

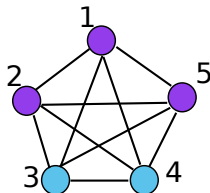
# Signal Processing Techniques for Interpolation in Graph Structured Data

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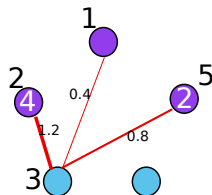
# An example of recommendation system

- ▶ Five movies
- ▶ a  $5 \times 5$  similarity matrix
- ▶ a user rating on movie 1,2,5
- ▶ predict his rating on movie 3,4



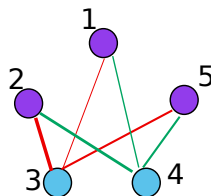
# k-nearest neighbors

- ▶ predict on movie 3
- ▶ suppose  $k=2$
- ▶ movie 2 and 5 are more similar to 3 than 1
- ▶ predicted rating on movie 3:  
$$\frac{1.2 \times 4 + 0.8 \times 2}{1.2 + 0.8}$$



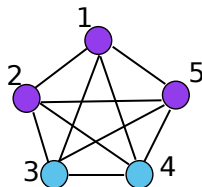
# Issues

- ▶ discard mutual information between movie 1,2,5
- ▶ predict rating 3,4 respectively



# Problem Reformulation

- ▶  $f(1), f(2), f(5)$  known
- ▶ *interpolate*  $f(3), f(4)$
- ▶  $\mathbf{f} = [f(1), f(2), f(3), f(4), f(5)]^T$
- ▶  $\mathbf{f} = f(1)\Theta_1 + f(2)\Theta_2 + f(5)\Theta_5$



# Band Limited Graph Signal Reconstruction

## Nyquist Shannon sampling theorem

If a continuous signal is band-limited, it can be reconstructed by discrete sampling without loss.

## Pesenson, Isaac

If a graph signal is band-limited, it is uniquely determined by their values on some sets of vertices.

# Reconstruction from Basis

## Critical Frequency

If the graph signal is band-limited, its spectrum decomposition has only components less than critical frequency  $\omega_S^*$ .

$$\mathbf{f} = \sum_i x_i \mathbf{v}_i \quad (1)$$

where  $\mathbf{v}_i$  is the eigenvector with corresponding eigenvalue less than  $\omega_S^*$ .

## Least Square

$\mathbf{f}$  known only partially, least square technique used to solve  $x_i$

# Numerical Results

## Dataset

- ▶ Student body test data with 488 records and 37 features.
- ▶ Use other features(excluding age) to predict the gender
- ▶ 80% training set, 20% test set, 5 fold cross validation

## Algorithm

- ▶ **Linear Discriminant Analysis** with average error rate at 0.4%
- ▶ **Graph Interpolation** with average error rate at 3%



# Issues

- ▶ Larger error rate
- ▶ Different choice of edge weight
- ▶ Heuristic critical frequency

## Acknowledgement

*Thanks for listening*