

CHAPTER-2

ATOMIC STRUCTURE.

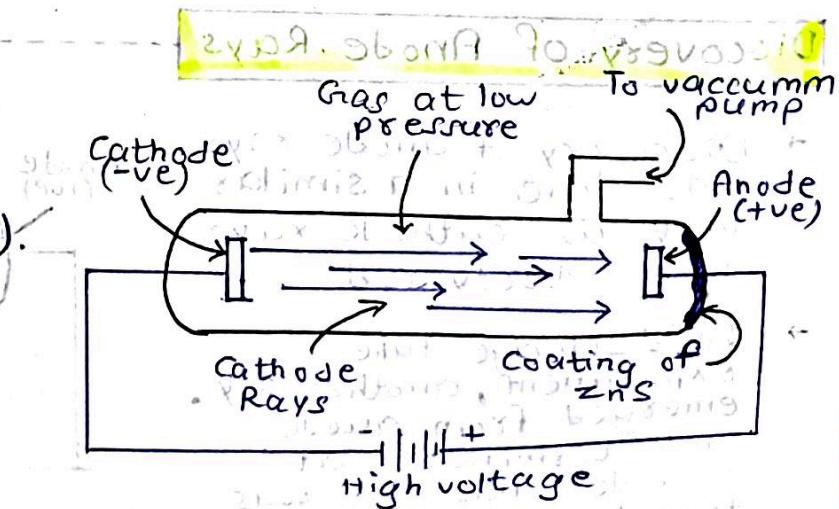
- At first, John Dalton proposed that atom is the smallest particle of matter and it cannot be divided.
- But, due to advance research it was found that atom can be divided into sub-atomic particles.

Sub Atomic Particles

Particle	Mass	Charge	Discovered by	e/m ratio
Electron (e ⁻)	$9.1 \times 10^{-31} \text{ kg}$ $9.1 \times 10^{-28} \text{ g}$	$-1.6 \times 10^{-19} \text{ C}$	J.J. Thomson 1897	$1.76 \times 10^{11} \text{ C/kg}$
Proton (p)	$1.67 \times 10^{-27} \text{ kg}$ $1.67 \times 10^{-24} \text{ g}$	$+1.6 \times 10^{-19} \text{ C}$	Rutherford 1911	$9.58 \times 10^7 \text{ C/kg}$
Neutron (n)	$1.67 \times 10^{-27} \text{ kg}$ $1.67 \times 10^{-24} \text{ g}$	0	James Chadwick 1932	

Discovery of Cathode Rays

- Discovery of cathode ray is the result of Faraday's discharge tube experiment.
- In his experiment, he passed current of very high voltage through a discharged glass tube and observed that a ray emerged out from cathode and terminates at anode.
- He termed this ray as 'cathode ray' because it emerged from cathode (-ve electrode).
- In this experiment, the voltage was very high (about 10000V) and the pressure inside the tube was very low.



Observations of this experiment :-

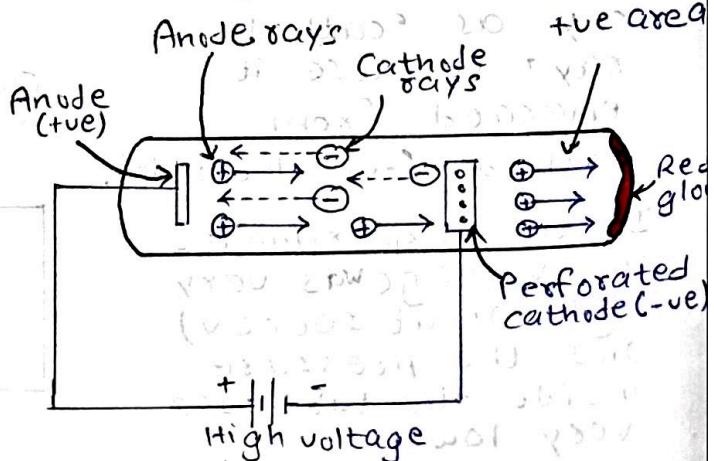
- Cathode rays travels in a straight path with a very high velocity.
- Cathode rays produces shadow of the object placed in its path.
- Cathode rays produced green glow when it struck on ZnS coating beyond anode.
- They affect photographic plates.
- They penetrate thin sheets of aluminium and other metals.
- Cathode rays caused movement in paddle wheel placed between electrodes. This indicates that the cathode rays have some mass.
- When electric and magnetic fields are applied, cathode rays deflected from their path. This shows that cathode rays have some charge.
- The direction of deflection shows that cathode rays have -ve charge on them.
- The charge to mass ratio is same for all cathode rays irrespective of the gas used in the tube.

Conclusion made from this experiment:-

- From this experiment, it was observed that cathode rays have some mass and they have -ve charge.
- Later, these rays are termed as 'electron', considering that they are the basic constituent of all the atoms.

Discovery of Anode Rays

- Discovery of anode rays was done in a similar way as cathode rays were discovered.
- In discharge tube experiment, another ray emerged from anode and terminates at cathode. This ray was termed as 'anode ray'.



Observations:-

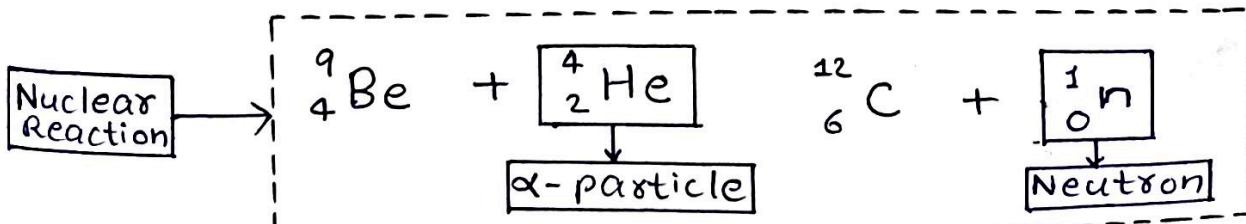
- Anode rays have similar properties like cathode rays.
- Like cathode rays, anode rays travels in a straight line with high velocity. They produces shadow of objects placed in their path.
- Anode rays like cathode rays, caused movement in paddle wheel. This indicates that anode rays also have some mass.
- The direction of deflection of anode rays by electric and magnetic field shows that they have +ve charge.
- For different gases used in the discharge tube, the charge to mass ratio of anode ray is different.

Conclusion :-

- In this experiment, it was observed that, like cathode rays, anode rays have some mass and they also carries +ve charge on themselves.
- Later, anode rays are termed as 'proton', considering they like electrons, they are also a basic constituent of all the atoms.

Discovery of Neutron

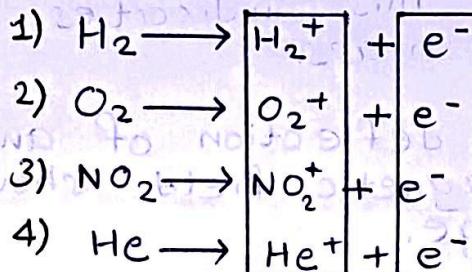
- James Chadwick in 1932 bombarded alpha particles on thin sheet of Beryllium.
- He observed not only carbon, but also an electrically neutral particle having mass slightly greater than that of proton was obtained.
- He termed this particle as 'neutron', considering like electrons and protons, neutron's are also a basic constituent of all the atoms.



Dependency of e/m ratio of 'e-' & 'p'

- Charge to mass ratio (e/m ratio) of electrons depends upon nothing. They are independent of gas used in discharged glass tube.
- But, in case of protons, it depends upon the gas used in discharged glass tube.

Reason



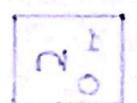
In each case, every gas release same electron.

In each case, every positive ion is different.

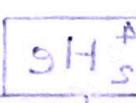
That's why, the e/m ratio of cathode rays is independent of nature of gas. While, e/m ratio of anode rays depends upon nature of gas.

Story after discovery of Sub Atomic Particles

- Once, Dalton said that atoms can never be divided. But after the discovery of subatomic particles, he failed.
- Thereafter, different atomic models were discovered.
- They are as follows:-
 - (i) Thomson's Atomic Model
 - (ii) Rutherford's model
 - (iii) Bohr's model
 - (iv) Quantum mechanical model



Neutral



X-Hydrogen

Thomson's Model of an Atom

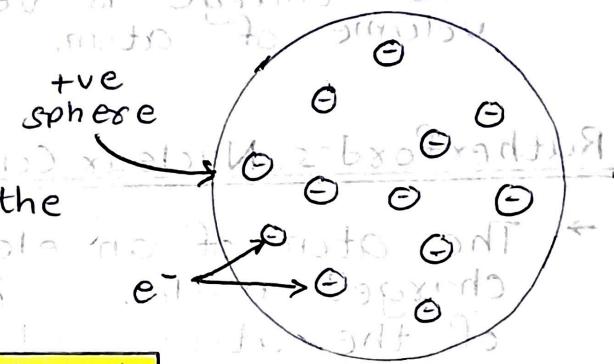
- This model is also known as 'plum pudding' model or 'watermelon model'.

After discovery of e^- , Thomson assumed that:-

- Atoms are spherical in shape.
- Atoms consists of +ve charged sphere.
- Electrons are embedded in the sphere to maintain electrical neutrality.

Drawback :-

- Thomson doesn't explained the location of +ve charge.



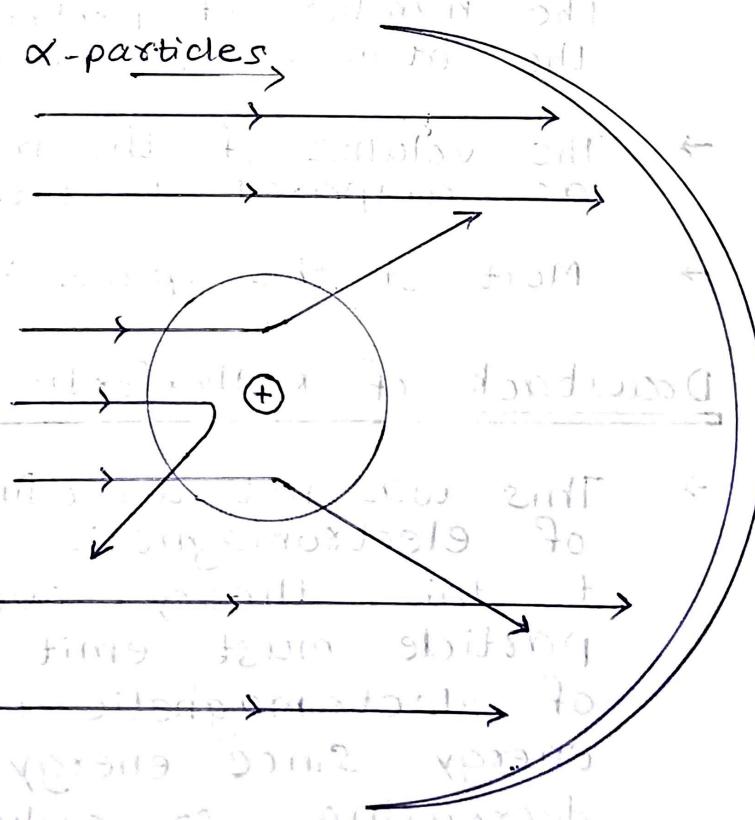
Rutherford's α -Scattering Experiment

- Rutherford bombarded α -particles on a thin sheet of gold which was surrounded by photographic plate.

Observations :-

- Most of the alpha particles passed α -particles away without any deflection.

- Few alpha particles were deflected by small angle while a very few were deflected by large angle.



- Very few alpha particles were deflected by an angle of 180° and set back their path.

Conclusion :-

- Most of the α -particles passed away undeflected, it means that most of the space inside an atom is empty.
- Very few α -particles deflected by large angles, it means that there is the presence of concentrated +ve charge in an atom.
- Very few α -particles deflected by the angle of 180° , it means that volume of concentrated +ve charge is very less as compared to the volume of atom.

Rutherford's Nuclear Concept of the Atom :-

- The atom of an element consists of a small +vely charged nucleus which is situated at the centre of the atom and which carries almost the entire mass of the atom.
- The electrons are distributed in the empty space of the atom around the nucleus in different concentric circular paths called orbit.
- The number of electrons in orbits is equal to the number of protons in the nucleus. Hence, the atom is electrically neutral.
- The volume of the nucleus is negligibly small as compared to the volume of the atom.
- Most of the space in the atom is empty.

Drawback of Rutherford's Model:-

- This was not according to the classical theory of electromagnetic proposed by Maxwell. According to this theory, every accelerated charged particle must emit radiation in the form of electromagnetic waves and loses its total energy. Since energy of electrons keep on decreasing, so radius of the circular orbit should also decrease and ultimately the electron should fall in nucleus.

→ It could not explain the line spectrum of H-atom.

Properties of Charge

→ $Q = ne$ (charge is quantized).

→ Charge are of two types:

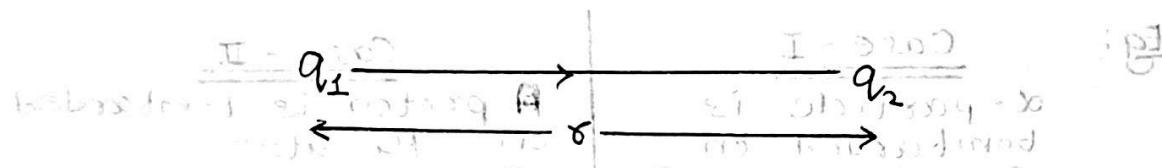
(i) Positive Charge

(ii) Negative Charge

$$e = -1.6 \times 10^{-19} C$$

$$p = +1.6 \times 10^{-19} C$$

→ Charge is a scalar quantity, and the force between the charges acts along the line joining the charges.



The magnitude of the force between the two charges placed at a distance is given by

$$F_E = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

(Electrical force)

$$\frac{1}{4\pi\epsilon_0} = K$$

(constant)

→ Potential energy between 2 charged particles

$$P.E. = \frac{K q_1 q_2}{r}$$

$$K = 9 \times 10^9$$

→ If a charged particle q is placed on a surface of potential V then the potential energy of the charge is qV .

Eg: If a charge q is placed on a surface of potential 5V. Then find P.E.

$$\Rightarrow P.E. = qV = 1.6 \times 10^{-19} \times 5 = 8 \times 10^{-19} CV \text{ Ans}$$

Eg: If α -particle is placed on the surface of potential 10V. Then find P.E.

⇒ α -particle has 2+ charge.

$$\therefore P.E. = qV = 2 \times 1.6 \times 10^{-19} \times 10 = 3.2 \times 10^{-18} CV \text{ Ans}$$

Closest Distance of Approach

- If an α -particle is bombarded towards nucleus of an atom. The minimum distance between α -particle and nucleus is called closest distance of approach.
- Closest distance of approach depends upon magnitude of repulsion.
- If force of repulsion is more, then closest distance of approach is more. If force of repulsion is less, then closest distance of approach is less.
- The force of repulsion depends upon how much charge the bombarded particle have.

Eg:

Case - I

α -particle is bombarded on Au atom.

Here,

$$q_1 q_2 = 158$$

Case - II

A proton is bombarded on Au atom.

Here,

$$q_1 q_2 = 79$$

Thus in case - I force of repulsion is more. Therefore, α -particle has more closest distance of approach.

Note: Force of repulsion jitha kam, particle nucleus ke utha najdik ja sakte hai. And distance of closest approach bhi utha hi kam hogा.

RBI: $q_1 q_2$ more, distance more.

For α -particle

$$d_c = \frac{4KZe^2}{m_\alpha \cdot v_\alpha^2}$$

$$K = 9 \times 10^9$$

z = Atomic no.

e = Charge of $1e^-$

m_α = Mass of α -particle

v_α = Velocity of α -particle

For any other charge particle

$$d_c = \frac{2K(\bar{z}\bar{e})\bar{q}}{mv^2}$$

q = charge on that particle

m = mass of that particle

v = velocity of that particle

Size of the Nucleus

- Radius of atom $\approx 10^{-10}$ m or 10^{-8} cm
- Radius of nucleus $\approx 10^{-15}$ m or 10^{-13} m
- Ratio of volume of nucleus to the volume of atom :

$$\Rightarrow \frac{\text{Vol}^m \text{nucleus}}{\text{Vol}^m \text{atom}} = \frac{\frac{4}{3} \pi r^3}{\frac{4}{3} \pi R^3} = \left(\frac{10^{-15}}{10^{-10}} \right)^3 = (10^{-5})^3$$

$$\Rightarrow 10^{-15}$$

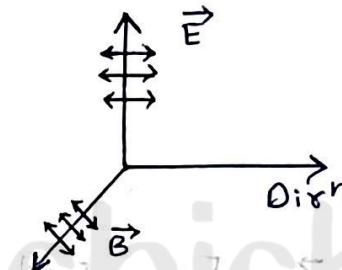
∴ ratio of volume of nucleus to volume of atom is 10^{-15} .

Wave Nature of Electromagnetic Radiation

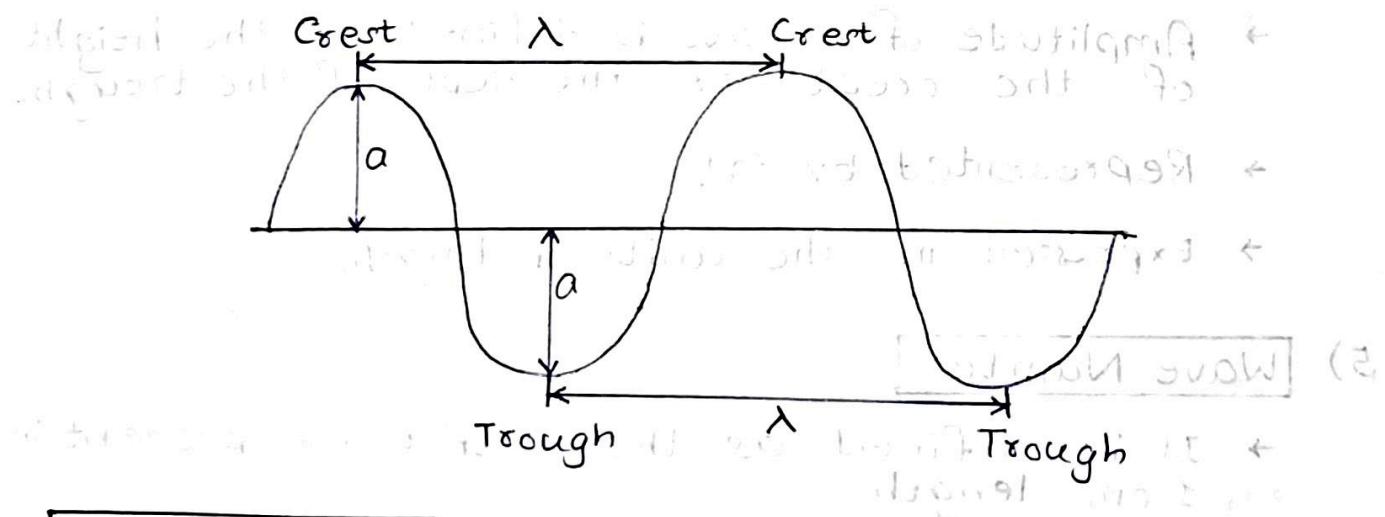
→ EM waves

- Oscillating Magnetic Field = E
 - Oscillating Electric Field = B
 - Direction of Propagation
- All of these are mutually perpendicular to each other.

$$E < B$$



Some important characteristics of a wave:-



1) Wavelength (λ)

→ Wavelength of a wave is defined as the distance between any two consecutive crests or troughs.

→ Unit : $1 \text{ Å} = 10^{-10} \text{ m}$, $1 \text{ pm} = 10^{-12} \text{ m}$, $1 \text{ nm} = 10^{-9} \text{ m}$

2) Frequency (ν)

- Frequency of a wave is defined as the number of waves passing through a point in one second.
- It is represented by ' ν '(nu).
- Unit: Hertz (Hz), sec^{-1}

$$\nu = \frac{C}{\lambda}$$

$$\nu = \frac{1}{T}$$

T = Time Period

3) Velocity

- velocity of a wave is defined as the linear distance travelled by the wave in one second.
- Represented by 'v'.
- Unit: cm/s or m/s (ms^{-1})



$$v = \lambda \nu$$

λ = Wavelength

ν = Frequency.

For EM wave: $v = c = 3 \times 10^8 \text{ m/s}$

So, $c = \lambda \nu$

4) Amplitude

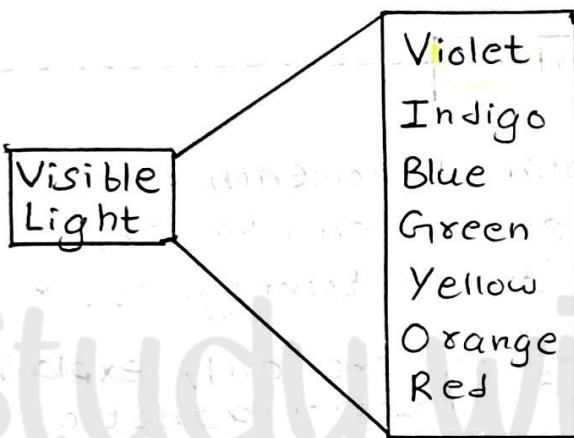
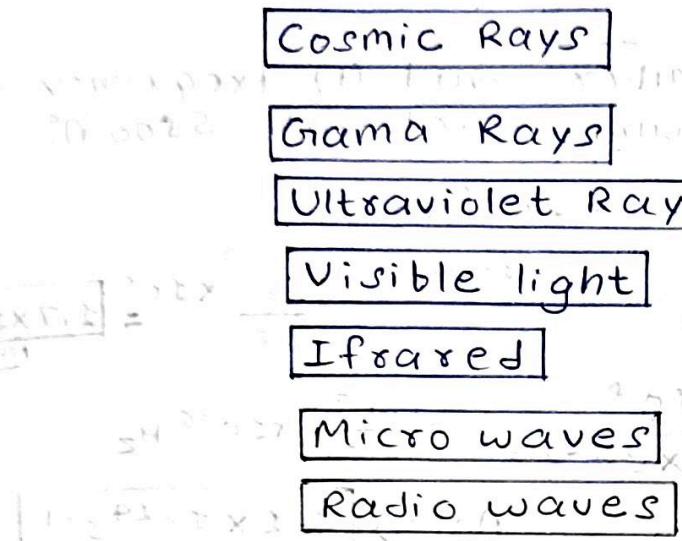
- Amplitude of a wave is defined as the height of the crest or the depth of the trough.
- Represented by 'a'.
- Expressed in the units of length.

5) Wave Number

- It is defined as the no. of waves present in 1 cm length.
- Reciprocal of wavelength.
- Represented by ' $\bar{\nu}$ ' (nu bar).
- Unit: cm^{-1}

$$\bar{\nu} = 1/\lambda$$

Order of wavelength in Electromagnetic Spectrum:



$$\lambda_{\max} = \text{Red}$$

$$\lambda_{\min} = \text{Violet}$$

Since, $v \propto \frac{1}{\lambda}$

$$v_{\max} = \text{Violet}$$

$$v_{\min} = \text{Red}$$

Q.1 The Vividh Bharti station of AIR, Delhi, broadcasts on a frequency of 1368 KHz. Calculate the wavelength of the **radio** radiation emitted by transmitter.

$$\Rightarrow v = 1368 \text{ kHz} = 1368 \times 10^3 \text{ Hz}$$

$$c = v\lambda$$

$$\lambda = \frac{c}{v} = \frac{3 \times 10^8}{1368 \times 10^3} = 219.3 \text{ m}$$

Q.2 The wavelength of the visible spectrum extends from violet (400nm) to red (750nm). Express these wavelengths in frequencies. ($1 \text{ nm} = 10^{-9} \text{ m}$)

$$\Rightarrow \lambda_v = 400 \text{ nm} = 400 \times 10^{-9} \text{ m}$$

$$\lambda_r = 750 \text{ nm} = 750 \times 10^{-9} \text{ m}$$

$$\Rightarrow v_v = \frac{c}{\lambda_v} = \frac{3 \times 10^8}{400 \times 10^{-9}} = 7.5 \times 10^{14} \text{ Hz}$$

Aus

$$\Rightarrow \frac{C}{\lambda} = v_f = \frac{3 \times 10^8}{750 \times 10^{-10}} = 4 \times 10^{24} \text{ Hz}$$

Ans

Q.3 Calculate (a) wavenumber and (b) frequency of yellow radiation having wavelength 5800 Å.

$$\Rightarrow \lambda = 5800 \text{ Å} = 5800 \times 10^{-10} \text{ m}$$

$$(a) \bar{v} = \frac{1}{\lambda} = \frac{1}{5800} \times 10^{-10} = \frac{1}{58} \times 10^6 = 1.7 \times 10^6 \text{ m}^{-1}$$

$$(b) v = \frac{c}{\lambda} = \frac{3 \times 10^8}{5800 \times 10^{-10}} = \frac{3}{58} \times 10^{26} \text{ Hz}$$

$$\underline{\text{Ans}} \Rightarrow [5.1 \times 10^{24} \text{ s}^{-1}]$$

Particle Nature of EM Radiation

- Some of the experimental phenomenon such as diffraction and interference can be explained by the wave nature of electromagnetic radiation.
 - However, some phenomenon are only explained by particle nature of electromagnetic radiation.
- Eg: (i) Black Body Radiation
(ii) Photoelectric Effect

Black Body Radiation

- When solids are heated they emit a wide range of wavelengths.
- The ideal body, which emits and absorbs all frequencies is called a black body.
- The radiation emitted by such a body is called black body radiation.
- The exact frequency distribution of the emitted radiation from a black body depends only on its temperature.

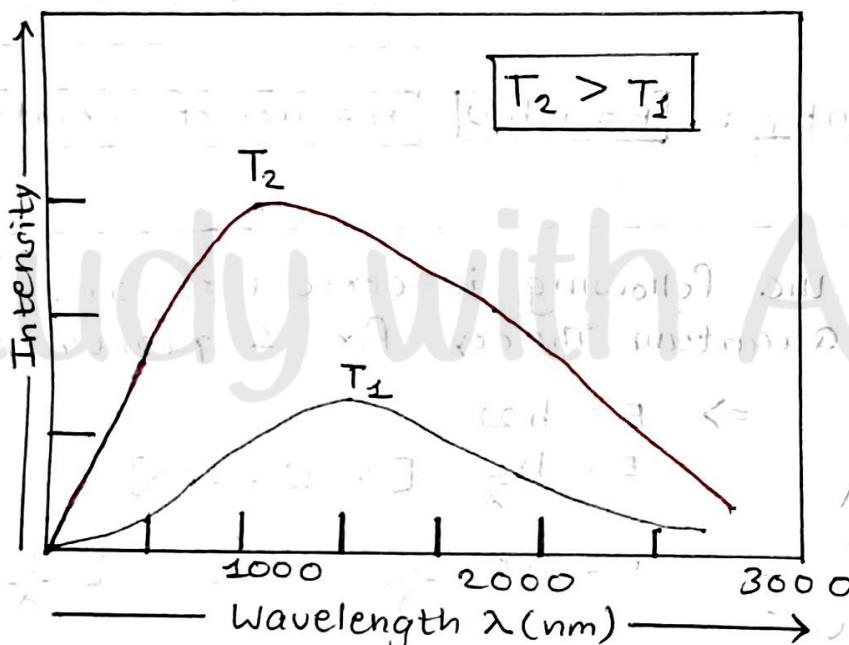
Example : • When an iron rod is heated, it changes its colour on increasing temperature.

Red \rightarrow Orange \rightarrow Yellow \rightarrow Bluish White

Temperature \rightarrow

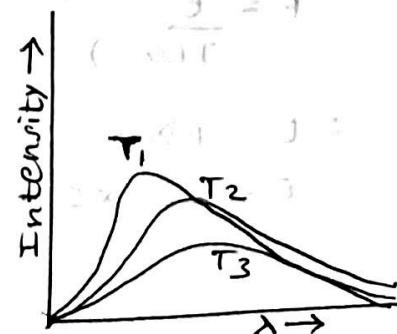
- The change in colour shows that it emits radiations of different frequencies.
- It also emits UV, IR, etc. but our eyes can only detect VIBGYOR.

Wavelength Intensity relationship graph :-



Ques Consider the graph of Black body radiation at 3 different temperatures T_1, T_2, T_3 . Compare T_1, T_2 and T_3 .

- \Rightarrow
- $T_1 < T_2 < T_3$ \times
 - $T_1 = T_2 = T_3$ \times
 - $T_1 > T_3 > T_2$ \times
 - $T_1 > T_2 > T_3$ \checkmark



Plank's Quantum Theory

- Proposed by Max Planck.
- Quanta → Small Packets.
- Transfer of energy is done in quanta (small packets).
- For light, Quanta = Photons

According to Planck's Theory :-

$$h = 6.6 \times 10^{-34}$$

→ The energy of a quanta is directly proportional to the frequency.

→ For 1 quanta : $E \propto \nu$

$$E = h\nu$$

$E =$ Energy

$\nu =$ Frequency

$h =$ Planck's constant

→ For n quanta : $E = nh\nu$

$n =$ no. of quanta

Q.1 Which of the following is correct regarding Planck's Quantum Theory for 1 quanta (MCQ).

(a) $E = h\nu \checkmark \Rightarrow E = h\nu$

(b) $E = hc\nu X \Rightarrow E = hc\frac{\nu}{\lambda} [\because \nu = 1/\lambda]$

(c) $E = \frac{hc}{\lambda} \checkmark \Rightarrow E = h c \times \frac{1}{\lambda} = hc\bar{\nu} = [\because \frac{1}{\lambda} = \bar{\nu}]$

(d) $E = hc\bar{\nu} \checkmark$

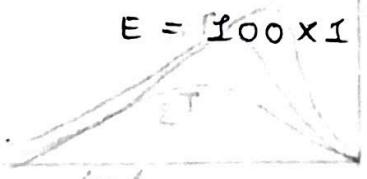
Q.2 Consider 100W Surya bulb emitting yellow light ($\lambda = 500 \text{ nm}$). Find no. of photons emitted by the bulb in 1 sec.?

⇒ Power = Energy emitted per second.

$$P = \frac{E}{T(\text{sec.})}$$

$$\therefore E = P \times t$$

$$E = 100 \times 1 = 100 \text{ J}$$



$$\Rightarrow E = nh\frac{c}{\lambda}$$

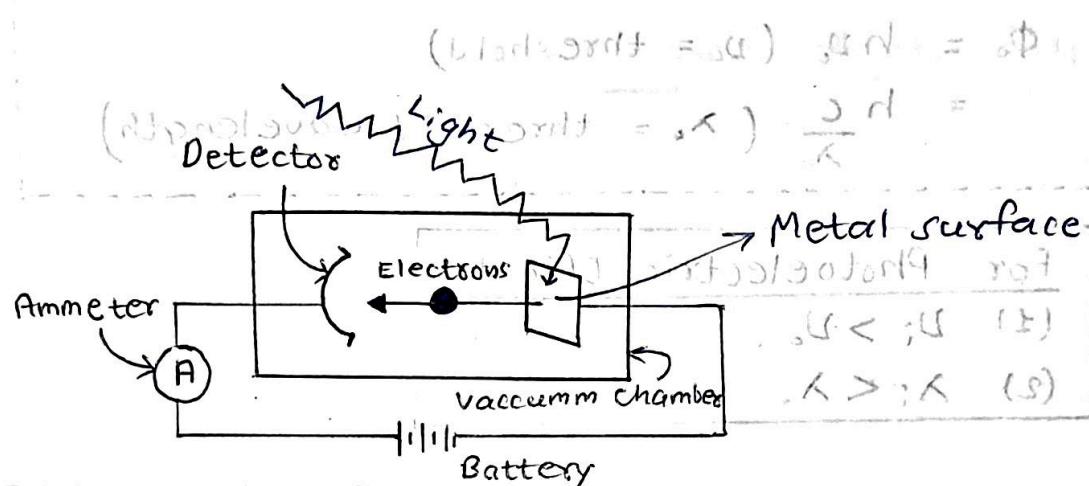
$$100 = n \times \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{500 \times 10^{-9}}$$

$$n = \frac{5 \times 10^4 \times 10^{-9}}{6.6 \times 3 \times 10^{-26}} = \frac{5}{20} \times 10^{20}$$

$$\text{Ans} \Rightarrow 2.5 \times 10^{20} \text{ photons}$$

Photo Electric Effect

- When monochromatic light fall (incident) on metal surface and e^- is ejected from the metal surface, this phenomena is called photoelectric effect.
- Monochromatic \rightarrow Single frequency wali light.



Results observed in this experiment were:-

- The electrons are ejected from the metal surface as soon as the beam of light strike on the surface.
- The no. of electrons ejected is proportional to the intensity or brightness of light.
- For each metal, there is a characteristic minimum frequency, v_0 (threshold frequency) below which photo electric effect is not observed. At a frequency $v > v_0$, ejected electrons come out with certain kinetic energy. The kinetic energies of these electrons increase with the increase of frequency of the light used.

Albert Einstein Equation :-

$$E_i = \Phi_0 + KE_{max}$$

E_i = Energy of incident radiation

Φ_0 = Work function of metal

KE_{max} = Maximum kinetic energy of photo e⁻

$$\Rightarrow E_i = \Phi_0 + (\text{KE})_{\text{max}}$$

$$h\nu_i = (\Phi_0 + \frac{1}{2}m_e v_e^2)$$

ν_i = frequency of incident radiation

m_e = mass of e^-

v_e = velocity of e^-

$$\Phi_0 = h\nu_0 \quad (\nu_0 = \text{threshold})$$

$$= \frac{hc}{\lambda_0} \quad (\lambda_0 = \text{threshold wavelength})$$

For Photoelectric Effect:

$$(1) \nu_i > \nu_0$$

$$(2) \lambda_i < \lambda_0$$

Threshold Energy (Φ_0): Minimum energy required to eject a photo electron from metal surface.

In case if, $E_i = \Phi_0$, Then $\text{KE} = 0$.

Threshold Frequency (ν_0): The frequency corresponding to threshold energy.

$$\nu_0 = \frac{\Phi_0}{h}$$

If $\nu_i < \nu_0$, then photo electric effect doesn't occur.

Threshold Wavelength (λ_0): The wavelength corresponding to Φ_0 .

$$\Rightarrow \lambda_0 = \frac{hc}{\Phi_0}$$

$$\lambda_0 = \frac{hc}{\Phi_0}$$

If $\lambda_i < \lambda_0$, then photo electric effect occurs.

1 ev: Energy of electron accelerated under potential difference of 1 volt.

$$\Rightarrow KE = qV \\ = 1.6 \times 10^{-19} \times 1V \\ \therefore 1 \text{ ev} = 1.6 \times 10^{-19} \text{ J}$$

Q.1 If ϕ_0 of metal is 4.5 ev. Which of the following photons will emit photo e-?

\Rightarrow (i) $E_i = 5.0 \text{ ev}$

(ii) $E_i = 1.6 \times 10^{-19} \text{ J}$

(iii) $E_i = 4 \times 10^{-18} \text{ J}$

(iv) $E_i = 4.8 \text{ ev}$

\Rightarrow (i) $E_i > \phi_0$. It emit photo e-.

(ii) $E_i = 1.6 \times 10^{-19} \text{ J}$

$$= \frac{1.6 \times 10^{-19}}{1.6 \times 10^{-19}} \text{ ev} = 1 \text{ ev} > 4.5 \text{ ev}$$

\Rightarrow It emit photo e-

(iii) $E_i = 4 \times 10^{-18}$

$$= \frac{4 \times 10^{-18}}{1.6 \times 10^{-19}} \text{ ev} = 0.425 \text{ ev} > 4.5 \text{ ev}$$

\Rightarrow It emit photo e-

(iv) $E_i = 4.8 \text{ ev} > 4.5 \text{ ev}$. It emit photo e-

Q.2 Fill in the blanks :-

S.No.	ν_i	E_i	ϕ_0	PEE	$(KE)_{\max}$	$(Velocity)_{e^-}$
1	300 kHz	$19.8 \times 10^{-29} \text{ J}$	5 ev	X	X	X
2	500 kHz	$33 \times 10^{-29} \text{ J}$	5 ev	X	X	X
3	700 kHz	$46.2 \times 10^{-29} \text{ J}$	5 ev	X	X	X
4	1000 kHz	$6.6 \times 10^{-28} \text{ J}$	5 ev	X	X	X

(1) $\nu_i = 300 \text{ kHz}$
 $= 3 \times 10^5 \text{ Hz}$

$$E_i = h\nu_i \\ = 6.6 \times 10^{-34} \times 3 \times 10^5 \\ = 19.8 \times 10^{-29} \text{ J}$$

(2) $\nu_i = 500 \text{ kHz}$
 $= 5 \times 10^5 \text{ Hz}$

$$E_i = h\nu_i \\ = 6.6 \times 10^{-34} \times 5 \times 10^5 \\ = 33 \times 10^{-29} \text{ J}$$

$$(3) \nu_i = 700 \text{ kHz} \\ = 7 \times 10^5 \text{ Hz}$$

$$E_i = h\nu_i \\ = 6.6 \times 10^{-34} \times 7 \times 10^5 \\ = 46.2 \times 10^{-29} \text{ J}$$

$$(4) \nu_i = 1000 \text{ kHz}$$

$$= 10^6 \text{ Hz}$$

$$E_i = h\nu_i \\ = 6.6 \times 10^{-34} \times 10^6 \\ = 6.6 \times 10^{-28} \text{ J}$$

Various Forms of PEE equation :-

$$1) E_i = \Phi_0 + (KE)_{max}$$

$$2) h\nu_i = h\nu_0 + (KE)_{max}$$

$$3) h\nu_i = \Phi_0 + (KE)_{max}$$

$$4) h\nu_i = h\nu_0 + \frac{1}{2}mv^2$$

$$5) \frac{hc}{\lambda_i} = \frac{hc}{\lambda_0} + \frac{1}{2}mv^2$$

Q.3

$$\lambda_1 = 400 \text{ nm}$$

$$\lambda_2 = 500 \text{ nm}$$

$$\Rightarrow E_i = E_2 + E_3$$

$$\lambda_3 = ?$$

$$\frac{hc}{\lambda_i} = \frac{hc}{\lambda_2} + \frac{hc}{\lambda_3}$$

$$\frac{1}{\lambda_1} = \frac{1}{\lambda_2} + \frac{1}{\lambda_3}$$

$$\frac{1}{400} = \frac{1}{500} + \frac{1}{\lambda_3}$$

$$\frac{1}{\lambda_3} = \frac{1}{400} - \frac{1}{500}$$

$$\frac{1}{\lambda_3} = \frac{500 - 400}{400 \times 500}$$

$$\frac{1}{\lambda_3} = \frac{1}{2000} \Rightarrow \lambda_3 = 2000 \text{ nm}$$

$$2000 \text{ nm} = 2 \times 10^{-7} \text{ m}$$

$$= 2 \times 10^8 \text{ Hz}$$

$$E_i = h\nu_i \\ = 6.6 \times 10^{-34} \times 2 \times 10^8 \\ = 1.32 \times 10^{-25} \text{ J}$$

Important Points regarding Photoelectric Effect :-

- 1) No. of photo electrons depends upon intensity. And is independent of (E_i , ν_i or λ_i).
- 2) $(KE)_{\max}$ of photo electrons depends upon (E_i , ν_i or λ_i) and is independent of intensity.
- 3) Graph between ν_i and KE_{\max} :-

$$\text{Eqn} \Rightarrow h\nu_i = h\nu_0 + (KE)_{\max}$$

$$\Rightarrow (KE)_{\max} = h\nu_i - h\nu_0$$

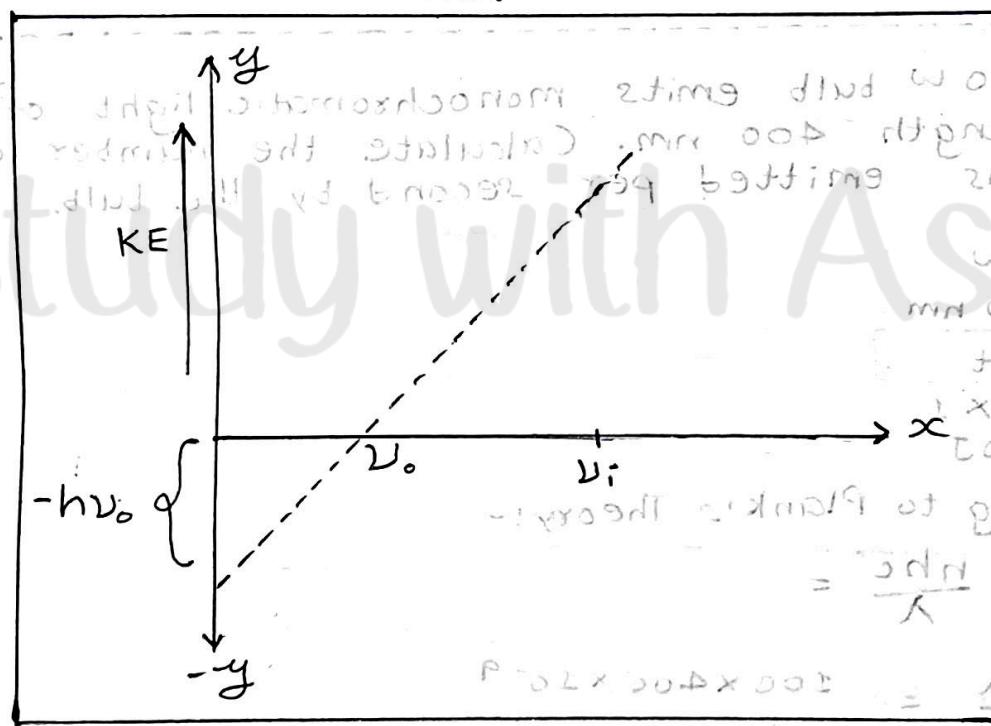
Comparing with $y = mx + c$

$$y = (KE)_{\max}$$

$$m = \text{slope} = h \text{ (Planck's constant)}$$

$$x = \nu_i$$

$$c = -h\nu_0$$



- Q.1** The threshold frequency ν_0 for a metal is $6 \times 10^{14} \text{ s}^{-1}$. Calculate the kinetic energy of an electron emitted when radiation of frequency $\nu_i = 1.1 \times 10^{15} \text{ s}^{-1}$ hits the metal.

$$\Rightarrow \nu_i = 1.1 \times 10^{15} \text{ Hz} = 1.1 \times 10^{14} \text{ Hz}$$

$$\nu_0 = 6 \times 10^{14} \text{ Hz} \Rightarrow (KE)_{\max} = h(1.1 \times 10^{14} - 6 \times 10^{14})$$

$$\Rightarrow h\nu_i = h\nu_0 + (KE)_{\max}$$

$$(KE)_{\max} = h\nu_i - h\nu_0$$

$$\text{so } (KE)_{\max} = h(\nu_i - \nu_0)$$

$$\Rightarrow (KE)_{\max} = h(1.1 \times 10^{14} - 6 \times 10^{14})$$

$$= 1.6 \times 10^{-34} \times 5 \times 10^{14}$$

$$= 3.3 \times 10^{-20} \text{ J}$$

$$\text{The answer} = 3.3 \times 10^{-19} \text{ J} \quad \text{Ans}$$

Q.2 When electromagnetic radiation of wavelength 310 nm fall on the surface of Sodium, electrons are emitted with KE = 1.5 eV. Determine the work function (Φ_0) of sodium.

$$\Rightarrow KE = 1.5 \text{ eV} \quad (\text{1 eV} = 1.6 \times 10^{-19} \text{ J})$$

$$KE = 1.5 \times 1.6 \times 10^{-19} \text{ J} = 2.4 \times 10^{-19} \text{ J}$$

$$\Rightarrow \lambda_i = 310 \text{ nm} = 310 \times 10^{-9} \text{ m}$$

$$E_i = \frac{hc}{\lambda_i} = \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{310 \times 10^{-9}} = 6.6 \times 10^{-19} \text{ J}$$

$$\Rightarrow E_i = \Phi_0 + (KE)_{\max}$$

$$\Phi_0 = E_i - (KE)_{\max}$$

$$= 6.6 \times 10^{-19} - 2.4 \times 10^{-19}$$

$$= 4.2 \times 10^{-19} \text{ J} \quad \boxed{\text{Ans}}$$

Q.3 A 100W bulb emits monochromatic light of wavelength 400 nm. Calculate the number of photons emitted per second by the bulb.

$$\Rightarrow P = 100 \text{ W}$$

$$\lambda = 400 \text{ nm}$$

$$E = P \times t$$

$$= 100 \times 1$$

$$\Rightarrow 100 \text{ J}$$

\Rightarrow According to Plank's Theory:-

$$E = \frac{nhc}{\lambda}$$

$$\Rightarrow n = \frac{E \lambda}{hc} = \frac{100 \times 400 \times 10^{-9}}{19.8 \times 10^{-26}}$$

$$= \frac{4 \times 10^{21}}{19.8}$$

$$= 0.2 \times 10^{21}$$

$$\boxed{\text{Ans} \Rightarrow 2 \times 10^{20} \text{ photons}}$$

Q.4 When em radiation of $\lambda = 30 \text{ nm}$ falls on the surface of sodium, electrons are emitted with a KE of $1.68 \times 10^5 \text{ J mol}^{-1}$. What is the minimum energy needed to remove an electron from sodium? What is the maximum wavelength will cause a photo electron to be emitted?

$$\Rightarrow \lambda_i = 300 \text{ nm}$$

$$KE = 1.68 \times 10^5 \text{ J/mol}$$

$$KE \text{ of } 1e^- = \frac{1.68 \times 10^5}{NA} \text{ J}$$

$$\Phi_0 = ?$$

$$\Rightarrow E_i = \Phi_0 + (KE)_{\max}$$

$$\frac{hc}{\lambda_i} = \Phi_0 + \frac{1.68 \times 10^5}{6 \times 10^{23}}$$

$$\frac{6.6 \times 10^{-34} \times 3 \times 10^8}{300 \times 10^{-9}} = \Phi_0 + \frac{1.68 \times 10^5}{6 \times 10^{23}}$$

$$6.6 \times 10^{-19} - \frac{1.68}{6} \times 10^{-19} = \Phi_0$$

$$\Phi_0 = \left(6.6 - \frac{1.68}{6}\right) 10^{-19} = \boxed{3.8 \times 10^{-19}} \text{ Ans}$$

$$\Rightarrow \Phi_0 = \frac{hc}{\lambda_0}$$

$$\Rightarrow \lambda_0 = \frac{hc}{\Phi_0} = \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{3.8 \times 10^{-19}}$$

$$= \frac{6.6 \times 3 \times 10^{-7}}{3.8} = \boxed{5.2 \times 10^{-7} \text{ nm}} \text{ Ans}$$

Bohr's Atomic Model

→ The electrons revolve around the nucleus with high velocities in certain fixed orbits, called levels.

→ There are two forces acting on it. Electrostatic force of nucleus, which provides centripetal force.

→ It's magnitude is equal to ze^2/r^2 , where z = atomic number, e = electronic charge,

r = radius of orbit.

Important Postulates :-

- 1) Atom has a nucleus where all protons and neutrons are present. The size of nucleus is very small and it is present at the centre of the atom.
- 2) -vely charged electrons revolve around the nucleus in circular orbits. The attraction force between nucleus and electron is equal to the centrifugal force on electron.

Coulomb force

$$F_c = \frac{kq_1q_2}{r^2} = \frac{k(ze)(e)}{r^2} = \frac{kZe^2}{r^2}$$

In circular motion

$$F_c = \frac{mv^2}{r^2}$$

$$\therefore \boxed{\frac{kZe^2}{r^2} = \frac{mv^2}{r^2}} \quad \text{(i)}$$

- 3) Electrons can revolve only in those orbits in which angular momentum ($mv\tau$) of electron is integral multiple of $h/2\pi$.

$$\boxed{\frac{h}{2\pi}, \frac{2h}{2\pi}, \frac{3h}{2\pi}, \frac{4h}{4\pi}}$$

$$\boxed{mv\tau = nh/2\pi} \quad \text{... (ii)}$$

m = mass of e^-
 v = velocity of e^-
 τ = distance b/w
nucleus & e^-

$n \in N$

- 4) The orbit in which electron can revolve is known as stationary orbit because in these orbits energy of electron is always constant.

- 5) Each stationary orbit is associated with definite amount of energy. Therefore, these orbits are also called as energy levels and are numbered as (1, 2, 3, 4, 5, ...) or (K, L, M, N, O, ...) from nucleus onwards.

$$\boxed{\text{Max no. of } e^- \text{ in an orbit} = 2n^2}$$

Where, $n = \text{no. of orbit}$

Eg: Max no. of e^- in N shell.

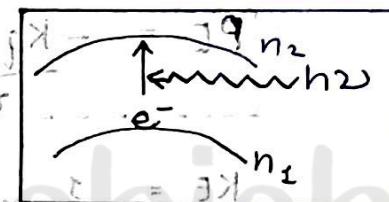
For N, $n = 4$

$$e^-_{\text{max}} = 2 \times 4^2 = \boxed{32}$$

- 6) The emission or absorption of energy in the form of photon can only occur when electron jumps from one stationary state to another.

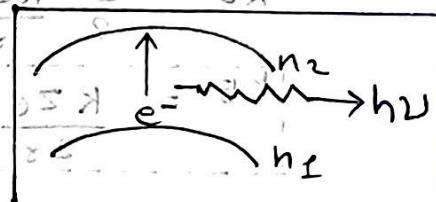
If electron jumps in higher orbit then it absorb energy.

$$(E_{n_2} - E_{n_1}) = h\nu$$



If electron jumps in lower orbit then it emit energy.

$$E_{n_2} - E_{n_1} = h\nu$$



Finding values of r , v and E :

- 1) For 'v' (velocity) of electron in n^{th} shell

$$\frac{KZe^2}{r^2} = \frac{mv^2}{r} \quad \dots (i)$$

$$mv^2 = nh/2\pi \quad \dots (ii)$$

Eqn - 1 :-

$$\frac{KZe^2}{r^2} = \frac{mv^2}{r}$$

$$KZe^2 = mv^2 r$$

$$KZe^2 = (mvr)v$$

Putting value of $mvr = nh/2\pi$ from eqn - 2

$$KZe^2 = \frac{nh}{2\pi} \cdot v$$

$$V_n = \frac{KZe^2 \times 2\pi}{nh}$$

$$V_n = \frac{2\pi K e^2}{h} \times \frac{Z}{n}$$

$$V_n = 2.188 \times \frac{Z}{n} \times 10^8 \text{ m/s}$$

2) For 'r' (distance b/w nucleus & electron)

$$V = \frac{2\pi k e^2}{h} \times \frac{z}{n} \quad \dots (i)$$

$$mv\gamma = \frac{nh}{2\pi} \quad \dots (ii)$$

Putting value of 'v' from eqn 1 :-

$$r = \frac{nh \times hn}{2\pi m \times 2\pi k e^2 z}$$

From eqn 2 :-

$$mv\gamma = \frac{nh}{2\pi}$$

$$r = \frac{nh}{2\pi \times mv}$$

$$r = \frac{h^2}{4\pi^2 k e^2 z}$$

$$r_n = 0.529 \frac{n^2}{z} \text{ Å}$$

$$r_n \propto n^2/z$$

3) For 'E_n' (energy of electron in Bohr orbit)

$$PE = -\frac{kq_1 q_2}{r} = -\frac{kze^2}{r}$$

$$KE = \frac{1}{2} mu^2$$

$$KE = \frac{1}{2} \frac{kze^2}{r} \left[\because \frac{mu^2}{r} = \frac{kze^2}{r^2} \right]$$

$$KE = \frac{kze^2}{2r}$$

$$Total Energy = KE + PE$$

$$KE = \frac{kze^2}{2r} \quad \dots (i)$$

$$PE = -\frac{kze^2}{r}$$

$$TE = \frac{kze^2}{2r} + \left(-\frac{2kze^2}{r} \right) = \frac{kze^2 - 2(kze^2)}{2r} = -\frac{kze^2}{2r}$$

$$E_n = -13.6 \cdot \frac{z^2}{n^2} \text{ ev/atom}$$

$$E_n = -1312 \cdot \frac{z^2}{n^2} \text{ KJ/mol}$$

$$E_n = -313.6 \cdot \frac{z^2}{n^2} \text{ kcal/mol}$$

Q.1 Find the energy of 1st and 2nd orbit of He⁺ ion.

\Rightarrow He⁺ ($z = 2$)

$$E_1 = -13.6 \times \frac{2^2}{1^2} = -13.6 \times 4 = \boxed{-54.4 \text{ eV}}$$

$$E_2 = -13.6 \times \frac{2^2}{2^2} = \boxed{-13.6 \text{ eV}}$$

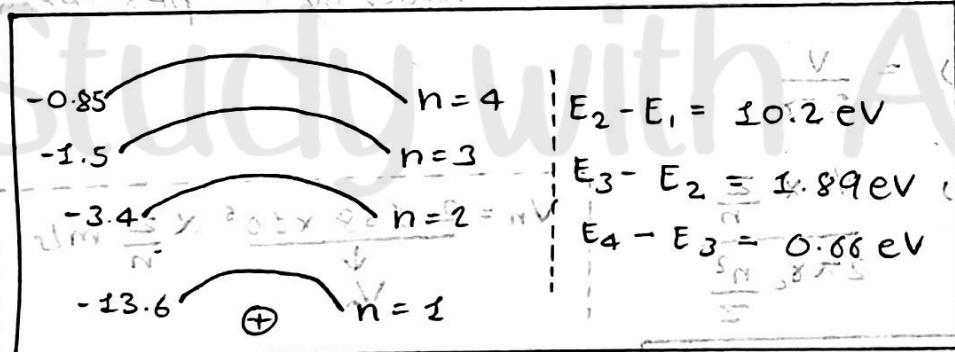
Q.2 Find the energy of first 4 orbits of H-atom.

$$\Rightarrow E_1 = \left[\frac{-13.6 \times 1^2}{1^2} + \frac{-13.6 \times 1^2}{2^2} \right] = -13.6 \text{ eV}$$

$$E_2 = -13.6 \times \frac{1^2}{2^2} = -13.6 \times \frac{1}{4} = \boxed{-3.4 \text{ eV}}$$

$$E_3 = -13.6 \times \frac{1^2}{3^2} = -13.6 \times \frac{1}{9} = \boxed{-1.5 \text{ eV}}$$

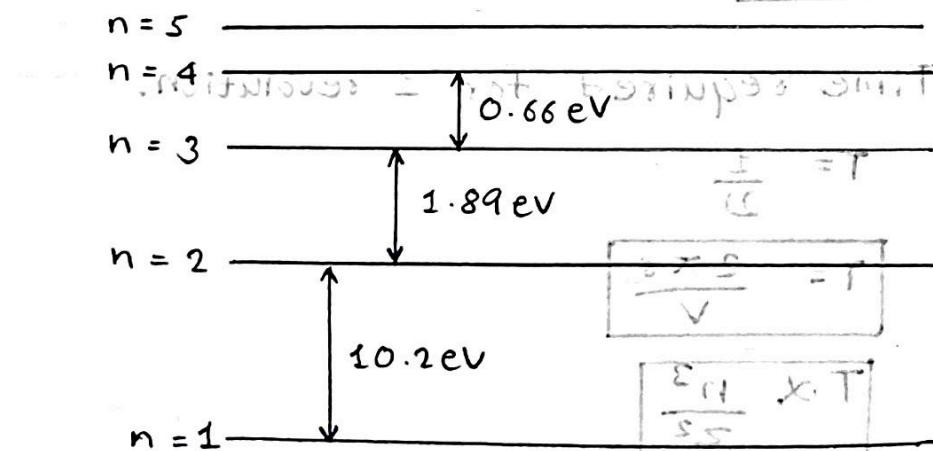
$$E_4 = -13.6 \times \frac{1^2}{4^2} = -13.6 \times \frac{1}{16} = \boxed{-0.85 \text{ eV}}$$



$$A \frac{Z^2 \times R^2 Z^2}{S^2} = n^6$$

$$\frac{Z^2}{S^2} \times \frac{R^2}{Z^2} = 16$$

H - atom



Bohr's model
Decreasing distance between orbits

Energy distance between two orbits

$$E_{n_1} = -13.6 \times \frac{Z^2}{n_1^2} \quad \dots (i) \quad (S=S) \quad \text{V9P.12-1}$$

$$E_{n_2} = -13.6 \times \frac{Z^2}{n_2^2} \quad \dots (ii) \quad \text{V9P.12-1} = \frac{S_S \times Z \cdot E_L}{S_L} = S_S$$

$$\Delta E_n = E_{n_2} - E_{n_1} = -13.6 \times \frac{Z^2}{n_2^2} - \left(-13.6 \times \frac{Z^2}{n_1^2} \right)$$

$$\Delta E_n = V_9 \frac{13.6 \times Z^2}{n_2^2} \left[\frac{1}{n_2^2} - \frac{1}{n_1^2} \right] = S_S$$

$$\Delta E_{n_2} = 13.6 \times Z^2 \left[\frac{1}{n_2^2} - \frac{1}{n_1^2} \right] = S_S$$

Frequency and Time period of Revolution :-

Frequency : Number of revolution made by e^- per second.

$$\nu = \frac{V}{2\pi r} = 1.5 \times 10^6 \text{ Hz} \quad (r = R)$$

$$\nu = V_0 \times \frac{Z}{n} \quad \text{V}_0 = \frac{2.188 \times 10^6 \times Z}{n} \text{ m/s}$$

$$\nu = \frac{V_0}{2\pi r_0} \times \frac{Z^2}{n^3}$$

$$r_n = \frac{0.529 \times n^2}{Z} \text{ Å}$$

$$\nu \propto \frac{Z^2}{n^3}$$

Time period

Time required for 1 revolution.

$$T = \frac{1}{\nu}$$

$$T = \frac{2\pi r}{V}$$

$$T \propto \frac{n^3}{Z^2}$$

Q.1 Find the ratio of time period of an e^- for 2nd orbit of He^+ to 4th orbit of Li^{2+} .

$\Rightarrow \text{He}^+ [z_1 = 2] \quad [n_1 = 2]$

$\text{Li}^{2+} [z_2 = 3] \quad [n_2 = 4]$

$T_{\text{He}^+} = \frac{n_1^3}{z_1^2} \times T_{\text{Li}^{2+}}$

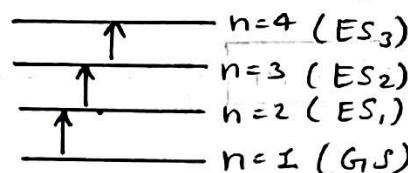
$T_{\text{Li}^{2+}} \times \frac{(2)^3}{z_1^2} = \frac{(2)^3 \times 3^2}{2^2 \times (4)^3} = \frac{9}{32} = \boxed{9 : 32}$

Ans

Few Important Definitions (Single e^- -species) :-

1) **Ground State**: $n = 1$ (First orbit).

2) **Excited State**: Orbit other than $n = 1$, i.e., $n = 2, 3, \dots$



$$\text{no. of ES} = n - 1$$

3) **Ionisation Energy**: Energy required to move an e^- from ground state ($n = 1$) to $n = \infty$.

$$\# n_1 = 1, n_2 = \infty$$

$$\Delta E = IE = 13.6 \times z^2 \left[\frac{1}{1^2} - \frac{1}{\infty^2} \right]$$

$$\therefore IE = 13.6 \times z^2 \text{ eV} \quad [\because 1/\infty^2 = 0]$$

Eg: (i) H-atom = $13.6 \times 1^2 \Rightarrow 13.6 \text{ eV}$

(ii) $\text{He}^+ = 13.6 \times 2^2 \Rightarrow 54.4 \text{ eV}$

(iii) $\text{Li}^{2+} = 13.6 \times 3^2 \Rightarrow 122.4 \text{ eV}$

4) **Excitation Energy**: Energy required to move an e^- from GS ($n_1 = 1$) to any excited state (n_2).

$$\Delta E_n = EE = 13.6 \times z^2 \left[\frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$

$$EE = 13.6 \times z^2 \left(1 - \frac{1}{n_2^2} \right) \text{ eV/atom}$$

Eg: EE of He^+ ion if e^- transits from GS to 6th ES.

$$z = 2, n_1 = 1, n_2 = 7$$

$$\Rightarrow \Delta E = 13.6 \times 2^2 \left(1 - \frac{1}{49} \right)$$

$$= 13.6 \times 4 \left(\frac{48}{49} \right) \approx 53.3 \text{ eV}$$

Ans

5) Separation or Binding Energy :-

Energy required to move an e^- from n_1 (any excited state) to $n_2 = \infty$.

$$SE = \Delta E_n = 13.6 \times Z^2 \left[\frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$

$$SE = 13.6 \times Z^2 \left(\frac{1}{n_1^2} - 0 \right) \quad \because \left(\frac{1}{\infty^2} = 0 \right)$$

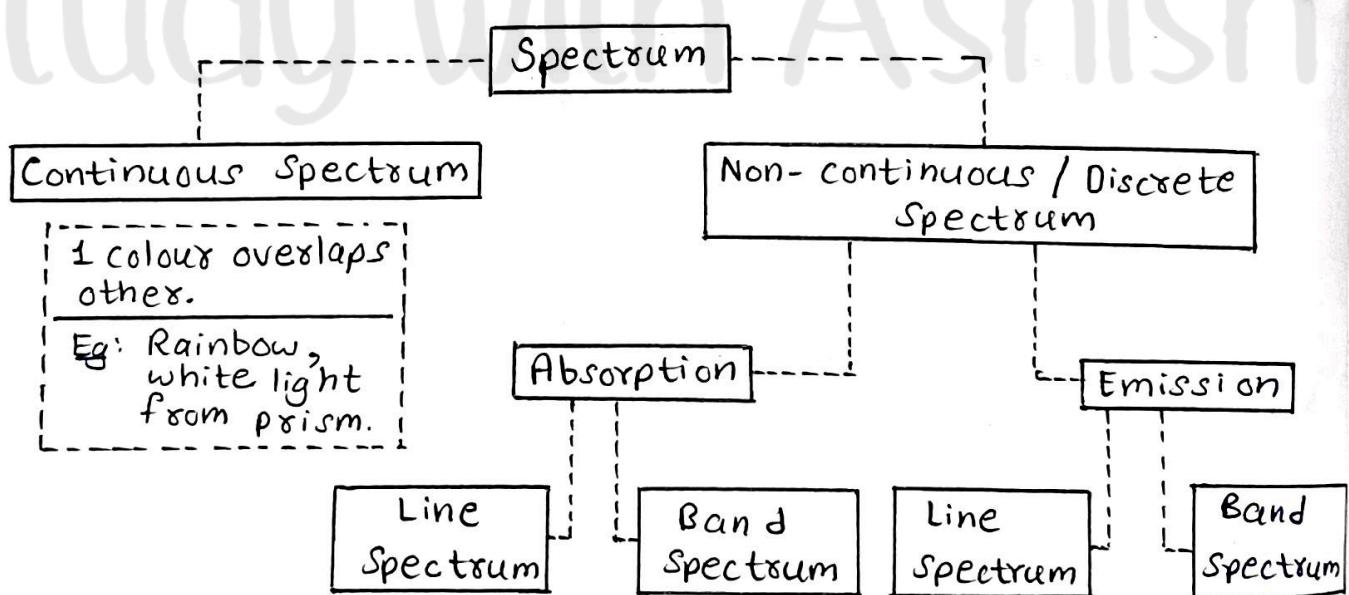
$$\therefore SE = 13.6 \times \frac{Z^2}{n_1^2}$$

Eg: SE for 3rd ES of He^+

$$\Rightarrow Z = 2 \\ n_1 = 4$$

$$\Rightarrow SE = 13.6 \times \frac{2^2}{4^2} = 13.6 \times \frac{4}{16} = \frac{13.6}{4} = \boxed{3.4 \text{ eV atom}}$$

Types of Spectrum



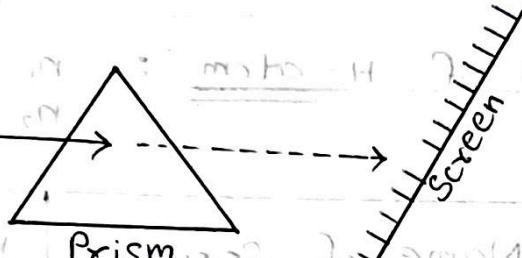
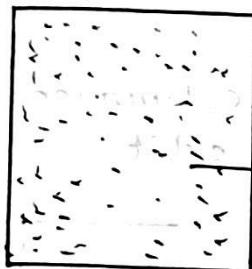
- Absorption : e^- jumps to higher orbit (absorbs light).
- Emission : e^- goes back to lower orbit (emits light).

In our syllabus : Non Continuous \rightarrow Emission \rightarrow Line Spectrum

Emission Spectrum of H-atom

- Spectrum of any atom is always line spectrum.
- Emission spectrum means transition of e- from higher orbit to lower orbit.

Sample of H-atom
(excited)



- Suppose that there is a sample of H-atoms (excited state) (energy ↑). High energy means e- is in any other orbit other than $n=1$. If we stop giving energy to the electron, it jumps in lower orbit and emits photon. And this photon can be observed by placing a prism. The photons are observed as line spectrum on the screen. So this is called line spectrum of H-atom.

Note 1

Jab tak electron ko energy mil rahi hai tab tak of excited state me raha. Jab energy milna band hoga tab electron lower orbit me de-excite de-excite hoga aur photon emit karega.

Note 2

Spectrum kisi atom ka fingerprint hota hai.

Rydberg Formula :-

$$\Delta E_n = 13.6 \times z^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) \dots \textcircled{1}$$

From Plank's Theorem :-

$$\text{Energy of a photon} = h\nu = \frac{hc}{\lambda}$$

$$\Delta E_n = \frac{hc}{\lambda} \dots \textcircled{2}$$

From eqn $\textcircled{1}$ and $\textcircled{2}$:-

$$\frac{hc}{\lambda} = 13.6 \times z^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

$$\frac{1}{\lambda} = \frac{13.6}{hc} \times z^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

$$\frac{1}{\lambda} = R z^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) = \Sigma$$

$$\therefore \text{Rydberg Formula} \Rightarrow \frac{1}{\lambda} = RZ^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

$$R = \text{Rydberg constant} = 109678 \text{ cm}^{-1} = 109700 \text{ cm}^{-1}$$

$$= 10970000 \text{ m}^{-1} = 1.1 \times 10^7 \text{ m}^{-1}$$

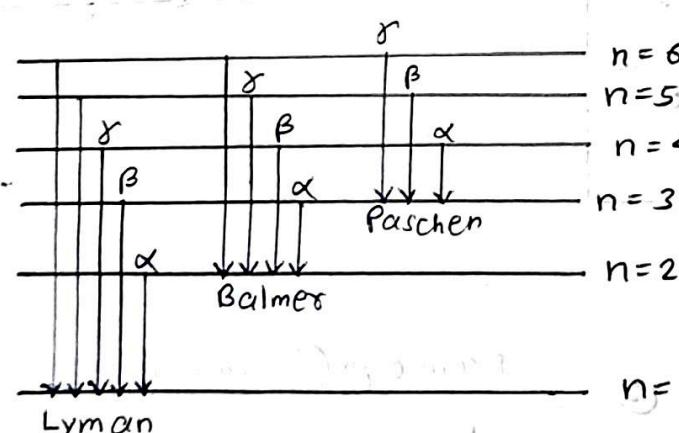
$$\frac{1}{R} = 9.12 \times 10^{-6} \text{ cm} = 912 \text{ Å}$$

Spectrum of H-atom : n_1 = final destination
 n_2 = initial orbit

No.	Name of Series	n_1	n_2	Type
1	Lyman Series	1	2, 3, 4, 5, ...	UV
2	Balmer series	2	3, 4, 5, ...	Visible
3	Paschen Series	3	4, 5, 6, ...	IR
4	Brakett Series	4	5, 6, 7, ...	IR
5	Pfund Series	5	6, 7, 8, ...	IR
6	Humphrey Series	6	7, 8, 9, ...	IR

Terms :-

- 1) α line = nearest transition (1st line) \rightarrow Lyman
- 2) β line = 2nd line \rightarrow Balmer
- 3) γ line = 3rd line \rightarrow Paschen
- 4) δ line = 4th line \rightarrow Brakett
- 5) ϵ line = 5th line \rightarrow Pfund
- 6) ζ line = 6th line \rightarrow Humphrey



Max. energy = min. $\lambda = \alpha \rightarrow n_1$
 Min. energy = $\lambda_{\max} = \alpha$ line

$$n = 1 \left(\frac{1}{\lambda_1^2} - \frac{1}{\lambda_2^2} \right)^{-1} \approx 1.181 \times 10^4$$

$$\left(\frac{1}{\lambda_1^2} - \frac{1}{\lambda_2^2} \right)^{-1} = \frac{1}{\lambda}$$

$$\frac{1}{\lambda} = \left(\frac{1}{\lambda_1^2} - \frac{1}{\lambda_2^2} \right)^{-1} = \frac{\lambda}{\lambda_1^2 - \lambda_2^2}$$

1) Lyman Series

Transition ($n_2 \rightarrow n_1$)

$$n_1 = 1$$

$$n_2 = 2, 3, 4, \dots$$

Ryd. Formula :

$$\frac{1}{\lambda} = R Z^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

λ for α line :-

$$n_1 = 1, n_2 = 2$$

$$\frac{1}{\lambda} = R \times 1^2 \left(\frac{1}{1^2} - \frac{1}{2^2} \right)$$

$$\frac{1}{\lambda} = R \left(\frac{4-1}{4} \right)$$

$$\frac{1}{\lambda} = \frac{3R}{4}$$

$$\therefore \lambda_{\alpha} = \frac{4}{3R}$$

λ for β line :-

$$n_1 = 1, n_2 = 3$$

$$\frac{1}{\lambda} = R \times 1^2 \left(\frac{1}{1^2} - \frac{1}{3^2} \right)$$

$$\frac{1}{\lambda} = R \times \frac{8}{9}$$

$$\therefore \lambda_{\beta} = \frac{9}{8R}$$

λ for γ line :-

$$n_1 = 1, n_2 = 4$$

$$\frac{1}{\lambda} = R \times 1^2 \left(\frac{1}{1^2} - \frac{1}{4^2} \right)$$

$$\frac{1}{\lambda} = R \times \frac{15}{16}$$

$$\therefore \lambda_{\gamma} = \frac{16}{15R}$$

λ maximum :-

$\lambda_{\text{max}} = \text{energy}_{\text{min.}} = \alpha\text{-line}$

$$n_1 = 1, n_2 = 2$$

$$\therefore \lambda_{\text{max}} = \frac{4}{3R} \text{ (solved above)}$$

λ_{minimum} :-

$\lambda_{\text{min.}} = \text{energy}_{\text{max.}} = \infty \rightarrow n_1$

$$n_1 = 1, n_2 = \infty$$

$$\frac{1}{\lambda} = R \times 1^2 \left(\frac{1}{1^2} - \frac{1}{\infty^2} \right)$$

$$\frac{1}{\lambda} = R (1-0)$$

$$\therefore \lambda_{\text{min.}} = \frac{1}{R}$$

2) Balmer Series

$$n_1 = 2$$

$$n_2 = 3, 4, 5, \dots$$

Ryd. Formula :

$$\frac{1}{\lambda} = R Z^2 \left(\frac{1}{2^2} - \frac{1}{n_2^2} \right)$$

λ for α line :-

$$n_1 = 2, n_2 = 3$$

$$\frac{1}{\lambda} = R \times 1^2 \left(\frac{1}{4} - \frac{1}{9} \right)$$

$$\frac{1}{\lambda} = R \left(\frac{9-4}{36} \right)$$

$$\frac{1}{\lambda} = \frac{5R}{36}$$

$$\therefore \lambda_{\alpha} = \frac{36}{5R}$$

λ for β line :-

$$n_1 = 2, n_2 = 4$$

$$\frac{1}{\lambda} = R \times 1^2 \left(\frac{1}{4} - \frac{1}{16} \right)$$

$$\frac{1}{\lambda} = R \left(\frac{4-1}{16} \right)$$

$$\frac{1}{\lambda} = R \left(\frac{3}{16} \right)$$

$$\therefore \lambda_{\beta} = \frac{16}{3R}$$

λ for γ line :-

$$n_1 = 2, n_2 = 5$$

$$\frac{1}{\lambda} = R \times 1^2 \left(\frac{1}{4} - \frac{1}{25} \right)$$

$$\frac{1}{\lambda} = R \left(\frac{25-4}{100} \right)$$

$$\therefore \lambda_{\gamma} = 100/21R$$

$\lambda_{\text{minimum}}:$

$$n_1 = 2, n_2 = \infty$$

$$\frac{1}{\lambda} = R \times z^2 \left(\frac{1}{4} - \frac{1}{\infty^2} \right)$$

$$\frac{1}{\lambda} = \frac{R}{4}$$

$$\therefore \lambda_{\text{min}} = \frac{4}{R}$$

$\lambda_{\text{maximum}}:$

$$n_1 = 2, n_2 = 3$$

$$\frac{1}{\lambda} = R(z)^2 \left(\frac{1}{4} - \frac{1}{9} \right)$$

$$\therefore \lambda_{\text{max}} = \frac{36}{5R}$$

3) Paschen Series

$$n_1 = 3$$

$$n_2 = 4, 5, 6, \dots$$

Ryd. Formula :

$$\frac{1}{\lambda} = R(z)^2 \left(\frac{1}{3^2} - \frac{1}{n_2^2} \right)$$

Note

The no. of different λ found in any transition contributes different spectral line.

Maximum no. of spectral line for any transition (all lines are included)

$$= \frac{(n_2 - n_1)(n_2 - n_1 + 1)}{2}$$

Eg: For e⁻ transition from 5th excited state to 1st excited state. Find the total maximum lines.

$$\Rightarrow n_1 = 2, n_2 = 6$$

$$\Rightarrow \frac{(6-2)(6-2+1)}{2} = \frac{4 \times 5}{2} = 10 \text{ Ans}$$

4) Brakett Series

$$n_1 = 4, n_2 = 5, 6, 7, \dots$$

Ryd. Formula :

$$\frac{1}{\lambda} = R(z)^2 \left(\frac{1}{4^2} - \frac{1}{n_2^2} \right)$$

$$\left(\frac{1}{16} - \frac{1}{n_2^2} \right) \times 2R = \frac{E}{\lambda}$$

5) Pfund Series

$$n_1 = 5$$

$$\left(\frac{1}{5^2} - \frac{1}{n_2^2} \right) \times 2R = \frac{E}{\lambda}$$

Ryd. Formula :

$$\frac{1}{\lambda} = R \times z^2 \left(\frac{1}{25^2} - \frac{1}{n_2^2} \right)$$

6) Humphery series

$$n_1 = 6$$

$$n_2 = 7, 8, 9, \dots$$

Ryd. Formula :

$$\frac{1}{\lambda} = R \times z^2 \left(\frac{1}{36^2} - \frac{1}{n_2^2} \right)$$

Maximum spectral for any particular series
= $(n_2 - n_1)$

- 1) Lyman $\rightarrow (n_2 - 1)$
- 2) Balmer $\rightarrow (n_2 - 2)$
- 3) Paschen $\rightarrow (n_2 - 3)$
- 4) Brakett $\rightarrow (n_2 - 4)$
- 5) Pfund $\rightarrow (n_2 - 5)$
- 6) Humphery $\rightarrow (n_2 - 6)$

Limitations of Bohr's Model

- 1) Bohr's theory doesn't explain the spectrum of multi e⁻ species.
- 2) Why the angular momentum of the revolving e⁻ is equal to $nh/2\pi$, has not been explained by Bohr's theory.
- 3) Bohr inter-related quantum theory of radiation and classical laws of physics without any theoretical explanation.
- 4) Bohr's theory does not explain the fine structure of spectral lines. Fine structure of the spectral line is obtained when spectrum is viewed by spectroscope of more resolution power.
- 5) Bohr's theory does not explain the splitting of spectral lines in the presence of magnetic field (Zemman's effect) or electric field (Stark's effect).

de-Broglie Duality

→ Light has dual nature (particle, wave).

→ e⁻ also has dual nature.

- Particle = mass, momentum, kinetic energy
- Wave = λ , v , amplitude.

→ Every matter have wave associated to it.

$$\text{Energy of particle} \Rightarrow E = mc^2 \dots \textcircled{1}$$

$$\text{Energy of wave} \Rightarrow \frac{hc}{\lambda} = E_n \dots \textcircled{2}$$

From eqn $\textcircled{1}$ and $\textcircled{2}$:-

$$\frac{hc}{\lambda} = mc^2$$

$$\therefore \lambda = \frac{h}{mv} = \frac{h}{P}$$

Here, λ = de Broglie wavelength

m = mass of particle

v = velocity of particle

P = momentum = mv

$$\lambda = \frac{h}{mv}$$

(For matter)

(Having mass)

$$\lambda = \frac{hc}{E}$$

(For photon)

(Massless)

→ de Broglie duality does not hold good for particle with greater mass. It explains only lighter particles (e⁻, p, α , n, etc.).

Ques. 1 Find the wavelength associated to a car with mass 400 kg and moving with velocity 180 km/h.

$$\Rightarrow m = 400 \text{ kg}$$

$$v = 180 \text{ kmph}$$

$$h = 6.6 \times 10^{-34}$$

$$\lambda = \frac{h}{mv} = \frac{6.6 \times 10^{-34}}{400 \times 50}$$

$$= \frac{6.6 \times 10^{-34}}{20000}$$

$$\lambda \Rightarrow 3.3 \times 10^{-38} \text{ m Ans}$$

(negligible)

Ques. 2 Find λ for e- moving with velocity $2.188 \times 10^6 \text{ m/s}$.

$$\Rightarrow m = 9.1 \times 10^{-31} \text{ kg}$$

$$v = 2.188 \times 10^6 \text{ m/s}$$

$$\Rightarrow \lambda = \frac{h}{mv} = \frac{6.6 \times 10^{-34}}{9.1 \times 10^{-31} \times 2.188 \times 10^6} = \frac{6.6 \times 10^{-9}}{9.1 \times 2.188}$$

Ans $\Rightarrow 0.33 \times 10^{-9} \text{ m}$

de-Broglie wave length in terms of kinetic energy :-

$$mv = p$$

Sq. both side:-

$$(mv)^2 = p^2$$

$$m^2 v^2 = p^2$$

$$mv^2 = \frac{p^2}{m}$$

Multiplying by $\frac{1}{2}$ both side:-

$$\frac{1}{2}mv^2 = \frac{p^2}{2m}$$

$$KE = \frac{p^2}{2m} \text{ or } p^2 = 2m(KE)$$

$$\therefore p = \sqrt{2m(KE)}$$

$$\lambda = \frac{h}{mv} = \frac{h}{p}$$

Hence,

$$\lambda = \frac{h}{\sqrt{2m(KE)}}$$

Note: KE of any particle if placed b/w potential difference of V volt is $KE = qV$

q = charge of particle
 V = voltage

$$\lambda = \frac{h}{\sqrt{2m(KE)}} = \frac{h}{\sqrt{2m(qV)}}$$

$$\frac{h}{P}$$

$$\frac{h}{mv}$$

$$\frac{h}{\sqrt{2m(qV)}}$$

$$\frac{h}{\sqrt{2m(KE)}}$$

$$\frac{(for \alpha)}{0.101 \text{ \AA}} \frac{1}{\sqrt{V}}$$

$$\frac{0.286}{\sqrt{V}} \text{ \AA} \frac{1}{(for p^+)} \text{ \AA}$$

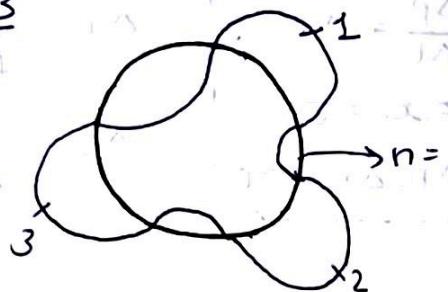
$$\frac{\sqrt{150/V}}{\text{ \AA}} \frac{1}{(for e^-)}$$

Explanation of angular momentum of e⁻ from de-Broglie's eqn.

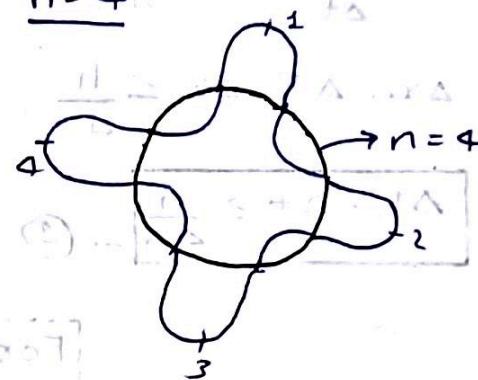
→ e⁻ moves in an orbit in the form of a wave.

→ The no. of waves in any orbit = no. of that orbit.

Eg: n = 3



n = 4



→ **For nth orbit (Proof)**

$$\text{no. of waves} = n$$

$$\text{wavelength} = \lambda$$

$$\text{Total length of } n \text{ wave} = n\lambda$$

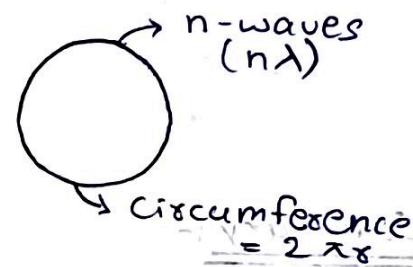
$$\text{Circumference of circle} = 2\pi r$$

$$\Rightarrow n\lambda = 2\pi r$$

$$\text{de Broglie's } \lambda = \frac{h}{mv}$$

$$\Rightarrow \frac{nh}{mv} = 2\pi r$$

$$mvr = \frac{nh}{2\pi}$$



$$\text{Note: } \frac{h}{2\pi} = \hbar$$

Heisenberg Uncertainty Principle (HUP)

→ It is impossible to measure simultaneously the exact momentum and position of a particle as small as an electron.

$$\Delta x \cdot \Delta p \geq \frac{h}{4\pi} \dots ①$$

Δx = uncertainty in position

Δp = uncertainty in momentum

$$\Delta x \cdot m \cdot \Delta v \geq \frac{h}{4\pi} \dots ②$$

Δv = uncertainty in velocity

$$\Delta x \cdot \Delta p \geq \frac{h}{4\pi}$$

Multiplying & dividing by Δt :

$$\Delta x \cdot \frac{\Delta p}{\Delta t} \cdot \Delta t \geq \frac{h}{4\pi}$$

$$\Delta x \cdot \Delta F \cdot \Delta t \geq \frac{h}{4\pi}$$

$$\boxed{\Delta E \cdot \Delta t \geq \frac{h}{4\pi}} \quad \dots \textcircled{3}$$

$$\begin{aligned}\frac{\Delta p}{\Delta t} &= \Delta F \\ F \cdot x &= E \\ \Delta F \cdot \Delta x &= \Delta E\end{aligned}$$

Δt = uncertainty in time

ΔF = uncertainty in force

ΔE = uncertainty in energy

For question solving

$$\Delta x \cdot \Delta p = \frac{h}{4\pi}$$

$$h = 6.6 \times 10^{-34}$$

$$\pi = 22/7$$

Summary:-

$$\boxed{\Delta x \cdot \Delta p \geq \frac{h}{4\pi}}$$

$$\boxed{\Delta x \cdot m \Delta v \geq \frac{h}{4\pi}}$$

$$\boxed{\Delta E \cdot \Delta t \geq \frac{h}{4\pi}}$$

Δx = uncertainty in position

Δp = uncertainty in momentum

Δv = uncertainty in velocity

ΔE = uncertainty in energy

Δt = uncertainty in time

Quantum Mechanical Model of an atom

→ Derived from Schrodinger Equation.

→ e⁻ is a wave. It follows an equation which is called "e⁻ wave function" [Ψ].

→ Ψ is function of [r, θ, φ]

$$\Psi(r, \theta, \phi) = \underbrace{f(r)}_{\text{radial part}} \cdot \underbrace{f(\theta)}_{\text{angular part}} \cdot f(\phi)$$

θ & ϕ = angle

r = distance

- Radial Part $\rightarrow f(r)$ depends upon 2 no. (n, l)
- Angular Part $\rightarrow f(\theta)$ depends upon 2 no. (l, m)
 $f(\phi)$ depends upon 1 no. (m)

n - principal quantum no.
 l - azimuthal quantum no.
 m - magnetic quantum no.

Schrödinger Wave Equation :-

$$\left[\frac{d^2\psi}{dx^2} + \frac{d^2\psi}{dy^2} + \frac{d^2\psi}{dz^2} + \frac{8\pi^2m}{h^2}(E-V)\psi = 0 \right]$$

$\rightarrow E$ = Total energy

$\rightarrow V$ = Potential energy

After solving this eqn we get value of ' ψ '

$$\Psi(r, \theta, \phi) = \underset{n, l}{f(r)} \cdot \underset{l, m}{f(\theta)} \cdot \underset{m}{f(\phi)}$$

Orbital : The 3-D space around a nucleus where e⁻ finding probability is greater than 95%.

Node : The region around nucleus where e⁻ finding probability is almost zero.

Radial Nodes

Radial part = 0
 $f(r) = 0$

Also known as
'spherical nodes'

No. of radial
node = $n - l - 1$

Nodes

$$\begin{aligned} \text{Total Nodes} &= AN + RN \\ &= l + n - l - 1 \\ TN &= n - 1 \\ AN &= l \\ RN &= n - l - 1 \end{aligned}$$

Angular Nodes

Angular part = 0
 $f(\theta) \cdot f(\phi) = 0$

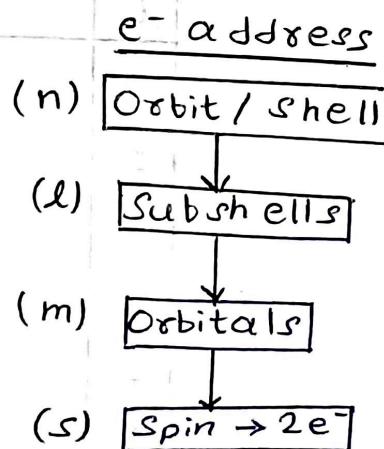
Also known as
'angular nodes'

No. of angular
node = l

Quantum Numbers

They are the set of 4 numbers which defines the position of e⁻ in an atom.

- 1) Principal Quantum no.
- 2) Azimuthal Quantum no.
- 3) Magnetic Quantum no.
- 4) Spin Quantum no.



Principal Quantum No. (n)

- It tells us about orbit in which e^- is present.
- It also tells us about energy of an e^- .
- $n \rightarrow$ Bohr Orbit. (1, 2, 3, 4, ..., K, L, M, N, ...)
- Angular momentum of e^- in an orbit = $\frac{nh}{2\pi}$ or $h\bar{n}$.
- It also tells us about size of orbit.

Maximum no. of e^- in any orbit = $2n^2$

Maximum no. of orbital in any

$$\text{orbit} = \frac{2n^2}{2} = n^2$$

n	Max. no. of e^-	Max. no. of orbitals
2	$2 \times 2^2 = 8$	$2^2 = 4$
3	$2 \times 3^2 = 18$	$3^2 = 9$
4	$2 \times 4^2 = 32$	$4^2 = 16$
5	$2 \times 5^2 = 50$	$5^2 = 25$
6	$2 \times 6^2 = 72$	$6^2 = 36$

Azimuthal Quantum No. (l)

- Also known as subsidiary quantum no. or angular momentum quantum no.
- It tells us about subshell.
- Value of l tells us about shape of orbital.
- The value of l depends upon ' n '. [$l = 0$ to $(n-1)$.]

l	Shape	Subshell
0	Spherical	s-subshell
1	Dumble	p-subshell
2	Double dumble	d-subshell
3	Complex	f-subshell
4	Complex	g-subshell
5	Complex	h-subshell

n	Possible value of l	Subshell
1	0	1s - subshell
2	0 1	2s - subshell 2p - subshell
3	0 1 2	3s - subshell 3p - subshell 3d - subshell
4	0 1 2 3	4s - subshell 4p - subshell 4d - subshell 4f - subshell

→ Angular momentum of an e^- in an orbital
 $= \sqrt{l(l+1)} = \frac{h}{2\pi}$

Orbit	Orbital Angular momentum
s	0
p	$\sqrt{2}\ h$
d	$\sqrt{6}\ h$
f	$\sqrt{12}\ h$

Magnetic Quantum No. (m)

- It tells us about orientation of orbitals.
- Its value depends upon ' l '.
- Possible values of $m = (-l \text{ to } +l)$.
- Total no. of possible value = $(2l+1)$

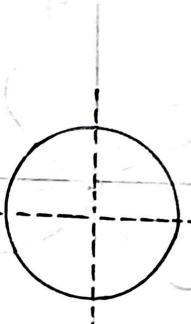
$$[-l, \dots, -2, -1, 0, 1, 2, \dots, l]$$

- Each value of ' m ' represents 1 orbital.
- Total no. of orbital in a subshell = $2l+1$
- Total no. of e^- in a subshell = $2(2l+1)$

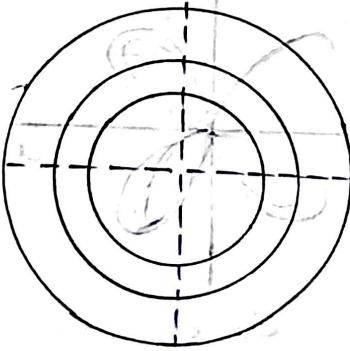
a) S-subshell

- Shape = spherical
- $l=0$
- $m = -l \text{ to } +l = 0$
- Total possible value = $2l+1$
 $= 2 \times 0 + 1$
 $= 1$

∴ An s-subshell contains 1 orbital.



1s



2s

b) p-subshell

$$\rightarrow l = 1$$

$$\rightarrow m = (-1 \text{ to } +1)$$

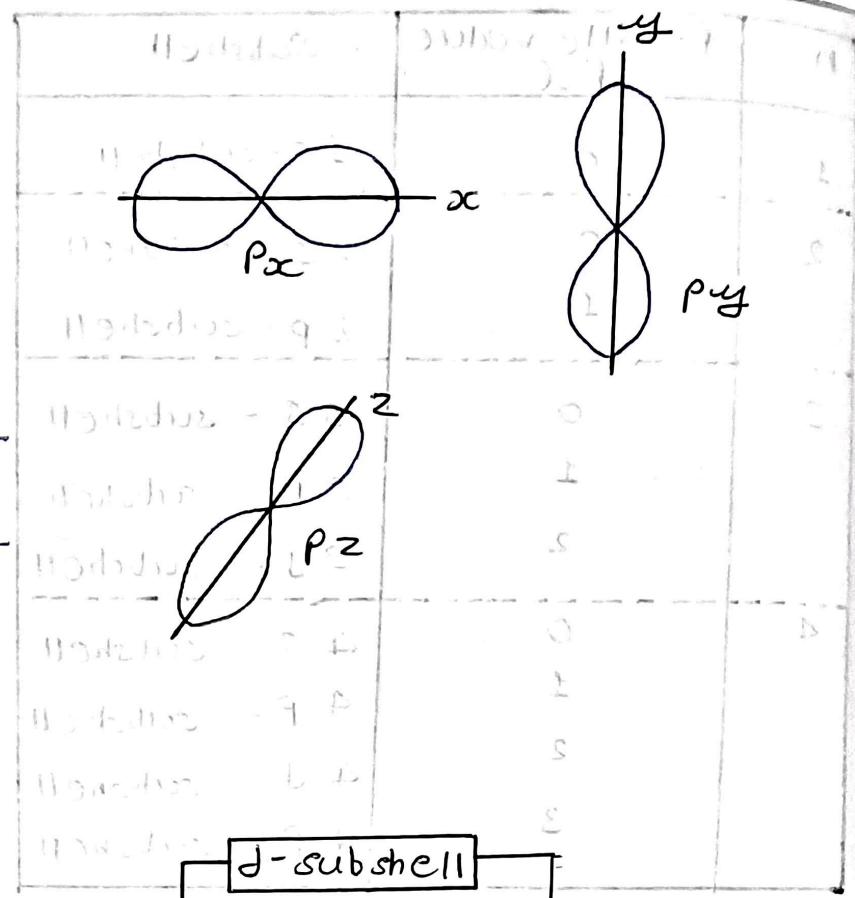
$$= -1, 0, +1$$

$$\rightarrow \text{Total possible values} = (2l+1)$$

$$= 2 \times 1 + 1$$

$$= 3$$

$\therefore p$ -subshell contains 3 orbitals.



c) d-subshell

$$\rightarrow l = 2$$

$$\rightarrow m = (+2 \text{ to } -2)$$

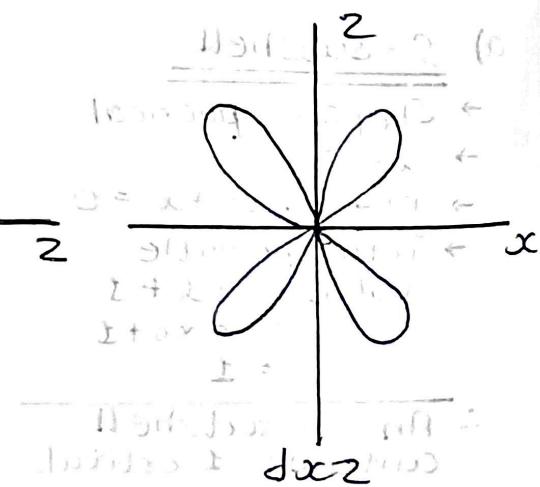
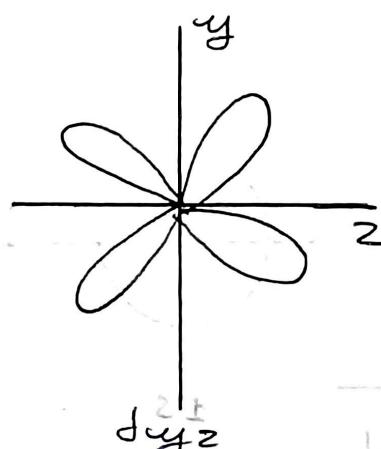
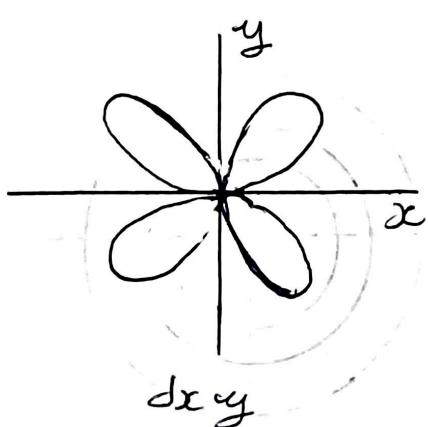
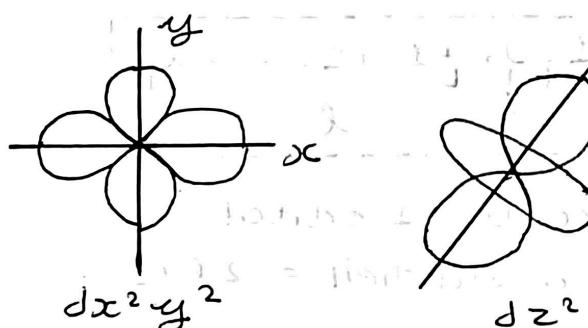
$$= -2, -1, 0, +1, +2$$

$$\rightarrow \text{Total possible values} = (2l+1)$$

$$= 2 \times 2 + 1$$

$$= 5$$

$\therefore d$ -subshell contains 5 orbitals.

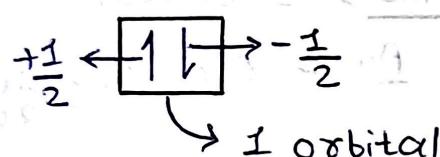


Spin Quantum No. (s)

→ Electronic spin

→ Clockwise = $+\frac{1}{2}$ or \uparrow or $\uparrow\downarrow$

→ Anticlockwise
= $-\frac{1}{2}$ or \downarrow or $\uparrow\downarrow$



Note: Spin only magnetic moment

$$M_s = \sqrt{n(n+2)} \text{ B.M.}$$

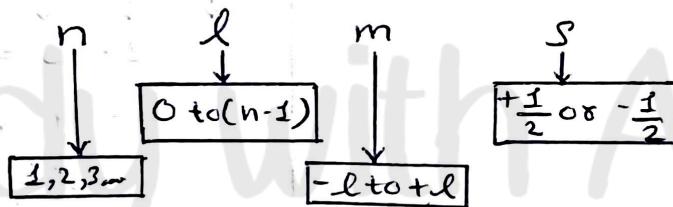
Unit

(Bohr Magneton)

n = no. of unpaired electron

Questions from Q.no.

Type - 1: Correct set of quantum no.



Eg: Which of the following set is possible?

n	l	m	s
1) 4	3	-2	$-\frac{1}{2}$
2) 5	4	+5	$+\frac{1}{2}$
3) 4	4	0	$-\frac{1}{2}$
4) 6	2	0	$-\frac{1}{2}$
5) 3	0	-1	$+\frac{1}{2}$

Type - 2: Maximum no. of e-

→ In an orbit

$$\text{Max. no. of } e^- = 2n^2$$

$$\text{Max. no. of orbital} = n^2$$

→ In a subshell

$$\text{Max. no. of } e^- = 2(2l+1)$$

$$\text{Max. no. of orbital} = 2l+1$$

→ In an orbital

$$\text{Max. no. of } e^- = 2.$$

Eg: Find max. no. of e-

$$\begin{array}{ll} 1) n=4 & 2) n=4, l=2 \\ (\text{Orbit}) & (\text{Subshell}) \\ 2n^2 = 2 \times 4^2 & 2(2l+1) \\ = 32e^- & 2(2 \times 2 + 1) \\ & = 10e^- \end{array}$$

$$3) n=4, l=2, m=-2 \\ (\text{1 orbital}) = 2e^-$$

$$4) n=4, l=2, m=-2, s=+\frac{1}{2} \\ \text{max} = 1/e^-$$

5) Max. e⁻ in (n=4, m=-1)

⇒ 'l' is missing

⇒ In that case, intermediate Q. no. ki sabhi possible values ko manenge.

⇒ n=4, $l = 0, 1, 2, 3$
S P D F

S → [0]

P → [-1 0 +1]

D → [-2 -1 0 +1 +2]

F → [-3 -2 -1 0 +1 +2 +3]

⇒ 3 orbitals

Ans: 6 e⁻ (1 orbital = 2e⁻)

6) l=3

⇒ max. e⁻ in subshell = $2(2l+1)$

$$= 2(3 \times 2 + 1)$$

$$= 2 \times 7$$

$$\text{Ans: } 14 \text{ e}^{-}$$

7) n=3, s = + $\frac{1}{2}$

⇒ l, m → all possible value

n=3 (orbit)

3s, 3p, 3d (subshell)

$$\downarrow \quad \downarrow \quad \downarrow$$

$$1 + 3 + 5 = 9 \text{ orbital}$$

Total = 9 orbital

$$\left(+\frac{1}{2} \right) \quad \left(-\frac{1}{2} \right)$$

$$9e^{-} \quad 9e^{-}$$

Type - 3: No. of nodes

→ RN = n - l - 1 (Radial node)

Eg: Find no. of RN for

1) 2s

n=2

l=0

n-l-1

2-0-1

Ans: 1

2) 3s

n=3

l=0

n-l-1

3-0-1

Ans: 2

3) 3p

n=3

l=1

n-l-1

3-1-1

Ans: 1

4) 3d

n=3

l=2

n-l-1

3-2-1

Ans: 0

5) 6p

n=6

l=1

n-l-1

6-1-1

Ans: 4

→ AN = l (Angular node)

S → 0

P → 1

D → 2

F → 3

→ TN = l-1 (Total nodes)

Eg: Find TN for 6d

⇒ n=6, l=2 ⇒ TN = 6-1 = 5

Electronic Configuration

- There are 3 rules for electronic configuration.
 - 1) Aufbau's Principle
 - 2) Hund's Rule
 - 3) Pauli's Exclusion

Aufbau's Principle

- Aufbau principle gives a sequence in which various subshells are filled up depending on the relative order of the energies of various subshells.
- Principle: The subshell with min. energy is filled up first. When this subshell obtained max. quota of e^- then the next subshell with higher energy starts filling.

$$\boxed{\text{Energy} \propto (n+l)}$$

Eg: Value of $(n+l)$ for -

$$1) 1s = 1+0 = 1 \quad 4) 3s = 3+0 = 3$$

$$2) 2s = 2+0 = 2 \quad 5) 3p = 3+1 = 4$$

$$3) 2p = 2+1 = 3 \quad 6) 3d = 3+2 = 5$$

$$\boxed{(n+l) \uparrow (\text{Energy}) \uparrow}$$

Note: For $2p$ and $3s$ the value of $(n+l)$ is same

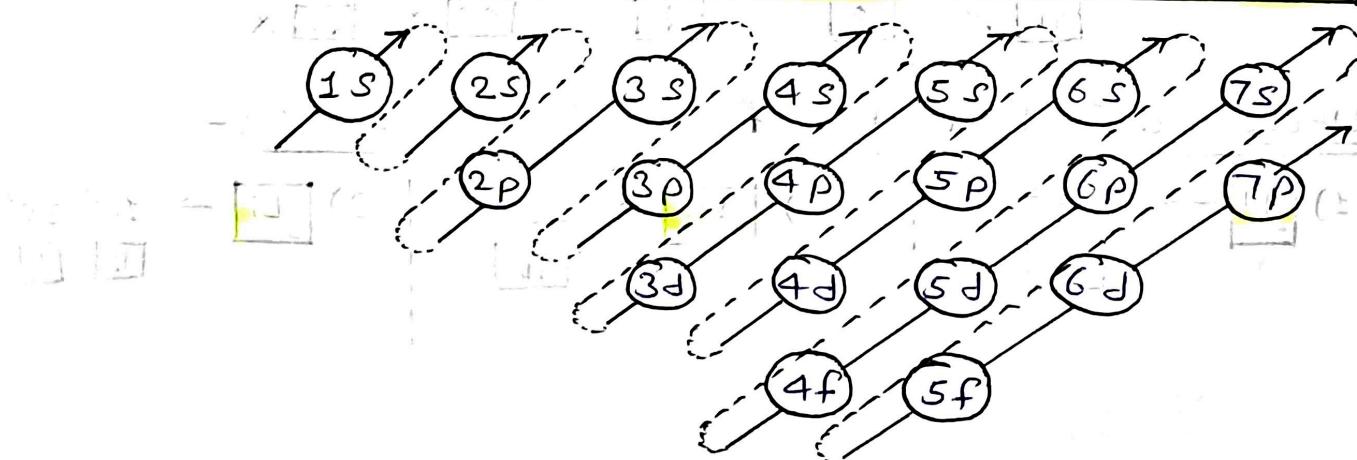
$$2p = 2+1 = 3$$

$$3s = 3+0 = 3$$

In that case, the subshell which has greater value of n , has more energy.

$$\therefore 2p < 3s$$

- Sequence : $1s < 2s < 2p < 3s < 3p < 4s < 3d < 4p < \dots$



→ Important Note: - For single e⁻ species

Energy \propto 'n' only

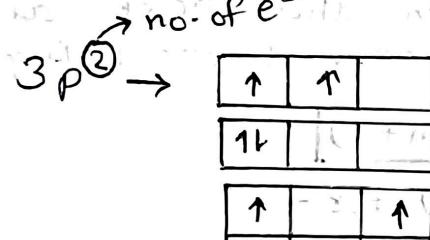
Eg: H-atom

$$1s < (2s = 2p) < (3s = 3p = 3d) < (4s = 4p = 4d = 4f)$$

Hund's Rule of Maximum Spin Multiplicity

→ For degenerate orbitals e⁻ first filled up singly then pairing takes place.

→ Degenerate orbital: Orbital with same energy.
All orbitals of a subshell are degenerate.



EK subshell me jab tak sabhi orbital me ek e⁻ na aa jaye hum pairing nahi karenge.

Eg: Which of the following is not according to Hund Rule?

1)

↑	↑	↑
---	---	---

 (It follows)

2)

1↓	↑	
----	---	--

 (Doesn't follow)

3)

+	↓	+
---	---	---

 (It follows)

4)

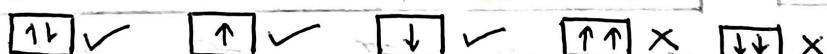
↓	1↓	
---	----	--

 (Doesn't follow)

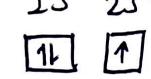
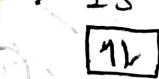
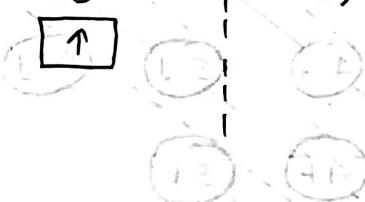
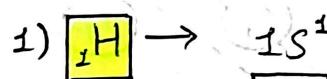
Pauli's Exclusion Principle :-

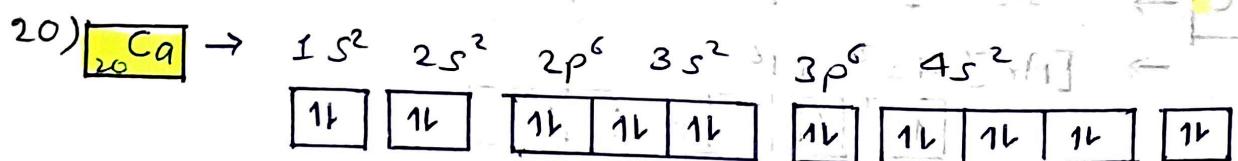
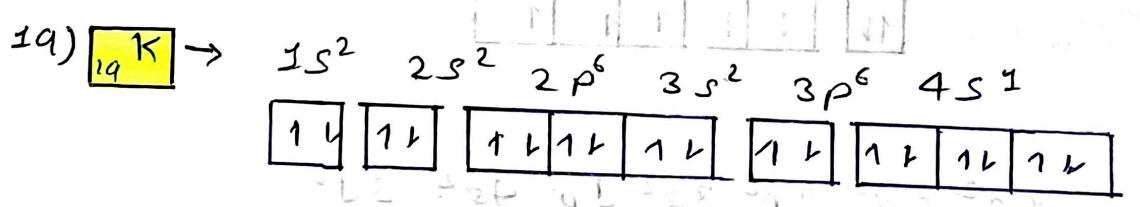
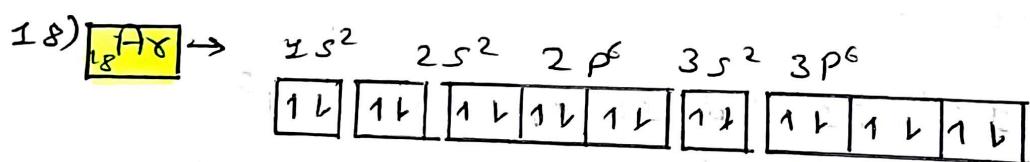
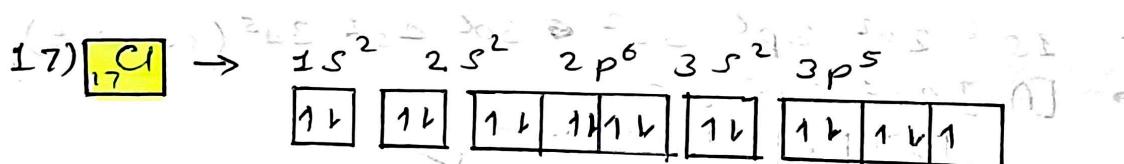
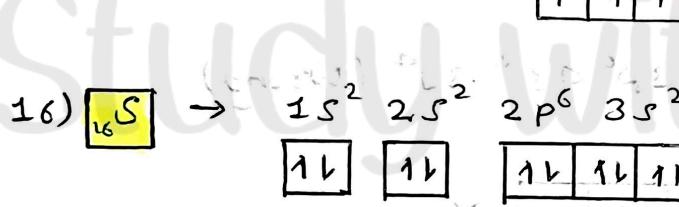
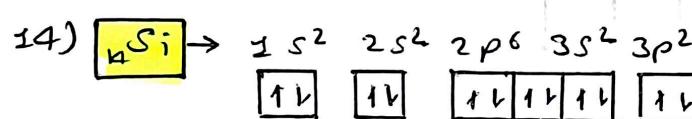
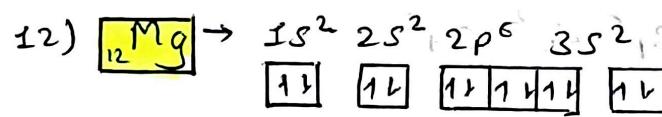
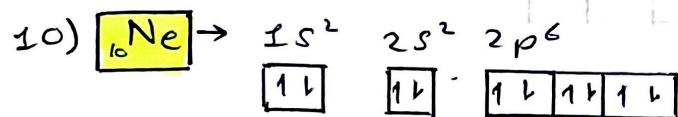
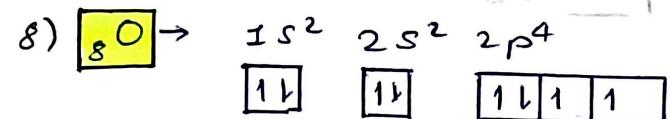
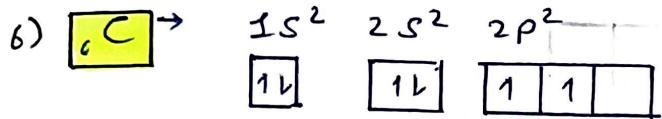
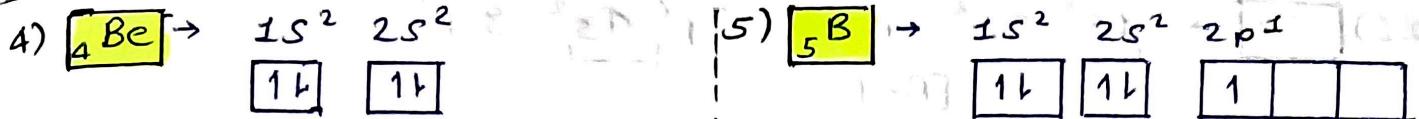
→ No two e⁻ in an atom can have same values of all 4 quantum no.

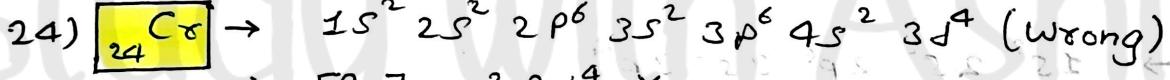
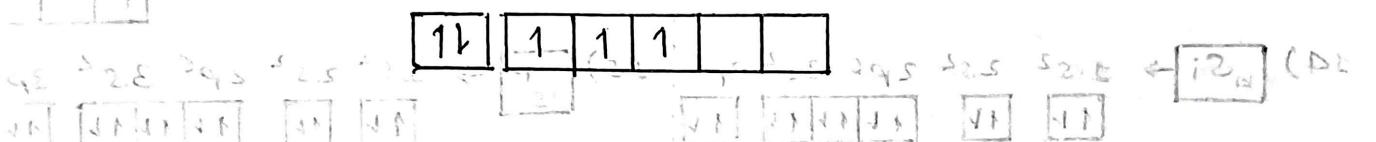
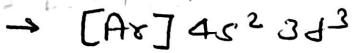
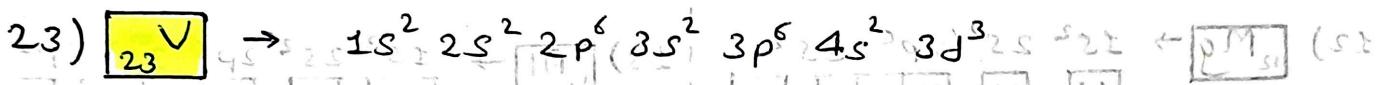
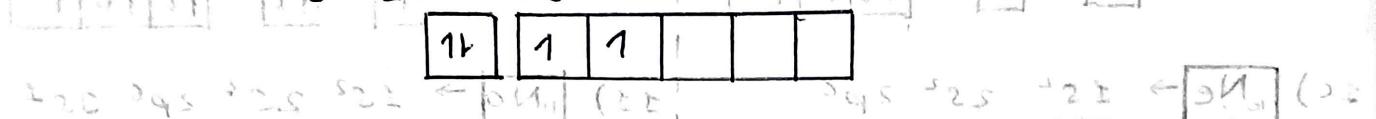
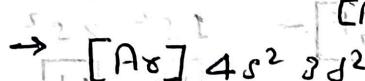
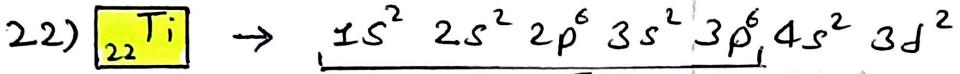
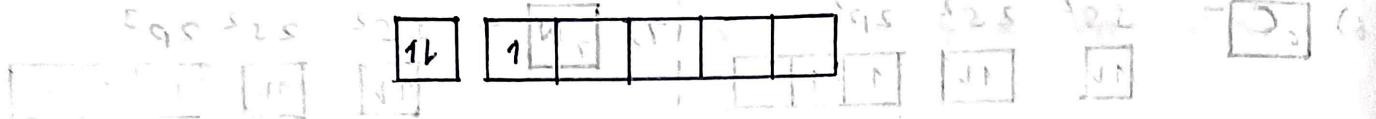
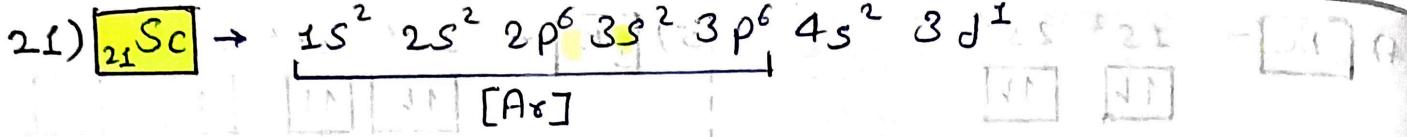
→ Orbital can accommodate maximum 2 e⁻ with opposite spin.



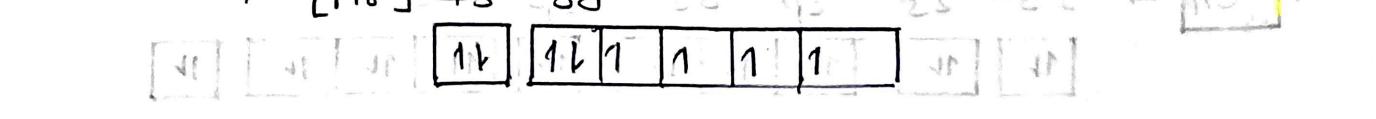
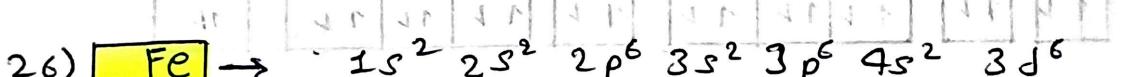
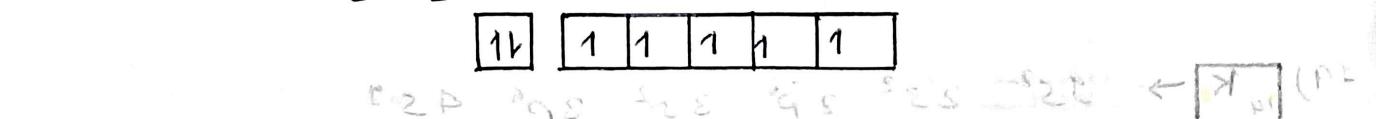
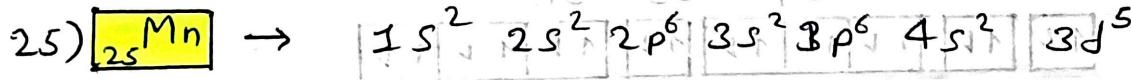
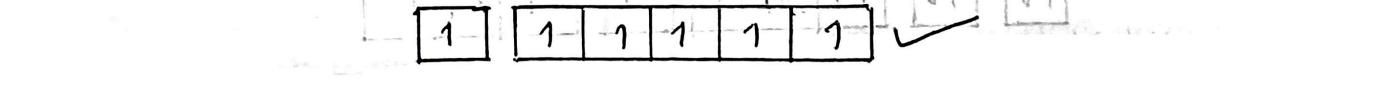
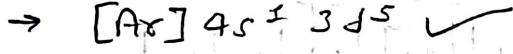
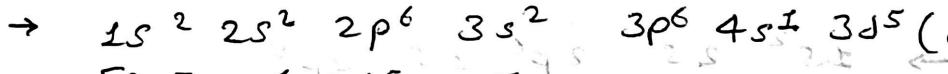
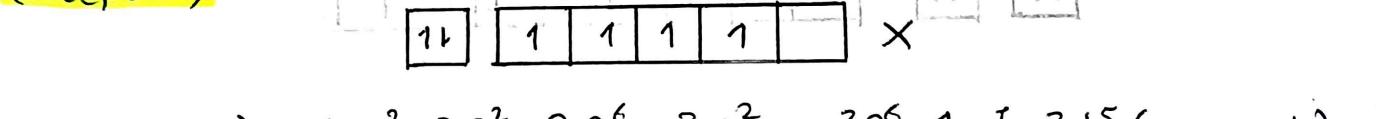
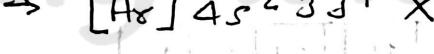
Electronic Configuration from Z = 1 to Z = 30 :-

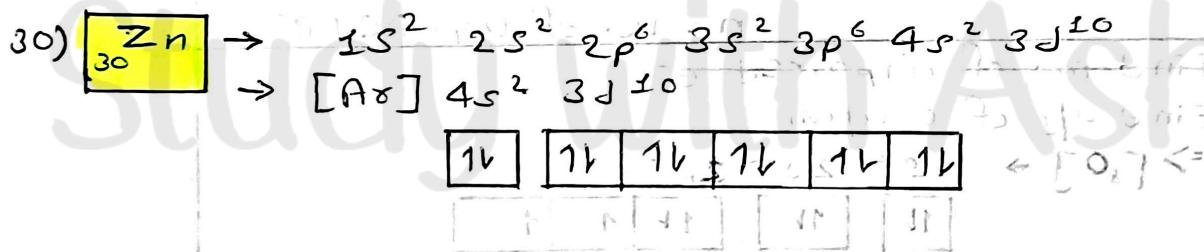
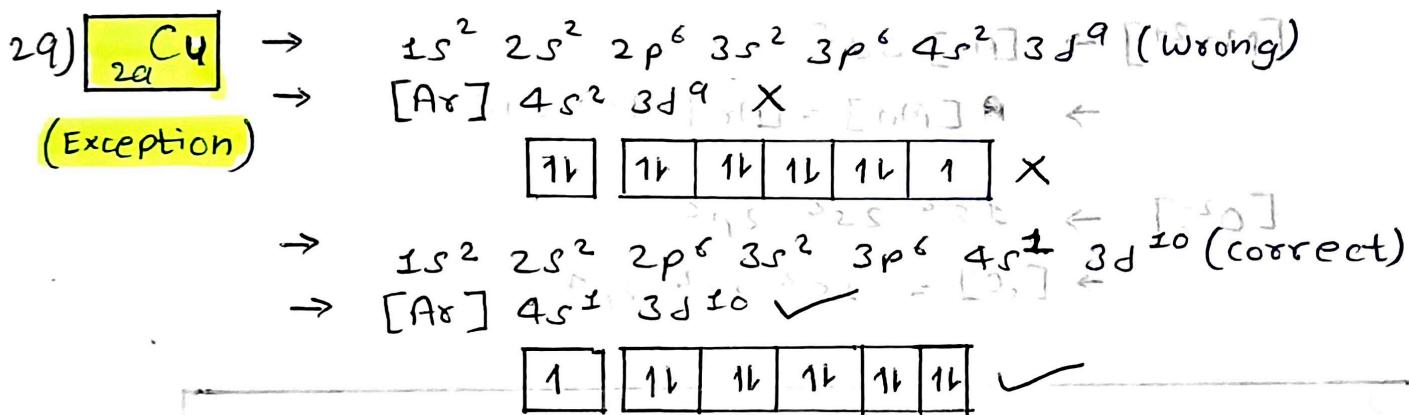
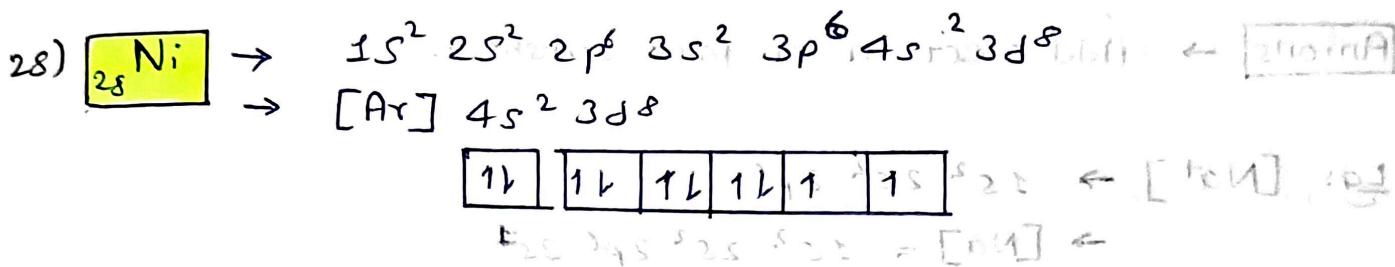
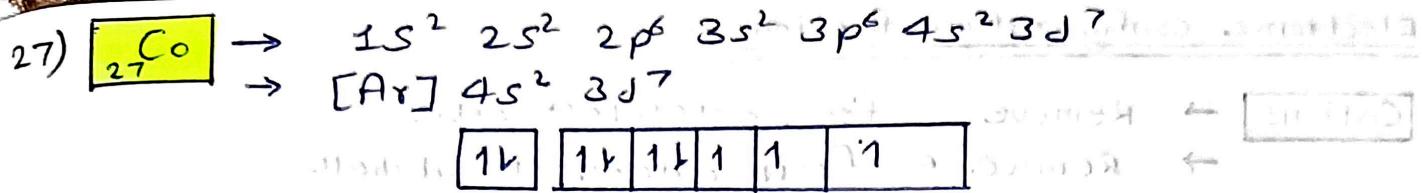






(Exception)





Explanation for exception to $(n+l)$ rule (Co and Cu) :-

- Half filled and fully filled orbitals are more stable.
- There are 2 reasons (for extra stability of half filled orbital):

1) Symmetry

d^5	1	1	1	1	1
Symmetrical					

d^7	1s	1s	1s	1s	1s
Unsymmetrical					

d^{10}	1s	1s	1s	1s	1s
Symmetrical					

2) Exchange Energy

Same spin wale e^- apas me exchange ho sakte hain.

No. of exchange ↑ Stability ↑

d^5	1	1	1	1	1
	4	3	2	1	0

Total exchange = 10

d^4	1	1	1	1
	3	2	1	0

Total exchange = 6

d^{10}	1s	1s	1s	1s	1s
	4	3	2	1	0

Total exchange = 20

Electronic Configuration for ions :-

- Cations** → Remove e^- from outermost orbit.
 → Remove e^- from outermost subshell.
 → Remove e^- from 4s between 3d and 4s.

- Anions** → Add electron in last subshell.

Eg: $[Na^+]$ → $1s^2 2s^2 2p^6$
 $\rightarrow [Na] = 1s^2 2s^2 2p^6 3s^1$

$[Mn^{2+}] \rightarrow [Ar] 3d^5$
 $\rightarrow [Mn] = [Ar] 4s^2 3d^5$

$[O^{2-}] \rightarrow 1s^2 2s^2 2p^6$
 $\rightarrow [O] = 1s^2 2s^2 2p^4$

Spin only magnetic moment (μ_s) = $\sqrt{n(n+2)}$ B.M.

n = no. of unpaired e^- .

Eg: Find no. of unpaired e^-

Find μ_s of O-atom

$$\Rightarrow [O] \rightarrow 1s^2 2s^2 2p^4$$

↑	↑	↑	1	1
---	---	---	---	---

$$\Rightarrow \text{unpaired } e^- (n) = 2$$

$$\Rightarrow \mu_s = \sqrt{2(2+2)} = \sqrt{8} \text{ BM Ans}$$

up.e ⁻	μ_s
-------------------	---------

$$1 \rightarrow \sqrt{1(1+2)} = \sqrt{3} \text{ BM}$$

$$2 \rightarrow \sqrt{2(2+2)} = \sqrt{8} \text{ BM}$$

$$3 \rightarrow \sqrt{3(3+2)} = \sqrt{15} \text{ BM}$$

$$4 \rightarrow \sqrt{4(4+2)} = \sqrt{24} \text{ BM}$$

Note: If μ_s is given

$$\text{Eg: } \mu_s = 4.84 \text{ BM}$$

Integer part → decimal part

Then integer part is no. of unpaired e^-

μ_s	up.e ⁻
1.73	1
2.85	2
4.84	4
5.87	5

Graphs

1) $\Psi(r) / f(r) / R(r) \text{ vs } r$

For s -subshell -

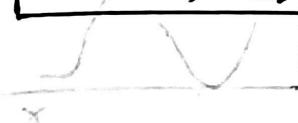
$$r = 0; \Psi(r) > 0$$

$$r = \infty; \Psi(r) = 0$$

For p, d, f subshell -

$$r = 0; \Psi(r) = 0$$

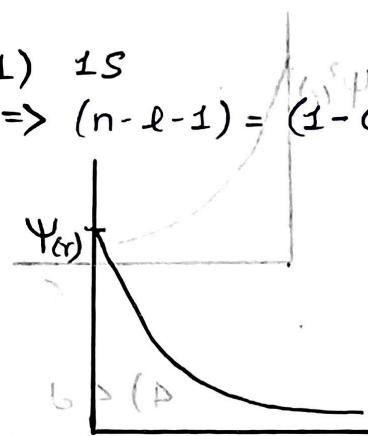
$$r = \infty; \Psi(r) = 0$$



Note: The graph cuts x -axis $(n-l-1)$ times other than origin.

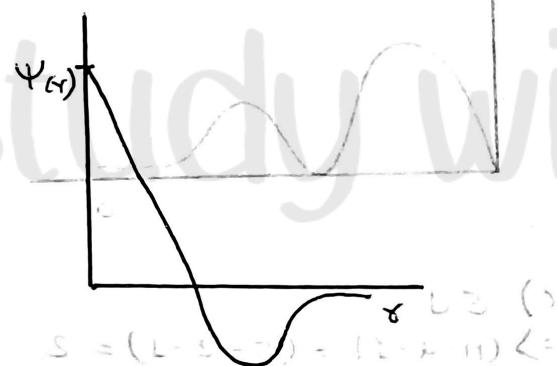
1) $1s$

$$\Rightarrow (n-l-1) = (1-0-1) = 0$$



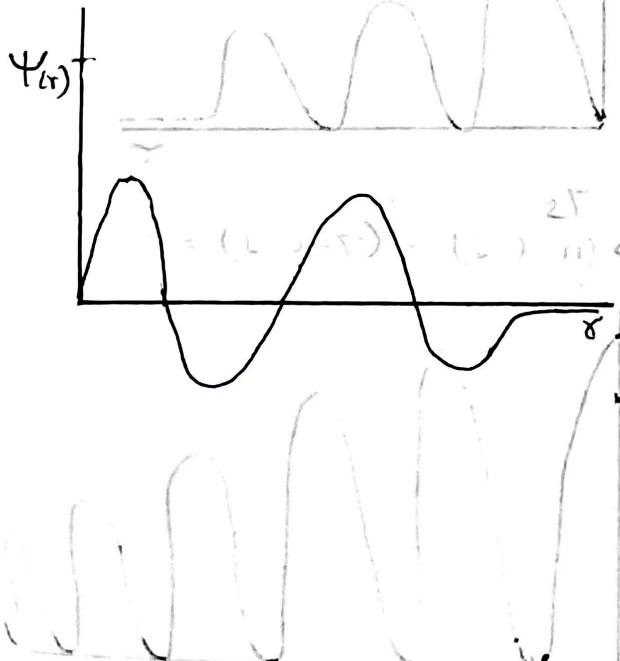
2) $2s$

$$\Rightarrow (n-l-1) = (2-0-1) = 1$$



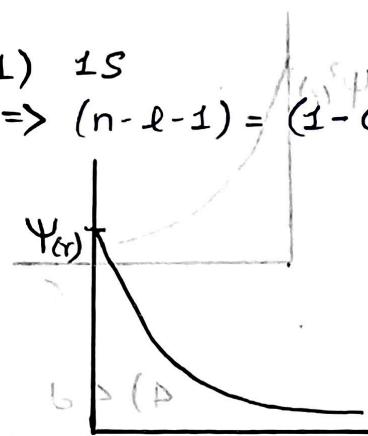
4) $6d$

$$\Rightarrow (n-l-1) = (6-2-1) = 3$$



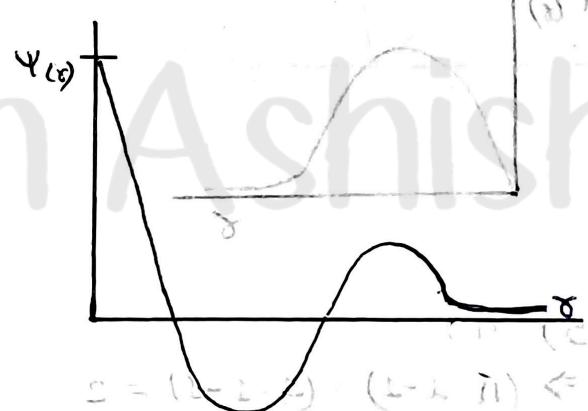
1) $1s$

$$\Rightarrow (n-l-1) = (1-0-1) = 0$$



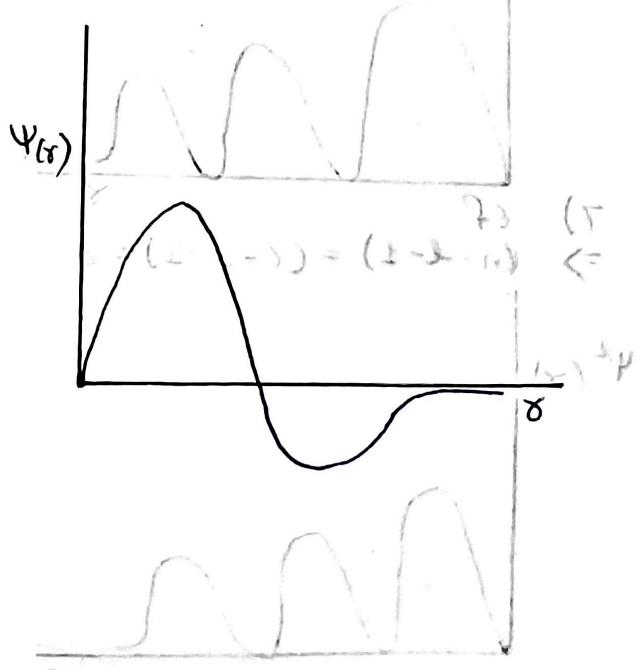
3) $3s$

$$\Rightarrow (n-l-1) = (3-0-1) = 2$$



5) $3p$

$$\Rightarrow (n-l-1) = (3-1-1) = 1$$



2) $\Psi^2(r) / R^2(r) / f^2(r)$ vs r

For S-orbital

$$r=0; \Psi^2(r) > 0$$

$$r=\infty; \Psi^2(r)=0$$

For S, P, D

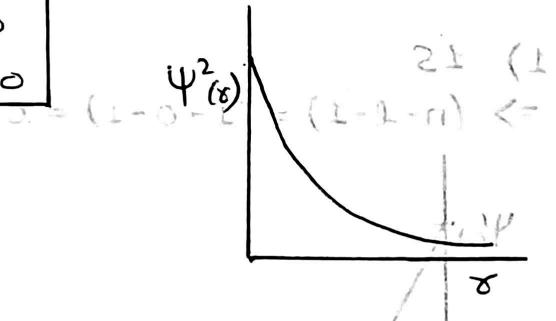
$$r=0; \Psi^2(r)=0$$

$$r=\infty; \Psi^2(r)=0$$

Note: Due to square graph never be -ve.

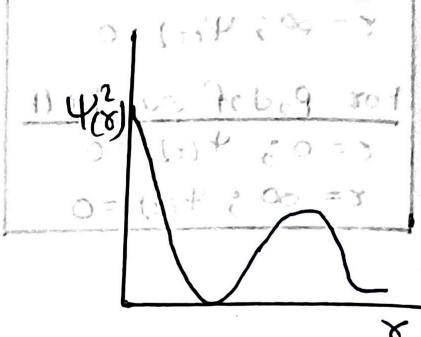
1) 1S

$$\Rightarrow (n-l-1) = (1-0-1) = 0$$



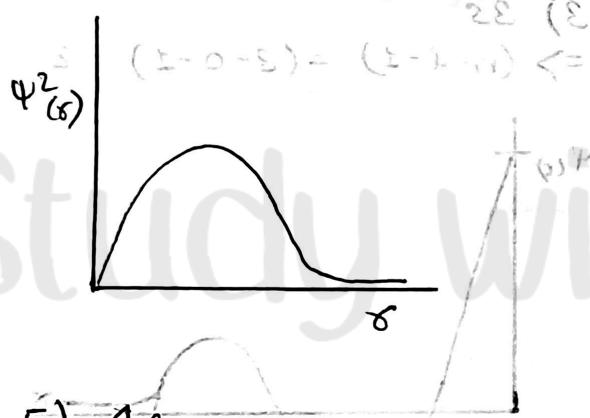
2) 2S

$$\Rightarrow (n-l-1) = (2-0-1) = 1$$



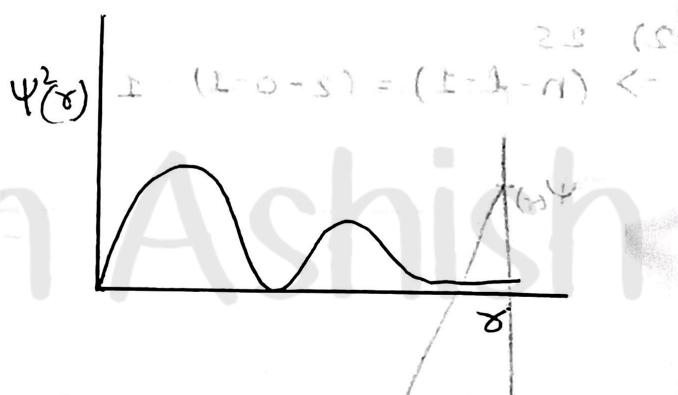
3) 2P

$$\Rightarrow (n-l-1) = (2-1-1) = 0$$



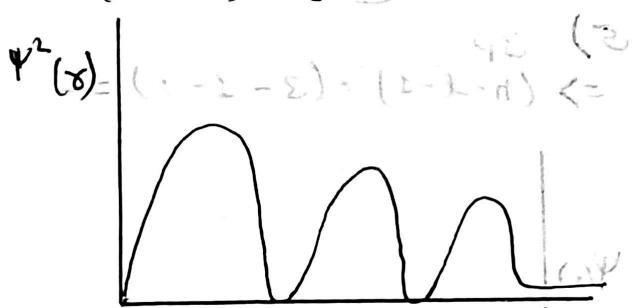
4) 4D

$$\Rightarrow (n-l-1) = (4-2-1) = 1$$



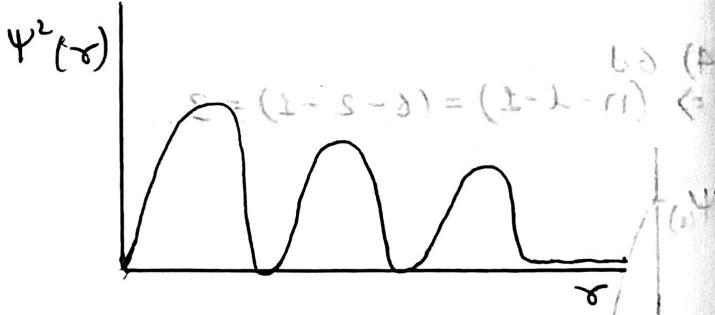
5) 4P

$$\Rightarrow (n-l-1) = (4-1-1) = 2$$



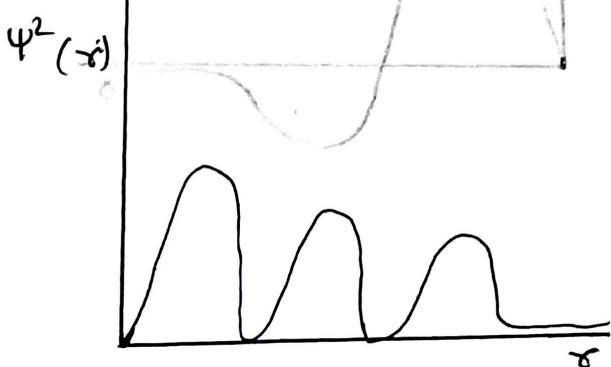
6) 5D

$$\Rightarrow (n-l-1) = (5-2-1) = 2$$



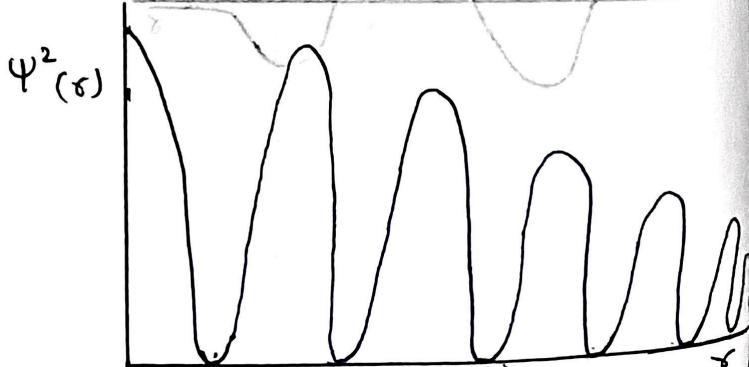
7) 6F

$$\Rightarrow (n-l-1) = (6-3-1) = 2$$



7) 7S

$$\Rightarrow (n-l-1) = (7-0-1) = 6$$



3) - RPDF (Radical Probability Distribution Function)

$$P(r) = 4\pi r^2 \Psi^2(r) \cdot dr$$

For s, p, d, f

$$r=0; \text{RPDF}=0$$

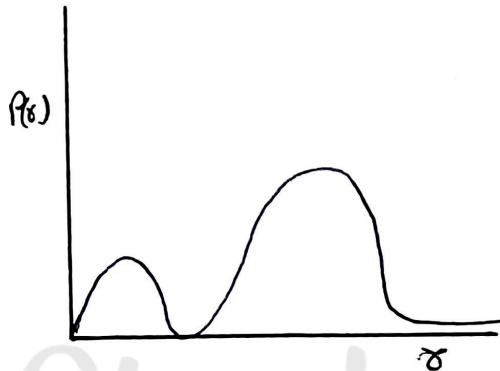
$$r=\infty; \text{RPDF}=0$$

→ -ve nahi hoga

→ x-axis ko other than origin ($n-l-1$)

→ Peak badhta jayega.

1) $2s$
 $\Rightarrow (n-l-1)$
 $(2-0-1) = 1$



2) $5p$
 $\Rightarrow (n-l-1)$
 $(5-1-1) = 3$

