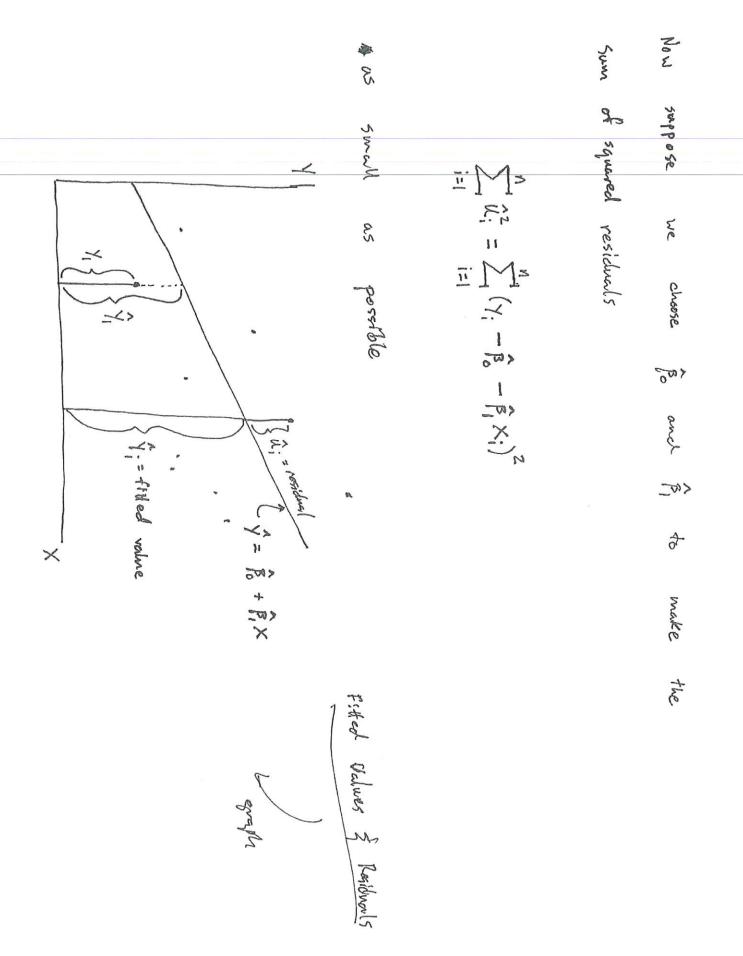
	Recall that	
$\sum_{i=1}^{N} (x_i - \overline{x}) (y_i - \overline{y})$ $\sum_{i=1}^{N} (x_i - \overline{x})^2$	the defined the OLS (andinary least spaces) estimators and B, as	

DATA 5600

4/11/2022

for any Lhen There MI 200 À. J. sesidue actual XIX: 72 a given Intercept and stope. a filled value for every observation in the the value we <u>~</u>₩) Y: and its fitted value: and 2 for observation i is the difference û; = 1: -9 = 1: - 1: - 1: X; " ""> _00> predict for y define + >01 > .× a fitted value When for y ×××× sample. between



* Day. 15 06 Maret changes when X increases by one unit. Equivalently From E homina have F cuses interest. It tells us the amount by which obtained STE the h < 00_ slope estimate 4Wo AY = BAX = AT/AX regression line: - By × × which we can write as sto ha

Ex: 2.3 P. 33

For the In thousands of dollars. population of CEO'S, let y be commonl solary

y= 1,452. 6 indicates a salary of \$1,452,600. Example y= 856.3 indicates a salary of \$856,300 and

let x be the average return on equity (roe) for the CEO's for the previous three years. POE is defined in terms of net income Then as a percentage of common equity. For example, it X= 10 average return on equity is 10% かってい

7 Bodard study the relation ship between the simple model roe and ceo compensation,

salary = B, + B, roe + U

F In thousands of dollars, when return on equity increases by one parameter B, measures the change in annual salary,

Ustas per centage point. collected from Business week Be cause dust a on 150 solutes for a sample of 10=209 for 1990 a high role is good for a firm we expect p, >0 we obtain

Q: How If roe = 0 then predicted solary is the intercept 963.191, Next we can write the predicted change in salary as a function of the Which equals \$963, 1911 strice salary is measured in thousands. change in voe: do ve interpret this? Salery = 963.191 + 18.501 ree

predicted to change by about 18:5

or \$18,500

If roe

changes by one percentage point 1 roe = 1 then

salvy is

1 salary = 18.501 stree

B

of roc. Suppose, for example, that roc = 30 then We can Which is salary > use this to predict salaries at different values just over \$1.5 = 963.191 + 18.501(30) = 1,518,221 m: Wion

We con

define

7 88

 $=\sum_{i=1}^{n}(\lambda^{i}-\lambda^{j})^{2}$

To explained sum of squares (SSE)

SSH 1 \(\frac{1}{\sqrt{1}} - \frac{1}{\sqrt{1}} \)

residual sum of squares (SSR)

SSR

and the

755 spread out the Y; are in the sample. measures the tabul sample variation in Y: - that is how

NB: dividing 557 by (n-1) gives the sample vowiance of

SSE measures the sample variation in
$$\frac{2}{3}$$
.

SSR measures the sample variation in $\frac{2}{3}$.

We can write

SST = SSE + SSR

Groodness of Fit

Groodness of Fit

 $\frac{2}{3}$ = $\frac{2}{3}$

NB: see p. 39

go book

29

72 0 C R2 4 1 De usually multiply by 100 R2 to explain ed percentage is the is interpreted as the fraction of the sample variation y that is explained by X ratio of the explained variation compared to total variation, of the sample variation in y that is × get the

that we will vely on.	estimates. But we will need to state a few assumptions	he will short by establishing that ols & sixes unbiased	population.	of B and B, over different random samples from the	This will be a discussion of the sampling distributions (PDF)	Bo and B defined we can assess their statistical proparties.	Now that we have mostlement was rules (estimators) for	Statistical Proporties of the OLS Estimaters
-----------------------	--	---	-------------	--	---	--	--	--

NB: Y is	S A S	Where		to the	in the	A Sumption
related to X linearly in B's (this is really as stance population DGP)	slope, respectively.	to and By are the population intecept	Y = Bo + B X + U	explanatory variable, x, and the error, u as	population model, the experimed variable y, is related	SLR.2 - Linear in Parameters

E

are not	The sample	Assumption		& llowing	We have	Assumption
all the same value.	le antcomes on X, namely EX; , i=1,, n}	SLR. 3 - Sample Variation in the Explanator Variable	Y = Bo + B1 X + W	the population model	a random & sample of size 1, \(\(\x_{i}, y_{i} \): i=1,2,, n\\ \\ \},	SLRIZ - Random Sampling

67

5 Unbrused ness of OLS Ustre and other SLR.1 through SLR.4 |Tr | (3) Words 11 11 ~~» is unblased for Bo and B, is unbiased for B,

Which 4] (x; -x) (y; -x) =] (x; -x) y; 50 estimentor < 100 5 1. (x, \x), となる SSTx 53 11 200 [=1] (x: -x) (po + p, x; +u;) +0 557_x 000

Mon Using the Recall write $\sum_{i=1}^{N} (x_i - x_i) \beta_i + \sum_{i=1}^{N} (x_i - x_i) \beta_i x_i + \sum_{i=1}^{N} (x_i - x_i) \alpha_i$ We MAZCH they-11 can wride the numerostor P. Z(x; -x) + P. Z(x; -x)x; + Z(x; -x)u; preparties of Z(x; ~ x) =0 numerator SSTx = 2/12: -x3 (as we have defined it) tre and that $2(x; -x)x_i = 2(x; -x)^2 = 55T_x$ surmation 23 sparator & , we B SSTx + 2 (x; -x) 4;

And	Where			Pulling This
Mow	(-		_0x>	This
E	<u>,</u>	11	11	800
can	, ,	-00	_04	the
798	\ \times 1	× × / × × × +	+	denominate
at a		7 7 7 4 r	\$57x (X: -x)n:	who
E(B)		~	a.	gives

Thus, β_{i} : $E(\beta_{i}) = \beta_{i} + E \int_{\infty} \sum_{i=1}^{n} \sum_{i=1}^{$

Methodish wit!

2 a cross 10014 < W 0 44:5 <\ VI -D2 XI 11 4 11 これも 1000 B + 8 x +u; 11 Į, M X 30 8 4 + P, X + R 9 straight forward. Sp+ 1 X) 11 Wo β + (β₁ - β) X Can ト)

[hus Then Since 50 200 × CAN conditional M 臣(成)=0. 6000 K COLOR my that E(B,-B) = B,-B, =0 11 11 2. /1 WO unbiased on the values Now struce we + E[(B, -B)x] + E(a) $+ E[(\beta, -\beta)\widehat{x}]$ of the W know × that E(g) = 15,

so tret

	of the	The err	Assumption	ve will	Variances
$Var(u x) = 6^2$	explanatory variable. In other words,	error It has the same variance given any value	SLR. 5 - Homo skedasticity	I state an additional ass umption	of the OLS Estimators
		10			

Recurse
$$Var(u|x) = E(u^2|x) - [E(u|x)]^2$$
 and $E(u|x) = 0$

Le can say that $E(u^2|x) = Var(u) = 6^2$. I.E. b/c

 $E(u|x) = 0$

It is often called the error variouse or distinbute unitate

The conditional mean and conditional variouse of y:

 $E(y|x) = 8 + 8/x$
 $Var(y|x) = 8^2$

NB: it is sample not sample we are talkery about here!

(8)

7 E(82) = 62 and Which Se(()= 6/1557x = 6/(2/(x; -x)2) Sugiformissons 11 Standard error of B (2-2) 22 d2 SLR. 1 through SLR. 5 an unbrused estructor 11 3 - 2 DB: Recall that i; = Y; -Y; and Y = 3 + 5 X;

AX

unblased

sime to