



---

# State Space Modelling for Ferromagnetic Detection

Richard Hodgskin-Brown

*Commercial in Confidence | © Metrasens Ltd. 2022*

---

May 10, 2022

**T**his document aims to give a general overview of the problem of intelligent ferromagnetic detection, especially as it relates to the Metrasens product “Skout”, a passive ferromagnetic security screening device. An attempt is made to formulate a simplified version of this problem in the language of state space models, and a roadmap outlining further improvements to this simplified approach is given.

## 1 Overview

Metrasens are developing a new class of ferromagnetic detection systems to provide greater capability in several markets, with urban security being a particular target. This new generation of systems is designed to not only detect the presence of ferromagnetic objects, but to discriminate threat items from benign objects carried by the general population: for example, a perfect system should ignore a mobile phone but raise an alarm for an assault rifle. The wide range of benign ferrous items carried day-to-day by the populace, in combination with the complex and varied nature of the potential threat items, make this a considerably difficult problem. In the simplest case, in which passive magnetometers are used to record the intrinsic ferromagnetic signature of the traversing items, there is a limited amount of information available to make

this classification. Advanced signal processing and machine learning techniques are therefore being researched to enhance the performance to a satisfactory level, and it is believed that sequential Bayesian estimation techniques may be a powerful technique to apply to this problem.

Though in principle these techniques might be applied to any of the new technologies in development, this project will focus on applying to these methods to the upcoming product named Skout. This technology utilises a set of magnetometers to measure the magnetic field (“B-field”) passively produced by traversing ferrous objects. These can be measured over a window of time to produce a multivariate time-series (MTS), which is the basic data format which needs to be processed by a detection algorithm.

The basic idea for classification has been to “fit” the input MTS to a physical model, giving an intuitive, interpretable set of model parameters. These parameters can then be used to make a detection decision, likely strongly incorporating anomaly/outlier detection due to the unpredictable nature of the threat set and the inherent difficulty of collecting large quantities of high-quality threat data. Including an intermediary space with interpretable parameters is believed to be crucial: only small datasets are able to be obtained, with potential heavy systematic bias in the threat sets especially, meaning that automatically learned or statistical features could be highly unreliable. Physical

features help mitigate this, in theory, as only features which are intrinsic to the objects themselves (such as moment strength and object length) are sent to the classifier, and poorly understood abstract features are avoided.

The fitting step is currently being performed using the Levenberg-Marquardt technique to perform a non-linear least squares optimisation, minimising the residuals between the recorded MTS and a simulated traversal with a given set of model parameters. Although the global minimum of the objective function is typically being located correctly, this approach has a number of inherent shortcomings, which motivates the search for an improved inversion technique.

## 2 Skout System

This technology consists of a set of modular pillars which surround a walkthrough channel. Each pillar contains six triaxial magnetometers, each capable of capturing a full three-dimensional measurement of the magnetic field (“B-field”) at a point in space. A window of data is recorded from the sensors over a range of samples, and a detection decision is made on this data: if the traversing object/objects are considered to be a threat, an alarm is raised.

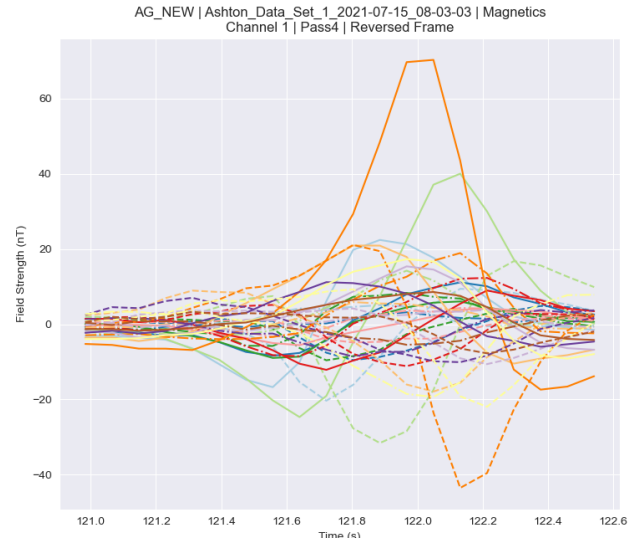
## 3 Raw Data format

A Skout pillar contains six triaxial magnetometers, resulting in 18 signals per pillar (x, y, z field components are from each triaxial set are recorded separately). A channel is bordered by two pillars, so 36 magnetometer signals are recorded for a given traversal through the system. The sensors are sampled at a constant rate of 12.2 Hz, producing a 36-dimensional MTS. Currently we are considering time windows with a length of twenty samples, though this is not set in stone<sup>1</sup>; this produces an MTS of length 20 and width 36 (i.e.  $x \in \mathbb{R}^{36 \times 20}$ ). A typical window of Skout data is shown in Figure 1.

## 4 Physical Model

In our current detection approach, the raw data window is “fitted” to a physical model, the parameters of which are used to make a detection decision. This model is a simplified representation of what might be occurring during the traversal, informed by the physics team’s domain knowledge in magnetics. In this model, a ferromagnetic object producing an idealised magnetic field travels on a specified trajectory through the Skout

<sup>1</sup>This could be increased for the purposes of this investigation, but in practice there will be a fundamental limit: a window size too large will contain signals from the traversals before or after the pass in consideration.



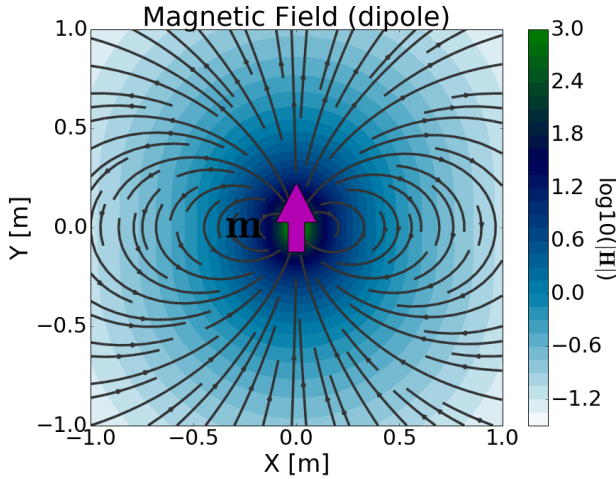
**Figure 1:** A typical example of a Skout recording. This is a 36-dimensional time series representing the B-field measured at each sensor throughout a traversal, in this case a member of the public passing through at Ashton Gate stadium.

channel, resulting in magnetic field measurements at the sensors which change over the course of the trajectory. The field pattern at the sensors for a given time sample is dependent on three things:

1. **The relative position of the ferromagnetic object and the sensors.** The magnetic field surrounding objects drops off sharply with distance, so objects located far from the sensors will produce a weaker measurement.
2. **The orientation of the ferromagnetic object.** The field pattern produced by physical objects is not spherically symmetric, therefore the orientation of the object as it is carried through will affect the resultant field.
3. **The magnetic properties of the object.** A more strongly magnetised object will produce a greater field measurement at the sensors. For the point dipole model, this is parameterised by the moment strength, which is the magnitude of the moment vector. More complex magnetic models may include parameters defining the size or shape of the ferrous object.

## 5 Magnetic Models

The simplest model of a magnetic object is the “point dipole”, a field pattern equivalent to that which would be produced by an infinitely small current loop or bar magnet. It can be thought of as the field produced by two magnetic monopoles (“point charges”) of equal and opposite charge, in the limit that the separation between them is reduced to zero (though it is worth noting that individual magnetic monopoles do not truly



**Figure 2:** Note: from !!!, see references. This figure plots the magnetic field surrounding a point dipole which is oriented upwards ( $\mathbf{H}$  is directly proportional to  $\mathbf{B}$ ).

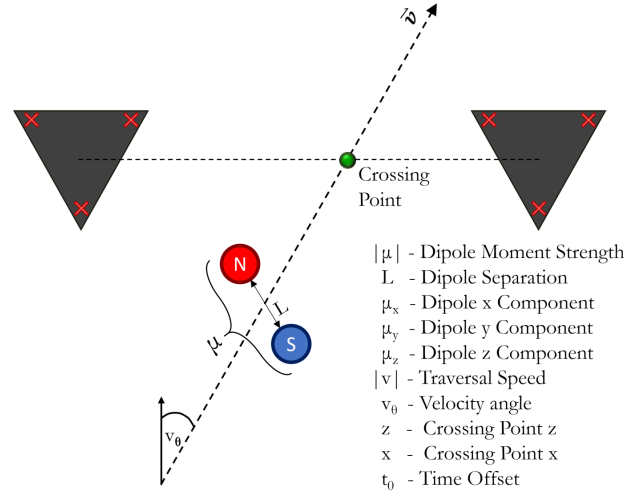
exist in nature). This field pattern has cylindrical symmetry, and can be defined completely by a “magnetic dipole moment” vector (often denoted  $\mathbf{m}$  or  $\boldsymbol{\mu}$ ) which describes both strength and orientation of the dipole. The B-field produced by a point dipole source is given by the following equation:

$$\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi} \left[ \frac{3\mathbf{r}(\mathbf{m} \cdot \mathbf{r})}{\|\mathbf{r}\|^5} - \frac{\mathbf{m}}{\|\mathbf{r}\|^3} \right], \quad (1)$$

where  $\mathbf{B}$  is the magnetic field vector,  $\mathbf{r}$  is the displacement between the dipole and the point being measured,  $\mu_0$  is the permeability of free space (a constant), and  $\mathbf{m}$  is the magnetic moment. The magnetic field produced by this model is plotted in Figure 2; further information can be found in !!! and !!! in the references.

A natural generalisation of this model is what we have termed the extended dipole. This consists of two magnetic monopoles with finite separation; as such, it is not strictly physical, but is a better approximation for extended ferrous objects which are not point-like in nature. This model can be described completely by a moment vector, as before, and the object “length” (i.e. the separation between the monopoles). This provides two parameters (the magnitude of the moment vector and the object length) describing the intrinsic magnetic properties of the object which can then be used for classification.

More sophisticated magnetics models are under consideration to provide additional magnetics parameters for classification. If this project is successful, a natural next step might be to augment this process with these advanced magnetic models.



**Figure 3:** Model currently in use: An extended dipole, with magnetic moment strength  $|\boldsymbol{\mu}|$ , dipole vector components  $\mu_x$ ,  $\mu_y$ ,  $\mu_z$ , and dipole separation (“length”)  $L$ , traverses the channel with speed  $|\mathbf{v}|$ , velocity angle  $v_q$ , and time offset  $t_0$ , intersecting the sensing plane at a crossing point with dimensions  $x$ ,  $z$ .

## 6 Current Levenberg-Marquardt Implementation

The current detection approach uses the Levenberg-Marquardt algorithm to fit a window of data to the physical model. The following assumptions are currently made: the object follows a straight line path, remains at a constant height (i.e. the velocity has no  $z$ -component), moves at a constant speed, and does not rotate along its trajectory. An extended dipole model is used for the magnetics due to the extra parameter it provides, although our implementation can handle the point dipole case too. Figure 3 gives a diagrammatic representation of this model.

The physical model provides a simulation of the magnetic field at the sensors recorded over the length of a window. The squared error between this simulation and the recorded data is used to define a cost function, which is highly nonlinear with no known analytic derivative. This is therefore a nonlinear optimisation problem, and the Levenberg-Marquardt algorithm is used to find the global minimum. Sixty start-points carefully chosen across the parameter space are used to ensure the located minimum is the global rather than local minimum – in practice, this has proven to be robust for our problem, and the global minimum is typically found.

## 7 Weaknesses of the Current Approach

Our implementation of the Levenberg-Marquardt algorithm works as intended: the global minimum of the cost function is located. The shortcomings arise due to

the inherent limitations with formulating the problem in this manner. In particular:

- The current problem formulation contains very strong assumptions about the traversal trajectory: straight line, constant velocity, no orientation changes, etc. This is clearly a big oversimplification, as objects carried by human beings during a typical walkthrough will have many accelerations and deviations in the trajectory. It is also incapable of dealing with sloped surfaces and stoppages.
- There is no easy way to include prior information about the distribution of the model parameters. Currently this is being done by editing the cost function to impose sensible limits on the fitted parameters, but this is clunky and ignores detailed information about the prior distributions that is already known.
- The end result of the fit is a point estimate of the optimum model parameters. A probability distribution over the model parameters would provide greater interpretability and more information to send to the classifier [A full distribution over the model parameters would incorporate very nicely into our current anomaly detection approach.].

It is possible that the trajectory errors might be diminished by adopting a sequential fitting approach with Lev-Mar, however for many samples there is not enough information to get a reliable fit in a noisy environment. In addition, the strong correlations between samples is ignored with this approach, and information from the fit of one sample can not easily be utilised to influence the fit of the next. For this reason, we are hopeful that a sequential Bayesian approach might overcome the inherent shortcoming of our current fitting technique.

## 8 State Space Formulation

Our problem can be described well in the language of state space models. We have a hidden state, which describes the magnetic properties, orientation, position, and velocity of the object at a given time sample, and a transition model, which updates the position of the object between samples and is a function of the state. The measurement model is given by the sensor B-field measurements at each position in the pillar, and is again a function of the state.

To demonstrate a proof of principle with this approach, it might be best to avoid excess complexity at first. A good place to start might therefore be with a point dipole, straight line trajectory model. In this case, our problem might be formulated like this:

State:

Transition model:

Measurement model:

The measurement model is clearly nonlinear, and will become even more complex if a more sophisticated

magnetic model is used. The prior distributions for the model parameters are not necessarily Gaussian, for example, the measured benign moments appear to more closely match a lognormal distribution, and multiple modes are a possibility. Consequently, a simple Kalman filter is insufficient for our problem. We are also somewhat computationally constrained, as any solution will eventually have to run in real-time on embedded hardware. The AKKF method therefore appears a promising fit for our purposes.

It is important to note that the critical model parameter that needs to be estimated is the moment strength (along with any other parameters describing the intrinsic magnetic properties in more complex magnetic models), as this is what the detection decision will be based on. In the simplest case, this is constant along the trajectory, and so there is no requirement to perform any kind of real-time tracking. A full window of data can therefore be used to perform the parameter estimation, making this a smoothing problem rather than a filtering problem using the terminology defined by [!!!!]. As only a small subset of the state parameters are necessary for classification, the other parameters might then be marginalised out (though in this case, it would be useful to store these distributions prior to the marginalisation, as they have scientific utility separate from their usefulness in classification).

## 9 Data

Metrasens can provide a great deal of data to assist with this project. We have working simulators in Matlab and Python, covering a range of models, which can be used to provide simulated data to verify the implementation with a known ground truth. The real test for this method, however, will be its performance on genuine data recorded by the Skout system.

These recordings could cover a range of scenarios. We can record controlled traversals, using test objects with known magnetic properties, constrained to accurate straight-line traversals using a non-magnetic trolley system. We can also record data with more realistic trajectories to verify that we can cope with this scenario using more complex trajectory models. If the method is showing promise, we can evaluate its use on real Skout recordings taken during public screening data collection events. This is very messy and noisy data which is the gold standard for any detection algorithm we might try.

## 10 Adding Complexity

If we successfully verify the simple model described in [!!!!!!], we can think about adding complexity to our model to improve its performance on real datasets. There are many different forms this could take, some of which are listed below:

- Advanced magnetic models: the point dipole model only provides one useful parameter for classifying the objects, which is the dipole moment strength. Experience tells us that this is not enough to successfully discriminate threat and benign objects. The current Lev-Mar implementation uses an extended dipole model, which provides an extra “length” parameter which can be sent to a classifier, so this would be a natural next step. More sophisticated magnetic models are under consideration, but are primarily in the research stage at the moment. See section [!!!!].
- Improved transition model: one of the major perceived strengths of this approach is its ability to handle more complex and unpredictable object trajectories. As such, it would be beneficial to add complexity to the transition model to move beyond straight-line, constant velocity trajectories. A good place to start might be the random accelerations model: [!!!!] Other augmentations, such as allowing the objects to rotate, may also add value.

## 11 Advanced Features

Comment about the advanced features goes here!!

- Signal differences: One of the challenges passive detection systems face is dealing with magnetic interference from distant sources. Signals from distant objects have the characteristic that the “common-mode” component of the signal (that which appears on all sensors simultaneously) is much greater than the differences between signals. For this reason, we typically fit our models to the differences between signals rather than the raw signal itself, in effect using the system as a gradiometer. Replicating this process in the measurement model could considerably improve the performance in a real-world scenario.
- Multiple object models: an unfortunate reality when screening the public using this technology is that people often carry multiple ferrous objects, for example, someone might carry a phone in their pocket, whilst wearing headphones. In this scenario, a single object fit will produce unreliable results. Augmenting the state to describe multiple objects might therefore improve the quality of information sent to the classifier.
- Interference sources: Urban environments contain many sources of magnetic interference: traffic, subways, electrical equipment, nearby members of the public, to name just a few. Robustness against this type of interference could be critical in achieving the level of performance necessary for this technology to work effectively. It might be possible to change the model to include basic interference sources to combat this.

- Signal processing: The raw signals from the magnetometers are not used directly in the detection algorithm; some signal processing procedures are applied. The most important is probably the application of a high-pass filter, which removes drift in the sensors and offsets due to changes in the magnetic background. The filtering process also distorts the signals, however, which may lead to less accurate parameter estimation. It is proposed that this might be mitigated by incorporating the filtering process (or other preprocessing procedures) into the model: the state could contain extra parameters corresponding to the state of the filter at each timestep, and the measurement function would contain an extra procedure to apply the filtering process to the measured field.

## References

- Defining the Magnetic Dipole* (n.d.). [https://em.geosci.xyz/content/maxwell1\\_fundamentals/dipole\\_sources\\_in\\_homogeneous\\_media/magnetic\\_dipole\\_definition/index.html](https://em.geosci.xyz/content/maxwell1_fundamentals/dipole_sources_in_homogeneous_media/magnetic_dipole_definition/index.html). Accessed: 07-05-2022.
- Hyperphysics Dipole* (n.d.). <http://hyperphysics.phy-astr.gsu.edu/hbase/magnetic/magfie.html>. Accessed: 07-05-2022.
- Wiki Dipole* (n.d.). [https://en.wikipedia.org/wiki/Magnetic\\_dipole](https://en.wikipedia.org/wiki/Magnetic_dipole). Accessed: 07-05-2022.