Chapter 4 - Inference in the MLP

Knowing they

E(B.)= B;

ond tact

S.e. (p) = [SST: (1-R])]1/2

isn't quite enough to do inference.

We need to make un assumption about the distribution.

We will make one additional assumption:

normally distributed with zero meen and versiones the explanatory vorintes x13 -- 1 xx and 3 Assumption MLR. 6 - Barmality The population error U is independent of

U~N(M=0,62)

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びいか to Assumptions MLR. I through MLR. 6 Classical Linear Regression Model (CLR). we have

A succinct way to a ssumptions of the CLM summorite the population U

Y /x ~ N(B+B,x,+B2x2 + · · · + Bxxe, 62)

Where (p. K is shorthand for (x, , x2, -- , x4)

(W)

Under the CLM assumptions MLR. 1 through MLR. 6, tenditional on the sample values of the independent

Variables

Note:

is given in chapter 3. Therefore

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~ Mo, 1)

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Where

Testing Hypotheses about a single Papulation Parameter

our population model is

and we assume that it satisfies the UR assumptions. Then

Where in odel. (k slope parameters and the intercept) Kt 1 is the number of unknowns in the population

the null hypothesis

To .. 5. = 0

where I corresponds to any of the k explanatory variables. In simple language, this means that after the vartibles X1,1×2,..., xj-1, xj+1, ..., xk have been accounted for X; has no effect on the expected value of y.

consider the wage regression

wage = Bo + B, educ + B2 exper + B3 tenure + U

and education have been accounted for, the number of years in the work force (exper) has no effect on nourly wage. This is economically interesting. If true, it implies that a person's work history does not affect mage. If \$270, then prior work experience contributes to productivity, null hypothesis Ho: 12=0 mems that, once termre

and hence wage.

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the t startistic of B.

The Appropriate Rejection Regions:

- When H1: B, 70 the rejection region is to > c

1 When H1: P5 <0 the rejection region is to <-c

When HI: Ps. 70 the rejection region is Ital > C

d=.1 or d=.05

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C is the critical value for some ghon of level

Our sample contains n = 408 high schools in michigan in 1993. We can use these duta to test the mull hypothesis that school size has no effect on standardized test scores Performence is measured by the percentage of students receiving against the alternative that size has a negedive effect. a pussing score on the Michigan Educational Assessment Program (MEAP) standardized tenth-grade much test (must 10). Shoot size is measured by student enrollnent (enroll).

The mull by pothesis is

Ho: Bensoll = 0

H1: Benroll < 0

We control for . overage annual teacher compensation (a praxy to

(Kot comp) and the number of staff per 1000 students (staff).

The estimated equestion, with standard errors is

= 2.274 (8.113) + .000016 tot comp + .048 Xxxxx (1000.) (40.) ,0002 envol (2002)

80h = U

P2= .0541

The coefficient on enroll is 7,0002 is in agreement that larger discould schools hamper performance.

Since N-K-1=404 404, we can use the standard normal distribution. For d=.05, the critical volue is -1.65

t = -0.0002 ~ -0.91

our t studistic is

t > critical value -1.96 => We tail to reject Ho.

We conclude that enroll is not statistically significant at the d=.05

level.

Unoldridge's estimates and standard errors

$$t = \frac{\hat{R}_{sirpred}}{se(\hat{R}_{sirpred})} = \frac{-0.083}{0.026} = |-3.19| = 3.19$$

Ho: B: =0 is the most common hypothesis, but some times

we want to test whether B; is equal to some other

given constant.

Generally,

where aj is the hypothesized value of

the appropriate t statistic is

Standard error

(estimate - hypothesized value)

The p-value for testing the null hypothesis

Ho: B: =0

against the two-sided alternative is

P (171 > 141)

in which I is a to distributed random workble with M-k-1 degrees of freedom and t is the numerical value

of our t statistic.

See Figure 4.6

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O/-

p-value = P(T) > 1.75) = 2 \* P(T >1.85) = 2 \* (.0359)

11 8140.

NB: in R code:

pool = 2 \* (1 - pt(1:85, df=40)) 2901 4140.0

8160.0 Z

P FTW!





Hypothesis testing focuses on the Authorital significance . We also need to pay attention to the magnitude B: in addition to the size of the

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少さかま

Statistical stanificance of X; is entirely determined by the size of top, , where as practical significance is related to the size (and sign) of B. economic Signiff Cource 3

دنه P. is whomse " or because use (Pi)" is small. can be statistically significant either because

A variable can seem important even it its effect is very small in practical terms!

Using the fact that (Fig - Bi) Sec (R) ~ tn-k-1

leads to a simple rule for confidence internals for the unknown population 13. A 95% CI Ñ

B. + C. Se (B)

5 which c is the 97.5th parcentile in 5

triky distribution

We know how to test whether a particular variable has no partial effect on the dependent variable: He may want to test whether a group of variables has no effect on the dependent variable. More precisely, the mull hypothesis is that a group of vorrables has no effect on Y, once another set of variables has been controlled for. the ttest!

Consider the model pluyer's saleries: that explains major league buse bull

log(schary) = Bo + B, Years + B gamesyr + B bang

+ By hownsyr + B rbisyr + U

where

however - home ours por your rbisyr = runs batted in per year gamestr = average games played por year Solary = total 1993 salary baves = coreer batting average (e.g. baves = 250) years = years in the MLB

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suppose we want to test that once years in the league has been controlled for, statistics measuring performance (barg, hoursyo, bisyo) gonesyo have no effect on wary. The mull by pothesis is

Ho: 13 = 184 = 18 = 0

H. Not Ho

The null has 3 exclusion restrictions. It to then then burg, hrunsyr, and roisyr have no effect on log(salry) after years and gamesyr have been controlled for

We call this a joint hypothesis test.

las(solvy) = Po + P, Years + Pz gamesyr + U

In the context of hypothesis testing, we could this the pestruted model and the original mode! the

unrestricted model

The restricted model always has fever parameters he restricted model.

F statistic defined to

F= (SSR, -SSRur)/9 SSRur/(n-k-1)

in which

SSRY ) i the residual sum of squeres of the restricted model

55Rar = the residual sum of squares of the un restricted mode

q = dfr - dfar is the numerator degrees of freedom

Recall that df = number of observations - number of estime ted perameters

Note: df, > dfur ble n= the same for both

degrees of freedom in the unvestricted medel SSR in the denominator of F is divided by the

n-k-1 = denominator degrees of freedom = diar

Ex: in the base built example if n= 353

Hur = 353 - 6 = 347 } = 353 - 9 = 344 } = 353 - 9 = 344 } = 3 = 3

F ~ Fq, n-6-1

DINCE a scritical value is selected the rejection

TT V C

region is

If Ho is rejected we & say that the set of explanatory variables excluded from the restricted model are jointly statistically significent.

fx: for bese built ( See p. 147) we have

126

1) (198.311 - 183.186) 183. 186 7 × 5 × 5 ~ 9.55

d= :05 c= 2.76, for d= :01 c= 4.13

F= 9.55 is well above the 1% souther I value

so we soundly reject the null that bourg, hoursyou and rbisyr have no effect on log(salary)

=> They are jointly statistically significant!

NB" ALSO SSEUT (M-K-1)
F= (SSEV SSEUT) (M-K-1)
9

p-value = P(F > F)

in which of is an Frankon variable with (9, 17-k-1) degrees of freedom and t is the actual value of our F startistic series our sample of derta.

Ho: B1 = B2 = -.. = BK = 0

HI: Not Ho

the restricted model

Y= 130 + U

NB: just the constant

Note: this is the F statistic that

R spits out from I'm with

a corresponding p-value

