B

y and Most of X econometrics deals with relating two random that represent some population. varia bles

Usually, we are interested in "explaining y in terms of X" We confront (ad least) 3 issues in this process:

since there is never an exact relationship between two variables, do we allow for other factors to affect y?

(1) What How can we be sure we are capturing a ceteris relationship between y and x? is the functional relationship between y and x? > >= fcx)? pari bus

We start by writing down an equestion relating y to X 29 : Smonley

11 Po + P, X + U

This 40 equestion interest. It is called the Simple Regression Model. is assumed to hold for the population

M 12:5 model:

explained variable (the variable me are interest in explaining)

explanatory variable (the variable we believe affects y)

(represents other factors affecting 4) error or disturbance term

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The simple Regression Model adhresses the issue of the functional relationship between y and X. It the either" factors in it are held fixed, so that the change in it is zero, we were X has a linear effecting on y.

Dy= B, Dx, it Due o

The change in y is just the change in X multiplied by 13. We call By the slope parameter; it is of primary interest

econometrius

The parameter B is the constant term or the Intercept . parameter.

Ex: 2.1 Nooldridge Pp. 24

model Suppose Saybean yield is determined by the

yield = Po + P, Pertilizer + U

y= yield x = fertilizer

It may contain factors such as landquality, rainfull,

The coefficient P, measures the effect of fertilizer on soybean yield, helding all else southent

syield = p & tertilizer

EX: 5.2 A model that relates on includual's educations Wage equation

to wage -

Wage = B + B court 4

change in hourly wage the given another year of If wage is measured in dollars per hour and educ is education. musured in years of education, then B, measures the

The linearity of

Y = B, + B, X + U

implies that a one-unit charge in x has the Same effect on Y, regardless of the value of Y.

Sometimes, his is unrealistic. For example, in the wage-education example we might believe that there is an increasing relationship, than the previous year of education does. We will allow for Such that an additional year of education increases wases by more

effects like this later.

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touclustons about how X affects Y. important question is are we able draw cetaris paribus

Lackers seen that By does measure constant ( in u) now & affects y, holding all

causality. It for example, there is a third factor in il with this later. Basically though, correlation is not the same as Unfortunately this not the onel of the causality issue. We will deal ERUSES both y and x then we can have problems

In the wage equation we might have a factor "unimal ability" in U. The econometricion will vantorble, but it aborty relates to both Y and X. never observe this called

nothing 73 long as Mon is lest by assuming an intercept term we will make Bo is included in the equestry 22 assumption about U. As

E(u) =0

if E(u) to but we include "sucked" into \$ Hechnical statestical term ox the mean of d will get

Note:

code: nonzero \_ mean. V I simulation to show the

P

(D)

addithonal (cruckal) assumption regarding how related. A natural measure of the association between 2 and X

variables is the correlation coefficient.

Socs linearly related. Assuming that X and u are unrelated in ٦ long may to defining and ۶ \ \ \ 9 Bo + B, X + 4 uncorrelated, then they are not how it and it should be uncorrelated

of X (huch as X2). ð unfartamodely, it is not energh. It is be uncorrelated with X but correlated with functions possible for

expectation of a siven X. Namely A stronger (better) assumption involves the and it senal

E(u/x) = E(u)

conditional distribution.

This says that the average value of the unobservables is the same across all withouts of the population determined by X, and that the common average is just the everage of the marginal distribution of it.

iu H

we can't learn anything about the average value of it

knowing K. Here (in this situation) this is desirable.

NB: This is called mean independence assumption of

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Combining (namely that  $\mathcal{E}(u) = 0$ ) we have that this with our earlier assumption about

E(u/x) = 0

is called Zero conditional mean assumption

Assume that it is the same as innate ability". This assumption requires that the average level of ability is the same regardless of the years of education.

Note: Probably too strong an assumption as more able " are more likely to be more educated

Lero more fartilizer is given to higher-quelity plats of land then the expected value of it changes with the level of for tilizar not hold. the fertilizer example, it tertilizer amounts are conditional mean assumption will had. It knever independently of other features of plots then the And the saw constituent mean a sumption will

Jyl By the so conditional mean assumptions of her B, another interpretation.

(80)

the expected value of (some x)

Taking

·Y = Po + PX + U

op of

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E (1/x) =

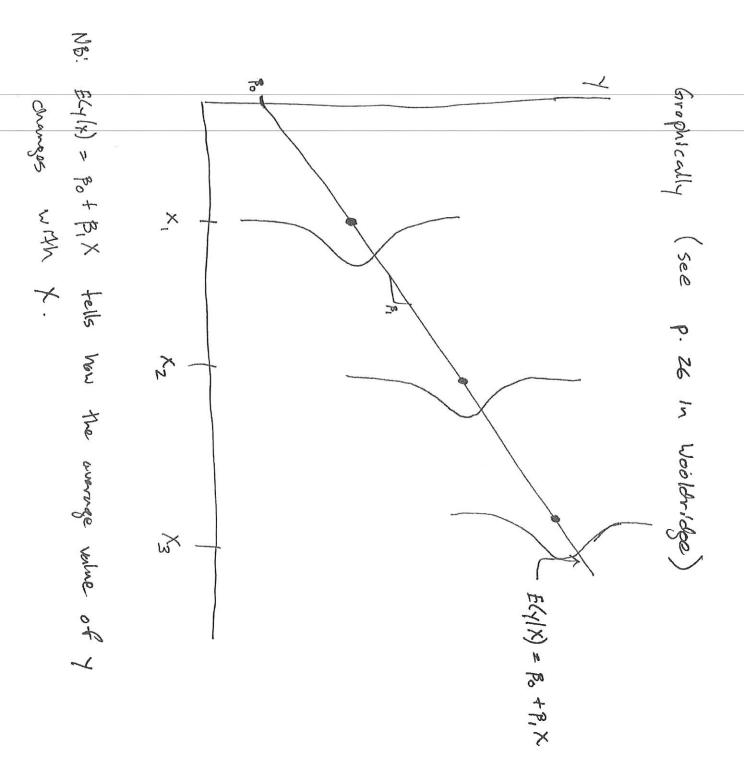
0,

+ B X + E(A(x)

0

= Bo + B1 X

てんら The expected value of y by BI. Says that a one-unit charge to X changes



Let Ordinary Define un estimentor une use a sample of data! the {(xinyi): i=1,..., n} denote a random sample of size 3 to get estimates for population Lenst Squares Estimates from the population. pop ulution These are drown from parameters BOB?

ix th Hore because õ × 7. 11 か 11 N it contains all factors affecting Y; other than X; all other footers offecting with the annual annual annual sawings other than X; is the every " " Sortugs income CARON Bo + B, X, + U; 1 = 1, ..., n form for the 1th 03 household i's Can observation write

E(u) = 0

which can be written

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Cov(xu) = E(xu) = 0

EX: totiliter

treat X as fixed

E(X(Y-BO-RX))

0

and

E(y-180-18,K) 20

Equation Given Counter parks \* 9 1 Zx; (y: - Po - Po x;) 上之(4:一度一度以) =0 ~1 Can 11 १ळ sample of data ₹ + and 50 7007 <∞\_ |× re written 2 0 Z solve 25 will choose the sample 举 \*

(B)

Simple Where Then t NO set once E < Vo < 000 > 11 WAR No ~() given y and x have \\ \\ < Wo and 3 (X) (1) Slope -x =:W= 21termes estimate by it is of B, T, and X

Which 1 V V Drapping the Mx (4:-4) Se 1 x, [y; - (y - Bx) - Bx] =0 (1X I (does not affect the solution) and plussing re arrange Trab Equation (\* \*) 25 yields

5. TX XX (X: -A) Using properties of かんか  $=\sum_{i=1}^{\infty}(x_i-x_i)(x_i-x_j)$ Summadion operators ( see Appendix A)

Note: There the sle pe This is simply the sample divided by the sample variance 3 \_04> 11 estimator long as 2 (x. -x) (y: -y) z. (× √x) ς Ξ. (× x) x Š  $\sum_{i=1}^{N} (x_i - x_i)^2 > 0$ & X covariance of X and y