

Team1:

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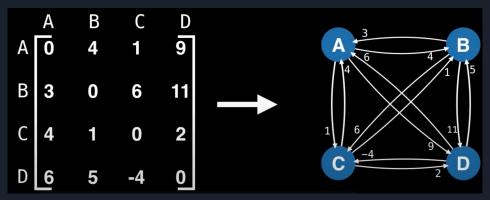
TSP: Introduction

Let $L=\sum \sum x(i,j) d(i,j)$; We want to find:

$$L^* = \min \sum \sum x(i, j) d(i, j)$$

In other words - given a complete graph, find the shortest **Hamiltonian cycle** in the graph.

NP-complete - no known efficient (i.e., polynomial time) algorithm.



Proposed implementation of algorithms

Naive solution/Dynamic Programming

- 1. (Exact) Naive: Brute force search over N!
- 2. (YZ)(Exact) Held Karp (Dynamic Programming) O(n^2 2^n)
- 3. (TY) (Approximate) Nearest Neighbour
- 4. (SW)(Approximate) Lin Kernighan
- 5. (WZ) (Approximate) Christofides 1.5* L*
- 6. (NS) (Approximate) Simulated Annealing
- 7. (NS) (Approximate) Ant colony optimization

Algorithm Main Ideas

1. Naive - O(n!)

Try all permutations and see which one is the shortest path (using brute force search).

2. Held-Karp - $O(n^22^n)$

Based on dynamic programming and solve TSP "bottom-up".

$$G(i, s) = min \{ C_{ik} + G(i, s-\{k\}) \}$$

3. Nearest Neighbour

One of the first algorithms solves TSP approximately. The salesman starts at a random city and repeatedly visits the nearest city until all have been visited.

Algorithm Main Ideas

1. (Approximate) Lin - Kernighan O(N^2.2)

Lin-Kernighan is one of the best heuristics for solving the symmetric travelling salesman problem. It belongs to the class of local search algorithms.

- 2. **(Approximate) Christofides** 1.5* L*: If the cities follow the triangle inequality, which is a+b>c, that this algorithm has 3/2 approximation guarantee.
- 3. **(Approximate) Simulated Annealing** arrive at solution by (~exhaustively) exploring the state space
 - Random, iterative improvements to the path length
 - Always accept improvements; decaying probability of accepting setbacks to encourages state exploration
- 4. **(Approximate) Ant colony optimization** based on behavior of real-life ant colonies
 - Randomly explore space, leaving "pheromones" to help later ants find good paths

Project Design Requirements

Program language: C++, Python (Networkx for visualization).

Dataset: TSPLIB

Test plan: Use (some) of the proposed algorithms to generate approximate solutions to various TSP datasets.

- How far from the optimal are the resulting paths?
- Performance of each algorithm?
- Statistics for the randomized algorithms
- Agreement with theoretical upper and lower bounds?



References:

For some introductory reading:

https://en.wikipedia.org/wiki/Travelling salesman problem https://en.wikipedia.org/wiki/Christofides algorithm

Detailed Algorithmic Implementations
"Simulated Annealing", Per Brinch Hansen June 1992

Ant Colony Optimization, Marco Dorigo and Thomas Stützle

Dataset Documentation

https://www.math.uwaterloo.ca/tsp/data/index.html http://comopt.ifi.uni-heidelberg.de/software/TSPLIB95/

Thank You