

Continuous Time (aka Euclidian Hamiltonian) Cluster Monte Carlo*

Affine: $a_t \rightarrow 0$

$$S = - \sum_{t,i} K_i^0 s_{t,i} s_{t+1,i} - \sum_{\langle i,j \rangle} K_{ij}^\perp s_{t,i} s_{t,i}$$

$$H = \sum_i \Gamma_i \sigma_i^x + \sum_{\langle i,j \rangle} \tilde{K}_{ij} \sigma_i^z \sigma_j^z$$

$$K_{ij} = a_t \tilde{K}_{ij} \quad , \quad e^{-2a_t K_i^0} = \tanh(a_t \Gamma_i)$$

- A state space (real value decay times)

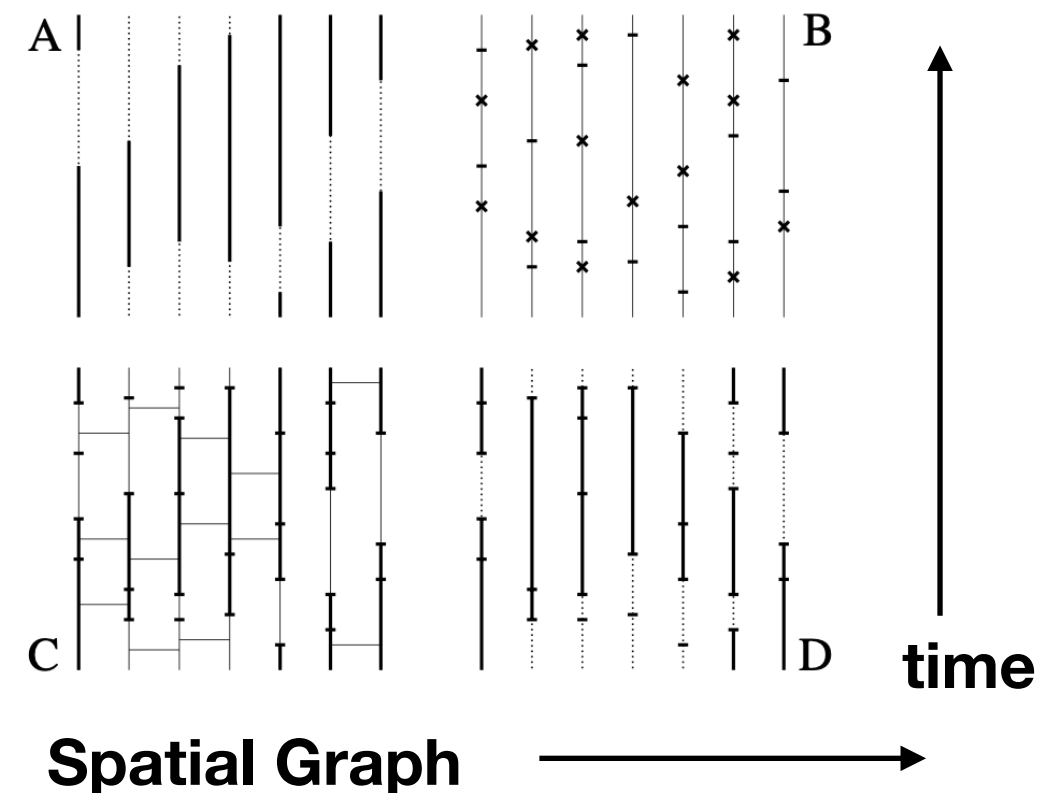
- B Poisson Decays:

$$P(t) = \Gamma e^{-\Gamma t}$$

- C. Spatial Percolation

$$P_{ij} = 1 - e^{-2\Delta t_{\text{overlap}} \tilde{K}_{ij}}$$

- D. SW Flip clusters for new state A



Pretty Easy to Program with Connected Components Graph algorithms:
Works for 1 + d Radial Quantization (Sphere) Ising/SUSY/Warped AdS etc

*See: 1998: [H. Rieger](#), [N. Kawashima](#)

Application of a continuous time cluster algorithm to the Two-dimensional Random Quantum Ising Ferromagnet

Duality: $\cosh(2a_t K_i^0) \cosh(a_t \Gamma_i) = 1$