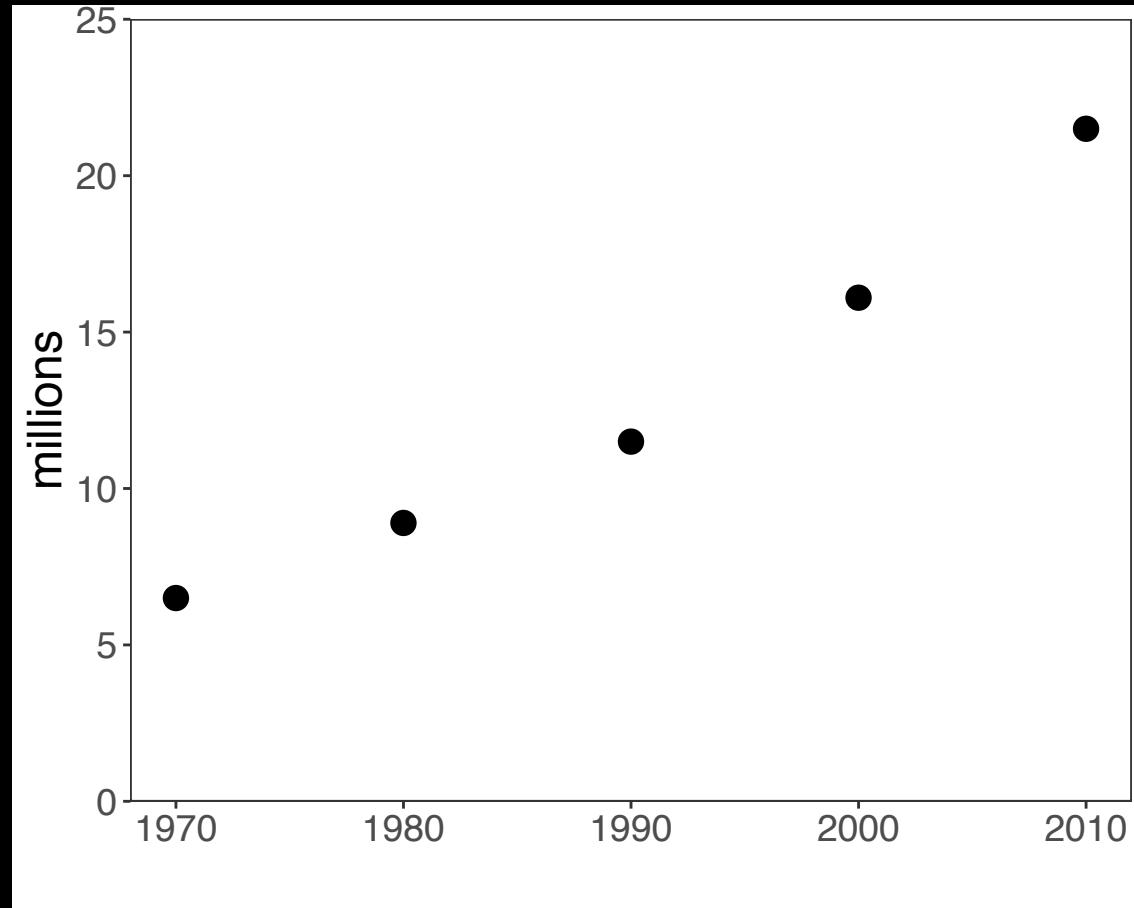
3. Mechanistic Model:



$$P_{t+1} = P_t + b * P_t - d * P_t$$

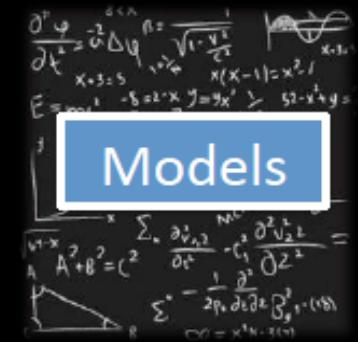
$$P_{t+1} = P_t + r * P_t$$

4. Data:



Source: World Bank

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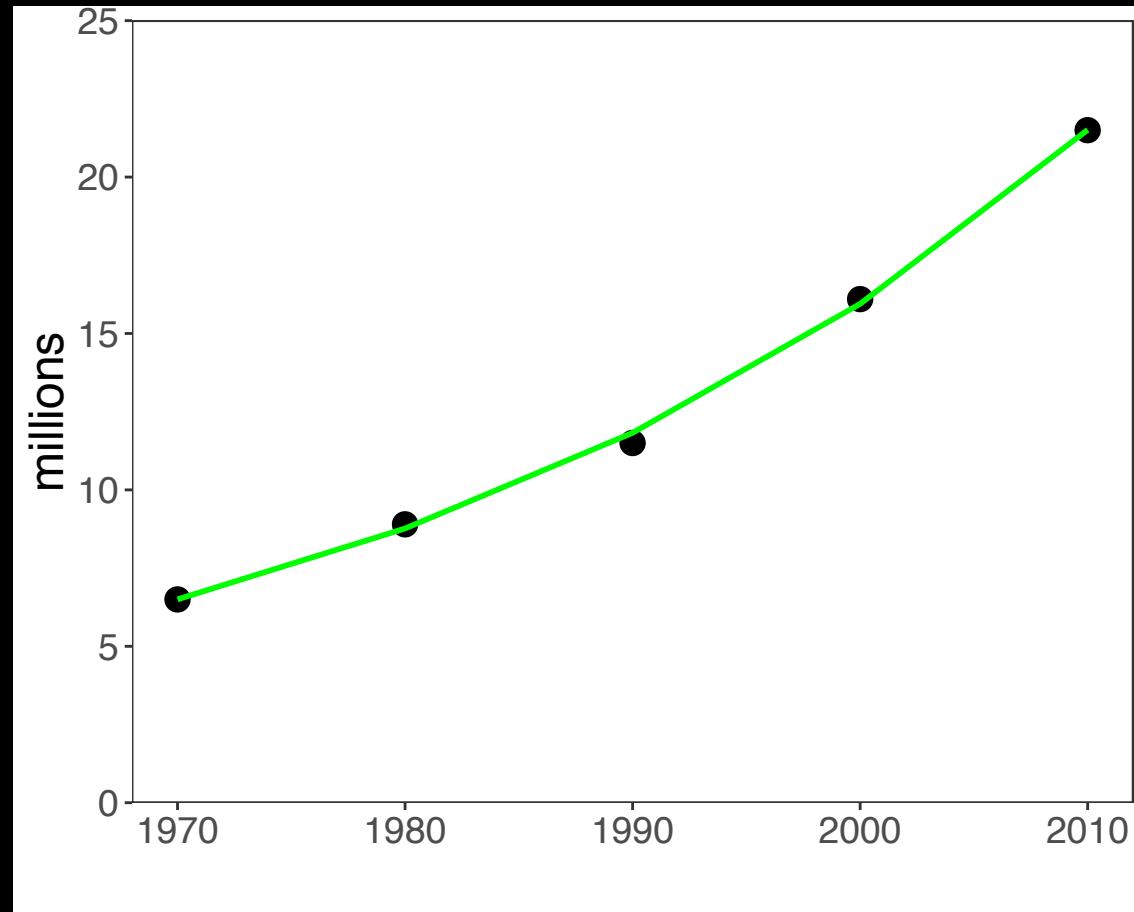
3. Mechanistic Model:



5. Evaluation:

$$r = .349/\text{person}/\text{yr}$$

4. Data:



What can we conclude from this fitted model?

Mechanistic Models: Beware!

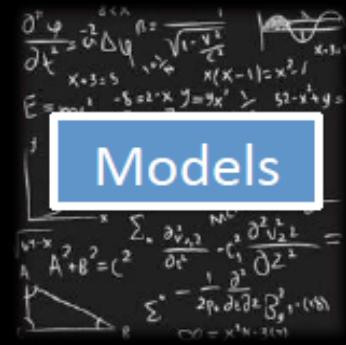
- Parameters used in the mechanistic models sometimes are not measurable!

A chalkboard filled with mathematical equations, including:
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 $\sum_{n=1}^{\infty} \frac{\partial^2 V_{n,2}}{\partial t^2} = \frac{1}{c^2} \frac{\partial^2 V_{n,2}}{\partial x^2}$, $V_{n,2}(x,t) = \frac{1}{2\pi} \frac{\partial^2}{\partial x^2} \delta_{n,2}^2 \cdot (V_0)$,
A right-angled triangle diagram with legs labeled a and b , and hypotenuse c .

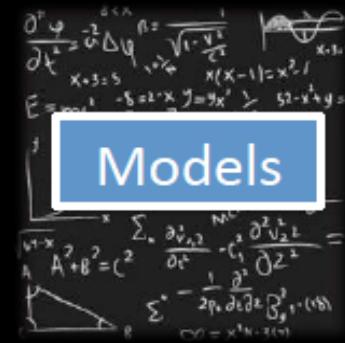
Models

Mechanistic Models: Beware!

- Parameters used in the mechanistic models sometimes are not measurable!
- Simulations can be computationally intensive



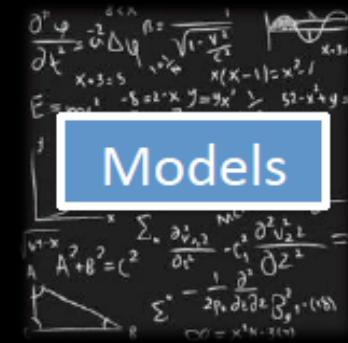
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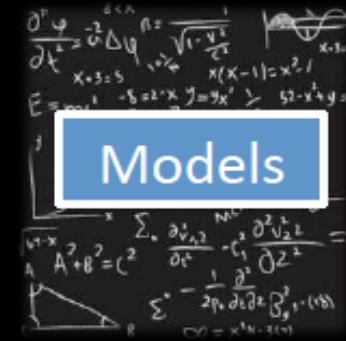


“All models are wrong but some are useful...”

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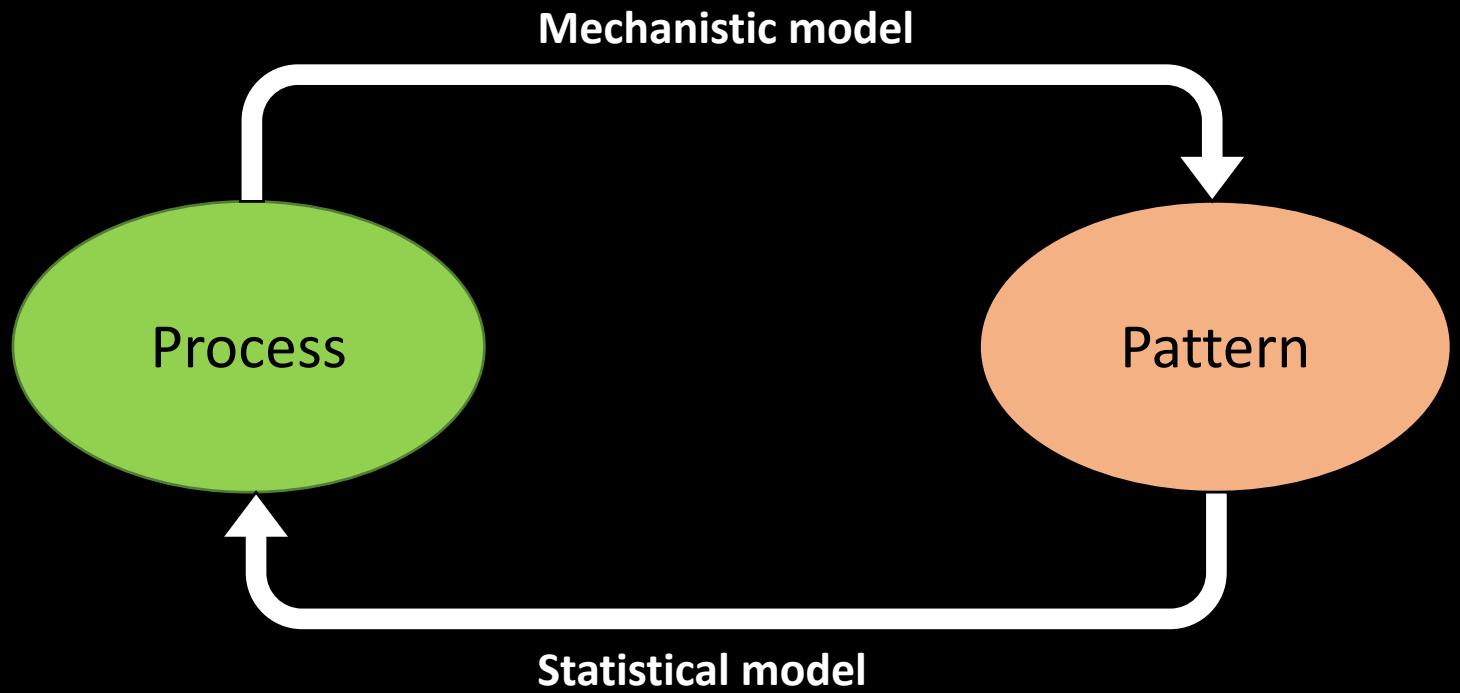
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We use models to both **predict** and **explain**.

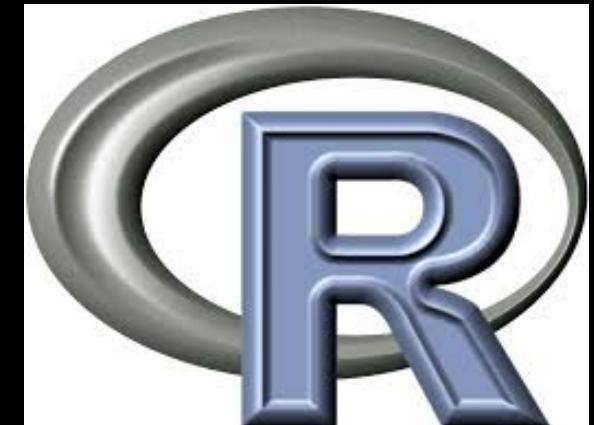
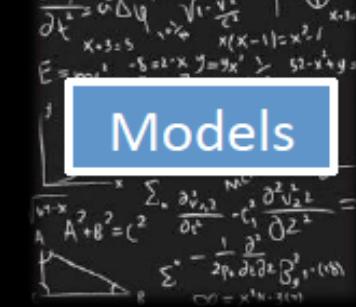
It is ideal when statistical and mechanistic models meet:

A small rectangular window in the top right corner contains several mathematical expressions. At the top, it shows a partial derivative of a function Ψ with respect to t , resulting in a term involving $\frac{\partial^2 \Psi}{\partial t^2}$. Below this, there's a calculation involving $x+3=5$ and $x(x-1)=x^2-1$. Further down, it shows $E = \sum_{i=1}^n -S_i = k \cdot x \cdot j = g x^2$ and $52 - 4^2 \cdot y =$. At the bottom, there's a diagram of a triangle with base R and height H , with the formula $\sum_{i=1}^n -2 \frac{\partial^2 \Psi}{\partial z_i^2} \cdot \vec{B}_g^T \cdot (\vec{z}_i)$ written next to it.



A Tool for E²M²

- Computer power keeps increasing
- Language/software
 - Fortran, C, C++
 - Julia, Java, Python
 - Matlab, Maple, Mathematica,
 - SAS, SPSS, Stata
- Specific programs
 - Vortex, RAMAS, NetLogo for IBM
 - NicheMapper for physiology, iLand for forest dynamics
 - MaxEnt for species distribution modeling
 - Zonation for reserve selection etc...
- The compromise: R---very powerful for
 - Visualization
 - Data formatting and sorting
 - Statistical analyses
 - Simulation (mechanistic model)



Goals for this lecture

- To explain what we're doing here
- To define "science"
- To define "data"
- To define "models"
- To introduce many different types of models
 - Statistical
 - Mathematical
- To introduce the "E" in E^2M^2
 - Ecology
 - Epidemiology

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What is Epidemiology?

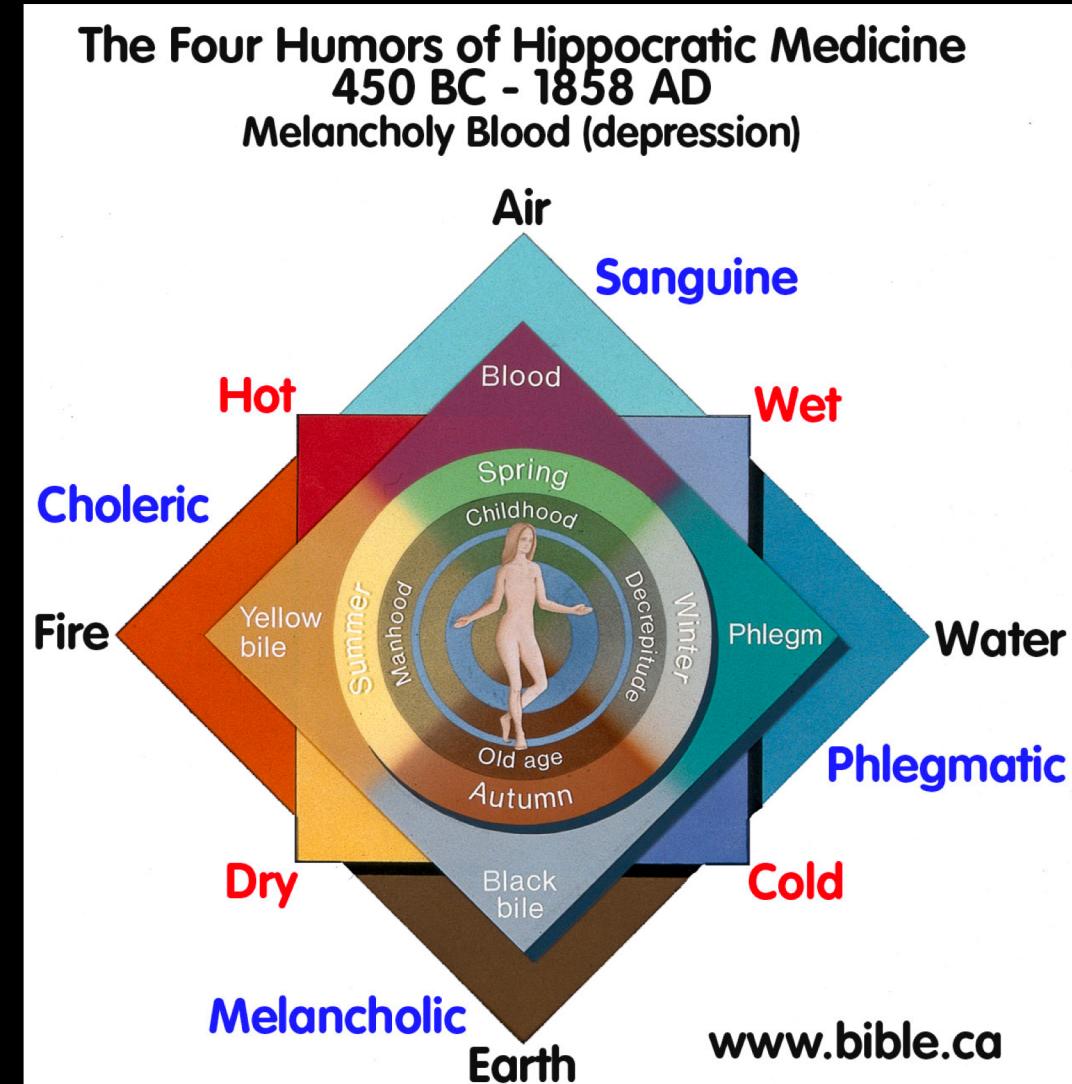
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- Emphasis on the study and analysis of the distribution and determinants of health and disease (“risk factors”)

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Models in Epidemiology

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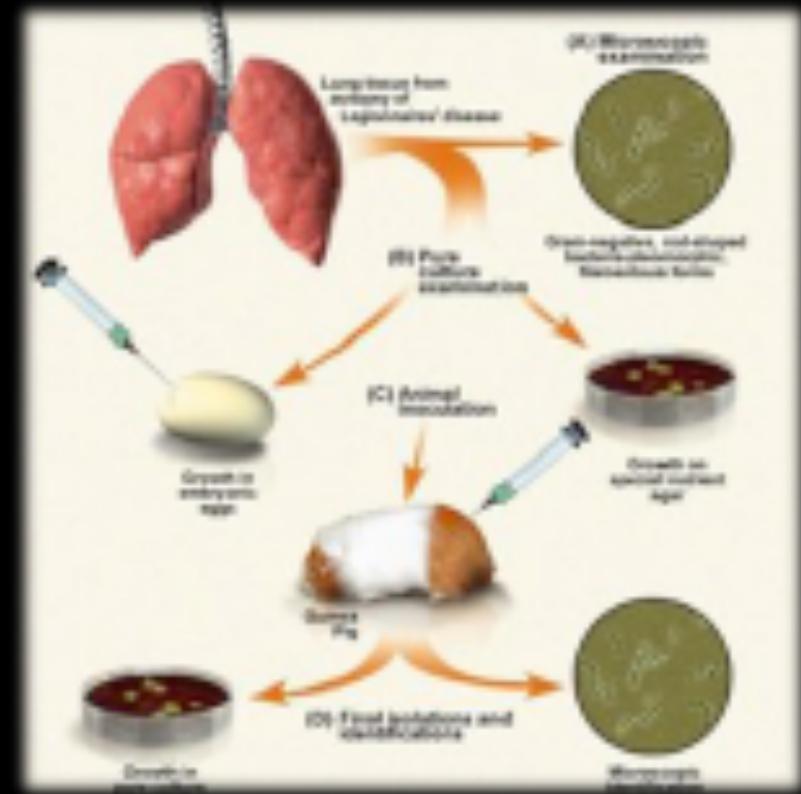
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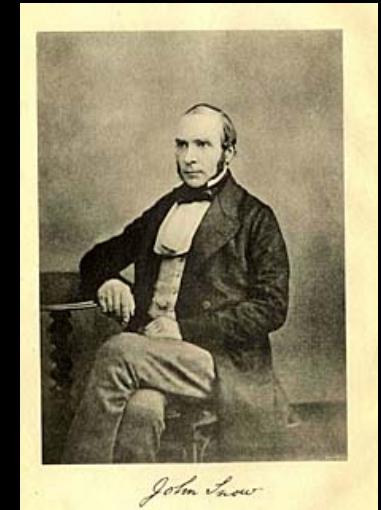
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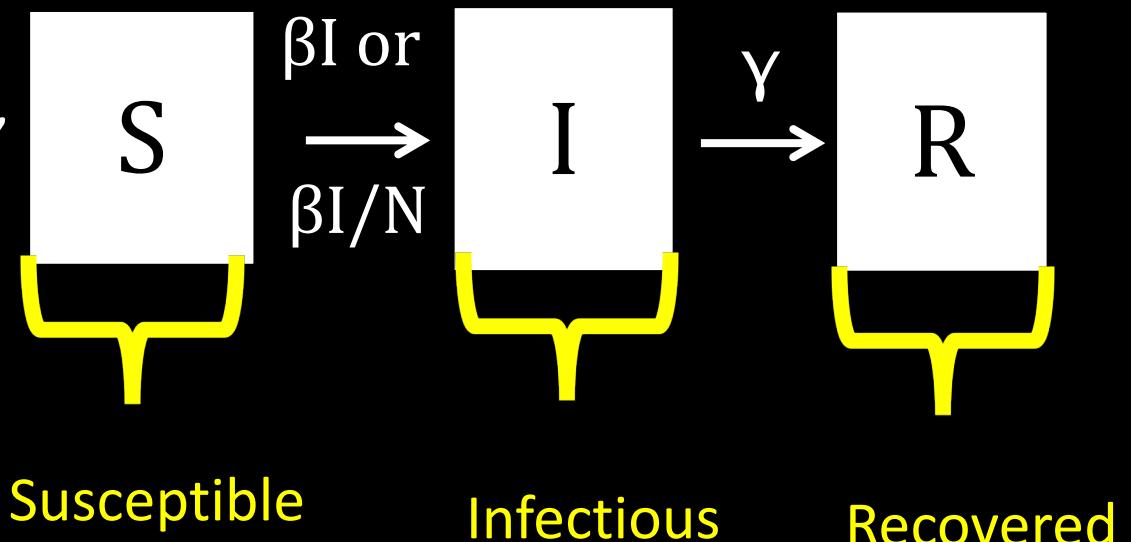
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 - Kermack and McKendrik (1927)



What is Ecology?

- The study of the **interactions** of organisms and their environment
 - Coined in 1866 by German scientist Ernst Haeckel
 - Nile crocodiles opening mouths for sandpipers (Herodotus)
- Emphasis on explaining **dynamical processes** in nature

Models in Ecology

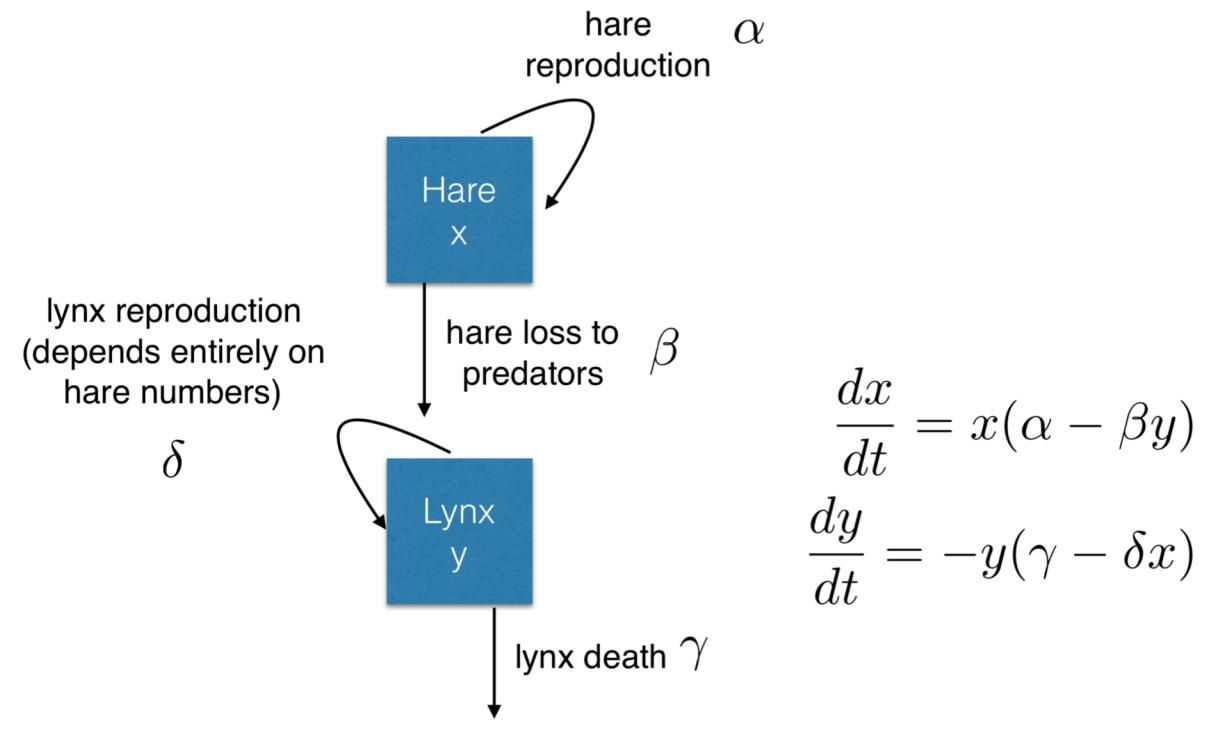
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Models in Ecology

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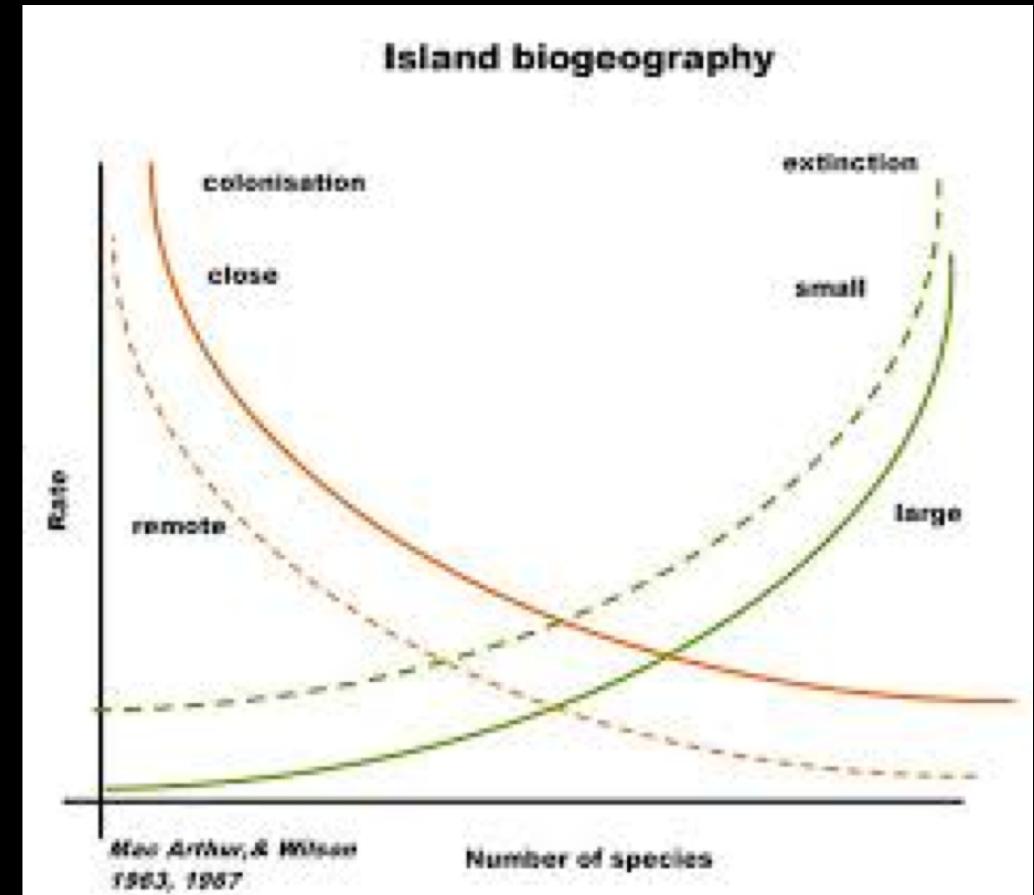
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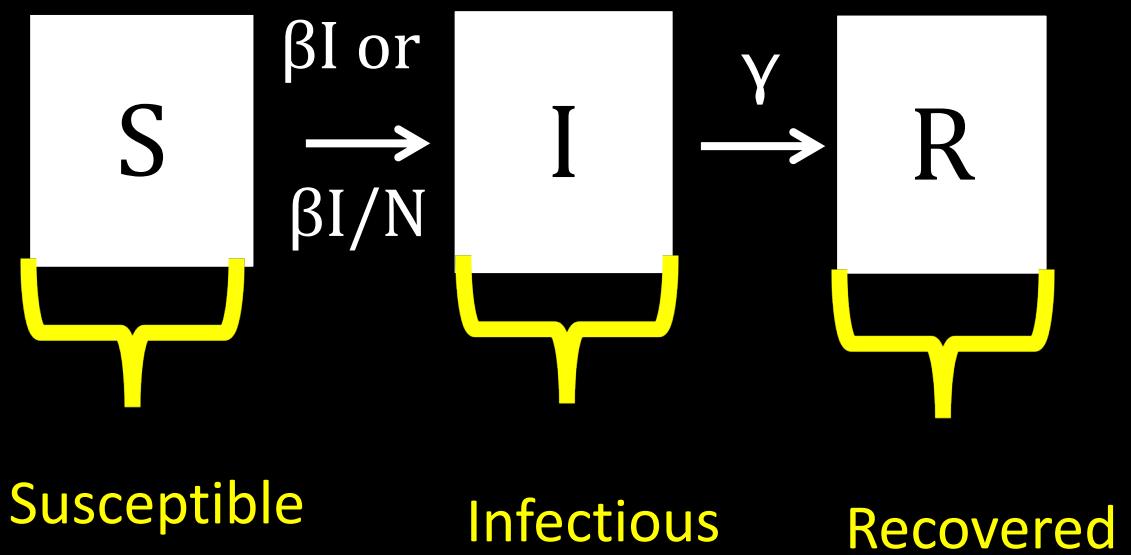
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5. Disease Ecology
 - Anderson and May (1980s)
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Misaotra!